The following full text is a publisher's version.

For additional information about this publication click this link.
http://hdl.handle.net/2066/91788

Please be advised that this information was generated on 2019-09-01 and may be subject to change.
Evolutionary optimization of rotational population transfer

Arnaud Rouzée,1,4,* Omair Ghafur,1 Konstantin Vidma,2 Arjan Gijsbertsen,1 Ofer Shir,3 Thomas Bäck,3 Afric Meijer,2 Win J. van der Zande,2 David Parker,2 and Marc J. J. Vrakking1,4

1FOM Institute for Atomic and Molecular Physics (AMOLF), Science Park 104, NL-1098 XG Amsterdam, The Netherlands
2Institute of Molecules and Materials, Radboud University Nijmegen, Toernooiveld 1, NL-6500 GL Nijmegen, The Netherlands
3Leiden Institute of Advanced Computer Science (LIACS), Niels Bohrweg 1, NL-2333 CA Leiden, The Netherlands
4Max Born Institut, Max Born Strasse 2A, D-12489, Berlin, Germany

(Received 15 October 2009; revised manuscript received 11 April 2011; published 16 September 2011)

We present experimental and numerical studies on control of rotational population transfer of NO($J = 1/2$) molecules to higher rotational states. We are able to transfer 57% of the population to the $J = 5/2$ state and 46% to $J = 9/2$, in good agreement with quantum mechanical simulations. The optimal pulse shapes are composed of pulse sequences with delays corresponding to the beat frequencies of states on the rotational ladder. The evolutionary algorithm is limited by experimental constraints such as volume averaging and the finite laser intensity used, the latter to circumvent ionization. Without these constraints, near-perfect control ($>98\%$) is possible. In addition, we show that downward control, moving molecules from high to low rotational states, is also possible.

DOI: 10.1103/PhysRevA.84.033415 PACS number(s): 33.80.—b, 33.20.Sn, 42.50.—p

I. INTRODUCTION

The emergence of the idea that coherent light-matter interactions allow one to exert control over the dynamics of atomic and molecular systems has changed the nature of research into these systems from passive observation to active control. One important challenge concerns the manipulation of ground-electronic-state vibrational and rotational populations since most reactions take place on the lowest energy surface. Several schemes have been proposed and tested experimentally to control the initial quantum state preparation of molecular samples. Resonant photoabsorption, two-color Raman excitation, and stimulated emission pumping are common techniques to state selectively prepare atoms or molecules prior to their use in a collision experiment. A further interesting preparation scheme is stimulated rapid adiabatic passage (STIRAP) [1], where two narrowband nanosecond lasers are used to accomplish complete population transfer from an initial state to a selected target state. STIRAP has been used to generate vibrationally pure samples [2] and can be viewed as the first example of the use of coherent control as a means to achieve quantum state preparation in a controlled manner.

Rapid progress in the development of femtosecond lasers and pulse shaping technology has helped considerably in putting ideas for controlling laser-molecule interactions into practice. Using ideas that derive from the seminal paper by Rabitz on “teaching lasers to control molecules” [3], many examples currently exist where shaped laser pulses have been optimized by a genetic or evolutionary algorithm in order to accomplish a desired task or to optimize a desired end result (see, e.g., [4–8]). The remarkable success of these experiments can be understood from the fact that feedback-controlled optimization drives quantum systems to perfect control, provided that no constraints are placed on the controls [9]. However, one should realize that in any experimental realization, a substantial number of constraints exist, such as the bandwidth of the laser, the algorithm used to control the feedback loop, and the parametrization or fidelity of the amplitude, phase, and polarization shaping applied to the laser pulse or, as we encounter in this paper, the intensity limit imposed by the ionization potential of a molecule. So far, optimal control experiments can be divided into two categories. On the one hand, there are experiments in idealized two- and three-level systems, where perfect control can be exerted that can be understood in terms of analytical solutions of the time-dependent Schrödinger equation [9]. On the other hand, there are experiments in more complex, many-level systems, where some degree of optimization is achieved, but where a mechanistic interpretation of the exerted control and an assessment of the degree of optimization are very challenging.

In this paper we present studies on rotational ladder climbing in the NO molecule (starting from a single initial rotational state) under the influence of moderately intense femtosecond laser pulses subjected to phase-shaping. We note that a rotational ladder as used here has no upper bound. Therefore, the possibility to populate only one of its rungs is certainly not obvious. Nevertheless, we show that a high degree of selectivity in the transfer of a population to a desired final state can be achieved. The degree of population transfer can be well understood if the experimental constraints are accounted for. Moreover, we show that starting from a single high rotational state, a very high degree of population transfer can be achieved toward a selected lower rotational state. This result is particularly important in the context of research on cold molecules, where a laser control scheme such as the one suggested in this study can be used to guide the molecule toward low-$J$ states.

II. EXPERIMENTAL PROCEDURE

The experimental setup used in these experiments has been described before [10,11]. Briefly, a state-selected molecular beam containing NO molecules in the low-field-seeking state of the $J = 1/2$ $\Lambda$ doublet was generated using a hexapole

*a.rouzee@amolf.nl*
state selector (see Fig. 1). The NO molecules were excited by a shaped femtosecond laser pulse that was created by passing approximately 5-mJ, 90-fs laser pulses through a computer-controlled 640-pixel spatial light modulator (SLM) placed at the center of a 4$f$ zero-dispersion line. The shaped laser pulse was focused onto the NO beam with a 400-mm lens, leading to rotational excitation via successive stimulated Raman transitions. Populations in each rotational state of NO were probed 200 ns after the femtosecond laser interaction using $(1 + 1)$ resonance-enhanced multiphoton ionization (REMPI) through the $A^2\Sigma^+\leftarrow X^2\Pi$ excited state of the NO molecule [12]. To this end, a 20-$\mu$J, near-226-nm probe laser pulse from a frequency-doubled tunable dye laser operated at 12.5 Hz was used. The probe laser beam, polarized along the pump laser polarization, was focused with a 200-mm lens, ensuring a beam waist smaller than that of the pump laser. After acceleration with a DC field, the NO$^+$ ions resulting from ionization with the near-226-nm pulse were detected by a set of microchannel plates and then integrated using a boxcar integrator. The ion signal was then recorded at different probe wavelengths around 226 nm by tuning the dye laser. Optimization of the population in states $J = 5/2$ and $J = 9/2$ was carried out by maximizing the ion signal at a fixed wavelength of the dye laser corresponding to the spectral line $R_{21}(J = 5/2)$ and $R_{21}(J = 9/2)$, respectively [see Fig. 2(b)]. The algorithm used in the optimizations was the $(\mu, \lambda)$ covariance matrix adaptation evolution strategy (CMA-ES) (see, e.g., [13]). Briefly, a randomly sampled initial population of $\lambda$ candidate spectral phase functions $\phi(\omega)$ underwent experimental evaluation. The best $\mu$ phases were selected and recombined to produce new offspring. Before using these offspring, Gaussian variations, relying on auxiliary strategy parameters [14] that were self-adaptively updated, were applied. This was repeated until convergence was reached. In the reported experiments a $(\mu = 8, \lambda = 16)$ strategy was deployed. To improve the convergence time, only the 250 pixels of the SLM where the majority of the pulse bandwidth was contained were varied by the algorithm.

### III. RESULTS AND DISCUSSION

Figure 2(a) shows a recorded REMPI spectrum following the excitation of state-selected NO($J = 1/2$) molecules with a Fourier transform-limited (FTL) laser pulse that was focused to an intensity of $4 \times 10^{13}$ W/cm$^2$. When no femtosecond laser pulse is applied to the molecules (not shown here), the recorded spectrum exhibits three lines, corresponding to the $Q_{11}$, $Q_{21} + R_{11}$, and $R_{21}$ spectroscopic branches. As the ions are extracted in a DC electric field, the initial-state $J = 1/2$, $\epsilon = -1$ population is partly mixed with the opposite parity state (20%), which was taken into account in the analysis. With the laser excitation, new spectral lines appear due to the rotational population redistribution by the pump laser field. This population redistribution occurs via $\Delta J = 1$ and $\Delta J = 2$ transitions [11]. In order to extract the final NO($J$) populations from this measurement, each observed spectral line was integrated over a range of 0.01 cm$^{-1}$ and divided...
by the corresponding Hön-London coefficient [15], which was corrected for laser-induced alignment [16] (note that \( m \) is conserved along the pump laser polarization). The normalized discrepancies attributed to the fluctuation of the NO (red) columns]. A good overall agreement is found, with small number of rotational states, none of which accumulates more was corrected for laser-induced alignment [16] (note that between time delay corresponds approximately to the beating period and consists of two peaks that are separated by 400 fs. These pulse at

As reported by Meijer et al. [17], a 2.6-ps timing is not optimal since it also depletes the state \( J = 5/2 \) due to further excitation to the \( J = 9/2 \) state. To avoid the population transfer toward higher \( J \) states, the algorithm splits the first pulse in the train into two peaks, allowing maximization of the population in state \( J = 5/2 \) while minimizing the population in the \( J = 9/2 \) state. The optimum laser pulse shape for NO(\( J = 9/2 \)) is different. As before, three pulses separated by 2.4 ps can be recognized, with an additional pulse appearing about 1.3 ps after the second, most intense pulse, that approximates the beating period between \( J = 5/2 \) and \( J = 9/2 \) (\( \tau = 1.26 \) ps).

To test whether the observed population transfer to NO(\( J = 5/2 \)) and NO(\( J = 9/2 \)) can be viewed as a satisfactory experimental outcome, optimal control calculations were performed by solving the time-dependent Schrödinger equation [11]. As in the experiment, optimizations were performed guided by the CMA-ES [13]. To reflect the pulse-shaping process implemented experimentally, the energy was kept constant during the optimization procedure and the electric field was written in the frequency domain with the phase \( \phi(\omega) \) discretized into 128 parameters \( \phi_\alpha \) (pixels taken as a top-hat shape [18]). The maximum observed population transfer to NO(\( J = 5/2 \)) or NO(\( J = 9/2 \)) was evaluated over seven trials with the CMA-ES and plotted as a function of the peak intensity of the 90-fs laser pulse from which the shaped laser pulses were derived. In Fig. 4 a summary of these calculations and a comparison with calculations performed using an FTL pulse are shown. The calculations were performed over an intensity range from 0 to 14 \( \times \) \( 10^{13} \) W/cm\(^2\). We note that experimental optimizations could only be performed up to an intensity of 4 \( \times \) \( 10^{13} \) W/cm\(^2\), since higher intensities led to unacceptable amounts of multiphoton ionization by the IR laser [19], which is not included in our numerical model. As Fig. 4 clearly shows, FTL pulses are not optimal for achieving selective population transfer, as the highest
population transfer to NO\((J = 5/2)\) is only 33.8\% (at a peak intensity of \(2.6 \times 10^{13} \text{ W/cm}^2\)), while the highest population transfer to NO\((J = 9/2)\) is only 25\% (at an intensity of \(4 \times 10^{13} \text{ W/cm}^2\)). When increasing the intensity of an FTL pulse, the population distribution is spread over a large range of rotational states resulting in a drop in transfer efficiency to a particular state. However, when increasing the intensity, the CMA-ES procedure consistently leads to a better population transfer to a target state. The highest population that we observed was 98.9\% for optimizations targeting NO\((J = 5/2)\) and 97.7\% for optimizations targeting NO\((J = 9/2)\). Figure 4 suggests that without the constraint imposed by the finite pulse energy, a 100\% yield may be possible [14], a remarkable result in an infinite ladder system. At an intensity of \(4 \times 10^{13} \text{ W/cm}^2\), which is our best estimate of the intensity reached in the experiment when the laser pulse is compressed to an FTL laser pulse, the highest yield in our optimal control simulations targeting NO\((J = 5/2)\) and NO\((J = 9/2)\) is 70.4\% and 42\%, respectively. Considering the uncertainty in the intensity as well as the intensity fluctuations, these values are quite close to those obtained experimentally. We note that the pulse shapes found experimentally and theoretically (see Fig. 5) are very similar. In the case of \(J = 5/2\), the pulse shape is dominated by three peaks separated by 2.6 ps, with a similar substructure around the first pulse at \(-2.6\) ps. This solution is, moreover, quite robust since the algorithm always found this pulse sequence over the seven runs performed. Upon increasing the intensity in our calculations, this robustness vanishes. The solutions found by the algorithm become rather complicated and are different for each run. Each run still achieves a very high degree of population transfer. Our experimental results in which a unique solution is found show that constraints not only impact the efficiency of the optimization process, but also impose limitations on the controllability of the system, influencing the number of qualitatively different solutions that can accomplish the task at hand [9].

One may ask if a high controllability is also achievable when starting from a high rotational state and attempting a downward transfer. Transferring the rotational population from a high-\(J\) state to a lower rotational state is interesting in the context of the production of cold molecular samples. The production of translationally cold NO molecules was shown by Chandler and co-workers [20]. In that experiment, a translationally cold sample of NO molecules results from inelastic collisions with argon atoms. Essentially all slow NO molecules in the experiment by Chandler et al. are in the \(J = 15/2, m_a = 1/2\) state, where \(m_a\) is the projection of \(J\) on the kinematic apse \(\hat{a}\), defined as the direction of the difference between the momentum after and that before collision. With a
linearly polarized laser pulse, \( m \) is conserved; in general, this complicates cooling using shaped intense laser pulses, but by choosing the laser polarization along the kinematic apse, the desired transition is \( (J = 15/2, m = 1/2) \rightarrow (J = 1/2, m = 1/2) \). This is just the opposite of the rotational ladder climbing discussed in the first part of this work. Also, in this case, ionization imposes a restriction on the maximum laser intensity in the optimized pulse, which complicates downward transfer from NO\( (J = 15/2) \). To demonstrate downward transfer using a shaped laser pulse, Fig. 6 shows the result of a simulation starting from molecules initially prepared in the \( J = 15/2, m = 1/2 \) state. In this simulation, we have used a penalty factor proportional to the ionization rate of NO \[19\]. As Fig. 6 shows, 73.4% of the population was transferred to the \( 1 \) state from NO starting from molecules initially prepared in the \( J = 15/2, m = 1/2 \) state. In this simulation, we have used a penalty factor proportional to the ionization rate of NO \[19\].

In conclusion, we have shown that a high degree of rotational-state selectivity can be achieved in many-level open systems using a shaped laser pulse. The degree of selectivity is limited in our experiment by the maximum intensity that can be used. Controlling the rotational-state distribution starting from a high rotational state is also feasible. This may be important in the context of cold molecule research, where the ability to actively guide the population from high rotational states to the ground rotational state of the molecule can help in the preparation of ultracold molecular samples.

**ACKNOWLEDGMENTS**

This work is part of the research program of the Stichting voor Fundamenteel Onderzoek der Materie (FOM), which is financially supported by the Nederlandse organisatie voor Wetenschappelijk Onderzoek (NWO).

---