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Electron energy spectrum of the spin-liquid state in a frustrated Hubbard model

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Non-local correlation effects in the half-filled Hubbard model on an isotropic triangular lattice are studied within a spin polarized extension of the dual fermion approach. A competition between the antiferromagnetic non-collinear and the spin liquid states is strongly enhanced by an incorporation of a k-dependent self-energy beyond the local dynamical mean-field theory. The dual fermion corrections drastically decrease the energy of a spin liquid state while leaving the non-collinear magnetic states almost non-affected. This makes the spin liquid to become a preferable state in a certain interval of interaction strength of an order of the magnitude of a bandwidth. The spectral function of the spin-liquid Mott insulator is determined by a formation of local singlets which results in the energy gap of about twice larger than that of the 120 degrees antiferromagnetic Neel state.

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I. INTRODUCTION

In some special cases, quantum fluctuations can destroy an ordered state even at zero temperature. The study of such “quantum phase transitions” due to zero-point fluctuations is a hot subject in modern condensed matter physics. These fluctuations are especially important in frustrated systems. A prototype of classical frustrated spin system is the Ising model on a triangular lattice with nearest-neighbor antiferromagnetic interaction. The ground state of this model has a macroscopically large degeneracy and the addition of quantum spin-flip terms results into a formation of spin-liquid state known as “resonating valence bonds” (RVB). There are strong experimental evidences that the RVB is the ground state of some Mott insulators: organic salt $\kappa$-(ET)$_2$Cu$_2$(CN)$_3$ and spinel oxide on the frustrated hyperkagome lattice Na$_3$Ir$_3$O$_8$.

Theoretical description of the materials with the RVB Mott insulating state requires an accurate choice of parameters of the model. The Hubbard model on a triangular lattice with nearest-neighbor hopping is the simplest choice, though its validity can be questioned. First, recent ab-initio calculations suggest that the family of Mott insulators: organic salt $\kappa$-(ET)$_2$Cu$_2$(CN)$_3$ and spinel oxide on the frustrated hyperkagome lattice Na$_3$Ir$_3$O$_8$.

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state in comparison with the DMFT results. For the 120° Neel State the corrections are much smaller so that the spin liquid state has a lower total energy than the Neel-ordered phase in a certain range of parameters. We calculate the electron energy spectrum by means of the DF scheme utilizing the continuous time quantum Monte Carlo solver at low temperatures.

II. METHOD

In the spirit of a mean-field theory the whole lattice problem is mapped to the single impurity, in this case to a single-impurity Anderson model subject to a self-consistent condition. Such a dynamical mean-field theory (DMFT) restricts an investigation to studying only local correlation effects. For frustrated quantum systems this approximation is obviously not applicable. In order to take into account non-local corrections two approaches are implemented: (i) the long-ranged correlations for the anti-ferromagnetic ordering are included by introducing the spin polarization to the effective bath, (ii) the short-ranged correlations are incorporated within the dual fermion technique - it is based on a transformation to new dual fermionic variables, which makes the diagrammatic expansion over non-linearity much more effective.

We start with a single-site DMFT-like problem. For a given impurity with a yet undefined dynamical hybridization function \( \Delta_{\omega \sigma} \), which describes the interaction with a fermionic bath of surrounding lattice, the effective action for single-impurity Anderson model is written in the following way:

\[
S_{\text{imp}} = \sum_{\omega \sigma} \left( \Delta_{\omega \sigma} - \mu - i \omega \right) c_{\omega \sigma}^\dagger c_{\omega \sigma} + U \int_0^\beta n_{\uparrow \sigma} n_{\downarrow \sigma} d\tau, \quad (1)
\]

where \( \omega, \sigma = \uparrow, \downarrow \) labels the spin projections, \( U \) is an on-site Coulomb interaction, \( \mu \) is a chemical potential, and \( \beta \) is an inverse temperature. The solution of this problem can be obtained numerically by the CTQMC solve. Along with the one-particle Green’s function \( g_{\omega \sigma} = -i \langle c_{\omega \sigma}^\dagger c_{\omega \sigma} \rangle \) one can obtain the higher order correlators, such as the two-particle Green’s function \( \chi_{1234}^{(4)} = \langle T c_{\sigma_1}(\tau_1) c_{\sigma_2}(\tau_2) c_{\sigma_3}^\dagger(\tau_3) c_{\sigma_4}^\dagger(\tau_4) \rangle \) and the corresponding vertex function

\[
\gamma_{1234}^{(4)} = g_{12}^{-1} g_{23}^{-1} \left[ \chi_{1'2'3'4'} - (g_{1'3'} g_{2'4'} - g_{1'4'} g_{2'3'}) \right] g_{3'1}^{-1} g_{4'2}^{-1} \quad (2)
\]

We now need to establish the connection between the single-site model and original lattice problem. The whole lattice is divided into supercells, combined of three atoms. The Fourier transforms over both the supercell and cluster spatial indices are utilized, which corresponds to the DCA-like scheme.

\[
G(\mathbf{r} = \mathbf{R}_M + \mathbf{r}_1, \mathbf{r}' = \mathbf{R}_{M'} + \mathbf{r}_j) = \sum_{\mathbf{k}, \mathbf{k}'} G_{\mathbf{k} \mathbf{k}'}(\mathbf{K}) e^{i\mathbf{K} (\mathbf{R}_M - \mathbf{R}_{M'})} e^{i(\mathbf{k} \mathbf{r}_1 - \mathbf{k}' \mathbf{r}_j)}, \quad (3)
\]

\( \mathbf{R}_M \) is a radius vector of the supercell, \( \mathbf{r}_1 \) points to a site inside it. \( \mathbf{K} \) is defined inside a Brillouin zone of a supercell, \( \mathbf{k} \) is its basis vector. In this notation, the Hamiltonian of the Hubbard model can be written as follows:

\[
\hat{H} = \sum_{\mathbf{K} \mathbf{k} \mathbf{k'}} \varepsilon_{\mathbf{k} \mathbf{k}'}(\mathbf{K}) c_{\mathbf{k} \mathbf{k'}}^\dagger(\mathbf{K}) c_{\mathbf{k} \mathbf{k'}}(\mathbf{K}) + \sum_i U \hat{n}_i^\dagger \hat{n}_i, \quad (4)
\]

where index \( i \) labels a site of the lattice. For the supercell approach the dispersion law is given by \( \varepsilon_{\mathbf{k} \mathbf{k}'}(\mathbf{K}) = \varepsilon(\mathbf{k} + \mathbf{k}') \delta_{\mathbf{k} \mathbf{k}'} \) with the spectrum of a triangular lattice:

\[
\varepsilon(\mathbf{K}) = \alpha \mathbf{k}_1 + \beta \mathbf{k}_2 = -2t \left[ \cos \frac{2\pi}{3}(\alpha + \beta) + \cos \frac{2\pi}{3}(\alpha + 2\beta) + \cos \frac{2\pi}{3}(\alpha - 2\beta) \right] + \frac{J}{2} (-\mathbf{k}_x + 2\mathbf{k}_y), \quad (5)
\]

where \( \mathbf{k}_1, \mathbf{k}_2 \) are non-collinear basis vectors of the supercell in the reciprocal space: \( \mathbf{k}_1 = \frac{1}{3}(\mathbf{k}_x + \mathbf{k}_y), \mathbf{k}_2 = \frac{1}{3}(\mathbf{k}_x - 2\mathbf{k}_y), \) \( |\mathbf{k}_1| = |\mathbf{k}_2| \), where \( \mathbf{k}_x, \mathbf{k}_y \) are the basis vectors of the reciprocal triangular lattice.

After adding and subtracting an arbitrary hybridization function into the action for the Hubbard model, one can obtain:

\[
S[c, c^\dagger] = \sum_i S_{\text{imp}}^{(i)} - \sum_{\mathbf{K} \mathbf{k} \mathbf{k'}} c_{\mathbf{k} \mathbf{k}'}^\dagger(\mathbf{K}) \Delta_{\omega \mathbf{k} \mathbf{k'}}^\omega - \varepsilon_{\mathbf{k} \mathbf{k}'}(\mathbf{K}) c_{\mathbf{k} \mathbf{k}'}(\mathbf{K}) \quad (6)
\]

It should be mentioned that the \( \mathbf{k} \) dependence of \( \Delta_{\omega \mathbf{k} \mathbf{k'}}^\omega \) arises from the spatial Fourier transform over internal sites of the supercell. In case of all sites being equivalent \( \Delta_{\omega \mathbf{k} \mathbf{k'}} = \Delta_{\omega} \delta_{\mathbf{k} \mathbf{k'}} \).

The further steps of the dual fermion scheme for a supercell are similar to the cluster DCA approach. Utilizing Hubbard-Stratonovich transformation to new fermionic variables and integrating out the original degrees of freedom one can obtain a new fermionic problem, which is even more complex that the original one, but it allows to be efficiently treated by a diagrammatic expansion by a right definition of a yet arbitrary hybridization function \( \Delta_{\omega \mathbf{k} \mathbf{k'}}^\omega \). It is chosen in a way for the trivial case of no diagrammatic expansion of the self energy of the dual variables to be equivalent to the DMFT. We use a first non-zero term in the diagrammatic expansion of a dual self-energy:

\[
\Sigma_{\mathbf{k} \mathbf{k'}}^{4}\gamma_{1'2'3'4'}^{(4)} = \sum_{2'3'4'}^{234} g_{2'3'}^{4} G_{2'2'}^{4} G_{2'3'}^{3} \gamma_{1'2'3'4'}^{(4)} \quad (7)
\]

The important long ranged corrections to the single-site DMFT scheme are introduced in formula (6). It should be noted that the dual fermion Green’s function consists only of non-local part while the vertex function is local and obtained within a single-impurity Anderson mode.
In order to introduce non-collinear spin-dependent DF-scheme one can rotate spinors for different sites of a supercell. The local Green’s function for a given site is obtained as follows:

\[ g_{\omega i} = \hat{U}_i (\frac{\pi}{2}, \pm \frac{2\pi}{3}) \hat{g}_i \hat{U}_i^* (\frac{\pi}{2}, \pm \frac{2\pi}{3}), \]  

(7)

where \( \hat{U} \) is a spin 2 \( \times 2 \) rotation matrix.

The total energy \( \langle \hat{H} - \mu \hat{N} \rangle \) for different states has been calculated in the following form\(^{[23]}\)

\[ \langle \hat{H} \rangle = \langle \hat{H}_0 + \hat{V} - \mu \hat{N} \rangle, \]  

(8) 

\[ \langle \hat{H}_0 \rangle = -t \sum_{\sigma} G_{0\sigma}(\tau = 0+), \]  

(9) 

\[ \langle \hat{H}_0 + 2V - \mu \hat{N} \rangle = \left( \frac{\partial G_{0\sigma}(\tau)}{\partial \tau} \right)_{\tau \rightarrow 0+} \]  

(10)

This procedure requires the Fourier transform of the Green’s function to the imaginary time domain. Since the CT-QMC solver provides a bare Green’s function on finite number of Matsubara frequencies, this could be a serious source of numerical errors. The interaction expansion solver\(^{[23]}\) produces low noise at the high Matsubara frequencies and allows to fit an asymptotic tail of the Green’s Function.

### III. RESULTS

In order to calculate the energetics of a triangular lattice, 2-3 different independent runs consisting of 20-30 DMFT iterations and following 15-25 DF iterations were done with the lattice size of 32 \( \times \) 32. The interaction expansion QMC solver\(^{[23]}\) was used for which the QMC error becomes sufficient at high values of \( U \). The obtained data was averaged, and the corresponding statistical error is plotted on the graphs. The spin-polarized phase in the insulating regime hence being constructed by spin rotation represents the Neel state. The unpolarized DMFT insulating phase has only local correlations and does not possess any magnetic ordering. It will be shown that the non-polarized insulating DF phase is constructed by singlet corrections to a local self-energy and therefore perturbatively describes the spin-liquid state.

#### A. Total energy calculations

The results for a total energy per site \( \langle \hat{H} + \mu \hat{N} \rangle = \langle \hat{H} \rangle + U/2 \) and averaged square of magnetic moment \( \langle m^2 \rangle \) as a function of \( U/t \) in the region of \( 8 < U/t < 14 \) for various states at half-filling, \( \beta t = 10 \) are presented at Figures 1 and 2 respectively. The separate curves for the phase transition from a metallic to a spin liquid state and from a metallic to a 120° Neel state were obtained. The phase transition to a spin liquid state occurs at \( U/t = 9.6 \pm 0.2 \), the hysteresis at \( U/t = 8.25 - 9.4 \pm 0.2 \) represents a first order transition from the metallic to the Neel ordered state.

At first, it can be seen from the energy graph that there is an essential difference between the DMFT and DF results for the spin liquid case. Non-local corrections favour the unordered insulating state. Without DF-corrections this phase never corresponds to the ground state in the whole studied region and remains metallic up
to $U/t < 11.2 \pm 0.2$. This is in agreement with the previous DMFT calculation.\footnote{29} Thus the first non-vanishing diagram in the DF approach lowers the total energy of the unordered insulating state to make it favourable in the region of $9.5 < U/t < 13$. The dual corrections in the Neel phase are small and do not change the behaviour of this phase. At higher values of $U/t$ the curves of total energies of Neel and spin liquid state become close and cannot be distinguished within the statistical error of the method. Nevertheless, since the dual corrections vanish at high $t$\footnote{29} one would expect that the total energies of DMFT and DF curve will become equal, with the Neel ordering curve to dominate in this region.

A formation of local magnetic moments with the increasing of $U/t$ is captured in the Figure 2 ($\beta t = 10$). It can be seen that in the insulating region both spin liquid and $120^0$ Neel states possess well-defined magnetic moments thus differing by a type of ordering. The dual correction for the unordered state significantly enhances a formation of magnetism in the region of Mott transition, thus emphasizing the role of singlet correlations. As for the Neel phase these corrections are small and magnetic ordering is formed even at lower value of $U$, which means that a static spin ordering is essentially captured on the DMFT level.

B. The density of states and the nonlocal self-energy

The densities of states $N(E)$ for the strongly correlated metallic state are shown in the Figure 3. One can clearly see a three-peak structure typical for the systems at the metal side of Mott transition, namely, two Hubbard bands and central “Kondo” quasiparticle peak.\footnote{22} This general structure is very similar both in the local DMFT and the non-local DF approximations. There is an essential difference between the solutions related to the shape of the Kondo peak. The density of states at the Fermi level in the local approximation is fixed by the sum rule, namely, $N(0)$ should be equal to its value for noninteracting electrons.\footnote{22} In the DF approach, this is no more the case and one can see that the non-local corrections suppress the height of the Kondo peak at larger $U$.

The densities of states for the Neel and spin liquid states are shown in the Figure 4. One can see that the spin liquid solution has a wider gap than the Neel state. This agrees with the RVB-picture as a liquid formed by local singlets.\footnote{2} Indeed, local singlet must have a spectrum inherited from a spectrum of a two-site cluster. To emphasize this feature, we show a spectrum of the isolated 2-atom cluster with the same value of $t$ with black ticks in the Fig. 4. The grey ticks represent value $\pm U/2$. As one can see from the inset of the Fig. 4, the non-local corrections to nearest-neighbor self-energy in the spin-liquid case are much larger than in the Neel state and dominate the low-frequency spectrum. This reflects an importance of nonlocal dynamical fluctuations for the spin liquid state. On the contrary, for the Neel phase a most of the nonlocality is reflected in the static ordering and is therefore taken into account already at the DMFT level. This corresponds to the results of the Fig. 2.

IV. DISCUSSION

Some approximations have been made in our consideration, and they should be discussed in the context of the phase diagram of the model studied. The main of them are a finite-temperature consideration and taking
The dual fermion corrections are, in general, sufficient in the intermediate values of $U/t$ at the order of a magnitude of the bandwidth. The picture obtained by including first non-zero diagram corresponds to an idea of a spin-liquid as a state which can be observed in certain region of parameter $U/t$ with metallic and Neel ordered states to occur outside of this range. This corresponds to what is provided in the literature. At the Fig. 2 it was shown that an inclusion of singlet corrections sufficiently enhances the magnetism and makes the formation of magnetic state to occur at lower values of $U$. Our calculations have been done using a leading diagram only and we expect higher order diagrams to shift the value of $U_{c1}$ even lower, so that a spin liquid state should have a monotonically increasing total energy curve - that is illustrated by a dashed line in the Fig. 1. We expect a spin liquid ground state to be extended to the region beyond current $U_{c1} = 9.6$ and a Neel ordered state to appear after the spin liquid. To have more quantitative description of a phase diagram one has to include a series of diagrams, such as ladder, which may lead to a formation of bounded singlet states.

The upper critical value $U_{c2} \geq 14$ looks overestimated due to a finite temperature. Indeed, thermal fluctuations in general destroy an ordering. The most clear case is a half-filled Hubbard lattice, where an ordered ground state is realised at any (even infinitesimal) $U$, due to so-called perfect nestling. However, DMFT calculations at relatively small temperature $\beta = 20$ show a phase diagram with the ordering destroyed by local fluctuations of magnetic momenta up to $U \approx 1[10]$. Speaking about the energy dependencies presented in the Fig. 1, we expect that lowering the temperature should shift the energy of the Neel state down.

V. CONCLUSIONS

In summary, the Hubbard model on a triangular lattice is investigated within a framework of spin-polarized dual fermion approach. The ordering of 120° Neel phase is described by an introduction of a non-collinear spin-polarization via a spinor rotation to the effective bath. The DMFT approximation works well for this type of ordering since non-local correlations are relatively small. On the contrary the solution with a non spin-polarized bath which describes the spin-liquid state has strong non-local corrections. This leads to a significant change in the phase diagram at low temperatures - the DF approach produces an insulating state with the lower total energy compared to that of a 120° state in a certain region of parameter $U/t$. Note that the simple DMFT solution gives an artificial Fermi liquid at these parameters. The densities of states for a spin-liquid phase has much larger insulating gap than for a non-collinear Neel state. Due to sufficient non-local corrections the dual fermion approach can capture the essential physics of a spin-liquid phase.

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