The following full text is a publisher's version.

For additional information about this publication click this link.
http://hdl.handle.net/2066/27751

Please be advised that this information was generated on 2019-04-18 and may be subject to change.
Amorphous dielectric behavior of incommensurate ferroelectric (Pb$_{0.45}$Sn$_{0.55}$)$_2$P$_2$Se$_6$ at low temperatures

M. M. Maior, S. A. J. Wiegers, F. C. Penning, H. van Kempen, and J. C. Maan

High Field Magnet Laboratory and Research Institute for Materials, University of Nijmegen, Nijmegen, The Netherlands

(Received 5 April 1996)

The complex dielectric susceptibility, $\varepsilon = \varepsilon' + i\varepsilon''$, of the incommensurate ferroelectric (Pb$_{0.45}$Sn$_{0.55}$)$_2$P$_2$Se$_6$ has been measured at various frequencies (300 Hz–100 kHz) and excitation voltages (0.15–7.5 V/mm) in the temperature range from 10 to 500 mK. It is found that $\varepsilon'$ of the crystal studied, similarly to amorphous materials, exhibits a minimum in the millikelvin temperature region. The real part of the dielectric constant at the high-temperature side of this minimum shows an appreciable frequency dependence, and the temperature where the minimum occurs, $T_{min}$, obeys a power-law dependence on the frequency. This amorphous dielectric behavior of an incommensurately modulated crystal can be described using the two-level system model. We have also observed a strong dependence of $\varepsilon'$ on the magnitude of the measuring electric field at the low-temperature side of the minimum. We suggest that this nonlinear dielectric behavior is associated with a variation of the height of the potential barriers in the two-level systems as a function of the electric-field strength.

I. INTRODUCTION

It is well known that at low temperatures ($T<1$ K) the properties of amorphous materials differ considerably from the properties of crystals. In particular, amorphous solids exhibit a linear temperature dependence of the specific heat, a $T^2$ dependence of the thermal conductivity, and a characteristic temperature and frequency dependence of ultrasonic and dielectric properties, which can all be accounted for by a phenomenological tunneling model. In this model it is assumed that in amorphous materials localized excitations with very low energy exist. These excitations are associated with the spatial disorder inherent for amorphous solids which distinguishes them from crystalline solids. Physically these excitations correspond to the movement of atoms or groups of atoms in a double-well potential. The energy splitting due to tunneling of atoms from one minimum to another needed to explain the properties of amorphous solids below 1 K is very small (less than $10^{-4}$ eV). In contrast to high temperatures, where the change of the configuration state occurs by thermal activation, at low temperature this occurs through a tunneling process. Although admittedly not amorphous, some ferroelectric crystals have been found to possess thermal and dielectric properties similar to those of amorphous materials. They exhibit a large dielectric response, which makes dielectric measurements on these materials a very sensitive tool for the investigation of amorphous behavior at very low temperatures.

In this paper we report measurements of the dielectric constant of a ferroelectric (Pb$_{0.45}$Sn$_{0.55}$)$_2$P$_2$Se$_6$ mixed crystal at temperatures below 1 K. At temperatures below $\sim$120 K this compound is in an incommensurate phase. The loss of translational symmetry along the vector of the incommensurate modulation renders the properties of this compound close to those of amorphous materials. Furthermore, the substitution of Sn atoms by Pb atoms causes some structural disorder in the crystal. The high value of the dielectric constant at low temperatures (the main contribution of which comes from the relaxation dynamics of the incommensurate modulation), as well as the two effects mentioned above make this crystal a very attractive object for the study of amorphous behavior of crystalline materials. This is particularly so with respect to the nonlinear dielectric effect (dependence of the dielectric constant on the applied ac electric field) observed in some amorphous materials. The nature of this effect has not yet been elucidated. It should be mentioned that in amorphous solids this effect is weak, which makes a quantitative and even a qualitative analysis difficult.

The technical importance of the material studied here has been demonstrated by its use as a sensitive and tunable thermometer at low temperatures, unaffected by large magnetic fields (up to 20 T). However, here we will focus on a comparison between the dielectric properties of (Pb$_{0.45}$Sn$_{0.55}$)$_2$P$_2$Se$_6$ and those of amorphous dielectric solids.

In the following we report on measurements of the dielectric constant of a (Pb$_{0.45}$Sn$_{0.55}$)$_2$P$_2$Se$_6$ crystal made as a function of temperature, applied electric field, and frequency. We show that the observed dielectric behavior resembles that of amorphous dielectric solids in many respects. We compare the observed frequency dependence of $\varepsilon$ with a calculation based on the two-level system (TLS) model and give a tentative explanation for the observed electric-field dependence.

II. EXPERIMENT

The (Pb$_{0.45}$Sn$_{0.55}$)$_2$P$_2$Se$_6$ crystal was grown using a Bridgman technique. The crystal (typical size 10 mm in diameter and 25 mm long) was cut and polished to obtain platelets (size 5×5×0.8) perpendicular to the [100] direction. The samples had sputtered electrodes, which were connected to stainless-steel coaxial wiring with silver paint and a small amount of epoxy.

The measurements of the temperature dependence of the dielectric constant at various excitation voltages (from 0.01 to 50 V/cm) at frequency 1 kHz were performed using an
The samples were mounted in the plastic mixing chamber of an adapted SHE dilution refrigerator. Temperatures down to 10 mK were measured with two types of thermometers in the mixing chamber: calibrated Speer 100 Ω carbon resistors and a CMN thermometer.

III. RESULTS

To demonstrate the similarity between amorphous dielectrics and the present compound, the temperature dependence of $\varepsilon'$ and $\varepsilon''$ at various frequencies are shown in Figs. 1 and 2, respectively. To compare experimental results with theory, the variations of the $\varepsilon'$ with temperature, frequency, or electric field are presented in reduced form: $\Delta \varepsilon'/\varepsilon'(T_0) = [\varepsilon'(T, \omega, U) - \varepsilon'(T_0, \omega_0, U_0)]/\varepsilon'(T_0, \omega_0, U_0)$. At high temperatures, where $\varepsilon'$ increases with temperature, we find a logarithmic temperature dependence for $\Delta \varepsilon'/\varepsilon'(T_0)$. For almost all frequencies a pronounced minimum in $\Delta \varepsilon'/\varepsilon'(T_0)$ is observed at $T = T_{\text{min}}$. Only at the lowest frequency used (300 Hz), the minimum in the $\Delta \varepsilon'/\varepsilon'(T_0)$ dependence is unobservable in the temperature region studied. With an increase in the frequency the minimum becomes observable and gradually shifts to higher temperatures. As is clear from Fig. 1, dielectric dispersion (frequency dependence of $\varepsilon$) occurs in the whole temperature region studied. However the depth of the dispersion at temperatures below $T_{\text{min}}$ is smaller than above $T_{\text{min}}$. Moreover, below $T_{\text{min}}$ the dispersion in question comes to a close: its edge lies at frequencies around 50 kHz. At the same time $\varepsilon'(T)$ above $T_{\text{min}}$ decreases monotonically as a function of frequency in the whole frequency range studied.

Concomitant with the minimum in $\varepsilon'$, we observe a maximum in $\varepsilon''$. The maximum in $\varepsilon''(T)$ gradually disappears as the frequency increases (Fig. 2): at $f \approx 10$ kHz the $\varepsilon''(T)$ curves flatten out. As the minimum of $\Delta \varepsilon'/\varepsilon'(T_0)$ is shifted with an increase in frequency, the part of the $\varepsilon''(T)$ curve corresponding to the rapid decrease in $\varepsilon'$ is shifted to higher temperatures as well. At $T > T_{\text{min}}$ the slope of $\Delta \varepsilon'/\varepsilon'(T_0)$ curve is nearly constant for all frequencies.

As can be seen from Fig. 1, the $\Delta \varepsilon'/\varepsilon'(T_0)(T)$ dependences are typical for amorphous dielectric behavior, which is characterized by a minimum. The temperature of the minimum, $T_{\text{min}}$, depends on the excitation frequency: $T_{\text{min}}$ is shifted upwards with increasing frequency. This behavior is well described by a power law: $T_{\text{min}}$ varies proportional to $\omega^{0.5}$.

To show the dependence of $\varepsilon'(T)$ on the strength of the applied ac electric field, the temperature dependence of the real part of the complex dielectric constant, $\varepsilon'$ at various excitation voltages at 1 kHz, is presented in Fig. 3. We present in Fig. 4 the $\varepsilon'(T)$ dependence only for the highest measuring voltages, since the low measurement accuracy of

---

**FIG. 1.** Temperature dependence of $\Delta \varepsilon'/\varepsilon'(T_0)$ for (Pb$_{0.45}$Sn$_{0.55}$)$_2$P$_2$Se$_6$ crystal at various frequencies: 1–300 Hz, 2–500 Hz, 3–1 kHz, 4–3 kHz, 5–5 kHz, 6–10 kHz, 7–30 kHz, 8–50 kHz, and 9–100 kHz at excitation voltage of 0.2 V/cm; $\varepsilon'(T_0)$ is defined here as $\varepsilon'$ at $T=10$ mK.

**FIG. 2.** $\varepsilon'(T)$ at various frequencies.

**FIG. 3.** Temperature dependence of $\varepsilon'$ for (Pb$_{0.45}$Sn$_{0.55}$)$_2$P$_2$Se$_6$ crystal at different excitation voltages 1–0.15; 2–0.30; 3–0.50; 4–1; 5–3.75; 6–7.5 V/cm.
smooth decrease in the dielectric constant beginning at \(\sim 50\) K continues until very low temperatures. This suggests that the amorphous part of the dielectric response of the crystal at very low temperatures is due to the incommensurate modulation.

An unexpected peculiarity in the behavior of \(\varepsilon'\) is apparent from Fig. 3, where \(\varepsilon'\) is shown to exhibit a strong dependence on the amplitude of the measuring field near the minimum and in temperature region below \(T_{\text{min}}\). The nonlinear effect observed becomes negligibly small at higher temperatures, at least in the voltages used.

The imaginary part of \(\varepsilon\), \(\varepsilon''\), grows with increasing temperature and after passing the maximum becomes nearly temperature independent. At the highest excitation voltages the maximum becomes less pronounced: \(\varepsilon''\) as a function of temperature shows a plateau. At higher temperatures \(\varepsilon''\) tends to the same value for various measuring fields.

IV. DISCUSSION

We first discuss the temperature dependence of the dielectric constant at fixed voltage but with varying frequency. As can be seen from the frequency-dependent data, the dielectric properties of the \((\text{Pb}_{0.45}\text{Sn}_{0.55})_2\text{P}_2\text{Se}_6\) crystal exhibit amorphous behavior at low temperatures: the occurrence of a minimum in \(\varepsilon'\) that shifts with frequency and a logarithmic temperature dependence on either side of the minimum. This fact has also been observed in some ferroelectric single crystals as well as in polycrystalline ferroelectrics\(^2,3\) and has been associated with the presence of ferroelectric domains. However, we have verified that amorphous behavior at low temperatures occurs also in single-domain ferroelectric samples. In particular, the characteristic minimum in \(\varepsilon'\) is observed in both single-domain and poly-domain crystal \(\text{Sn}_2\text{P}_2\text{Se}_6\) which crystallizes at low temperatures in the ferroelectric phase. Thus, the microscopical nature of the amorphous behavior of ferroelectrics at low temperatures is not yet entirely known.

The crystal we are dealing with is in the incommensurate phase at low temperatures. The large dielectric response in the incommensurate phase is caused by a high polarizability of the incommensurate structure. Upon lowering the temperature below 50 K the dielectric susceptibility of \((\text{Pb}_{0.45}\text{Sn}_{0.55})_2\text{P}_2\text{Se}_6\) sharply decreases. It has been suggested that this effect is caused by freezing of the relaxation dynamics of the incommensurate modulation pinned by defects\(^4\).
mic dependence of $\Delta \varepsilon'/\varepsilon'(T_0)$ on temperature occurs above $T_{\text{min}} \cdot$ At low frequencies the relaxation contribution remains large until very low temperatures. Because of this, the minimum in $\Delta \varepsilon'/\varepsilon'(T_0)$, in particular at 300 Hz, is not observable. As the frequency increases the relaxation contribution is gradually suppressed. At frequencies above 50 kHz the dielectric dispersion, at least below 50 mK, is not observed anymore. This implies that the relaxation contribution at these frequencies is completely suppressed and consequently the dielectric response measured resulted only from the resonant scattering mechanism. Indeed, as can be seen in Fig. 1, (dashed line) the temperature dependence of $\Delta \varepsilon'/\varepsilon'(T_0)$ is in this case logarithmic, which is in good agreement with the theory outlined above.

Thus, the deviation of the temperature behavior of $\Delta \varepsilon'/\varepsilon'(T_0)$ from logarithmic dependence with an approach to $T_{\text{min}}$ from above results from the fact that $\tau_{\text{min}}$ for certain TLS’s becomes comparable to $\omega^{-1}$ and subsequently those TLS’s do not take part in the relaxation process. However, $\tau_{\text{min}}$ cannot be considered as a characteristic quantity of the system, since it has a certain distribution defined by the distribution of energies $E$. A rough estimate of some average $\tau_{\text{min}}$ can be made, assuming that the conditions $\omega \tau_{\text{min}} \approx 1$ and $E = \Delta_0 = kT$ are satisfied at $T_{\text{min}} \cdot$ Using the temperature dependence of $\tau_{\text{min}}$ we have estimated the coupling constant $g$ from Eq. (1) to be approximately equal to $4.7 \times 10^{-10} \ J$. This value is of the same order of magnitude as for disordered ferroelectrics$^7$ and amorphous solids.$^5$ (The sound velocity $v_{\text{sa}}$ was taken from Ref. 8.)

Figure 5(b) shows the results of a numerical integration of a more elaborate expression from which Eq. (3) was obtained.$^7$ The presented curves have been calculated with $t_{\text{max}}/t_{\text{min}} = 10^{10}$ and $E_{\text{max}}/k = 10 \ K$. For comparison, in Fig. 5(a) the temperature dependences of the relaxation contribution of $\Delta \varepsilon'/\varepsilon'(T_0)$ derived from our experimental data are shown. The experimental curves were obtained by subtraction of the resonant contribution to $\varepsilon'$ from the observed $\varepsilon'$. The linear part of the $\varepsilon' (\ln T)$ curve at a frequency of 100 kHz below $T_{\text{min}}$ and the extrapolation of this dependence to higher temperatures was taken as the resonant contribution. It is evident from these results that the temperature-frequency dependences of the relaxation contribution to $\varepsilon'$ is adequately described [correct to the $(B \cdot P)^{-1}$ coefficient] by the TLS model.

Furthermore, in Fig. 6 we present a plot of $\Delta \varepsilon'/\varepsilon'$ versus $\ln(\omega)$. The observed linear dependence in a rather broad temperature region is consistent with Eq. (4). The deviation from logarithmic behavior occurring at temperatures close to $T_{\text{min}}$ (Fig. 6, curve 2) is due to $1/\omega$ becoming comparable to $\tau_{\text{min}}$.

Turning now to the imaginary part of the dielectric constant, a plateau in the temperature dependence of $\varepsilon''$ (Fig. 2) is expected in the two-level systems model. There it results from the fact that the number of two-level systems ignoring the condition $\Delta_0 = kT$ and $\omega \tau = 1$ (TLS for which $\tau_{\text{min}}$ is smaller than $\omega^{-1}$) remains constant. In reality, $\varepsilon''$ of the $\{\text{Pb}_{0.45} \text{Sn}_{0.55}\} \text{P}_2 \text{Se}_6$ crystal in this temperature region shows a slight temperature dependence. This discrepancy between the TLS model and experiment with respect to the temperature behavior of $\varepsilon''$ is very likely caused by a not completely flat density of states distribution. The plateau in the $\varepsilon''(T)$ dependence at high frequencies ($\approx 10 \ kHz$) and the slight temperature dependence of $\varepsilon''$ in this temperature region at lower frequencies indicate that the density distribution is not completely constant due to the states with relatively long relaxation times $[\tau \approx \omega^{-1} = (2 \pi \times 10 \ kHz)^{-1}]$. It should be mentioned that the temperature of the minimum in the temperature dependence of $\Delta \varepsilon'/\varepsilon'(T_0)$ correlates with the temperature of the onset of abrupt decrease of $\varepsilon''$. Less pictorially this correlation can be seen at low frequencies when the minimum in $\varepsilon''(T)$ is not clearly defined and $\varepsilon''(T)$ shows a maximum instead of a plateau.

Finally we comment on the observed strong nonlinear behavior of the dielectric constant in our measurements. Actually, a nonlinear dielectric effect is not foreseen in the TLS model. However, our set of experimental data allows us to draw some conclusions to the nature of the effect. The analysis...
A strong argument in support of this interpretation is the result of a study of the voltage dependence of $\Delta \varepsilon / \varepsilon'_{\infty}$ at various frequencies and temperatures shown in Fig. 7. At temperatures below $T_{\min}$ and at the lowest frequency used, the dielectric nonlinearity is the greatest and almost frequency independent. That means that the number of two-level systems being involved in the relaxation dynamics with an increase in the measuring voltage is frequency independent if $\tau_{\min}(U \rightarrow 0) > \omega^{-1}$. At higher temperatures, when $\tau_{\min}$ is getting comparable to or smaller than $\omega^{-1}$ the nonlinear effect becomes weaker. And finally, at temperatures where $\tau_{\min} \ll \omega^{-1}$ and therefore the number of two-level systems in the “frequency window” remains unaltered at various voltages, the dielectric nonlinear effect becomes negligible.

A decrease in the imaginary part of the dielectric constant below $T_{\min}$ in the TLS model is attributed to the fact that a certain number of TLS go beyond the condition $\omega \tau = 1$. Therefore, it may be safely suggested that with an increase in the amplitude of the measuring field, those two-level systems in the relaxation dynamics which are practically eliminated from the process at lower field because of high barriers, will start to play a role again. In the TLS model it can be considered as a reduction of the effective height of the potential barriers. The minimum relaxation time for such two-level systems is smaller in comparison with the two-level systems subjected to a weak external electric field. As a result the minimum in the $\varepsilon'(T)$ and kink in the $\varepsilon''(T)$ dependences shift to higher temperatures. Thus, the dielectric nonlinearity can be attributed to the renormalization of the height of the barriers.

A similar conclusion with respect to the nature of the observed nonlinear dielectric behavior was reached for another amorphous system at low temperature in Ref. 5. The nonlinear behavior of the polarizability of this system was attributed to a voltage dependence of the number of contributing two-level systems. The power dependence of polarizability of the form $\alpha - \alpha_{\infty} - U^{1/2}$ was calculated in Ref. 5. We repeat here that curiously the voltage dependence of $T_{\min}$ in (Pb$_{0.45}$Sn$_{0.55}$)$_2$P$_2$Se$_6$ is adequately described by a power-law dependence as well. We have not yet formed a quantitative theory on this point.

V. CONCLUSION

We have shown that the crystalline material (Pb$_{0.45}$Sn$_{0.55}$)$_2$P$_2$Se$_6$ possesses dielectric properties which resemble greatly those of amorphous dielectric solids. We have pointed out that the strong nonlinear behavior of the dielectric constant in these materials can possibly, at least qualitatively, be incorporated in the TLS model. A quantitative basis is still lacking.

ACKNOWLEDGMENTS

M.M.M. would like to thank the Nederlandse Organisatie voor Wetenschappelijk Onderzoek (NWO) for the financial support. Part of this work was supported by Stichting voor Fundamenteel Onderzoek der Materie (FOM) which in turn is financially supported by NWO. The authors thank Drs. S.W.H. Eijt for assistance in preparing the manuscript.

---

$^*$Permanent address: Institute for Solid State Physics and Chemistry, Uzhgorod State University, 29400 Uzhgorod, Ukraine.

$^1$Present address: High Magnetic Field Laboratory, Max-Planck Institut für Festkörperforschung-Centre National de la Recherche Scientifique, Boîte Postale 166, F-38042 Grenoble Cedex 9, France.


