Self-annihilating or decaying dark matter in the Galactic halo might produce high energy neutrinos detectable with neutrino telescopes. We have conducted a search for such a signal using 276 days of data from the IceCube 22-string configuration detector acquired during 2007 and 2008. The effect of halo model choice in the extracted limit is reduced by performing a search that considers the outer halo region and not the Galactic Center. We constrain any large-scale neutrino anisotropy and are able to set a limit on the dark matter self-annihilation cross section of \((\sigma v) \approx 10^{-22} \text{ cm}^3 \text{s}^{-1}\) for weakly interacting massive particle masses above 1 TeV, assuming a monochromatic neutrino line spectrum.

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I. INTRODUCTION

There is compelling observational evidence for the existence of dark matter. Although knowledge of its underlying nature remains elusive, a variety of theories provide candidate particles [1]. Among those are supersymmetry [2] and universal extra dimensions [3], both of which predict new physics at the electro-weak scale and, in most scenarios, introduce a light, and stable (or long lived) particle that exhibits the properties of a weakly interacting massive particle (WIMP) [4]. WIMPs are an ideal dark matter candidate, predicted to have masses ranging from a few tens of GeV to several TeV. High energy neutrinos are expected to be produced as a result of the self-annihilation or decay of WIMPs. These neutrinos are detectable by high energy neutrino telescopes, making them powerful tools in the search for WIMPs and the investigation of their properties. In particular, they can be used to probe the self-annihilation cross section of dark matter candidates by looking for anomalous neutrino signals from the Galactic halo. Additionally, WIMPs could also be gravitationally captured by massive bodies like the Sun. If the annihilation rate of these captured WIMPs is regulated by the capture rate, then neutrino telescopes can be used to probe the WIMP-nucleon scattering cross section [5].

Recent observations of a GeV positron excess by PAMELA [6], and the energy spectra of electrons and positrons above 300 GeV measured by Fermi [7], H.E.S.S. [8], and ATIC [9] might hint at a dark matter annihilation signal. The observed lepton signals deviate from standard electron-positron production models [10], which could be due to limitations in the modeling, unaccounted nearby astrophysical sources (e.g. pulsars [11], supernova remnants [12,13]), or indicate a dark matter signal. To positively identify or reject a dark matter signal requires consistent results in multimessenger observations with γ-rays, electrons, and neutrinos. If the observed electron signals are interpreted as originating from dark matter annihilations, it would suggest the existence of a leptophilic
dark matter particle in the TeV mass range. Such a model would also result in significant high energy neutrino fluxes, through the decay of muons and \( \tau \)-leptons, and shows the importance of observations in the neutrino channel. A significant fraction of neutrinos could also be produced directly as part of the annihilation, producing a line feature in the resulting neutrino spectrum. Such a monoenergetic neutrino flux is also of specific interest since it can be used to set a model-independent limit on the total dark matter self-annihilation cross section for the region of parameter space where gamma-ray signals would dominate.

In this paper we discuss a search for neutrino signals produced by annihilating or decaying dark matter in the Galactic halo. The search is used to test the self-annihilation cross section by constraining the product of cross section and velocity averaged over the dark matter velocity distribution, \( \langle \sigma v \rangle \), and to probe the lifetime, \( \tau \).

The search focuses on the outer Milky Way halo, where the dark matter density distributions are relatively well modeled. We do not include the Galactic Center region and thus remove any strong dependence on the choice of the halo profile. We quantify the residual weak dependence and present constraints on the dark matter self-annihilation cross section and lifetime in a model-independent way for a set of selected benchmark annihilation and decay channels, respectively.

The paper is organized as follows: in the next section we describe the detector used for the data taken during 2007–2008 which is the base for our analysis. Sec. III discusses how we obtain an expected neutrino flux at Earth using different dark matter distributions and annihilation channels. In Sec. IV we describe our data selection criteria and analysis strategy, which is followed by a discussion of the associated systematic uncertainties in Sec. V. Section VI presents the result of the search, and Sec. VII puts it in context with other experiments. Section VIII concludes by summarizing the results and giving an outlook for related searches.

II. THE ICECUBE NEUTRINO OBSERVATORY AND EVENT SELECTION

The IceCube Neutrino Observatory, located at the geographic South Pole, consists of the IceCube neutrino telescope and the IceTop air shower array. IceTop covers a surface area of one square-kilometer above the IceCube “in-ice” detector, and is designed to measure cosmic ray air showers with energies between approximately 300 TeV to 1 EeV. The in-ice detector instruments a volume of one cubic kilometer of Antarctic ice with 5160 digital optical modules (DOMs) deployed at depths between 1450 m and 2450 m (see Fig. 1). The DOMs are distributed over 86 electrical cable bundles (strings) that handle power transmission and communication with electronics located on the surface. Each DOM consists of a 25 cm Hamamatsu R7081-02 photomultiplier tube connected to a waveform recording data acquisition circuit. The data acquisition is capable of resolving pulses with nanosecond precision and has an effective dynamic range of 200 photoelectrons per 15 ns.

IceCube detects all flavors of active neutrinos through Cherenkov light emission from secondary particles created when a neutrino interacts in the ice. Muon neutrinos are of particular interest since their extended tracklike topology makes them relatively simple to identify. Furthermore, the
elongated tracks of the muons permit a relatively accurate reconstruction of the neutrino direction with approximately a few degrees precision at the detection threshold of 100 GeV. Neutrinos with energies down to about 10 GeV can be identified in a densely instrumented sub-detector, DeepCore [22], which has been operating since early 2010 (see Fig. 1). In this analysis, we use data taken with an intermediate construction stage of the in-ice detector, comprising 22 strings.

The primary background in the search for neutrinos originates from cosmic ray air showers. When high energy cosmic rays enter the Earth’s upper atmosphere they produce extended air showers, a part of which includes high energy pions and kaons. The decay of these mesons results in a continuous stream of neutrinos and muons. These are known as atmospheric muons and neutrinos, and their flux is regulated by the path length and time the parent particles had in the atmosphere to lose energy or decay. The resulting neutrino spectrum obeys a power law with a spectral index of $\gamma = 3.7$ [23,24]. High energy muons are capable of travelling long distances through matter before they eventually decay, resulting in a down-going muon flux at the IceCube detector. In contrast, neutrinos below 100 TeV can traverse the Earth without significant absorption losses. To distinguish between a muon produced from a charged current interaction of a muon neutrino from those produced in the atmosphere, we select only tracks that enter the detector from below the horizon. Given the 22-string detector configuration (see Fig. 1) for the analysis presented here, the total trigger rate was approximately 550 Hz, dominated by down-going atmospheric muons. A preselection at the South Pole for up-going reconstructed tracks reduces the data rate to 20 Hz, which is sent by satellite to be processed offline.

### III. Halo Profiles and Signal Expectations

Recent advances in N-body simulations [25] and gravitational lensing observations [26] have provided reliable predictions of the dark matter density distribution in the Milky Way (MW). While the outer regions of the dark matter halo of the Milky Way (several kpc away from the Galactic Center) are relatively well modeled, the structure of its central region is still a matter of debate since it can neither be resolved in simulations, nor directly measured. Not surprisingly, halo models generally show very similar behavior at large distances from the Galactic Center, but differ significantly in their predictions near it. This effect is shown in Fig. 2, where the dark matter density, $\rho(r)$, predictions from several spherically symmetric halo profiles obtained from N-body simulations are compared. We show four different distribution functions which are used in our analysis. Since we only use neutrinos from the northern sky, the effective dark matter densities which dominate the analysis are those between a distance from roughly 4 kpc to 20 kpc from the Galactic Center. In this range the various halo profiles are relatively consistent in their description of the dark matter density. This agreement allows us to constrain the dark matter self-annihilation cross section with minimal halo profile dependence.

We use the Einasto [27,28] and Navarro-Frenk-White (NFW) [29] profiles as benchmark models, while the Moore [30], and Kravtsov [31] profiles were applied as extreme cases to estimate the impact of halo model choice on the result. The Einasto profile is given by:

$$\rho(r) = \rho_{-2} \times e^{(-2/\alpha)(r/r_s)^{\alpha-1}}$$  \hspace{1cm} (1)$$

with $\alpha = 0.16$ [32], $r_s = 20$ kpc, and $\rho_{-2}$ normalized to a dark matter density $0.3 \text{GeV cm}^{-3}$ at the solar system’s orbit in the Galaxy ($R_{sc} = 8.5$ kpc). The remaining three profiles can be described by the following function:

$$\rho(r) = \frac{\rho_0}{\left(\frac{r}{r_s}\right)^\gamma \left[1 + \left(\frac{r}{r_s}\right)^\alpha\right]^\frac{\beta-\gamma}{\alpha}}.$$  \hspace{1cm} (2)$$

where the variables ($\alpha$, $\beta$, $\gamma$, $r_s$) [33] take different numerical values (listed in Table I) for the three models. The normalizations are chosen such that the mass contained within the orbit of the Solar System in the Galaxy provides the appropriate dark matter contribution to the local rotational curves, and yields a local dark matter density $\rho_{sc} = \rho_{NFW}(R_{sc}) = 0.3 \text{GeV cm}^{-3}$ for the NFW profile.

The expected neutrino flux, $\phi_\nu$, from dark matter self-annihilations is proportional to the square of the dark matter density integrated along the line of sight $J(\psi)$:

$$J(\psi) = \int_0^{l_{max}} \rho^2 \sqrt{R_{sc}^2 - 2lR_{sc} \cos \psi + l^2} \frac{dl}{R_{sc}^2 \rho_{sc}^2}.$$  \hspace{1cm} (3)$$

where $\psi$ is the angular distance from the Galactic Center and $l_{max}$ is the upper limit of the integral, defined as...
TABLE I. Summary of the parameters of Eq. (2) used in this analysis.

<table>
<thead>
<tr>
<th>Halo Model</th>
<th>(\alpha)</th>
<th>(\beta)</th>
<th>(\gamma)</th>
<th>(r_x/\text{kpc})</th>
<th>(\rho(R_{sc})/\text{GeV/cm}^2)</th>
</tr>
</thead>
<tbody>
<tr>
<td>NFW</td>
<td>1</td>
<td>3</td>
<td>1</td>
<td>20</td>
<td>0.3</td>
</tr>
<tr>
<td>Moore</td>
<td>1.5</td>
<td>3</td>
<td>1.5</td>
<td>28</td>
<td>0.27</td>
</tr>
<tr>
<td>Kravtsov</td>
<td>2</td>
<td>3</td>
<td>0.4</td>
<td>10</td>
<td>0.37</td>
</tr>
</tbody>
</table>

\[
l_{\text{max}} = \sqrt{(R_{\text{MW}}^2 - \sin^2\psi R_{sc}^2) + R_{sc} \cos\psi}. \quad (4)
\]

We adopt a halo size of \(R_{\text{MW}} = 40\) kpc. Contributions to the expected neutrino flux from beyond this range are small, and are discussed as part of our systematic studies of the result in Sec. VI.

The annihilation products are highly model dependent and we thus study extremes of the possible annihilation channels assuming a branching ratio of 100% for each of them in turn. We consider soft neutrino spectra produced from the annihilation into quarks \((\bar{b}b)\), and hard spectra as produced by annihilation into \(W^+W^-\) and \(\mu^+\mu^-\). In addition, we consider a neutrino line spectrum \((\chi\chi \rightarrow \nu\bar{\nu})\).

Neutrinos will have undergone extensive mixing through vacuum oscillations over the distances travelled across the Galaxy. We determine neutrino flavor oscillations in the long baseline limit \([34, 35]\), adopting values of \(\sin^2 2\Theta_{12} = 0.86\), \(\Theta_{23}\) maximal \((\Theta_{23} \approx \pi/4)\), and \(\Theta_{13} \approx 0\). The neutrino fluxes at Earth are then given by:

\[
\phi_\nu \approx \phi^0_{\nu} \pm \frac{1}{4} s_2
\]

and

\[
\phi_\nu \approx \phi^0_{\nu} \pm \frac{1}{8} s_2,
\]

where \(\phi^0_{\nu}\) is the flux at injection and \(s_2\) is defined as \(\sin^2 2\Theta_{12} (2\phi^0_{\nu} - \phi^0_{\bar{\nu}} - \phi^0_{\mu})\). Note that the expected fluxes for muon and tau neutrinos are equal.

The neutrino energy spectra were produced using DarkSUSY \([36]\), an advanced numerical software package for supersymmetric dark matter calculations, and are shown in Fig. 3.

The differential neutrino flux from the annihilation of neutralinos of mass \(m_\chi\) in the Galactic halo is given by \([33]\):

\[
\frac{d\phi_\nu}{dE} = \frac{\langle \sigma_A \rangle}{2} \int J(\psi) \frac{R_{sc} R_{sc}^2}{4\pi m_\chi^2} \frac{dN_\nu}{dE}.
\]

where \(\frac{dN_\nu}{dE}\) is the differential neutrino multiplicity per annihilation. Similar to the annihilation cross section, one can search for signals from decaying dark matter \([37, 38]\) and constrain the lifetime, \(\tau\). For decaying dark matter, the expected neutrino flux is proportional to the dark matter density along the line of sight, given by:

\[
J_d(\psi) = \int_0^{l_{\text{max}}} \rho(R_{sc}) J_d^2 \frac{d\psi}{dE} dl.
\]

The expected neutrino flux from the dark matter decay is then:

\[
\frac{d\phi_\nu}{dE} = \frac{1}{\tau} J_d(\psi) \frac{R_{sc} R_{sc}^2}{4\pi m_\chi^2} \frac{dN_\nu}{dE}.
\]

We use identical halo model parameters in both the dark matter annihilation and decay analyses. We assume a smooth halo profile and discuss the effect of substructure separately.

IV. DATA SELECTION

The search for a clustering of neutrinos to indicate an astrophysical neutrino source is one of the benchmark analyses performed by the IceCube collaboration. Such a “point source” search relies on muon neutrinos since the elongated tracks of the muons permit an accurate reconstruction of the neutrino direction. The 22-string detector configuration has produced a well understood neutrino candidate sample \([39]\), extracted using likelihood-based track reconstructions and selecting tracks from \(-5^\circ\) to \(85^\circ\) in declination. The shape of the likelihood function around the best-fit value is used to estimate the angular uncertainty of the reconstructed track \([40]\), while the number of optical modules in the event which record minimally scattered Cherenkov photons gives an additional handle on the quality of the reconstruction. Such “direct” photons are isolated via a time difference selection window between the expected arrival time of an unscattered photon, given the reconstructed track, and the registered DOM hit time. Near the horizon, the background from poorly reconstructed atmospheric muons is further reduced by an additional cut on the likelihood ratio of the best-fit track to the best-fit track constrained to be down-going. These applied
selection criteria remove the largest fraction of misreconstructed down-going events, maintaining a neutrino candidate sample with about 90% purity [39]. The final northern sky dataset consists of 5114 neutrino candidate events acquired in 275.7 days of livetime. Figure 4 shows the neutrino energy distribution of simulated events that pass all the selection criteria that are applied to the data events.

Assuming a given annihilation channel and dark matter halo profile, one can determine the expected neutrino flux (proportional to the dark matter annihilation cross section) for any given location on the sky. The flux is peaked in the direction of the Galactic Center, which is a prominent target for searches. However, the Galactic Center is located in the southern hemisphere at $266^\circ$ right ascension (RA) and $-29^\circ$ declination and therefore outside the field of view of IceCube for the selection criteria applied here.

In the northern hemisphere, regardless of the choice of halo model, dark matter annihilations would produce a large-scale neutrino anisotropy. The search for such an anisotropy affords distinct advantages for discovery. An observation of a flux from the Galactic Center would be more difficult to distinguish from other astrophysical sources or cosmic ray interaction with the interstellar medium. However, the Galactic Center is an excellent target to constrain the dark matter self-annihilation cross section for a given halo model and is the subject of a separate analysis.

To test for an excess flux of neutrinos, we define two regions on the northern sky. The first region will serve as our signal region (on-source) and is defined by a half-opening angle, $r_{\phi}$, around the Galactic Center. An equally sized region, offset by $180^\circ$ in RA, serves an off-source region (see Fig. 5). This choice is motivated by the robustness and simplicity of the ensuing analysis and minimizes systematic uncertainties due to azimuth angle dependent reconstruction efficiencies. For spherical halo profiles, the expected flux is a function of the angular distance from the Galactic Center, $\phi$, and we count the total number of neutrino candidate events in each region. This makes the analysis maximally independent of halo profiles and provides sensitivity to both hard and soft neutrino spectra.

The difference in the expected number of neutrino events between the on-source and off-source region is given by:

$$\Delta N = (N_{\text{on}}^{\text{sig}} + N_{\text{off}}^{\text{bkg}}) - (N_{\text{off}}^{\text{bkg}} + N_{\text{off}}^{\text{sig}}),$$

where bkg/sig stand for background and signal, respectively. Background events are expected to be equally distributed in the on- and off-source regions, simplifying the prediction to $\Delta N_{\text{sig}} = N_{\text{on}}^{\text{sig}} - N_{\text{off}}^{\text{sig}}$. The signal expectation in both regions, and hence $\Delta N_{\text{sig}}$, is directly proportional to the dark matter self-annihilation cross section $\langle \sigma_A v \rangle$. To optimize the size of the on- and off-source region, we chose an example cross section $\langle \sigma_A v \rangle_0$ and predict the expected number of signal events $S = \Delta N_{\text{sig}}$ from simulations for different choices of $r_{\phi}$ [41]. For $r_{\phi} = 80^\circ$, the ratio of $S/\sqrt{B}$, where $B$ is the expected number of background events, is close to maximal for all considered halo profiles, while the on- and off-source regions remain well separated and do not overlap.

V. SYSTEMATIC UNCERTAINTIES

We first discuss the systematic uncertainty associated with the background estimation. By design, the background
can be determined from the data by comparing events in the on- and off-source regions, eliminating most detector related effects. Thus, only preexisting anisotropy in the data must be considered. The two dominant effects giving rise to an anisotropy are (1) an anisotropy in the cosmic ray flux producing the atmospheric muon neutrino flux and (2) variations in exposure for different RA.

A large-scale anisotropy in the cosmic ray flux has been observed both on the northern hemisphere by the TIBET air shower array [42] and the southern hemisphere by an IceCube measurement of the down-going muon flux [43]. The northern hemisphere anisotropy for cosmic ray energies around 50 TeV is relevant to this analysis. This energy range of cosmic ray showers contributes most in creating this analysis’ background up-going atmospheric muon neutrino flux. The overall scale of the measured cosmic ray anisotropy is about 0.2%, with peak values at RA = 60° and a minimum at RA = 180°. This is not aligned with an expected signal anisotropy from the Milky Way dark matter halo. To provide a conservative systematic uncertainty estimate, we assume the worst case of an aligned anisotropy, which peaks in one region and is minimal in the other. In such a scenario a difference of three events between on- and off-source regions would be observed, corresponding to a 0.2% systematic uncertainty on the number of background events.

The muon track reconstruction efficiency varies as a function of the zenith angle and azimuth angle [39,44]. Although the azimuth dependence is relatively uniform for the axially symmetric full IceCube detector, it is particularly pronounced in the partially instrumented 22-string detector configuration used for this analysis. As the Earth rotates, each detector alignment in RA gets equal exposure within one sidereal day. A small fraction of detector operations is dedicated towards scheduled detector maintenance, which is performed at times when communication with the South Pole can be established. The use of geosynchronous satellites introduces a bias in sidereal time, which means that fewer physics data runs are available for particular alignments of the detector in RA. The track reconstruction efficiency for a muon with azimuth angle \( \phi \) compared to one with the opposite direction \( \phi + 180° \) is almost identical. Hence, selecting symmetric on- and off-source regions shifted by 180° in RA reduces the effect due to azimuth angle dependent reconstruction efficiency significantly, as the chance of observing an event in the on-source region is almost identical to that of observing one in the off-source each time the detector is active. The total expected variation in the number of events due to exposure is approximately 0.1% (see Fig. 6).

It is possible, in principle, to correct for both the cosmic ray anisotropy and detector uptime effects. Because of their negligibly small impact compared to the background statistical uncertainty, such a correction has not been applied. The contribution from the cosmic ray anisotropy

![FIG. 6 (color online). The relative exposure variation as function of RA and shifted by 180° is shown. The absolute variation defines the signal acceptance uncertainty due to exposure (~1%), while the difference between the normal and rotated exposure defines the corresponding systematic uncertainty on the background estimate (~0.1%), (0.2%) and the uneven exposure (0.1%) are uncorrelated. We use 0.3% as a conservative estimate on the total systematic uncertainty on the number of background events in the on-source region (see Table II).]

The signal acceptance uncertainty is dominated by uncertainties in the ice properties and limitations in the detector simulation, which is uncorrelated with a number of theoretical uncertainties such as muon propagation, neutrino cross section, and bedrock uncertainty, each of which have been studied in previous analyses [39]. In addition, we consider the uncertainty due to Monte Carlo simulation statistics and detector exposure. The individual track pointing uncertainty (point spread function), on the order of 1°, is negligible in this analysis, which targets a large-scale anisotropy.

Our dominant systematic uncertainty, the limited knowledge of ice properties as a function of depth and limitations in the detector simulation, is expected to produce an observed discrepancy between data and simulation for events near the horizon [39]. For nearly horizontal tracks the disagreement is maximal, with 30% more events observed in data compared to simulation predictions. Since we use the data itself to predict the number of background events in the on-source region, this discrepancy does not affect the background estimate. However, the signal acceptance can

### TABLE II. Summary of systematic uncertainties on the background estimate.

<table>
<thead>
<tr>
<th>Effect</th>
<th>Sys. Uncertainty</th>
</tr>
</thead>
<tbody>
<tr>
<td>Cosmic ray anisotropy</td>
<td>0.2%</td>
</tr>
<tr>
<td>Exposure</td>
<td>0.1%</td>
</tr>
<tr>
<td>Total Background</td>
<td>0.3%</td>
</tr>
</tbody>
</table>
only be obtained from simulations. Hence, we must take this discrepancy into consideration for the signal acceptance uncertainty. The higher than expected observed data rate, when compared to simulation expectations, may indicate a contribution from misreconstructed down-going events, or a higher signal acceptance than expected. Both would cause the constraints presented later to be more conservative. The estimate for this systematic uncertainty in signal acceptance is 25%–30%.

The track reconstruction efficiency coupled with detector uptime (see Fig. 6) results in a systematic uncertainty on the signal acceptance of 1%. This uncertainty, combined with the theoretical uncertainties, results in a negligible contribution compared to the uncertainties in the optical properties of the ice. We therefore assume a 30% systematic signal acceptance uncertainty, primarily associated with that from the ice properties and limitations in the detector simulation.

An additional systematic uncertainty to consider in signal acceptance is related to the photon detection efficiency of the DOMs, measured to be 8% in the laboratory [21]. The effect of this uncertainty on the passing rate of reconstructed tracks is found to range from about 1% for energetic events (≥ 1 TeV), increasing to as much as 20% for lower energy events (≤ 200 GeV), as expected from annihilations assuming WIMPs of mass 200 GeV. We calculate this uncertainty for each of the considered WIMP masses and annihilation channels, then we add it in quadrature to the ice properties uncertainty discussed above.

To derive the total uncertainty on the signal acceptance, we have added the systematic signal acceptance uncertainty in quadrature to the statistical uncertainty (Monte Carlo statistics). The Monte Carlo statistics uncertainty ranges from 3%–6% (hard channels) and 4%–16% (soft channels) in the TeV mass range dark matter, and increases to 50% (hard channels) and 90% (soft channel) at \( m_x = 200 \text{ GeV} \).

VI. RESULTS

Except for examination of the data for quality assurance, the optimization of the size of the on-source region was performed entirely with simulated events, ensuring a blind analysis. In the final dataset we observed 1389 events in the off-source region and 1367 events in the on-source region, consistent with the null hypothesis. Figure 7 shows the distribution of these neutrino candidate events in declination and right ascension. To study the possibility of an anisotropy in an adjacent bin, we shift the on- and off-source regions in 60° steps. For each of the step bins, the ratio of \( N_{\text{on}} / N_{\text{off}} \) is consistent with one (see Fig. 8).

We compute constraints on the neutrino flux from dark matter annihilation from the Galactic halo. Given a specific \( \langle \sigma_A v \rangle_0 \) in signal simulations, the number of expected events for an arbitrary cross section \( \langle \sigma_A v \rangle \) is

\[
\Delta N_{\text{sig}}^\text{on} (\langle \sigma_A v \rangle) = \frac{\langle \sigma_A v \rangle}{\langle \sigma_A v \rangle_0} (\Delta N_{\text{sig}}^\text{on} (\langle \sigma_A v \rangle_0)).
\]

(11)

The cross-section limit at 90% C.L. is

\[
\langle \sigma_A v \rangle_{90} = \frac{\langle \sigma_A v \rangle_0}{\Delta N_{\text{sig}}^\text{on} (\langle \sigma_A v \rangle_0)}.
\]

(12)

where \( \Delta N_{90} \) is the limit at 90% C.L. for the number of signal events.

To determine \( \Delta N_{90} \), we construct a Neyman confidence belt. The one-sided 90% C.L. acceptance intervals are determined by a simple Monte Carlo, in which the numbers of events in the on- and off-source regions are assumed to be Poisson distributed over repeated measurements, with an average contribution of \( N_{\text{bkg}} = N_{\text{off}} = 1389 \pm 4(\text{sys}) \pm 37(\text{stat}) \). The 90% C.L. event upper limit \( \Delta N_{90} \) is calculated...
for various WIMP masses and annihilation channels using the appropriate signal expectation. Statistical and systematic uncertainties in the signal expectations are represented by log-normal distributions. For a 30% signal acceptance uncertainty, for example, the upper limit was found to be $\Delta N_{90} = 49$ for $\Delta N = -22$ events. For small signal acceptance uncertainties, where the log-normal distribution can be approximated by a Gaussian, results are consistent with the confidence interval constructed using the method by Lundberg et al. [45,46]. Our limit calculation of the on-source region also resembles a commonly used procedure by Li and Ma to compute the significance of an on-source observation [47]. The significance $\xi$ is defined as

$$
\xi = \frac{N_{on} - \eta N_{off}}{\eta \sqrt{N_{on} + N_{off}}} = \frac{\Delta N}{\sqrt{2} \times N_{off}}.
$$

(13)

Here $\eta$ is the ratio in exposure, or ratio of the size of the two regions. For our case of an equally sized on- and off-source region, $\eta = 1$.

Figure 9 shows the obtained exclusion limit compared to the “natural scale”, for which dark matter candidates are consistent with being a thermal relic [48,49]. Larger cross sections are possible if, for example, dark matter is produced nonthermally or acquires mass only in the late universe [50].

Applying the same procedure as that above for the annihilation cross section, we compute a 90% C.L. lower limit on the WIMP lifetime, $\tau$, as function of the WIMP mass, as shown in Fig. 10. We assume a line spectrum, $\chi \rightarrow \nu \tilde{\nu}$ and apply Eq. (9) for the expected neutrino flux. If dark matter is a thermal relic and unstable, the only requirement in order for it to be present today is that it has a lifetime much longer than the age of the Universe $T_U \approx 4 \times 10^{17}$ s.

Our limit calculation assumes smooth, spherically symmetric halo models. However, N-body simulations indicate that dark matter in the halo should have some substructure [51,52]. While this will have negligible effects on the expected neutrino flux from dark matter decay, the presence of substructure will enhance the self-annihilation rate since it is proportional to the square of the dark matter density. To quantify the average expected enhancement in the annihilation rate compared to a smooth dark matter distribution, one can define a boost factor as a function of the distance from the Galactic Center [53,54]:

$$
B(r) = \frac{\int \rho^2 dV}{\int (\rho)^2 dV},
$$

(14)

FIG. 9 (color online). 90% C.L. upper limit on the dark matter self-annihilation cross section for five different annihilation channels. Also shown are the natural scale (dotted line), for which the WIMP is a thermal relic [48,49], and unitarity bound (solid line) [61,62]. For the limit curves, the central line is for the Einasto and NFW profiles, while the shaded width identifies the extrema results from the Moore and Kravtsov profiles. We consider only smooth halo profiles. The limits for $\tau^+ \tau^-$ and $\mu^+ \mu^-$ overlay, due to their very similar high energy neutrino spectra.

FIG. 10 (color online). Lower limit on WIMP lifetime $\tau$ assuming $\chi \rightarrow \nu \tilde{\nu}$ at 90% C.L.

FIG. 11 (color online). Boost factor as function of the distance from the Galactic Center for the simplest model of [54] and a dark matter density using the NFW halo profile.
where we defined \( \bar{\rho} \) as the mean density of the smooth halo component. To determine the impact of a boosted neutrino flux on the expected neutrino signal in the on- and off-source regions we use the signal enhancement resulting from substructure in the halo following the simplest model of reference [54], as shown in Fig. 11.

We investigate the scaling of the limit due to a boost factor and the adopted size of the Galactic dark matter halo \( R_{MW} \) are given separately.

Another possible contribution to the neutrino flux from dark matter self-annihilations originates outside our Galaxy. This extragalactic flux[17] is expected to be isotropic and, hence, contributes equally to the on- and off-source regions. That is, any such additional flux would equally contribute to the number of events observed in the on- and off-source regions and hence make a flux limit based on the difference more conservative. Note also that the contribution from the extragalactic component is much smaller than the flux from within our Galaxy [33].

VII. COMPARISON TO PHENOMENOLOGICAL MODELS

There has been considerable debate about the nature of lepton signals observed by several instruments: a peak in the electron spectrum observed by ATIC [9], a GeV positron excess seen by PAMELA [6], and electron spectra measured by Fermi [7] and H.E.S.S. [8]. Observations could be interpreted as originating from dark matter self-annihilations, which would then be indicative of leptophilic dark matter candidates [14,15]. Alternatively, observations could also be explained through nearby astrophysical sources such as pulsars [11] or supernova remnants [12,13].

Since electrons lose significant energy during propagation, signals must originate within a distance of about 1 kpc from the Sun. While electron signals could only probe the local dark matter density, the presented large-scale...
anisotropy search probes a wider range of the Milky Way halo. Figure 13 compares the IceCube exclusion limit with a phenomenological interpretation [14] of electron measurements for two example annihilation channels ($\mu^+\mu^-\tau^+\tau^-$) and our chosen benchmark profile of Einasto. Even the small dataset used here allows this analysis to constrain models motivated by the anomalous lepton signals. Comparable results have been derived from gamma-ray observations of dwarf spheroidal galaxies, which have high light to mass ratios and are expected to be dark matter dominated. Fermi-LAT observations of various dwarf spheroidal galaxies have constrained the dark matter self-annihilation cross section and obtained limits below $10^{-24}$ cm$^3$ s$^{-1}$ for Draco and Ursa Minor for $m_\chi = 10$ GeV. For a WIMP mass of 1 TeV, the limits range between $10^{-20}$ cm$^3$ s$^{-1}$ and $10^{-22}$ cm$^3$ s$^{-1}$ [55] for various dwarf spheroidal galaxies. MAGIC has investigated Willman 1 [56] and Segue 1 and obtained limits around $10^{-22}$ cm$^3$ s$^{-1}$ and $10^{-23}$ cm$^3$ s$^{-1}$ for annihilation in $\mu^+\mu^-$ and $\tau^+\tau^-$, respectively, for WIMP masses between 200 GeV and 1.2 TeV [57]. VERITAS observed no significant gamma-ray excess from four dwarf spheroidals and derived an upper limit on the gamma-ray flux to constrain the self-annihilation cross section as a function of WIMP mass. The limit reduces to $10^{-22}$ cm$^3$ s$^{-1}$ for a WIMP mass of 300 GeV [58]. H.E.S.S. reported constraints on dark matter annihilation from the Sculptor and Carina dwarf galaxies and found that cross-section constraints on dark matter annihilation from the Sculptor and Ursa Minor for $m_\chi = 10$ GeV. For a WIMP mass of 1 TeV, the limits range between $10^{-20}$ cm$^3$ s$^{-1}$ and $10^{-22}$ cm$^3$ s$^{-1}$ [55] for various dwarf spheroidal galaxies. MAGIC has investigated Willman 1 [56] and Segue 1 and obtained limits around $10^{-22}$ cm$^3$ s$^{-1}$ and $10^{-23}$ cm$^3$ s$^{-1}$ for annihilation in $\mu^+\mu^-$ and $\tau^+\tau^-$, respectively, for WIMP masses between 200 GeV and 1.2 TeV [57]. VERITAS observed no significant gamma-ray excess from four dwarf spheroidals and derived an upper limit on the gamma-ray flux to constrain the self-annihilation cross section as a function of WIMP mass. The limit reduces to $10^{-22}$ cm$^3$ s$^{-1}$ for a WIMP mass of 300 GeV [58]. H.E.S.S. reported constraints on dark matter annihilation from the Sculptor and Carina dwarf galaxies and found that cross-section constraints range from $10^{-21}$ cm$^3$ s$^{-1}$ to $10^{-22}$ cm$^3$ s$^{-1}$ depending on the assumed dark matter halo model [59]. Limits can also be obtained from observations of $\gamma$-rays, produced via final state radiation, inverse Compton scattering, or synchrotron radiation, of the Galactic Center and Galactic ridge regions, as well as radio observation of the Galactic Center that constrain synchrotron radiation produced by $e^\pm$ in the local magnetic fields [14].

VIII. SUMMARY AND OUTLOOK

The IceCube candidate neutrino sample, collected during 2007–2008 in the 22-string configuration, has been used to search for a neutrino anisotropy as expected from dark matter self-annihilation in the Milky Way halo. Such an anisotropy was not observed and we have determined limits on the dark matter self-annihilation cross section $\langle \sigma_A \nu \rangle$ at 90% C.L. for WIMPs in the mass range from $200 \text{eV} \text{ to } 10 \text{ TeV}$. The IceCube detector sensitivity can be significantly improved by investigating the Galactic Center as a potential source. Such a search could be performed with the IceCube detector at a later construction stage and rely on selecting neutrinos interacting inside the detector volume [60]. It would be able to significantly improve the constraints on the dark matter self-annihilation cross section given a particular choice of halo model in the case of a non observation. A large-scale anisotropy study as performed here, however, might provide a more distinct discovery signal. In the case of the Galactic Center, a dark matter signal would be more difficult to distinguish from other astrophysical neutrino sources, such as point sources (source contamination) or cosmic ray interaction with the interstellar medium.

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