Direct Measurement of the W Boson Width
We present a direct measurement of the width of the W boson using the shape of the transverse mass distribution of $W \rightarrow e\nu$ candidate events. Data from approximately 1 fb$^{-1}$ of integrated luminosity recorded at $\sqrt{s} = 1.96$ TeV by the D0 detector at the Fermilab Tevatron $p\bar{p}$ collider are analyzed. We use the same methods and data sample that were used for our recently published W boson mass measurement, except for the modeling of the recoil, which is done with a new method based on a recoil library. Our result, $2.028 \pm 0.072$ GeV, is in agreement with the predictions of the standard model.

The gauge structure of the standard model (SM) of electromagnetic, weak, and strong interactions tightly constrains the properties and interactions of the carriers of these forces, the gauge bosons. Any departure from its predictions would be an indication of physics beyond the SM. The W boson is one of the carriers of the weak force and has a predicted decay width of

$$\Gamma_W = (3 + 2f_{QCD}) \frac{G_F M_W^3}{6\sqrt{2}\pi} (1 + \delta), \quad (1)$$

where $G_F$ is the Fermi coupling constant, $M_W$ is the mass...
of the $W$ boson and $f_{\text{QCD}} = 3(1 + \alpha_s(M_W^2)/\pi)$ is a QCD correction factor given to first order of the strong coupling constant $\alpha_s$. The radiative correction $\delta$ is calculated to be 2.1% with an uncertainty that is less than 0.5% in the SM [1]. Current world average values for $G_F$ [2] and $M_W$ [3] predict $\Gamma_W = 2.093 \pm 0.002$ GeV. Physics beyond the SM, such as new heavy particles that couple to the $W$ boson, could alter the higher order vertex corrections that enter into $\delta$ and modify $\Gamma_W$ [4].

Direct measurements of $\Gamma_W$ have been previously performed by the CDF and D0 collaborations [5–8]. The width has also been directly measured at the CERN LEP $e^+e^-$ collider [9]. The combined Tevatron average is $\Gamma_W = 2.056 \pm 0.062$ GeV, and the current world average is $\Gamma_W = 2.106 \pm 0.050$ GeV [6].

We present a direct measurement of $\Gamma_W$ using the shape of the transverse mass ($M_T$) distribution of $W \rightarrow e\nu$ candidates from $p\bar{p}$ collisions with center-of-mass energy of 1.96 TeV using data from approximately $1 \text{ fb}^{-1}$ of integrated luminosity collected by the D0 detector [10]. The transverse mass is defined as $M_T = \sqrt{2p_T^e p_T^\nu [1 - \cos(\Delta \phi)]}$, where $\Delta \phi$ is the opening angle between the electron and neutrino in the plane perpendicular to the beam axis, and $p_T^e$ and $p_T^\nu$ are the transverse momenta of the electron and neutrino, respectively. The fraction of events with large $M_T$ is sensitive to $\Gamma_W$, although it is also influenced by the detector responses to the electron and the hadronic recoil. We use a new data-driven method for modeling the hadronic recoil of the $W$ boson using a recoil library of $Z$ boson candidates [11]. Aside from the recoil modeling, the method for extracting $\Gamma_W$ is similar to that described in a recent Letter on a measurement of $W$ boson mass by the D0 collaboration [12].

The D0 detector includes a central tracking system, composed of a silicon microstrip tracker (SMT) and a central fiber tracker, both located within a 2 T superconducting solenoidal magnet and optimized for tracking candidates (5212 candidates with $100 < M_T < 200$ GeV) and 50 $< M_T < 200$ GeV. $Z$ boson candidate events are required to have two CC electrons with $p_T^{e,\nu} > 25$ GeV and $u_T < 15$ GeV. These selections yield 499 830 $W$ boson candidates (5272 candidates with $100 < M_T < 200$ GeV) and 18 725 $Z$ boson candidates with the invariant mass ($M_{ee}$) of the two electrons between 70 and 110 GeV.

The $W$ boson width is extracted by comparing the $M_T$ data distribution with distributions in simulated templates generated at different width values. The prediction (in number of events) of signal-plus-background is normalized to the data in the $50 < M_T < 100$ GeV window. A binned negative log-likelihood method is used to extract $\Gamma_W$ in the range $100 < M_T < 200$ GeV.

There are two main sources of events with high $M_T$: events that truly contain a high mass $W$ boson, and events with a $W$ boson whose mass is close to the $W$ boson mass central value but are produced with large $u_T$. This second category of events can be misreconstructed at high $M_T$ because of resolution effects and also because the magnitude of the recoil vector is systematically underestimated due to the response of the calorimeter to low energy hadrons, energy thresholds on the calorimeter energies, and magnetic field effects.

Another experimental challenge arises from the $p_T$ dependence of the electron identification efficiency, which can alter the shape of the $M_T$ distribution. The electron isolation requirement used in this analysis has a non-negligible dependence on the electron $p_T$ which is measured using a detailed GEANT-based Monte Carlo (MC) simulation [14] and tested using $Z \rightarrow ee$ events.

A fast MC simulation is used for the production of the $M_T$ templates. $W$ and $Z$ boson production and decay prop-
properties are modeled by the RESBOS event generator [15] interfaced with PHOTOS [16]. RESBOS uses gluon resummation at low boson \( p_T \) and a next-to-leading order perturbative QCD calculation at high boson \( p_T \). The CTEQ6.1M parton distribution functions (PDFs) [17] are used. PHOTOS is used for simulation of final state radiation (FSR). Photons and electrons that are nearly collinear are merged using an algorithm that mimics the calorimeter clustering algorithm.

The detector response for electrons and photons, including energy calibration, showering and energy loss models, is simulated using a parameterization based on collider data control samples, a detailed GEANT-based simulation of the detector, and external constraints, such as the precise measurement of the \( Z \) boson mass from the LEP experiments [18]. The primary control sample is \( Z \rightarrow ee \) events, although \( W \rightarrow \ell v \) events are also used in a limited way. The modeling of the electron energy response, resolution and selection efficiencies is described in [12]. The number of \( Z \) boson candidates in data sets scale for the systematic uncertainties related to the electron modeling in the simulation, which are listed in detail in Table I.

The modeling of the recoil is based on the recoil library obtained from \( Z \rightarrow ee \) events [11]. A Bayesian unsmeared procedure [19] allows the transformation of the two-dimensional distribution of reconstructed \( Z \) boson \( \hat{p}_T \) and the measured recoil momentum \( \hat{u}_T \) to one between the true \( Z \) boson \( \tilde{p}_T \) and the measured recoil \( \tilde{u}_T \). For each simulated \( W \rightarrow \ell v \) event with a generator-level transverse momentum value \( \tilde{p}_T \), we select \( \tilde{u}_T \) randomly from the \( Z \) boson recoil library with the same value of \( \tilde{p}_T \). The uncertainty on the recoil system simulation from this method is dominated by the limited statistics of the \( Z \) boson sample; other systematic uncertainties originate from the modeling of FSR photons, acceptance differences between \( W \) and \( Z \) boson events, corrections for underlying energy beneath the electron cluster, residual efficiency-related correlations between the electron and the recoil system, and the unfolding procedure. Previous \( M_W \) and \( \Gamma_W \) measurements have relied upon parametrizations of the recoil kinematics based on phenomenological models of the recoil and detector response. The library method used here includes the actual detector response for the hadronic recoil and also the correlations between different components of the hadronic recoil. This method does not rely on the GEANT-based simulation of the recoil system and does not have any tunable parameters. The overall systematic uncertainty on \( \Gamma_W \) due to the recoil model is found to be 41 MeV [11].

The backgrounds to \( W \rightarrow \ell v \) events are (a) \( Z \rightarrow ee \) events in which one electron is not detected, (b) multijet production in which one jet is misidentified as an electron and mismeasurement of the hadronic activity in the event leads to apparent \( \not{E}_T \), and (c) \( W \rightarrow \tau \nu \rightarrow e\nu\nu\nu \) events. The \( Z \rightarrow ee \) background arises mainly when one of the two electrons is in the region between the CC and EC calorimeters. It is estimated from events with one electron with a high-\( p_T \) track opposite in azimuth pointing towards the gap. The estimated background fraction is \((0.90 \pm 0.01)\%\) for \( 50 < M_T < 200 \) GeV. The background fraction from multijet events is estimated from a loose sample of candidate events without track match requirements and then selecting a subset of events which satisfy the final tighter track match requirement. From \( Z \rightarrow ee \) events, and a sample of multijet events passing the preselection but with low \( \not{E}_T \), we determine the probabilities with which real and misidentified electrons will pass the track match requirement. These two probabilities, along with the numbers of events selected in the loose and tight samples allow us to calculate the fraction of multijet events in the data set [20]. The background contamination from multijet events is estimated to be \((1.49 \pm 0.03)\%\) for \( 50 < M_T < 200 \) GeV. The \( W \rightarrow \tau \nu \rightarrow e\nu\nu\nu \) background is determined using a GEANT-based simulation to be \((1.60 \pm 0.02)\%\) for \( 50 < M_T < 200 \) GeV and is normalized to the \( W \rightarrow \ell v \) events in the same simulation. The overall background fraction is found to be \((4.36 \pm 0.05)\%\) with \( M_T \) between 100 and 200 GeV. The uncertainties on the normalization and shape of the backgrounds cause a 6 MeV systematic uncertainty on \( \Gamma_W \).

The systematic uncertainties in the determination of the \( W \) boson width are due to effects that could alter the \( M_T \) distribution. Uncertainties in the parameters of the fast MC simulation can affect the measurement of \( \Gamma_W \). To estimate the effects, we allow these parameters to vary by 1 standard deviation and regenerate the \( M_T \) templates. Systematic uncertainties resulting from the boson \( p_T \) spectrum are evaluated by varying the \( g_2 \) parameter of the RESBOS nonperturbative prescription within the uncertainties obtained from a global fit [21] and propagating them to the \( W \) boson width. Systematic uncertainties due to the PDFs are evaluated using the prescription given by the CTEQ collaboration [17]. Systematic uncertainties from the modeling of electroweak radiative corrections are obtained by comparisons with WGRAD2 [22] and ZGRAD2 [23]. The systematic uncertainty due to the \( M_W \) uncertainty is obtained by varying the input \( M_W \) by \( \pm 23 \) MeV [3].

<table>
<thead>
<tr>
<th>Source</th>
<th>( \Delta \Gamma_W ) (MeV)</th>
</tr>
</thead>
<tbody>
<tr>
<td>Electron response model</td>
<td>33</td>
</tr>
<tr>
<td>Electron resolution model</td>
<td>10</td>
</tr>
<tr>
<td>Hadronic recoil model</td>
<td>41</td>
</tr>
<tr>
<td>Electron efficiencies</td>
<td>19</td>
</tr>
<tr>
<td>Backgrounds</td>
<td>6</td>
</tr>
<tr>
<td>PDF</td>
<td>20</td>
</tr>
<tr>
<td>Electroweak radiative corrections</td>
<td>7</td>
</tr>
<tr>
<td>Boson ( p_T )</td>
<td>1</td>
</tr>
<tr>
<td>( M_W )</td>
<td>5</td>
</tr>
<tr>
<td>Total Systematic</td>
<td>61</td>
</tr>
</tbody>
</table>
We fit the $M_T$ data distribution to a set of templates generated with an input $W$ boson mass of 80.419 GeV at different assumed widths between a lower $M_T$ value and $M_T = 200$ GeV. The lower $M_T$ cut is varied from 90 to 110 GeV to demonstrate the stability of the fitted result. While the statistical uncertainty decreases as the lower $M_T$ cut is reduced, the systematic uncertainty increases. The lowest overall uncertainty is obtained for a lower $M_T$ cut of 100 GeV yielding $\Gamma_W = 2.028 \pm 0.039\text{(stat)} \pm 0.061\text{(syst)}$ GeV. The $M_T$ distributions for the data and the MC template with backgrounds for the best fit value are shown in Fig. 1, which also shows the bin-by-bin $\chi$ values defined as the difference between the data and the template divided by the data statistical uncertainty.

The methodology used to extract the width in this Letter is tested using $W$ and $Z$ boson events produced by a PYTHIA- or GEANT-based simulation and the same analysis methods used for the data. The fast MC simulation is separately tuned for this study. Good agreement is found between the fitted $\Gamma_W$ value and the input $\Gamma_W$ value within the statistical precision of the test.

The $\Gamma_W$ result obtained using the $M_T$ spectrum is in agreement with the predictions of the SM. We get consistent values of the $W$ boson width from fits to the $p_T$ distribution (2.012 $\pm$ 0.046(stat) GeV) and the $E_T$ distribution (2.058 $\pm$ 0.036(stat) GeV). The width can also be estimated directly from the fraction of events with $M_T > 100$ GeV, and this gives $\Gamma_W = 2.020 \pm 0.040\text{(stat)}$ GeV. The results are stable within errors when the data sample is divided into different regions of instantaneous Tevatron luminosity, run epoch, and different restrictions on $u_T$, electron $\eta_D$, $\bar{u}_T \cdot \bar{p}_T(e)$ and fiducial cuts on electron azimuthal angle.

As a further cross check of the recoil library method we also use it to measure the $W$ boson mass using the $M_T$ distribution over the region $65 < M_T < 90$ GeV. A value of $M_W = 80.404 \pm 0.023\text{(stat)} \pm 0.038\text{(syst)}$ GeV is found, in good agreement with the result, $M_W = 80.401 \pm 0.023\text{(stat)} \pm 0.037\text{(syst)}$ GeV, obtained using the same data set and the parameterized recoil model [12].

In conclusion, we have presented a new direct measurement of the width of the $W$ boson using 1 fb$^{-1}$ of data collected by the D0 detector at the Tevatron collider. A method to simulate the recoil system in $W \rightarrow e\nu$ events using a recoil library built from $Z \rightarrow ee$ events is used for the first time. Our result, $\Gamma_W = 2.028 \pm 0.039\text{(stat)} \pm 0.061\text{(syst)} = 2.028 \pm 0.072$ GeV, is in agreement with the prediction of the SM and is the most precise direct measurement result from a single experiment to date.

We thank the staffs at Fermilab and collaborating institutions, and acknowledge support from the DOE and NSF (USA); CEA and CNRS/IN2P3 (France); FASI, Rosatom and RFBR (Russia); CNPq, FAPERJ, FAPESP and FUNDUNESP (Brazil); DAE and DST (India); Colciencias (Colombia); CONACyT (Mexico); KRF and KOSEF (Korea); CONICET and UBACyT (Argentina); FOM (The Netherlands); STFC and the Royal Society (United Kingdom); MSMT and GACR (Czech Republic); CRC Program, CFI, NSERC and WestGrid Project (Canada); BMBF and DFG (Germany); SFI (Ireland); The Swedish Research Council (Sweden); Graduate Research Board, University of Maryland (USA); and CAS and CNSF (China).

*Visitor from Augustana College, Sioux Falls, SD, USA.
†Visitor from Rutgers University, Piscataway, NJ, USA.
‡Visitor from The University of Liverpool, Liverpool, United Kingdom.
§Visitor from SLAC, Menlo Park, CA, USA.
‖Visitor from Centro de Investigacion en Computacion-IPN, Mexico City, Mexico.
||Visitor from ECFM, Universidad Autonoma de Sinaloa, Culiacan, Mexico.
**Visitor from Universität Bern, Bern, Switzerland.
††Visitor from Universität Zürich, Zürich, Switzerland.
[13] The polar angle $\theta$ is defined with respect to the positive $z$ axis, which is defined along the proton beam direction. Pseudorapidity is defined as $\eta = -\ln \tan(\theta/2)$. $\eta_D$ is the pseudorapidity measured with respect to the center of the detector.