Search for Subsolar-Mass Binaries in the First Half of Advanced LIGO’s and Advanced Virgo’s Third Observing Run

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(Received 1 October 2021; revised 18 March 2022; accepted 7 June 2022; published 5 August 2022)

We report on a search for compact binary coalescences where at least one binary component has a mass between 0.2 $M_\odot$ and 1.0 $M_\odot$ in Advanced LIGO and Advanced Virgo data collected between 1 April 2019 1500 UTC and 1 October 2019 1500 UTC. We extend our previous analyses in two main ways: we include data from the Virgo detector and we allow for more unequal mass systems, with mass ratio $q \geq 0.1$. We do not report any gravitational-wave candidates. The most significant trigger has a false alarm rate of 0.14 yr$^{-1}$. This implies an upper limit on the merger rate of subsolar binaries in the range [220 – 24200] Gpc$^{-3}$ yr$^{-1}$, depending on the chirp mass of the binary. We use this upper limit to derive astrophysical constraints on two phenomenological models that could produce subsolar-mass compact objects. One is an isotropic distribution of equal-mass primordial black holes. Using this model, we find that the fraction of dark matter in primordial black holes in the mass range 0.2 $M_\odot < m_{PBH} < 1.0$ $M_\odot$ is $f_{PBH} \equiv \Omega_{PBH}/\Omega_{DM} \lesssim 6\%$. This improves existing constraints on primordial black hole abundance by a factor of ∼3. The other is a dissipative dark matter model, in which fermionic dark matter can collapse and form black holes. The upper limit on the fraction of dark matter black holes depends on the minimum mass of the black holes that can be formed: the most constraining result is obtained at $M_{\text{min}} = 1$ $M_\odot$, where $f_{DBH} \equiv \Omega_{DBH}/\Omega_{DM} \lesssim 0.003\%$. These are the first constraints placed on dissipative dark models by subsolar-mass analyses.

DOI: 10.1103/PhysRevLett.129.061104

Introduction.—The first detection of gravitational waves from a binary black hole (BBH) merger in 2015 [1] has given us a new way to study the Universe. Since then, dozens of gravitational waves (GWs) have been detected in Advanced LIGO [2] and Advanced Virgo [3] data. The LIGO Scientific, Virgo, and KAGRA Collaboration (LVK) have reported the discovery of GWs from approximately fifty BBHs, binary neutron stars (BNSs), or neutron star black hole mergers [4–6]. Further analyses on public data [7,8] have resulted in the discovery of other compact binaries [9–13]. The gravitational-wave sources presented in [4,5] are already being used to answer key questions including cosmological measurements [14–18], analyses of the mass and spin distribution of compact objects, their formation channels [19–28], and tests of general relativity [29–31].

The black holes detected with gravitational waves can have masses larger than those discovered in x-ray binaries [32–35]. Several GW sources have challenged our understanding of astrophysics and stellar evolution [36–44]. One such source is GW190521 [37,38], a system whose most massive black hole might have a mass in the pair instability mass gap [38,45–47] (but see, e.g., Refs. [48–53]). With a mass of ∼142 $M_\odot$, the merger product of GW190521 was likely an intermediate mass black hole [38,54]. At the other end of the mass spectrum, the lightest object in GW190814, a ∼2.6 $M_\odot$ compact object, was either the heaviest neutron star or the lightest black hole ever discovered [39,55–58].

There are no widely accepted astrophysical channels that predict the formation of subsolar-mass (SSM) objects significantly more compact than white dwarfs. Since the end point of stellar evolution of massive stars is either a neutron star or a supersolar-mass black hole, the existence of a compact object below 1 $M_\odot$ would be indicative of a new formation mechanism, and potentially of new physics.

One possible scenario for the formation of SSM black holes is the collapse of overdensities in the early Universe, resulting in primordial black holes (PBHs) [59–62]. The amplitude of primordial fluctuations on very small scales [63,64], together with the equation of state of the early Universe [65,66], determines the mass and abundance of these objects [67,68]. In particular, their masses might be in the range probed by ground-based detectors [64,69,70], and so the mass spectrum is constrained by gravitational-wave data [71–78]. Alternatively, if dark matter has a sufficiently complex particle composition, which allows for chemistry and dissipation, small compact objects could form through the cooling and gravitational collapse of dark matter halos [79–81]. If dark matter is sufficiently dissipative, compact objects would form through pathways similar to known...
astrophysical channels, with details dependent on the interactions specific to the dark sector. Dissipative dark matter models that produce black holes in the subsolar to supersolar range were recently constrained in [82] by analyzing LVK data. Another possibility is that ultralight bosonic fields clump together to form self-gravitating, horizonless compact objects, known as boson stars [83–85]. Their maximum mass depends on the mass of the bosonic particle, hence they might be subsolar if the latter is larger than $10^{-10}$ eV/c$^2$ [86,87]. Finally, some dark matter models predict the formation of $\sim 1 M_\odot$ black holes through the accumulation of dark matter particles in neutron star cores [88–94]. Black holes formed via this class of mechanisms would have masses comparable to or smaller than the mass of the neutron star.

Searches for compact binaries with at least one SSM component have been carried out in both Initial LIGO [95–97] and Advanced LIGO and Advanced Virgo data [98,99]. Advanced LIGO and Advanced Virgo data have more recently been analyzed in [100–102] for systems with lower mass ratios and higher eccentricities than those considered by the LVK. No detections were reported. In this Letter, we report the results of searches for SSM compact binaries in the first half of Advanced LIGO and Advanced Virgo’s third observing run (this is the first half of the third science run, henceforth O3a). While no sources are detected, we obtain limits on the abundance of monochromatic PBHs and black holes formed by dissipative fermionic dark matter.

Search.—The data used for this Letter were collected during O3a by the Advanced LIGO and Advanced Virgo interferometers between 1 April 2019 1500 UTC and 1 October 2019 1500 UTC. The data characterization and calibration were performed as described in Refs. [5,103–105] with the addition of a nonlinear removal of spectral lines [106,107].

We present results from three matched-filter based pipelines: GSTLAL [108–110], MBTA [111], and PyCBC [112–117]. These analyses correlate the data with a bank of templates that model the gravitational-wave signals expected from binaries in quasicircular orbit. The bank is designed to recover binaries with (redshifted) primary mass $m_1 \in [0.2, 10] M_\odot$ and secondary mass $m_2 \in [0.2, 1.0] M_\odot$. The lower mass bound is set for consistency with previous searches [98,99] and to limit the computational cost of the search. We additionally limit the binary mass ratio, $q \equiv m_2/m_1$, to range from $0.1 < q < 1.0$. We include the effect of spins aligned with the orbital angular momentum in the gravitational waveform used in the template bank [118]. When a binary component $m_i$ has a mass $m_i \geq 0.5 M_\odot$, we allow for a dimensionless component spin up to 0.9. For compact objects with $m_i < 0.5 M_\odot$, we limit the maximum dimensionless spin to 0.1. We chose to restrict the possible spin magnitude in the low-mass part of the template bank, and not to allow for spin precession in order to reduce the computational cost. All three searches use the same template bank, constructed using a geometric placement algorithm [119] with a minimum match [120] of 0.97. This ensures that no more than 10% of astrophysical signals can be missed due to the discrete template placement. We use the TaylorF2 waveform [121–131], including phase terms up to 3.5 post-Newtonian order, but no amplitude corrections.

This search covers a larger mass and spin range than the last LVK analysis for SSM objects [99]. As a result, we require approximately twice as many template waveforms to effectively cover the search parameter space. To reduce the computational cost of the search, we analyze the data from 45 Hz instead of 15 Hz (as in the searches described in [5]). We estimate that this restricted bandwidth results in a maximum loss of signal-to-noise ratio of 9%, relative to what would be obtained filtering from 15 Hz. In turn, this results in a maximum reduction of the surveyed volume of 24%.

The three pipelines used in this Letter are described in more detail in Refs. [5,107]. Here, we only highlight differences in the way each pipeline has been run for this analysis, as compared to Refs. [5,107].

GSTLAL’s [108–110] detection statistic is unchanged relative to Ref. [5]. GSTLAL reweights waveforms in the template bank according to the characteristics of the expected population [132]. However, because SSM populations are yet to be observed we use a population model uniform in template density for this search. GSTLAL uses a similar procedure to the one it employed in Ref. [39] and includes all events from the analyzed period in the noise background to provide a conservative false-alarm-rate estimate. As in previous SSM searches [98,99] we do not use a gating scheme to account for loud noise artifacts [108]; instead we rely on statistical data quality information from the iDQ algorithm [133,134].

The MBTA pipeline splits the matched filtering in two different frequency bands in order to reduce the computational cost [135,136]. The setup of the search is unchanged with respect to Ref. [111] with two exceptions in order to adapt to the extended duration of low mass binaries: we use longer stretches of data to perform fast Fourier transforms (FFTs) and to calculate the noise power spectral density (PSD). For the FFT, we use from seconds to hundreds of seconds of data, while the PSD update time is up to 2 times longer than for standard BNS searches, depending on the frequency region under consideration.

The PyCBC pipeline [112,114–117,137] is unchanged relative to the configuration described in Ref. [107]. However, the sine-Gaussian veto described in Ref. [138] is not used, due to the low total mass of the template bank.

Results.—No gravitational-wave candidates were identified by any of the search pipelines. The most significant candidate has a false-alarm rate of 0.14 yr$^{-1}$. The lack of
detections can be recast as an upper limit on the merger rate of compact binaries. First, we estimate the sensitivity of each search pipeline for binaries in a given population. This can be done by computing the surveyed time volume:

$$\langle VT \rangle = T \int dz \frac{dV}{(1+z)dz} \epsilon(z),$$  \hspace{1cm} (1)

where $T$ is the analyzed time and $\epsilon(z)$ is the efficiency. The efficiency represents the fraction of astrophysical sources in the population which are detectable at a redshift $z$. The efficiency can be written as the probability that a binary with parameters $\theta$ is detectable (a quantity often referred to as $p_{\text{det}}(\theta)$ in the literature, e.g., Ref. [19]) integrated over the distribution of all parameters but the redshift. Therefore, in order to calculate Eq. (1) we need to assume a model for the mass distribution, spin distribution, sky positions, and orbital orientations [139–141]. Since we are only sensitive to nearby ($z \lesssim 0.12$) sources we treat the merger rate as constant.

Each pipeline estimates its sensitivity by simulating gravitational-wave signals from a population of SSM compact binaries and adding them into the collected data. We simulate a population with a uniform distribution of source masses in the range $0.2 \ M_\odot < m_1 < 10.0 \ M_\odot$ and $0.2 \ M_\odot < m_2 < 1.0 \ M_\odot$. We make an additional detector frame mass cut $m_1 < 10 \ M_\odot$ ($m_2 < 1 \ M_\odot$) due to the template bank coverage. We reject binaries with mass ratios exceeding the $0.1 < q < 1.0$ bounds of our search. The dimensionless spins are again assumed to be oriented in the direction of the angular momentum for computational reasons. The spin magnitude is uniform in the range $-0.1 < \chi_k < 0.1$ ($-0.9 < \chi_k < 0.9$) when $m_k < 0.5 \ M_\odot$ ($m_k > 0.5 \ M_\odot$). The sources are uniform in comoving volume, isotropically distributed on the sphere, and randomly oriented. We use the Planck “TT, TE, EE+lowP + lensing + ext” cosmology [142].

Since the search sensitivity is primarily a function of chirp mass, $\mathcal{M} \equiv (m_1 m_2)^{3/5} / (m_1 + m_2)^{1/5}$ [143], we break this population into nine equally spaced chirp mass bins in the range $0.17 \ M_\odot < \mathcal{M} < 2.39 \ M_\odot$ to determine $\langle VT \rangle (\mathcal{M})$. 

Treating each chirp mass bin as a different population, labeled by an index $i$, we can use the surveyed time-volume [144] $\langle VT \rangle_i$ for each chirp mass bin to estimate a frequentist upper limit (90% confidence interval) on the merger rate of that population by using the loudest event statistic [98,99,145]:

$$R_{90,i} = \frac{2.3}{\langle VT \rangle_i}.$$  \hspace{1cm} (2)

This is shown in Fig. 1 for the three pipelines. Although the pipelines generally agree, differences in background estimation and ranking statistics can lead to $\langle VT \rangle$ measurements that agree to within $\mathcal{O}(30\%)$. In what follows, we use the MBTA results as our fiducial rate constraint. Instrumental calibration errors were at most $\sim 3\%$ in amplitude in the bandwidth relevant for our analysis, and usually much smaller [103]. At most, they could contribute a $\sim 10\%$ uncertainty in our $\langle VT \rangle_i$ measurement. We follow [19,107] and neglect their impact in the remainder of this work.

**Modeling dark matter constraints.**—For any astrophysical model that could generate SSM binaries, the merger rate upper limits can be used to set constraints on the model parameters. Here, we focus on two such models: formation of PBHs catalyzed by three-body interactions [146], and dark-matter black holes formed by late-time gravitational collapse of dark matter substructure [80].

We use a phenomenological model for PBHs, rather than a first-principles model derived from an inflationary potential (see, for example, [147,148] for work connecting PBH distributions to inflationary models). Following [146] we assume PBHs produced at a single mass, and randomly distributed in space (see Supplemental Material [149] for details). This model predicts a merger rate given the mass of the PBHs in the binary and the abundance of PBHs, parametrized as a fraction of the dark matter density, $f_{\text{PBH}} = \Omega_{\text{PBH}} / \Omega_{\text{DM}}$. By using the merger rate upper limits derived above, we can thus obtain an upper limit on $f_{\text{PBH}}$ as a function of the component mass of the black holes in the binary [146]. This is shown in Fig. 2.

In this analysis, it is assumed that the two objects in the binary have the same mass. Because the detectors’ sensitivity depends more strongly on the chirp mass than on the mass ratio, for this analysis we assume that the rate upper limits we presented above (which included unequal mass binaries) can be used to assess the rate of equal mass...
binaries: $R_{00}(\mathcal{M}, q = 1) \approx R_{00}(\mathcal{M})$. Under these assumptions, we find $f_{\text{PBH}} \lesssim 6\%$ for PBHs in equal-mass binaries with component objects in the range $[0.2 - 1.0] M_\odot$. The method of Ref. [161] may be used to interpret these constraints on generic PBH mass functions. Recent work [162–164] has shown that there are a number of mechanisms that can alter and suppress the PBH merger rate from that derived in Ref. [146] and used here; these include binary disruption from other close PBHs, clusters of black holes, and matter inhomogeneities [165]. Suppression of the theoretical merger rate leads to looser constraints on the allowable fraction of the dark matter contained in PBHs.

Next, we consider a dissipative dark-matter model which consists of two fermions, oppositely charged under a dark version of electromagnetism, together with a massless dark photon. The dark matter can form bound states analogous to atomic and molecular hydrogen, and dissipate energy by radiative processes including Bremsstrahlung, recombination, and collisional excitation [166]. In dense regions, some dark matter gas can cool efficiently enough for gravitational collapse to proceed, eventually forming black holes [80]. In contrast to the PBH case, here we assume a power-law distribution for the black hole masses, with an unknown low-mass cutoff. We calculate an upper limit on the fraction of the dissipative dark matter that ends up in black holes ($f_{\text{DBH}} \equiv \Omega_{\text{DBH}}/\Omega_{\text{DM}}$) as a function of the low-mass cutoff for the dark matter black holes, marginalized over all other parameters of the model (e.g., the slope of the dark matter black hole mass function). More details on the model are given in Supplemental Material [149], and the marginalization procedures are discussed in depth in [82]. In Fig. 3, we show our constraints. The lowest upper limit is found at $M_{\text{min}} = 1 M_\odot$, where $f_{\text{DBH}} \lesssim 0.003\%$. No meaningful constraints can be set for $M_{\text{min}} \lesssim 2 \times 10^{-2} M_\odot$ since below that mass none of the black holes in the population would be detectable with the current sensitivity, hence a nondetection does not yield any constraint.

**Conclusions and outlook.**—Gravitational waves from compact object mergers provide a unique probe of dark matter structures on the smallest scales. Here, we have considered two possible dark matter candidates: PBHs and fermionic dark matter particles that can dissipate and form dark matter black holes. Both of these formation mechanisms can potentially produce both subsolar and supersolar mass black holes. We have focused on the SSM regime, which cannot be populated with black holes by any known astrophysical channel.

We have used three different algorithms to search the data from O3a for compact binaries in which at least one of the component objects had a mass between $[0.2 - 1.0] M_\odot$. We have found no candidates, and obtained upper limits on the merger rate of SSM black holes in the range $[220 - 24200] \text{Gpc}^{-3} \text{yr}^{-1}$. The upper limit is dependent on the chirp mass of the source and shown in Fig. 1. These upper limits can be recast into limits on the physical parameters of SSM black holes populations.
By considering a phenomenological model for SSM PBHs in which the compact objects are all formed with the same mass, we have obtained a limit on the abundance of these black holes as a function of their mass at formation: $f_{\text{PBH}} \lesssim 6\%$ in the mass range, as seen in Fig. 2. This significantly improves microlensing and supernova-lensing constraints in the same mass region as well as our previous constraints from Ref. [99], though we note that there are uncertain mechanisms that can reduce the expected PBH merger rate and raise the allowed value of $f_{\text{PBH}}$ [162,163,165]. Our work focuses on a small slice of the mass spectrum; we refer the reader to [167] for constraints on this model across the full parameter space. We have also considered a model for fermionic dissipative dark matter, parametrized by the abundance of the black holes it produces, and by their minimum mass. The most stringent limit is obtained at $M_{\text{min}} = 1\ M_{\odot}$ for which $f_{\text{DBH}} \lesssim 0.003\%$, as shown in Fig. 3. The constraint on the minimum mass can be interpreted in two ways. The most straightforward is as a constraint on the Chandrasekhar limit of the fermionic particle progenitors of dark matter black holes [80], which constrains the mass of a dark fermion analogous to the proton to be in the range 0.66–8.8 GeV/c$^2$. Additionally, the minimum mass of black holes formed when the dark matter gas cools and fragments depends on the coldest temperature the gas can reach, that is, on the dark matter chemistry. For the model we considered, this temperature is set by the energy difference of the lowest energy molecular radiative transition. Therefore, a constraint on the minimum mass of any dark black holes also implies a constraint on the dark molecular energy spacing, although the precise relationship depends on astrophysical modeling.

In the coming years, the sensitivity of Advanced LIGO and Advanced Virgo will continue to improve [168], and the global network of detectors is expected to grow with the addition of KAGRA [169] and LIGO-Aundha [170]. These advances will allow for more stringent limits in the near future [171], or even the detection of a SSM compact object.

This material is based upon work supported by NSF’s LIGO Laboratory which is a major facility fully funded by the National Science Foundation. The authors also gratefully acknowledge the support of the Science and Technology Facilities Council (STFC) of the United Kingdom, the Max-Planck-Society (MPS), and the State of Niedersachsen/Germany for support of the construction of Advanced LIGO and construction and operation of the GEO600 detector. Additional support for Advanced LIGO was provided by the Australian Research Council. The authors gratefully acknowledge the Italian Istituto Nazionale di Fisica Nucleare (INFN), the French Centre National de la Recherche Scientifique (CNRS), and the Netherlands Organization for Scientific Research (NWO), for the construction and operation of the Virgo detector and the creation and support of the EGO consortium.

The authors also gratefully acknowledge research support from these agencies as well as by the Council of Scientific and Industrial Research of India, the Department of Science and Technology, India, the Science & Engineering Research Board (SERB), India, the Ministry of Human Resource Development, India, the Spanish Agencia Estatal de Investigación, the Vicepresidencia i Conselleria d’Innovació, Recerca i Turisme and the Conselleria d’Educació i Universitat del Govern de les Illes Balears, the Conselleria d’Innovació, Universitats, Ciència i Societat Digital de la Generalitat Valenciana and the CERCA Programme Generalitat de Catalunya, Spain, the National Science Centre of Poland and the European Union—European Regional Development Fund; Foundation for Polish Science (FNP), the Swiss National Science Foundation (SNSF), the Russian Foundation for Basic Research, the Russian Foundation for the European Commission, the European Regional Development Funds (ERDF), the Royal Society, the Scottish Funding Council, the Scottish Universities Physics Alliance, the Hungarian Scientific Research Fund (OTKA), the French Lyon Institute of Origins (LIO), the Belgian Fonds de la Recherche Scientifique (FRS-FNRS), Actions de Recherche Concertées (ARC) and Fonds Wetenschappelijk Onderzoek—Vlaanderen (FWO), Belgium, the Paris Île-de-France Region, the National Research, Development and Innovation Office Hungary (NKFIH), the National Research Foundation of Korea, the Natural Science and Engineering Research Council Canada, Canadian Foundation for Innovation (CFI), the Brazilian Ministry of Science, Technology, and Innovations, the International Center for Theoretical Physics South American Institute for Fundamental Research (ICTP-SAIFR), the Research Grants Council of Hong Kong, the National Natural Science Foundation of China (NSFC), the Leverhulme Trust, the Research Corporation, the Ministry of Science and Technology (MOST), Taiwan, the United States Department of Energy, and the Kavli Foundation. The authors gratefully acknowledge the support of the NSF, STFC, INFN, and CNRS for provision of computational resources. Funding for this project was provided by the Charles E. Kaufman Foundation of The Pittsburgh Foundation and the Institute for Computational and Data Sciences at Penn State. This article has been assigned the document number LIGO-P2100163-v8.

Note added.—Recently, Ref. [172] reported results on a search for binaries with no spin and component masses $m_1 \in (0.1\ M_{\odot}, 7.0\ M_{\odot})$, $m_2 \in (0.1\ M_{\odot}, 1.0\ M_{\odot})$ in O3a data. That search also reported no detections.

061104-5
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