Search for flavor changing neutral currents in decays of top quarks

Flavor changing neutral currents (FCNC) allow for transitions between quarks of different flavor but same electric charge. FCNC are sensitive indicators of physics beyond the standard model (BSM), because they are suppressed in the standard model (SM).

In this paper, we search for FCNC decays of the top (t) quark. Within the SM the top quark decays into a W boson and a b quark with a rate proportional to the Cabibbo-Kobayashi-Maskawa (CKM) matrix element squared, $|V_{tb}|^2$. Under the assumption of three fermion families and a unitary $3 \times 3$ CKM matrix, the $|V_{tb}|$ element is severely constrained to $|V_{tb}| = 0.999152^{+0.000030}_{-0.000045}$. While the SM branching fraction for $t \to Zq$ ($q = u, c$ quarks) is predicted to be $\approx 10^{-14}$, supersymmetric extensions of the SM with or without $R$-parity violation, or quark compositeness predict branching fractions as high as $\approx 10^{-4}$. The observation of the FCNC decay $t \to Zq$ would therefore provide evidence of contributions from BSM physics.

We analyze top-pair production ($t\bar{t}$), where either one or both of the top quarks decay via $t \to Zq$ or their charge conjugates (hereafter implied). Any top quark that does not decay via $t \to Zq$ is assumed to decay via $t \to Wb$. We assume that the $t \to Zq$ decay is generated by an anomalous FCNC term added to the SM Lagrangian

$$\mathcal{L}_{\text{FCNC}} = \frac{e}{2 \sin \theta_W \cos \theta_W} \bar{t} \gamma_\mu (v_{tqZ} - a_{tqZ} \gamma_5) q Z^\mu + h.c.,$$

where $q, t$, and $Z$ are the quantum fields for up or charm quarks, top quarks, and for the $Z$ boson, respectively, $e$ is the electric charge, and $\theta_W$ the Weinberg angle. We thereby introduce dimension-5 vector, $v_{tqZ}$, and axial vector, $a_{tqZ}$, couplings as defined in [6]. We find in [7, 8].

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We present a search for flavor changing neutral currents in decays of top quarks. The analysis is based on a search for $t\bar{t} \to \ell^+\ell^-+\text{jets}$ ($\ell, \ell' = e, \mu$) final states using 4.1 fb$^{-1}$ of integrated luminosity at $\sqrt{s} = 1.96$ TeV. We extract limits on the branching ratio $B(t \to Zq)$ ($q = u, c$ quarks), assuming anomalous $tuZ$ or $tcZ$ couplings. We do not observe any sign of such anomalous coupling and set a limit of $B < 3.2\%$ at 95% C.L.

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that the next-to-leading order (NLO) effects due to perturbative QCD corrections are negligible when extracting the branching ratio limits to the leading order (LO) in Eq. 1.

We investigate channels where the $W$ and $Z$ bosons decay leptonically, as shown in Fig. 1. The $u$, $c$, and $b$ quarks subsequently hadronize, giving rise to a final state with three charged leptons ($\ell = e, \mu$), an imbalance in momentum transverse to the $p\bar{p}$ collision axis ($E_T$, assumed to be from the escaping neutrino in the $W \rightarrow \ell\nu$ decay), and jets.

This is the first search for FCNC in $t\bar{t}$ decays with trilepton final states. This mode provides a distinct signature with low background, albeit at the cost of statistical power. The first measurement ($b \rightarrow s\ell$) was published in 1995 by the CLEO Collaboration 6. Numerous studies have been done since then to search for FCNC processes in meson decays, i.e., $b \rightarrow Zs$ in $B^+ \rightarrow K^{+}\ell^+\ell^-\bar{\ell}^-10,12$, $B \rightarrow K^*\nu\bar{\nu}13$, and $B_s,d \rightarrow \ell^+\ell^-$ or $s \rightarrow Zd$ in $K^+ \rightarrow \pi^+\nu\bar{\nu}10$. Using the $D^+ \rightarrow \pi^+\ell^+\ell^-\bar{\ell}^-$ final state in 1.3 fb$^{-1}$ of integrated luminosity, the D0 Collaboration has set the best branching ratio (B) limits on the FCNC $c \rightarrow Zu$ process at $B(D^+ \rightarrow \pi^+\ell^+\ell^-\bar{\ell}^-) = 3.9 \times 10^{-6}$ at 90% C.L. 17. There are theoretical arguments as to why top quark decays may be the best way to study flavor violating couplings of mass-dependent interactions 18,19. FCNC $tqZ$ and $tq\gamma$ couplings have been studied by the CERN $e^+e^-$ Collider (LEP), DESY ep Collider (HERA)20, and Fermilab $p\bar{p}$ Collider (Tevatron) experiments 21,22. The D0 Collaboration has recently published limits on the branching ratios determined from FCNC gluon-quark couplings using single top quark final states 23. The 95% C.L. upper limit on the branching ratio of $t \rightarrow Zq$ from the CDF Collaboration uses 1.9 fb$^{-1}$ of integrated luminosity, assumes a top quark mass of $m_t = 175$ GeV and uses the measured cross section of $\sigma_{t\bar{t}} = 8.8 \pm 1.1$ pb 24. This result excludes branching ratios of $B(t \rightarrow Zq) > 3.7\%$, with an expected limit of $5.0\% \pm 2.2\%$. To obtain these results, CDF exploited the two lepton plus four jet final state. This signature occurs when one of the pair-produced top quarks decays via FCNC to $Zq$, followed by the decay $Z \rightarrow ee$ or $Z \rightarrow \mu\mu$. The other top quark decays to $Wb$, followed by the hadronic decay of the $W$ boson. This dilepton signature suffers from large background, but profits from more events relative to the trilepton final states investigated in this Letter.

This analysis is based on the measurement of the $WZ$ production cross section in $\ell\nu\ell\ell$ final states 20 using 4.1 fb$^{-1}$ of integrated luminosity of $p\bar{p}$ collisions at $\sqrt{s} = 1.96$ TeV. We extend the selection by analyzing events with any number of jets in the final state and investigate observables that are sensitive to the signal topology in order to select events with $WZ \rightarrow \ell\nu\ell\ell$ decays that originate from the pair production of top quarks.

A detailed description of the D0 detector can be found elsewhere 27. Here, we give a brief overview of the main sub-systems of the detector. The innermost part is a central tracking system surrounded by a 1.9 T superconducting solenoidal magnet. The two components of the central tracking system, a silicon microstrip tracker and a central fiber tracker, are used to reconstruct $p\bar{p}$ interaction vertices and provide the measurement of the momentum of charged particles within the pseudorapidity range of $|\eta| < 2$ (with $\eta$ defined relative to the center of the detector). The tracking system and magnet are followed by the calorimetry that consists of central (CC) and end (EC) electromagnetic and hadronic uranium-liquid argon sampling calorimeters, and an intercryostat detector (ICD). The CC and two EC calorimeters cover $|\eta| < 1.1$ and $1.5 < |\eta| < 4.2$, respectively, while the ICD covers $1.1 < |\eta| < 1.4$. The calorimeter measures energies of hadrons, electrons, and photons. The muon system consists of a layer of drift tubes and scintillation counters inside a 1.8 T toroidal magnet. Two similar layers are outside of the toroidal magnet and the entire system covers $|\eta| < 2$.

An electron is identified from the properties of clusters of energy deposited in the CC, EC, or ICD that match a track reconstructed in the central tracker. Because of the lack of far forward coverage of the tracker, we define EC electrons only within $1.5 < |\eta| < 2.5$. The calorimeter clusters in the CC and EC are required to pass the isolation cut

$$E_{\text{tot}}(\Delta R < 0.4) / E_{\text{EM}}(\Delta R < 0.2) < 0.1$$

for “loose” electrons and $< 0.07$ for “tight” electrons, where $E_{\text{tot}}$ is the total energy in the EM and hadronic calorimeters, $E_{\text{EM}}$ is the energy found in the EM calorimeter only, and $\Delta R = \sqrt{(\Delta\phi)^2 + (\Delta\eta)^2}$, where $\phi$ is the azimuthal angle. For the intercryostat region (ICR), $1.1 < |\eta| < 1.5$, we form clusters from the energy deposits in the CC, ICD, or EC detectors. These clusters are identified as electrons if they pass a neural network requirement that is based on the characteristics of the shower and associated track information. A muon can-
candidate is reconstructed from track segments within the muon system that are matched to a track reconstructed in the central tracker. The trajectory of the muon candidate must be isolated from other tracks within a cone of $\Delta R < 0.5$, with the sum of the tracks’ transverse momenta, $p_T$, in a cone less than 4.0 GeV for “loose” muons and less than 2.5 GeV for “tight” muons. Tight muon candidates must also have less than 2.5 GeV of calorimeter energy in an annulus of $0.1 < \Delta R < 0.4$. Jets are reconstructed from the energy deposited in the CC and EC calorimeters, using the “Run II midpoint cone” algorithm [25] of size $\Delta R = 0.5$, within $|\eta| < 2.5$.

Monte Carlo (MC) samples of WZ and ZZ background events are produced using the Pythia generator [21]. The production of the W and Z bosons in association with jets ($W$+jets, $Z$+jets), collectively referred to as $V$+jets, as well as $t\bar{t}$ processes are generated using Alpgen [30] interfaced with Pythia for parton evolution and hadronization. In all samples the CTEQ6L1 parton distribution function (PDF) set is used, along with $m_t = 172.5$ GeV. The $t\bar{t}$ cross section is set to the SM value at this top quark mass, i.e., $\sigma_{t\bar{t}} = 7.46_{-0.67}^{+0.48}$ pb [51]. This uncertainty is mainly due to the scale dependence, PDFs, and the experimental uncertainty on $m_t$ [52].

All MC samples are passed through a Geant simulation of the D0 detector and overlaid with data events from random beam crossings to account for the underlying event. The samples are then corrected for the luminosity dependence of the trigger, reconstruction efficiencies in data, and the beam position. All MC samples are normalized to the luminosity in data using NLO calculations of the cross sections, and are subject to the same selection criteria as applied to data.

The signal process is generated using the Pythia generator with the decay $t \rightarrow Z q$ added. The Z boson helicity is implemented by reweighting an angular distribution of the positively charged lepton in the decay $t \rightarrow Z q \rightarrow \ell^+\ell^-q$ using CompHEP [34], modified by the addition of the Lagrangian of Eq. 1. The variable $\cos \theta^*$ used for the reweighting is defined by the angle $\theta^*$ between the Z boson’s momentum in the top quark rest frame and the momentum of the positively charged lepton in the Z boson rest frame. We assume in the analysis that the vector and axial vector couplings, as introduced in Eq. 1, are identical to the corresponding couplings for neutral currents (NC) in the SM, i.e., $v_{tuZ} = 1/2 - 4/3 \sin^2 \theta_W = 0.192$ and $a_{tuZ} = 1/2$, where $\sin^2 \theta_W = 0.231$. To study the influence of different values of the couplings, we also analyse the following cases: (i.a) $v_{tuZ} = 1, a_{tuZ} = 0$; (i.b) $v_{tuZ} = 0, a_{tuZ} = 1$; and (ii) $v_{tuZ} = a_{tuZ} = 1/\sqrt{2}$. As expected, the first two give identical results. The difference obtained by using cases (i), (ii), and using the values of the SM NC couplings is included as systematic uncertainty. Therefore, our result is independent of the actual values of $v_{tqZ}$ and $a_{tqZ}$. Since we do not distinguish $c$ and $u$ quark jets our results are valid also for $u$ and $c$ quarks separately.

The total selection efficiency, calculated as a function of $B = \Gamma(t \rightarrow Z q)/\Gamma_{tot}$, where $\Gamma_{tot}$ contains $t \rightarrow Wb$ and $t \rightarrow Zq$ decays only, can be written as

$$\epsilon_{t\bar{t}} = (1 - B)^2 \cdot \epsilon_{t\bar{t} \rightarrow W^+bW^--b}$$

$$+ 2B(1 - B) \cdot \epsilon_{t\bar{t} \rightarrow ZqW^--b} + B^2 \cdot \epsilon_{t\bar{t} \rightarrow ZqZq},$$

where the efficiency $\epsilon_{t\bar{t} \rightarrow W^+bW^--b}$ for the SM $t\bar{t}$ background contribution is used, along with the efficiencies $\epsilon_{t\bar{t} \rightarrow ZqW^--b}$ and $\epsilon_{t\bar{t} \rightarrow ZqZq}$ that include the FCNC top quark decays.

We consider four independent decay signatures: $ee\mu + E_T + X$, $e\mu\mu + E_T + X$, $\mu\mu\mu + E_T + X$, and $\mu\mu\mu + E_T + X$, where $X$ is any number of jets. We require the events to have at least three lepton candidates with $p_T > 15$ GeV that originate from the same $p\bar{p}$ interaction vertex and are separated from each other by $\Delta R > 0.5$. Jets are excluded from consideration unless they have $p_T > 20$ GeV. We also require that the jets are separated from electrons by $\Delta R > 0.5$. There is no fixed separation cut between the muon and jets but the muon isolation requirement rejects most muons within $\Delta R < 0.4$ of a jet. The event must also have $E_T > 20$ GeV, which is calculated from the energy found in the calorimeter cells and $p_T$ corrected for any muons reconstructed in the event. Furthermore, all energy corrections applied to electrons and jets are propagated through to the $E_T$.

Events are selected using triggers based on electrons and muons. There are several high-$p_T$ leptons from the decay of the heavy gauge bosons providing a total trigger efficiency for all signatures of $98\% \pm 2\%$.

To identify the leptons from the Z boson decay, we consider only pairs of electrons or muons, additionally requiring them to have opposite electric charges. If no lepton pair is found within the invariant mass intervals of $74–108$ GeV ($ee$), $65–115$ GeV ($\mu\mu$) or $60–120$ GeV ($ee\mu$, with one electron in the ICR) the event is rejected, else, the pair that has an invariant mass closest to the Z boson mass $M_Z$ is selected as the Z boson. The lepton with the highest $p_T$ of the remaining muons or CC/EC electrons in the event is selected as originating from the W boson decay. From simulation, this assignment of the three charged leptons to Z and W bosons is found to be $\approx 100\%$ correct for $ee\mu$ and $\mu\mu\mu$, and about $92\%$ and $89\%$ for the $ee\mu$ and $\mu\mu\mu$ channels, respectively.

Thresholds in the selection criteria are the same as in Ref. [26] and the acceptance multiplied by efficiency results are summarized in Table I for the FCNC signal. These values are calculated with respect to the total rate expected for all three generations of leptonic W and Z decays.

In addition to SM WZ production, the other major background is from processes with a Z boson and an additional object misidentified as the lepton from the W boson decay (e.g., from Z+jets, ZZ, and Zγ). A small background contribution is expected from processes such as W+jets and SM $t\bar{t}$ production. The WZ, ZZ, and $t\bar{t}$ backgrounds are estimated from the simulation, while the V+jets and Zγ backgrounds are estimated using data-
driven methods.

One or more jets in V+jets events can be misidentified as a lepton from W or Z boson decays. To estimate this contribution, we define a false lepton category for electrons and muons. A false electron is required to have most of its energy deposited in the electromagnetic part of the calorimeter and satisfy calorimeter isolation criteria for electrons, but have a shower shape inconsistent with that of an electron. A muon candidate is categorized as false if it fails isolation criteria, as determined from the total $p_T$ of tracks located within a cone $\Delta R = 0.5$ around the muon. These requirements ensure that the false lepton is either a misidentified jet or a lepton from the semi-leptonic decay of a heavy-flavor quark. Using a sample of data events, collected using jet triggers with no lepton requirement, we measure the ratio of misidentified leptons passing two different selection criteria, false lepton and signal lepton, as a function of $p_T$ when assigning the electromagnetic shower to the final state signature. The contribution from the V+jets background is estimated by scaling the number of events in this $Z+$false lepton sample by the corresponding $p_T$-dependent misidentification ratio.

Initial or final state radiation in $Z\gamma$ events can mimic the signal process if the photon either converts into an $e^+e^-$ pair or is wrongly matched with a central track mimicking an electron and the $E_T$ is mismeasured. As a result the $Z\gamma$ process is a background to the final state signatures with $W \rightarrow e\nu$ decays. To estimate the contribution from this background, we model the kinematics of these events using the $Z\gamma$ NLO MC simulation [33]. We scale this result by the rate at which a photon is misidentified as an electron. This rate is obtained using a data sample of $Z \rightarrow \mu\mu$ events containing a radiated photon, as it offers an almost background-free source of photons. The invariant mass $M(\mu\mu\gamma)$ is reconstructed and required to be consistent with the $Z$ boson mass. The $Z \rightarrow \mu\mu$ decay is chosen to avoid any ambiguity when assigning the electromagnetic shower to the final state photon candidate. As the $Z\gamma$ NLO MC does not model recoil jets, PYTHIA MC samples are used to estimate $Z\gamma$ background jet multiplicities and $E_T$. As the PYTHIA samples do not contain events with final state radiation, we find the fraction of $Z\gamma$ events in data and PYTHIA MC that pass our $E_T$ cut and take the difference as a systematic uncertainty.

After all selection criteria have been applied, we observe a total of 35 candidate events and expect $31.7 \pm 0.3$ (stat) $\pm 3.9$ (syst) background events from SM processes. The statistical uncertainty is due to MC statistics while the sources of systematic uncertainties are discussed later. Table I summarizes the number of events in each $n_{\text{jet}}$ bin. The observed number of candidate and background events for each topology, summing over $n_{\text{jet}}$, are summarized in Table II. In Tables I and II and all in the following figures, we assume a $B$ of 5%.

To achieve better separation between signal and background, we analyze the $n_{\text{jet}}$ and $H_T$ distributions (defined as the scalar sum of transverse momenta of all leptons, jets, and $E_T$), and the reconstructed invariant mass for the products of the decay $t \rightarrow Zq$.

The jet multiplicities in data, SM background, and in FCNC top quark decays are shown in Fig. 2. FCNC $t\bar{t}$ production leads to larger jet multiplicities and also a larger $H_T$. This is shown in Fig. 3.

To further increase our sensitivity we reconstruct the mass of the top quark that decays via FCNC to a $Z$ boson and a quark ($t \rightarrow Zq$). In events with $n_{\text{jet}} = 0$, this variable is not defined. In events with one jet, we calculate the invariant mass, $m_{l}^{\text{reco}} = M(Z, \text{jet})$, from the 4-momenta of the jet and the identified $Z$ boson, to reconstruct $m_t$. For events with two or more jets, we use the jet that gives a $m_{l}^{\text{reco}}$ closest to $m_t = 172.5$ GeV. The $m_{l}^{\text{reco}}$ distribution is shown in Fig. 3(a). In Fig. 3(b), we present a 2-dimensional distribution of $m_{l}^{\text{reco}}$ and $H_T$.

None of the observables in Figs. 2 and 3 show evidence for the presence of FCNC in the decay of $t\bar{t}$. We therefore set 95% C.L. limits on the branching ratio $B(t \rightarrow Zq)$. The limits are derived from 10 bins of the $H_T$ distributions for $n_{\text{jet}} = 0, 1$, and $\geq 2$. For the channels with $n_{\text{jet}} = 1$

<table>
<thead>
<tr>
<th>$n_{\text{jet}}$</th>
<th>Inclusive</th>
<th>0</th>
<th>1</th>
<th>$\geq 2$</th>
</tr>
</thead>
<tbody>
<tr>
<td>Channel</td>
<td>$\epsilon_{t \rightarrow ZqW-\ell}$ (%)</td>
<td>0.5</td>
<td>0.5</td>
<td>0.5</td>
</tr>
<tr>
<td>$\ell\ell\ell$</td>
<td>$1.65 \pm 0.24$</td>
<td>$7.65 \pm 1.45 \cdot 10^{-2}$</td>
<td>$0.57 \pm 0.09$</td>
<td>$1.00 \pm 0.15$</td>
</tr>
<tr>
<td>$\ell\ell\mu$</td>
<td>$1.92 \pm 0.18$</td>
<td>$6.77 \pm 1.60 \cdot 10^{-2}$</td>
<td>$0.58 \pm 0.06$</td>
<td>$1.17 \pm 0.11$</td>
</tr>
<tr>
<td>$\mu\mu\ell$</td>
<td>$1.23 \pm 0.13$</td>
<td>$3.37 \pm 0.73 \cdot 10^{-2}$</td>
<td>$0.34 \pm 0.04$</td>
<td>$0.84 \pm 0.10$</td>
</tr>
<tr>
<td>$\mu\mu\mu$</td>
<td>$1.48 \pm 0.19$</td>
<td>$3.05 \pm 0.74 \cdot 10^{-2}$</td>
<td>$0.38 \pm 0.06$</td>
<td>$0.66 \pm 0.15$</td>
</tr>
</tbody>
</table>
and \( n_{\text{jet}} \geq 2 \), we split each \( H_T \) distribution into 4 bins in \( m_{t}\text{rec} \), \( m_{t}\text{rec} < 120 \text{ GeV} \), \( 120 < m_{t}\text{rec} < 150 \text{ GeV} \), \( 150 < m_{t}\text{rec} < 200 \text{ GeV} \), and \( m_{t}\text{rec} > 200 \text{ GeV} \).

When calculating the limit on the branching ratio we consider several sources of systematic uncertainty. The systematic uncertainties for lepton-identification efficiencies are 15\% (\( ee \)), 11\% (\( e\mu \)), 9\% (\( \mu\mu \)), and 12\% (\( \mu\mu \)). The systematic uncertainty assigned to the choice of PDF is 5\%. In addition, we assign 9\% systematic uncertainty on \( \sigma_{t\bar{t}} \) [31]. This includes the dependence on the uncertainty of \( m_t \) [32]. Furthermore, \( m_t \) is changed from 172.5 GeV to 175 GeV in \( t\bar{t} \) MC samples with the difference in the result taken as a systematic uncertainty. We vary the \( v_{tqZ} \) and \( a_{tqZ} \) couplings as explained before Eq. 4 resulting in a 1\% systematic uncertainty on the acceptance. Due to the uncertainty on the theoretical cross sections for \( WZ \) and \( ZZ \) production, we assign a 10\% [37] systematic uncertainty to each. The major sources of systematic uncertainty on the estimated \( V+ \text{jets} \) contribution arise from the \( E_T \) requirement and the statistics in the multijet sample used to measure the lepton-misidentification rates. These effects are estimated independently for each signature and found to be between 20\% and 30\%. The systematic uncertainty on the \( Z\gamma \) background is estimated to be 40\% and 58\% for the \( ee \) and \( \mu\mu \) channels, respectively. Uncertainties on jet energy scale, jet energy resolution, jet reconstruction, and identification efficiency are estimated by varying parameters within their experimental uncertainties. For \( n_{\text{jet}} = 0 \) the uncertainty is found to be 1\%, for \( n_{\text{jet}} = 1 \) it is 5\%, and for \( n_{\text{jet}} \geq 2 \) it is 20\%. The measured integrated luminosity has an uncertainty of 6.1\% [37].

We use a modified frequentist approach [38] where the signal confidence level \( CL_s \), defined as the ratio of the confidence level for the signal+background hypothesis to the background-only hypothesis \( (CL_s = CL_{s+b}/CL_b) \), is calculated by integrating the distributions of a test statistic over the outcomes of pseudo-experiments generated according to Poisson statistics for the signal+background and background-only hypotheses. The test statistic is calculated as a joint log-likelihood ratio (LLR) obtained by summing LLR values over the bins of the \( H_T \) distributions. Systematic uncertainties are incorporated via

<table>
<thead>
<tr>
<th>( n_{\text{jet}} )</th>
<th>0</th>
<th>1</th>
<th>( \geq 2 )</th>
</tr>
</thead>
<tbody>
<tr>
<td>Background</td>
<td>25.66 ± 0.28 ± 3.26</td>
<td>5.06 ± 0.14 ± 0.56</td>
<td>0.92 ± 0.08 ± 0.09</td>
</tr>
<tr>
<td>( t\bar{t} \to WhZq )</td>
<td>0.20 ± 0.03</td>
<td>1.80 ± 0.27</td>
<td>3.87 ± 0.56</td>
</tr>
<tr>
<td>( t\bar{t} \to ZqZq )</td>
<td>0.002 ± 0.001</td>
<td>0.020 ± 0.003</td>
<td>0.050 ± 0.007</td>
</tr>
<tr>
<td>Observed</td>
<td>30</td>
<td>4</td>
<td>1</td>
</tr>
</tbody>
</table>

Table II: Number of observed events, expected number of \( t\bar{t} \) FCNC events, and the expected distribution for each \( n_{\text{jet}} \) bin with statistical and systematic uncertainties. The MC statistical uncertainty on the \( t\bar{t} \) signal is negligible, and we only present the systematic uncertainties. We assume \( B = 5\% \).

<table>
<thead>
<tr>
<th>Source</th>
<th>( eee )</th>
<th>( e\mu\mu )</th>
<th>( \mu\mu\mu )</th>
</tr>
</thead>
<tbody>
<tr>
<td>( WZ )</td>
<td>6.64 ± 0.07 ± 1.19</td>
<td>7.51 ± 0.08 ± 1.11</td>
<td>4.75 ± 0.06 ± 0.69</td>
</tr>
<tr>
<td>( ZZ )</td>
<td>0.33 ± 0.03 ± 0.06</td>
<td>1.76 ± 0.07 ± 0.17</td>
<td>0.46 ± 0.04 ± 0.07</td>
</tr>
<tr>
<td>( V+ \text{jets} )</td>
<td>0.60 ± 0.13 ± 0.11</td>
<td>0.40 ± 0.18 ± 0.17</td>
<td>0.48 ± 0.10 ± 0.01</td>
</tr>
<tr>
<td>( Z\gamma )</td>
<td>0.18 ± 0.05 ± 0.08</td>
<td>&lt; 0.001</td>
<td>0.66 ± 0.07 ± 0.38</td>
</tr>
<tr>
<td>( t\bar{t} \to WbWb )</td>
<td>0.04 ± 0.01 ± 0.01</td>
<td>0.04 ± 0.01 ± 0.01</td>
<td>0.05 ± 0.01 ± 0.01</td>
</tr>
<tr>
<td>Background</td>
<td>7.89 ± 0.16 ± 1.20</td>
<td>9.71 ± 0.21 ± 1.14</td>
<td>6.40 ± 0.14 ± 0.79</td>
</tr>
<tr>
<td>( t\bar{t} \to WbZq )</td>
<td>1.57 ± 0.22</td>
<td>1.73 ± 0.17</td>
<td>1.17 ± 0.13</td>
</tr>
<tr>
<td>( t\bar{t} \to ZqZq )</td>
<td>0.010 ± 0.001</td>
<td>0.029 ± 0.003</td>
<td>0.011 ± 0.001</td>
</tr>
</tbody>
</table>

Table III: Number of observed events, expected number of \( t\bar{t} \) FCNC events, and the expected distribution for each final state signature with statistical and systematic uncertainties. The MC statistical uncertainty on the \( t\bar{t} \) signal is negligible, and we only present the systematic uncertainties. We assume \( B = 5\% \).
Figure 3: \( H_T \) distribution of data, FCNC \( t\bar{t} \) signal, and expected background for events with (a) \( n_{jet} = 0 \), (b) \( n_{jet} = 1 \), and (c) \( n_{jet} \geq 2 \).

Gaussian smearing of Poisson probabilities for signal and backgrounds in the pseudo-experiments. All correlations between signal and backgrounds are maintained. To reduce the impact of systematic uncertainties on the sensitivity of the analysis, the individual signal and background contributions are fitted to the data, by allowing a variation of the background (or signal+background) prediction, within its systematic uncertainties [39]. The likelihood is constructed via a joint Poisson probability over the number of bins in the calculation, and is a function of scaling factors for the systematic uncertainties, which are given as Gaussian constraints associated with their priors.

We determine an observed limit of \( B(t \to Zq) < 3.2\% \), with an expected limit of \( < 3.8\% \) at the 95\% C.L. The limits on the branching ratio are converted to limits at the 95\% C.L. on the FCNC vector, \( v_{tqZ} \), and axial vector, \( a_{tqZ} \), couplings as defined in Eq. 1 using the relation given in [49]. This can be done for any point in the \((v_{tqZ}, a_{tqZ})\) parameter space and for different quark flavors \((u, c)\) since the differences in the helicity structure of the couplings are covered as systematic uncertainties in the limit on the branching ratio. Assuming only one non-vanishing \( v_{tqZ} \) coupling \((a_{tqZ} = 0)\), we derive an observed (expected) limit of \( v_{tqZ} < 0.19 \) \((< 0.21)\) for \( m_t = 172.5 \) GeV. Likewise, this limit holds assuming only one non-vanishing \( a_{tqZ} \) coupling. Figure 4 shows current limits from experiments at the LEP, HERA, and Tevatron colliders as a function of the FCNC couplings \( \kappa_{tuy} \) (defined in Ref. [49]) and \( v_{tqZ} \) for \( m_t = 175 \) GeV.

In summary, we have presented a search for top quark decays via FCNC in \( t\bar{t} \) events leading to final states involving three leptons, an imbalance in transverse momentum, and jets. These final states have been explored for
The first time in the context of FCNC couplings. In the absence of signal, we expect a limit of $B(t \to Zq) < 3.8\%$ and set a limit of $B(t \to Zq) < 3.2\%$ at the 95% C.L. which is currently the world’s best limit. This translates into an observed limit on the FCNC coupling of $v_{tqZ} < 0.19$ for $m_t = 172.5$ GeV.

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