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We present a search for Kaluza-Klein (KK) particles predicted by models with universal extra dimensions (UED) using a data set corresponding to an integrated luminosity of 7 fb$^{-1}$, collected by the D0 detector at a $\sqrt{s}$ center of mass energy of 1.96 TeV. The decay chain of KK particles can lead to a final state with two muons of the same charge. This signature is used to set a lower limit on the compactification scale of $R^{-1} > 260$ GeV in a minimal UED model.

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The existence of extra dimensions in addition to the 3 + 1 dimensions of space-time has been postulated as a possible solution to the problem of the large hierarchy of scales in the standard model (SM). In models with universal extra dimensions (UED) all particles propagate in the extra dimensions [1]. In this Letter, we study a minimal UED (mUED) model, which has only one extra dimension [2].

Each SM particle in the mUED model is associated with a set of excited Kaluza-Klein (KK) states when viewed in 3 + 1 dimensions. Since compactification of the extra dimensions leads to periodic boundary conditions, the KK states have discrete masses of the order of $R^{-1}$, where $R$ is the radius of the compact dimension. If one-loop corrections are applied, the mass spectrum of the KK modes also depends on a cutoff scale for boundary terms, which is chosen to be 10 TeV [2]. Gluon KK modes ($g_1$) are the heaviest particles, followed by quarks (SU(2) doublet $q_1$ or singlet $q_1$), gauge bosons (Z$_1/W_1$), leptons (SU(2) doublet $L_1$ or singlet $\ell_1$) and the KK photon ($\gamma_1$), which is the lightest KK particle (LKP) and does not decay. The LKP is also a dark matter candidate [3].

Previous searches for KK particles predicted by a modified UED model have been conducted by the D0 [4] Collaboration at the Fermilab Tevatron Collider and by the ATLAS [5] Collaboration at the CERN Large Hadron Collider (LHC) in diphoton final states. In this model, gravity mediation allows decays of the LKP into a photon plus a light KK graviton. A search for events with two leptons of the same charge, which can be interpreted in a mUED model, has been performed by ATLAS [6], but no dedicated study of the mUED model has so far
been performed at a collider. Constraints from precision electroweak data \cite{1}, from the measurements of the muon anomalous magnetic moment and of the $b \to s \gamma$ branching ratio \cite{2}, indicate that the scale $R^{-1}$ can be as low as $\approx 300$ GeV, making KK particles accessible at the Tevatron. In this Letter, the first search for mUED in the final state with two leptons of the same charge is presented using data corresponding to 7.3 fb$^{-1}$ of integrated luminosity collected by the D0 detector \cite{8} at $\sqrt{s} = 1.96$ TeV.

At the Tevatron, KK gluons or quarks are mainly produced in pairs, as shown in Fig.~1. In the subsequent cascade decay, up to four charged leptons are produced. Since the masses of the extra particles predicted by the mUED models are nearly degenerate, the leptons are emitted with low transverse momentum and might escape detection. In this analysis, we select events with two muons of the same charge.

![FIG. 1: (a) Production of a pair of KK quarks ($Q_1 \bar{Q}_1$), (b) Decay of a KK quark into a jet, two oppositely charged leptons, and the LKP. Double lines indicate KK excitations. A similar cascade decay occurs for the second KK quark leading to several leptons of the same charge in the final state.](image)

The D0 detector \cite{S} consists of tracking systems and calorimeters. The innermost part is a tracking system where charged particles are detected by the silicon microstrip (SMT) and central fiber (CFT) tracking detectors, located within a 2 T solenoid. The tracking system is surrounded by a liquid-argon/uranium calorimeter. Particle energies are measured in the electromagnetic and hadronic calorimeters within a pseudorapidity range of $|\eta| < 4.2$ \cite{9}. Jets are reconstructed with a cone algorithm using a radius of $R = 0.5$ \cite{10} in the calorimeter. The central and forward muon detectors are composed of a layer of wire chambers and scintillators in front of a 1.8 T toroid magnet and two layers outside the toroid. Missing transverse energy is measured from the vector sum of the calorimeter cell energies in the $xy$ plane \cite{11}. A correction for the energy response of muons, electrons and jets is applied.

The backgrounds from $Z+\text{jets}$, $W+\text{jets}$, and $t\bar{t}$ production are modeled by the ALPGEN \cite{12} Monte Carlo (MC) event generator, interfaced with PYTHIA \cite{13} for showering and hadronization. Diboson production ($WW$, $WZ$ and $ZZ$) is simulated by PYTHIA. The CTEQ6L1 parametrization of the parton distribution functions (PDF) are used \cite{14}. Higher order cross sections for diboson and $W/Z+\text{jets}$ production are calculated by MCFM \cite{15} and the cross section of $t\bar{t}$ pair production is taken from \cite{16}. The dominant source of background is pairs of muons with the same charge from heavy flavor jets. This background contribution is estimated from data and is described in detail in the following.

Signal MC events are generated for 9 different values of $R^{-1}$, covering the range from 200 to 320 GeV in steps of 15 GeV, using PYTHIA with the CTEQ5L PDF parametrization \cite{17}. The production cross sections and masses of KK particles are taken from PYTHIA. They are given in Table I for each $R^{-1}$ and with all KK gluon and quark production modes included. All decay mechanisms leading to like-charge dimuon final states are taken into account. The decay branching fractions for all KK particles are given by the mUED model. After simulating all cascade decays, approximately 1% of events have two like-charged muons.

<table>
<thead>
<tr>
<th>$R^{-1}$ (GeV)</th>
<th>Masses (GeV)</th>
<th>Cross Section (pb)</th>
</tr>
</thead>
<tbody>
<tr>
<td>200</td>
<td>$\gamma_1$</td>
<td>$Z_1$</td>
</tr>
<tr>
<td>215</td>
<td>201</td>
<td>230</td>
</tr>
<tr>
<td>230</td>
<td>216</td>
<td>245</td>
</tr>
<tr>
<td>245</td>
<td>231</td>
<td>260</td>
</tr>
<tr>
<td>260</td>
<td>246</td>
<td>274</td>
</tr>
<tr>
<td>275</td>
<td>261</td>
<td>289</td>
</tr>
<tr>
<td>290</td>
<td>276</td>
<td>304</td>
</tr>
<tr>
<td>305</td>
<td>291</td>
<td>319</td>
</tr>
<tr>
<td>320</td>
<td>306</td>
<td>335</td>
</tr>
</tbody>
</table>

Table I: Masses of KK particles for each $R^{-1}$ value used in the MC generation with corresponding total production cross section.

All signal and background MC events pass through the full GEANT-based simulation of the detector \cite{18} and are reconstructed using the same algorithms as used for data. To simulate detector noise and multiple $p\bar{p}$ interactions, MC events are overlaid with data events from random beam crossings.

Events are selected by requiring that they pass at least one single muon trigger condition. We require that each event must contain at least two muons of the same charge. The track in the muon system must be matched to a track in the central tracking system with detector $|\eta| < 1.5$. We reject cosmic rays by requiring the associated scintillator hits in the muon system to be consistent with originating from a $p\bar{p}$ collision, the distance of closest approach (dca) of the muon tracks to the $p\bar{p}$ interaction vertex to be less than 0.05 cm, and the differences between the $z$ coordinates of the dca of each muon and the $p\bar{p}$ interaction vertex to be $< 1$ cm. We require $\Delta \phi_{\mu\mu} < 2.9$ rad for the azimuthal angle between the two muons in order to reject multijet background in which there are back-to-back jets which can contain muons from semileptonic meson decay, and $\Delta \phi_{\mu\mu} > 0.25$ rad to reject muons originating from the same jet. The transverse momenta of the leading and next-to-leading muons have to be $15 < p_{T1} < 200$ GeV.
and $p_T > 10 \text{ GeV}$, respectively. The invariant mass of the muon pair must be in the range $M_{\mu\mu} < 250 \text{ GeV}$.

The upper limits on the muon $p_T$ and dimuon invariant mass reduce the number of events with one of the muon charges mis-reconstructed. In addition, we reject events with $E_T < 25 \text{ GeV}$, since multijet background dominates at low $E_T$.

To discriminate between isolated muons from signal and muons contained in jets, we define the isolation in the calorimeter, $I^{\text{cal}}$, as the sum of the energy deposited in the calorimeter within an annulus of $0.1 < R < 0.4$, divided by the muon $p_T$, and the isolation in the tracking detector, $I^{\text{trk}}$, as the sum of the $p_T$ of all charged particles within a cone of $R = 0.5$ around the muon, excluding the muon itself, divided by $p_T^\mu$. At least one of the two muons is required to be isolated with $I^{\text{cal}} < 0.4$ and $I^{\text{trk}} < 0.12$.

We estimate the multijet background by defining a signal and a background enriched sample. The signal enriched sample comprises events where the requirement on the isolation of the second muon in the tracking detector is relaxed to $I^{\text{trk}} < 0.25$. To define a background enriched sample, we require that the second muon fails the isolation requirement. A normalization factor is calculated for each jet multiplicity, given by the ratio of the number of events in the signal and background enriched samples in a multijet dominated region where the $p_T$ of the most isolated muon is $5 < p_T < 10 \text{ GeV}$. The multijet background is determined by multiplying the background enriched sample with this normalisation factor in the region where the $p_T$ of the most isolated muon is $> 10 \text{ GeV}$.

In the high $p_T$ region, there is a significant contribution to the background enriched sample from SM processes other than multijet, particularly from $W$+jets production, with an isolated muon from the $W$ boson decay and a non-isolated muon embedded in the jet. This SM background is modeled by applying the selection used to define the background enriched sample to MC events. The resulting SM background distributions, corrected with the same normalization factors as used for data, are subtracted from the corrected distribution of the background enriched data sample to obtain an estimate of the multijet background.

Events from $Z \rightarrow \mu\mu$ decays enter our sample mainly through mis-reconstruction of one of the muon charges. This background is estimated from simulation. We use data to determine the corresponding systematic uncertainty by comparing the two independent charge measurements in the central tracking detector and the muon detector. We determine the rate of muons with an incorrectly measured charge by counting the number of events where the two measurements disagree. The number of charge-flip events in data is in good agreement with the number of like-charged $Z \rightarrow \mu\mu$ events predicted by the simulation.

To improve the discrimination between signal and background a boosted decision tree (BDT) [20] is trained using $p_{T1}$, $p_{T2}$, $M_{\mu\mu}$, $\Delta \phi_{\mu\mu}$, and the number of jets as input variables. Further input variables are the $\chi^2$ of the fit of the muon tracks to reject badly reconstructed muons, the transverse masses $M_T = \sqrt{2E_Tp_T(1-\cos \Delta \phi(\vec{E}_T, \mu))}$ calculated separately for each muon, and the scalar product of $E_T$ and $p_{T2}$. This rejects multijet background events with small $E_T$ or $p_{T2}$.

The distributions of $E_T$ and $p_{T1}$ for data and background are shown Fig. 2 together with signal for $R^{-1} = 260 \text{ GeV}$. The BDT is trained separately for each signal point with different $R^{-1}$. The BDT output distribution is shown in Fig. 3 and the event yields in data are compared to the expected number of background and signal events in Table II. Signal is concentrated in the region where the BDT output is $> 0$.

Systematic uncertainties on the normalisation of both background and signal, including their correlations, are taken into account. These include theoretical uncertainties on SM background cross sections (7% $-$ 15%), the uncertainties on the rate of multijet background (40%), signal efficiency from choice of PDF parametrisation (4%), integrated luminosity (6.1%), jet energy scale (4%), rate of $Z/\gamma^*$ production with an incorrectly reconstructed muon charge (21%), trigger efficiency (6%) and

![FIG. 2: Distribution of (a) $E_T$ and (b) $p_{T1}$ for data and background, compared to a signal with $R^{-1} = 260 \text{ GeV}$. The shaded band shows the statistical uncertainty on the background estimation. All entries exceeding the range of the histogram are added to the last bin.](image-url)
TABLE II: Expected number of events for backgrounds, event yields in data and expected number of events for a signal with $R^{-1} = 260$ GeV after the final selection and requiring a BDT output > 0 (for illustrative purpose, this cut is not used for limit estimation). The total uncertainties are also given.

<table>
<thead>
<tr>
<th>Process</th>
<th>Final Selection</th>
<th>BDT output &gt; 0</th>
</tr>
</thead>
<tbody>
<tr>
<td>Diboson</td>
<td>21 ± 3</td>
<td>6 ± 1</td>
</tr>
<tr>
<td>Z+jets</td>
<td>39 ± 9</td>
<td>13 ± 3</td>
</tr>
<tr>
<td>W+jets</td>
<td>109 ± 14</td>
<td>38 ± 5</td>
</tr>
<tr>
<td>$tt$</td>
<td>6 ± 1</td>
<td>2 ± 1</td>
</tr>
<tr>
<td>Multijet</td>
<td>95 ± 41</td>
<td>63 ± 27</td>
</tr>
<tr>
<td>Total Background</td>
<td>271 ± 45</td>
<td>123 ± 28</td>
</tr>
<tr>
<td>Data</td>
<td>273</td>
<td>126</td>
</tr>
<tr>
<td>Signal</td>
<td>18 ± 1</td>
<td>18 ± 1</td>
</tr>
</tbody>
</table>

FIG. 3: Distribution of the BDT output for data and background, compared to a signal with $R^{-1} = 260$ GeV. The shaded band shows the statistical uncertainty on the background estimation.

FIG. 4: Observed and median expected 95% CL limits on $\sigma B(\mu^+ \mu^-)$ as a function of $R^{-1}$ compared to $\sigma B(\mu^+ \mu^-)$ calculated with the mUED model. The bands represent ±1 and ±2 standard deviations around the median expected limits.

muon reconstruction and isolation (2%).

The entire differential distribution of the BDT output is used to set limits on the product of the cross section and the branching ratio with the CLs method and a profiling technique to reduce the impact of systematic uncertainties. Observed and median expected upper limits at 95% CL on the product of the cross section $\sigma$ and the branching fraction $B$ into like-charged muon pairs are shown in Fig. 4 as a function of $R^{-1}$. The theoretical cross section of the mUED model intersects the expected limit at $R^{-1} = 275$ GeV and the observed at $R^{-1} = 260$ GeV, which corresponds to a mass of 317 GeV of the lightest KK quark in the mUED model.

In summary, we present a search for extra dimensions in the mUED model using 7.3 fb$^{-1}$ of integrated luminosity collected by the D0 experiment. The first direct lower limit on the compactification scale of the extra dimension in the mUED model is set as $R^{-1} = 260$ GeV.

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[9] The D0 detector coordinate system is right-handed with the $z$ axis pointing in the proton beam direction. The $y$ axis points upward and the azimuthal angle $\phi$ is measured from the $x$ axis. Pseudorapidity is defined as $\eta = -\ln[\tan(\theta/2)]$, where $\theta$ is the polar angle.
[11] Missing transverse energy is defined as $E_T = \sum_i (E_{T,x}^i, E_{T,y}^i)$, where $E_{T,x}^i = E_i^\parallel \sin \theta^i \cos \phi^i$, $E_{T,y}^i = E_i^\parallel \sin \theta^i \sin \phi^i$. Here $E_i^\parallel$ is the energy deposited in $i^{th}$ calorimeter cell and the angles $\theta^i$ and $\phi^i$ define the direction of $i^{th}$ calorimeter cell. We also define $E_T^\parallel = |E_T|$. 


