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**Measurement of the Z-boson mass
using $e^+e^- \rightarrow Z\gamma$ events
at centre-of-mass energies above the Z pole**

The L3 Collaboration

Abstract

Events from the $e^+e^- \rightarrow Z\gamma$ process with hard initial-state radiation collected with the L3 detector at centre-of-mass energies between 183 GeV and 209 GeV are used to measure the mass of the Z boson. Decays of the Z boson into hadrons or muon pairs are considered and the Z mass is determined to be 91.272 ± 0.032 (stat.) ± 0.033 (syst.) GeV, in agreement with the value measured at the Z resonance. Alternatively, assuming this measured value of the Z mass, the method determines the LEP centre-of-mass energy, found to be 175 ± 68 (stat.) ± 68 (syst.) MeV lower than the nominal value.

Submitted to *Phys. Lett. B*

1 Introduction

At the LEP collider, operating at centre-of-mass energies, \sqrt{s} , above the Z peak, the process $e^+e^- \rightarrow f\bar{f}\gamma$ frequently occurs with hard initial-state radiation (ISR). Due to the strong resonance in the reaction $e^+e^- \rightarrow Z \rightarrow f\bar{f}$, the energy of the ISR photon is such that the mass of the fermion pair recoiling against the photon is often close to the mass of the Z boson, m_Z . The strong forward peaking of the ISR process yields photons which usually remain undetected in the beampipe but in a small fraction of events they are detected.

Data recorded with the L3 detector [1] at $\sqrt{s} = 183 - 209$ GeV with a total integrated luminosity of 685 pb^{-1} , detailed in Table 1, are used to extract the mass of the Z boson, using Z decays into quark or muon pairs. The mass of the hadronic system after applying a kinematic fit, m_{eff} , is directly related to m_Z . In the case of muon pairs the event kinematics is fully determined by the measurement of the muon scattering angles, making use of the excellent polar angle resolution of the muon spectrometer. From the measured or reconstructed photon energy, E_γ , the effective centre-of-mass energy of the muon pair, $\sqrt{s'}$, is calculated as

$$\sqrt{s'} = \sqrt{s} \sqrt{1 - \frac{2 E_\gamma}{\sqrt{s}}}. \quad (1)$$

An unbinned likelihood fit is applied to the distribution of m_{eff} or $\sqrt{s'}$ to extract the Z mass. The value is compared with the precision measurement of L3, derived from the Z-lineshape scan at centre-of-mass energies around the Z pole [2]. This comparison serves as a cross check of the W-mass measurement which uses similar techniques. Assuming the Z mass measured around the Z pole, the method provides a measurement of the LEP centre-of-mass energy which is compared to the one determined by the LEP energy working group [3].

2 Monte Carlo simulation

The Standard Model predictions for the different final states are determined with the following Monte Carlo programs: KK2F [4] for $e^+e^- \rightarrow q\bar{q}(\gamma)$, $e^+e^- \rightarrow \mu^+\mu^-(\gamma)$ and $e^+e^- \rightarrow \tau^+\tau^-(\gamma)$, BHWIDE [5] for $e^+e^- \rightarrow e^+e^-(\gamma)$, PHOJET [6] for $e^+e^- \rightarrow e^+e^-$ -hadrons, DIAG36 [7] for $e^+e^- \rightarrow e^+e^-\mu^+\mu^-$, KORALW [8] for $e^+e^- \rightarrow W^+W^-$, with the exception of the $e\nu q\bar{q}'$ final state, which is modelled by EXCALIBUR [9], and PYTHIA [10] for $e^+e^- \rightarrow ZZ$ and $e^+e^- \rightarrow Ze^+e^-$. The response of the L3 detector is modelled with the GEANT [11] detector simulation program which includes the effects of energy loss, multiple scattering and showering in the detector material. The GEISHA program [12] is used to simulate hadronic interactions in the detector. Time-dependent detector inefficiencies are taken into account in the simulation.

3 Selection of hadronic events

To remove purely leptonic final states the event must have more than 12 calorimetric clusters. In addition, the transverse energy imbalance must be less than 25% of the visible energy and the sum of the cluster energies must be greater than 30% of \sqrt{s} , as shown in Figure 1a.

Hadronic final states from two-photon collisions are typically boosted along the beam direction. To reject these events we require the longitudinal energy imbalance not to exceed 80% of the visible energy. Additionally, the sum of the transverse energies of the hadronic clusters has to be greater than 15% of \sqrt{s} . Both cuts effectively remove the two-photon background.

Four-jet final states from W- and Z-pair production have a total hadronic energy close to \sqrt{s} . The clusters in these events are distributed more spherically than in the case of two-jet events from $Z\gamma$ production. For events with a sum of the hadronic energy greater than 70% of \sqrt{s} , the particles are boosted to the rest frame of the hadronic system. A cut on the thrust, T , of the boosted event, $T > 0.85$, removes four-jet events as shown in Figure 1b.

4 Selection of muon-pair events

Muons are reconstructed from tracks in the muon chambers in a fiducial volume of $|\cos\theta| < 0.9$. If only one muon track is present in the event, the signature of an additional minimum-ionizing particle in the inner detectors is required. Hadronic events are suppressed by requiring less than 15 calorimetric clusters. To reject cosmic-ray background, the time measured by one scintillator matched in azimuthal angle to a muon track has to be consistent with that of beam crossing within 5 ns. In addition, the distance of closest approach of at least one of the muon tracks to the interaction point in the plane perpendicular to the beam must be less than 1 mm.

The two muons are usually almost back-to-back in the plane perpendicular to the emitted photon. Therefore, the angle between the muon directions in that plane, $\Delta\phi$, is required to be greater than 175° , as shown in Figure 1c. The measured momentum, p_μ , of the muon which has the largest polar angle, θ_1 , has to be greater than 60% of the corresponding expected momentum, p_μ^{exp} , calculated according to

$$p_\mu^{\text{exp}} = \sqrt{s} \frac{\sin\theta_2}{\sin\theta_1 + \sin\theta_2 + |\sin(\theta_1 + \theta_2)|}, \quad (2)$$

where θ_2 is the polar angle of the other muon. Figure 1d shows the distribution of p_μ/p_μ^{exp} .

5 Mass reconstruction

In each selected event we search for an isolated photon. A photon candidate is a calorimetric cluster with an energy greater than 30% of \sqrt{s} . It has to be isolated, with at most one additional cluster within 15° of the candidate direction. In addition, the angle between the photon and the nearest track must be greater than 4.6° .

Hadronic events are forced into two jets using the DURHAM [13] algorithm, excluding photon candidates, if any. The pion mass is assigned to energy depositions matched with a charged track while clusters without a matching track are treated as massless. A kinematic fit is applied to the event, where the measured quantities are varied within their resolution and four-momentum conservation is imposed. If no high-energy photon is observed in the detector, a single photon is assumed to have escaped undetected along the beam direction. This improves the resolution of the two-jet effective mass by a factor of about 3. The distribution of the fitted mass, m_{eff} , is shown in Figure 2.

In muon-pair events, the photon energy is calculated from the reconstructed muon momenta using three-particle kinematics as

$$E_\gamma = \sqrt{s} \frac{|\sin(\theta_1 + \theta_2)|}{\sin\theta_1 + \sin\theta_2 + |\sin(\theta_1 + \theta_2)|}. \quad (3)$$

The θ_i are the angles between the muons and the photon direction. If no photon is detected they are the angles between the muons and the beam direction. The effective centre-of-mass

energy of the muon pair, $\sqrt{s'}$, is calculated using Formula 1 and its distribution is shown in Figure 3.

6 Fit method

Events with hard ISR are selected by requiring

$$70 \text{ GeV} < m_{\text{eff}} < 110 \text{ GeV}$$

for hadronic events and

$$80 \text{ GeV} < \sqrt{s'} < 100 \text{ GeV}$$

for muon-pair events. Data samples of 34081 and 799 events are selected for hadrons and muon pairs, respectively, with background levels of 3.2% and 6.2%.

To extract the Z mass from this data sample, an unbinned likelihood fit is applied to the measured differential cross section as a function of m_{eff} or $\sqrt{s'}$. The likelihood is defined as the product of the normalised differential cross sections of each event after selection cuts:

$$L(m_Z^{\text{fit}}) = \prod_i \frac{\frac{d\sigma}{d\xi}(\xi_i, m_Z^{\text{fit}}) + \frac{d\sigma_{\text{BG}}}{d\xi}(\xi_i)}{\sigma(m_Z^{\text{fit}}) + \sigma_{\text{BG}}}, \quad (4)$$

where m_Z^{fit} is the Z mass varied during the fit and ξ represents m_{eff} for the hadronic events and $\sqrt{s'}$ for the muon-pair events. The total and differential accepted cross sections of the signal are denoted as σ and $d\sigma/d\xi$, while σ_{BG} and $d\sigma_{\text{BG}}/d\xi$ are the total and differential cross sections of the background.

The box method [14] is used to obtain the accepted differential cross section. This method takes into account both detector resolution and selection efficiency effects. The accepted differential cross section is determined by averaging Monte Carlo events inside a ξ bin centered around each data event. The number of signal Monte Carlo events is scaled such that it agrees with the measured total cross section, while the number of background events is normalised to the integrated luminosity. This ansatz assigns fluctuations in the number of data events to the signal. Stable results are obtained with bin sizes chosen such that 500 signal Monte Carlo events are contained in each m_{eff} bin and 250 signal events in each $\sqrt{s'}$ bin. The size of the bins ranges from about 20 MeV in the m_{eff} peak to about 6 GeV in the m_{eff} tails and from 50 MeV in the $\sqrt{s'}$ peak to 3 GeV in the $\sqrt{s'}$ tails.

To simulate the effect of different values of the Z-boson mass with a finite number of Monte Carlo events, the signal Monte Carlo events are reweighted using the weights

$$\frac{d\sigma}{d\sqrt{s'}}(\sqrt{s'_i}^{\text{gen}}, m_Z^{\text{fit}}) \Big/ \frac{d\sigma}{d\sqrt{s'}}(\sqrt{s'_i}^{\text{gen}}, m_Z^{\text{MC}}), \quad (5)$$

where $\sqrt{s'_i}^{\text{gen}}$ is the generated effective centre-of-mass energy of each event and m_Z^{MC} is the value of the Z mass that is used in the Monte Carlo generation. The calculation of the differential cross section, $d\sigma/d\sqrt{s'}$, up to $\mathcal{O}(\alpha^2)$ of Reference 15 is used.

To confirm the linearity of the fitting method as well as to test for any possible bias, five Monte Carlo samples, each with about ten times the statistics of the data, are generated with different Z masses between 90 GeV and 92 GeV. The correct values for the mass of the Z boson are found by the fitting method within the statistical precision of the test.

7 Systematic uncertainties

The systematic uncertainties for the Z mass determination are listed in Table 2 and are detailed below.

To estimate the uncertainty due to hadronisation, three different Monte Carlo samples are generated which have the same underlying two-fermion events, but different hadronisation schemes, modelled by the programs ARIADNE [16], HERWIG [17] and PYTHIA. As the jets are formed from clusters that are either massless or assigned the pion mass, a different kaon or baryon content in data and Monte Carlo would lead to a bias in the extracted Z mass. For each of the three models the Monte Carlo events were reweighted in order to reproduce the mean kaon and proton multiplicity measured on the Z peak [18]. The mass of the jets plays a role in the kinematic fit and the differences of the jet masses produced by the different hadronisation schemes are also considered. A reweighting method is applied to reproduce the jet masses measured in data. The root-mean-square of the various Z masses obtained with the three Monte Carlo programs after the different reweighting procedures is assigned as the hadronisation systematic uncertainty.

The ratio of the measured jet energy to the energy calculated from the jet angles analogously to Formula 2, is shown in Figure 4a. The jet energy scale is confirmed at the percent level. The value of this ratio as a function of $\cos\theta$ allows for the recalibration of the energy measurement of hadronic clusters. Half of the difference to the mass obtained without recalibration is taken as systematic uncertainty. In addition, we scale the energy of the individual energy depositions by $\pm 0.5\%$. The difference to the value without scaling is taken as systematic uncertainty. The total uncertainty from energy calibration is the sum in quadrature of the two contributions.

The uncertainty due to the measurement of the jet polar angle is estimated by repeating the analysis with jets formed by calorimetric clusters that have a corresponding charged track and jets formed by the same clusters but using the polar angles from the correlated charged track instead of the angle measured in the calorimeter. The accuracy of the measurement of the muon polar angle is tested by comparing the default $\sqrt{s'}$ spectrum to the spectrum obtained using the angles of calorimetric clusters associated with the muons. The differences of m_{eff} or $\sqrt{s'}$ are calculated on an event-by-event basis and shown in Figures 4b and 4c, respectively. We assign half the difference of the average shifts of data and Monte Carlo as systematic uncertainties.

Additional clusters around detected photons, wrongly assigned to one of the jets, would affect the reconstructed Z mass. Removing all clusters in a 10° cone around the photon direction results in a negligible mass shift. In a similar way, calorimetric clusters from random noise, equally distributed in the calorimeters, would affect the reconstructed mass if they are not described by the Monte Carlo. The angular distribution of calorimetric energy relative to the corresponding jet axis is plotted in Figure 4d. Good agreement between data and Monte Carlo is seen. Removing all clusters outside a cone of 60° half-opening angle around the jet axis yields a negligible mass shift.

For both hadronic events and muon-pair events the uncertainty in the background level is evaluated by scaling the total cross section of the background Monte Carlo samples by $\pm 5\%$.

The theoretical uncertainty on the ISR modelling is tested by comparing results obtained with different ISR modelling schemes to different orders of α . This is done by using event weights given by the Monte Carlo generator KK2F as described in Reference 4. The differences between the results from $\mathcal{O}(\alpha^2)$ calculations with Coherent Exclusive Exponentiation with and without ISR/FSR interference is assigned as systematic uncertainty.

The stability of the box method is tested by changing the box sizes used in the fit. A small

shift is observed and quoted as systematic uncertainty. To test the results obtained with the maximum likelihood fit, we also apply a χ^2 fit of the Monte Carlo histogram to the measured m_{eff} distribution by reweighting individual Monte Carlo events. As a second test, we apply the maximum likelihood fit to the $\sqrt{s'}$ spectrum of the hadronic event sample, calculated using Formula 3 modified to include the effect of non zero jet masses. The results from both cross checks show no significant deviation from the default method. The uncertainty from limited Monte Carlo statistics is also considered.

The LEP beam energy has an uncertainty of 10 to 20 MeV [3] depending on \sqrt{s} . The relative error on the Z-boson mass is the same as that on the beam energy.

The systematic uncertainties are treated as fully correlated between the different energy points, except the uncertainty resulting from limited Monte Carlo statistics, which is treated as uncorrelated, and the uncertainties on the beam energy, where the correlation matrix from Reference [3] is used. A total systematic uncertainty of 39 MeV for the determination of the Z-mass from the hadronic channel and 21 MeV from the muon channel is found.

8 Results

The results for different values of \sqrt{s} are shown in Table 3. They are combined taking the systematic uncertainties into account. The combination yields

$$m_Z^{\text{qq}} = 91.271 \pm 0.031 \text{ (stat.)} \pm 0.039 \text{ (syst.) GeV}$$

for hadronic events and

$$m_Z^{\mu\mu} = 91.276 \pm 0.105 \text{ (stat.)} \pm 0.021 \text{ (syst.) GeV}$$

for muon-pair events. The results of the fit are shown in Figures 2 and 3. Averaging the results obtained from the hadronic and muon pair samples, including all correlations, yields

$$m_Z^{\text{meas}} = 91.272 \pm 0.032 \text{ (stat.)} \pm 0.033 \text{ (syst.) GeV.}$$

For the combination of hadron and muon-pair events, the uncertainty due to ISR modelling is treated as fully correlated. For the beam energy uncertainties the correlation matrix of Reference 3 is used. This value is in good agreement with the precision mass measurement, $m_Z = 91.1898 \pm 0.0031$ GeV [2].

The measurement can also be interpreted as a determination of the LEP centre-of-mass energy, \sqrt{s}^{meas} . A difference between the measured mass, m_Z^{meas} , and the precision mass, m_Z , can be attributed to a deviation from the nominal value, \sqrt{s} :

$$\Delta\sqrt{s} = \sqrt{s}^{\text{meas}} - \sqrt{s} = -\sqrt{s} \frac{m_Z^{\text{meas}} - m_Z}{m_Z}. \quad (6)$$

The value obtained from the observed Z mass,

$$\Delta\sqrt{s} = -0.175 \pm 0.068 \text{ (stat.)} \pm 0.068 \text{ (sys.) GeV,}$$

is consistent with no shift.

In conclusion, the Z mass measured in radiative events is in agreement with the determination at the Z pole, validating the method used for the measurement of the mass of the W boson. Interpreted as a determination of the centre-of-mass energy it agrees with the measurements by the LEP energy working group [3].

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- § Supported by the German Bundesministerium für Bildung, Wissenschaft, Forschung und Technologie
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- ¶ Also supported by the Hungarian OTKA fund under contract number T026178.
- ^b Supported also by the Comisión Interministerial de Ciencia y Tecnología.
- ‡ Also supported by CONICET and Universidad Nacional de La Plata, CC 67, 1900 La Plata, Argentina.
- △ Supported by the National Natural Science Foundation of China.

Year	$\langle\sqrt{s}\rangle$ [GeV]	Luminosity [pb^{-1}]
1997	182.7	55.5
1998	188.6	176.8
1999	191.6	29.8
1999	195.5	84.1
1999	199.5	83.3
1999	201.8	37.2
2000	204.8	79.0
2000	206.5	130.8
2000	208.0	8.3
Total		684.8

Table 1: Centre-of-mass energies and corresponding integrated luminosities.

Source	Uncertainty [MeV] (hadron channel)	Uncertainty [MeV] (muon channel)
Hadronisation	22	–
Energy calibration	16	–
Angular measurement	24	11
Background	3	<1
Initial-state radiation	4	11
Box Size	2	2
Monte Carlo statistics	8	9
LEP energy	11	11
Total	39	21

Table 2: Systematic uncertainties on the Z boson mass.

$\langle\sqrt{s}\rangle$ [GeV]	m_Z^{meas} [GeV] (hadron channel)	m_Z^{meas} [GeV] (muon channel)
182.7	$91.286 \pm 0.095 \pm 0.046$	$91.057 \pm 0.317 \pm 0.029$
188.6	$91.290 \pm 0.057 \pm 0.042$	$91.224 \pm 0.189 \pm 0.029$
191.6	$91.402 \pm 0.143 \pm 0.046$	$92.065 \pm 0.635 \pm 0.029$
195.5	$91.467 \pm 0.089 \pm 0.046$	$91.219 \pm 0.332 \pm 0.029$
199.5	$91.144 \pm 0.094 \pm 0.046$	$91.183 \pm 0.422 \pm 0.029$
201.8	$91.073 \pm 0.142 \pm 0.046$	$91.464 \pm 0.402 \pm 0.029$
204.8	$91.369 \pm 0.101 \pm 0.042$	$91.358 \pm 0.260 \pm 0.032$
206.5	$91.107 \pm 0.081 \pm 0.042$	$91.439 \pm 0.273 \pm 0.033$
208.0	$91.329 \pm 0.331 \pm 0.042$	$90.439 \pm 0.667 \pm 0.033$
Combined	$91.271 \pm 0.031 \pm 0.039$	$91.276 \pm 0.105 \pm 0.021$

Table 3: Results of the maximum likelihood fit for each \sqrt{s} value. The first uncertainty is statistical, the second systematic.

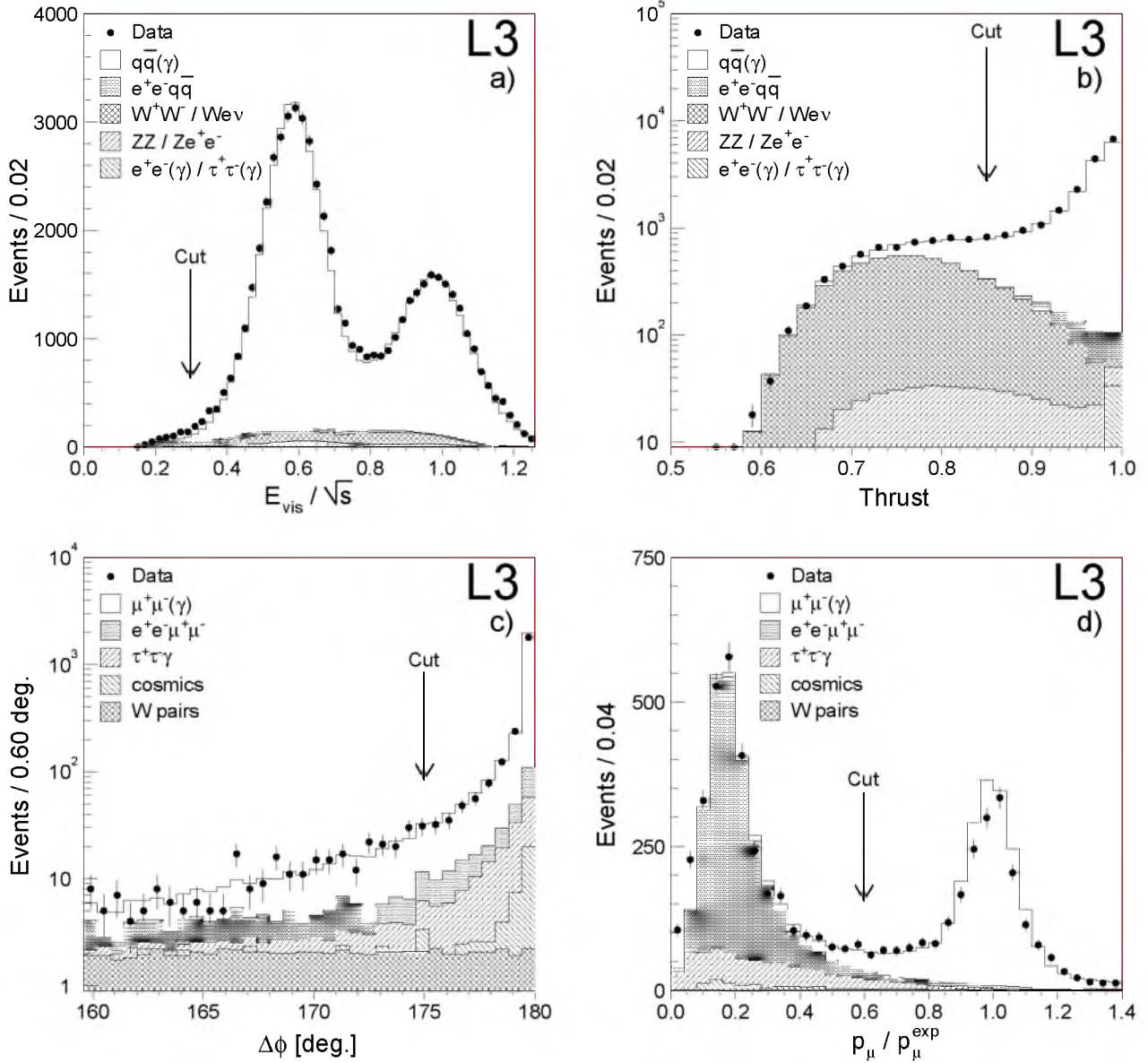


Figure 1: Variables used for the event selections: a) visible energy, normalised to \sqrt{s} , b) thrust in the centre-of-mass frame of the jets, c) angle between the muons in the plane perpendicular to the photon and d) measured muon momentum, normalised to the expected momentum.

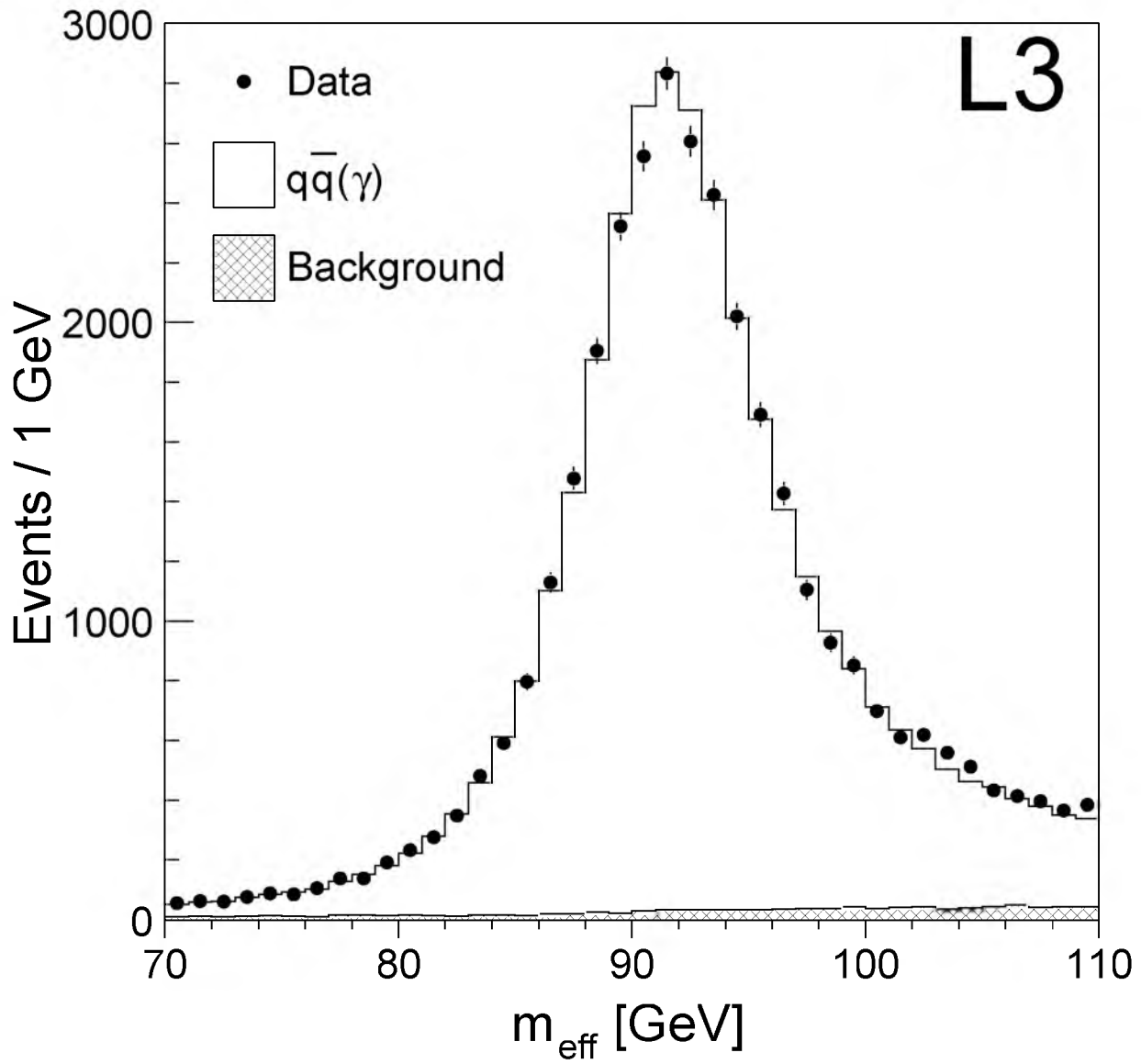


Figure 2: Distribution of the effective mass of the two-jet system after kinematic fit. The solid line shows the result of the fit which determines the Z boson mass.

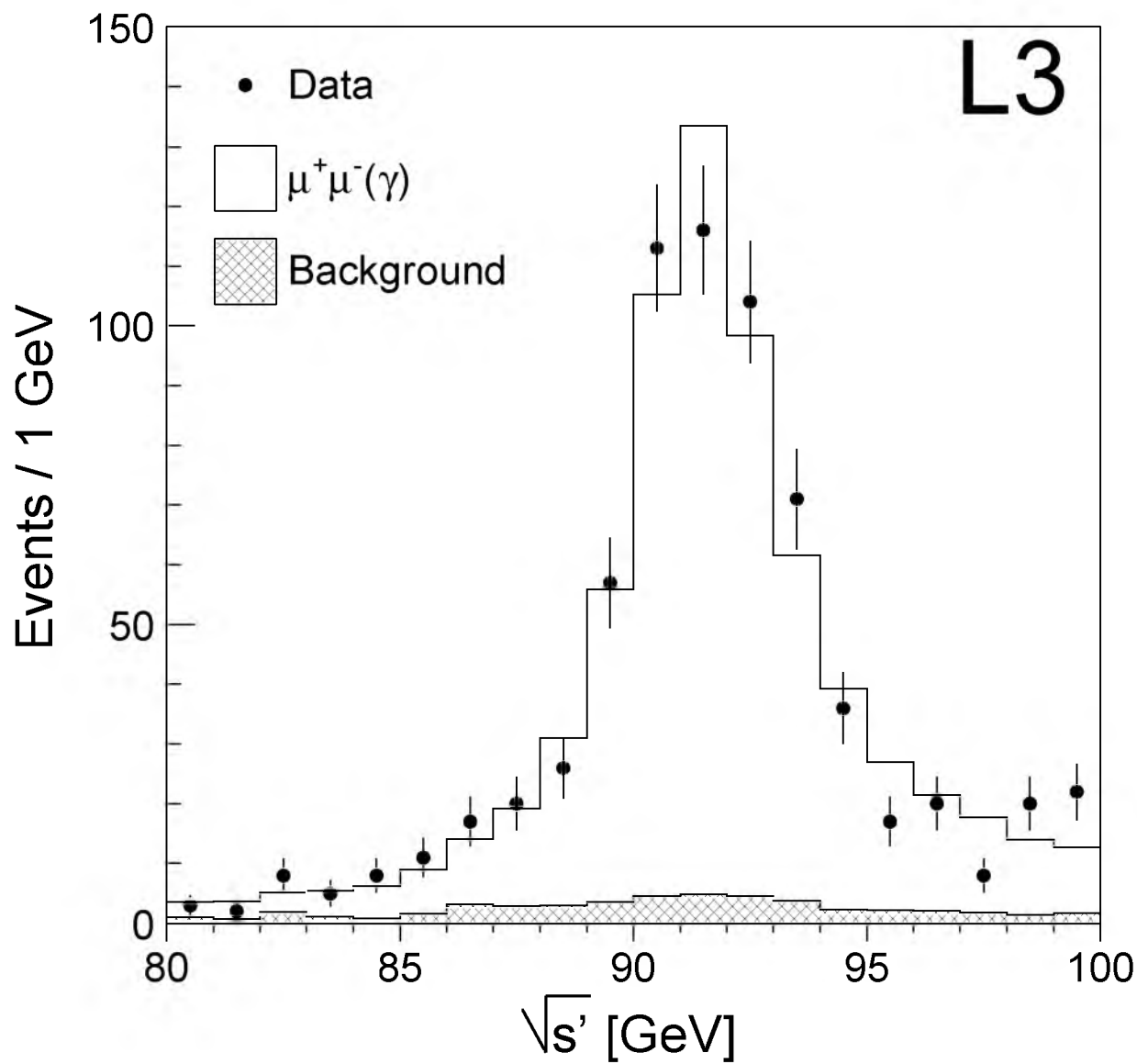


Figure 3: Distribution of the effective centre-of-mass energy for muon-pair events. The solid line shows the result of the fit which determines the Z boson mass.

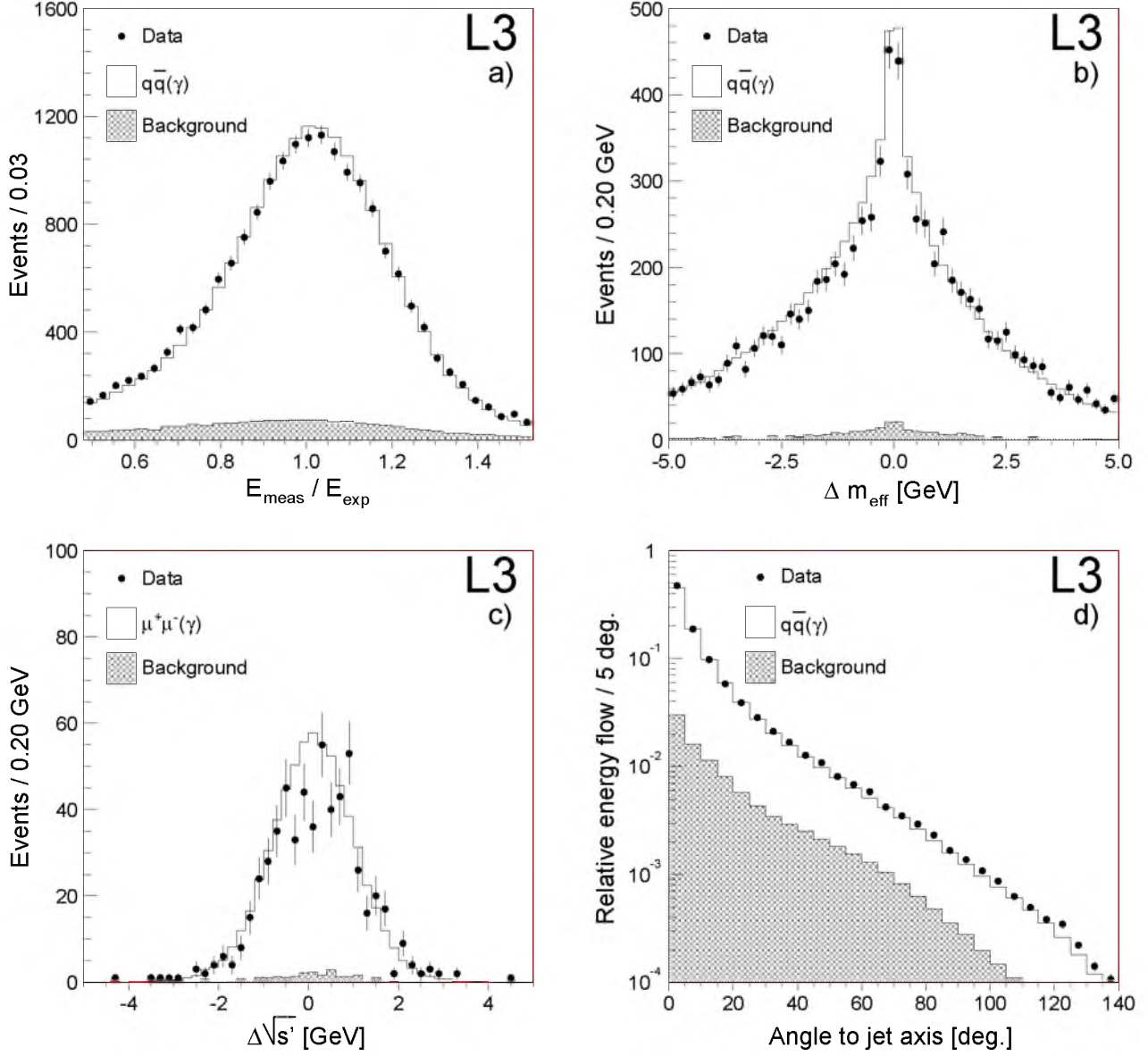


Figure 4: Variables used for systematic studies: a) ratio of measured jet energy and jet energy calculated from jet angles, b) difference, per event, of the effective mass as obtained using cluster or track angles, c) difference, per event, of the effective centre-of-mass energy, obtained by using polar angles from the direction of the muons or the corresponding calorimetric clusters, d) relative energy flow in a jet as a function of the angular distance from jet axis.