Subterahertz and terahertz spin and lattice dynamics of the insulating ferromagnet PbMnBO₄

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Orthorhombic PbMnBO₄ is a rare example of an insulating ferromagnet in which the magnetic properties, in particular the strong magnetic anisotropy, are determined by the Mn³⁺ Jahn-Teller ion. Here, we report on the detailed investigation of magnetic excitations in the subterahertz and terahertz frequency ranges, as well as lattice excitations in the terahertz range. Using polarized azimuthally resolved Raman spectroscopy, four branches of magnetic excitations were observed and assigned to one acoustic and three optical one-magnon modes. The coupling between ferromagnetic ordering at \( T_C = 31 \) K and the Jahn-Teller distortions of \([\text{MnO}_6]\) octahedra due to the spin-phonon interaction was directly observed for some specific phonon modes involved in these distortions. A spin-wave Hamiltonian was developed that allowed us to determine a unique set of exchange and effective anisotropy parameters. The intensity ratio of the anti-Stokes to Stokes acoustic magnon peaks is found to be anomalous and directly indicates the involvement of the magneto-optical parameters in the magnetic Raman scattering process.

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I. INTRODUCTION

A new field of magnetism, positioned as antiferromagnetic spintronics [1–5], promises to make significant progress towards higher frequencies for recording and reading information technology. However, many flourishing prospects in this field are blocked by difficulties in their practical implementation, mainly since reading information from antiferromagnets is not at all a trivial process due to the absence of a macroscopic magnetization intrinsic for ferromagnets. Additionally, the spin dynamics in ferromagnets is typically restricted to the few gigahertz to 10 GHz frequency range, which is much lower than the subterahertz and terahertz frequency range typical for antiferromagnets.

Nonetheless, the frequency range of ferromagnets can be extended by using materials with high magnetic anisotropy, which determines the frequency of ferromagnetic resonance (FMR). Remarkably, in some ferromagnets the FMR frequency can reach the terahertz region. Notable cases are CrI₃ [6,7] and VI₃ [8], with FMR frequencies of 2.3 and 0.55 THz, respectively. Thus, the search for potentially useful ferromagnetic systems continues; it started with long-known metallic films [9,10] and has moved to engineered heterostructures. Insulating ferromagnets are of particular interest due to the absence of the losses associated with itinerant electrons. Recently, two-dimensional limit engineering of the ferromagnetic structures was proposed in [11]. Also quasi-one-dimensional systems are appealing, such as the spin-anisotropic frustrated magnet FeI₂ in which hybridized quadrupolar excitations were observed, the physics of which is governed by \( S = 1 \) ferromagnetic chains [12]. However, even the occurrence of insulating ferromagnets is extremely rare, which undoubtedly restrains further progress on their potential applications.

One interesting example among the small group of bulk isostructural insulating magnets is PbMnBO₄. It belongs to an orthorhombic PbMBO₄ family, although other known members of the family with \( M = \text{Cr}^{3+} \) and \( \text{Fe}^{3+} \) are antiferromagnets. The synthesis and crystal and magnetic structures of PbMnBO₄ with Curie temperature \( T_C = 31 \) K and Weiss temperature \( \Theta = 52.7 \) K were described, along with magnetic susceptibility, x-ray, and neutron diffraction studies, in [13]. Magnetic susceptibility, heat capacity, and FMR for PbMnBO₄ were thoroughly investigated using high-quality single crystals in [14,15]. It was shown that the large single-ion-like anisotropy of this material results in a FMR gap of 112 GHz, which is unusually high for a ferromagnet. The mixed compound PbMn₁₋ₓFeₓBO₄ doped by Fe ions was studied in [16], which demonstrated that a small partial substitution leads to an increase of the Curie temperature, enhancement of the magnetic anisotropy, and reduction of the saturation magnetization. Nanofibers of PbMnBO₄ prepared with an electrospinning method were suggested for practical application in the field of nonlinear optics as described

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in [17]. Another study observed pronounced magnetostriction and excellent magnetocaloric performance of PbMnBO$_4$ in the vicinity of $T_C$ [18]. Several attempts based on the density functional theory (DFT) calculations were undertaken to predict the exchange structure [19,20]. Theoretical works on a nontrivial spin orientation transition and the noncollinear magnetic moments caused by the site-dependent single-ion anisotropy should also be noted [21,22].

Raman scattering on the structurally identical antiferromagnet PbFeBO$_4$ was conducted in [23], in which pronounced spin-phonon coupling was observed for some phonons; scattering on magnetic excitations, both an optical magnon and an intense two-magnon band, was observed and interpreted in terms of a linear spin-wave theory (LSWT) [24]. However, up to now, there have been no reports on lattice dynamics and spin dynamics beyond the FMR mode for PbMnBO$_4$. Thus, the goal of the present paper is a detailed investigation of the lattice and spin dynamics as a function of temperature and static magnetic field.

This paper is organized as follows. In Sec. II the crystal and magnetic structures of PbMnBO$_4$ are briefly reviewed. In Sec. III, the experimental details of the Raman setup for both temperature and magnetic field measurements are presented. Next, the two main sections follow for lattice dynamics (Sec. IV) and spin dynamics (Sec. V). In both sections, the polarization, temperature, and field-dependent properties of the observed excitations, phonons, and magnons are discussed in detail. Section V E is dedicated to the construction of the Heisenberg Hamiltonian with a minimal set of parameters and the derivation of the exchange and anisotropy constants based on experimentally observed magnetic excitations using linear spin-wave theory calculations. Section VI sums up and concludes the paper.

II. CRYSTAL AND MAGNETIC STRUCTURES

The crystal structure of PbMnBO$_4$ is characterized by the $mmm$ point group and the $Pnma$ space group (No. 62, $Z = 4$), and the lattice parameters determined with the use of x-ray diffraction (XRD) are $a = 6.7062$, $b = 5.9429$, and $c = 9.6418$ Å [13]. PbMnBO$_4$ is isostructural to PbFeBO$_4$ and other orthoborates [25–27], which have many structural similarities, such as edge-shared oxygen octahedra forming chains running along the $b$ axis and interconnected with rigid covalent [BO$_3$] groups and highly distorted square pyramid [PO$_4$] groups, as shown in Fig. 1. However, in contrast to both PbCrBO$_4$ and PbFeBO$_4$, in which Cr$^{3+}$ and Fe$^{3+}$ ions are in the orbitally nondegenerate state, the ground state of the Mn$^{3+}$ ions is orbitally degenerate, and therefore, these ions are Jahn-Teller active, which leads to more pronounced distortion (elongation) of the [MnO$_6$] octahedra [28,29]. Nevertheless, this distortion does not lead to an overall change in crystallographic symmetry. It was previously observed in structural experiments [13] and was proposed [14] as a leading mechanism to explain the ferromagnetic ground state (contrary to the antiferromagnets PbFeBO$_4$ and PbCrBO$_4$). One can expect that a pronounced difference between the Cr/Fe and Mn crystals should, in principle, be directly observed in Raman scattering spectra by comparing the phonons of the same symmetry.

III. EXPERIMENT

High-quality single crystals used in our study come from the same batch as those used in [14,15], in which a detailed description of the crystal growth process can be found. The bulk crystals are opaque, but the thin spalls are deep red colored, indicating a transparency window in the red part of the visible spectral range.

An excitation source of 660 nm (Thorus, LaserQuantum) was used to match the transparency window of PbMnBO$_4$ to maximize the scattering volume, reduce laser overheating, and avoid any resonance effects in light scattering. Careful examination of the laser power effect showed that a 0.5 mW excitation power provides negligible overheating while still maintaining a good signal-to-noise ratio. A set of Bragg filters (Optigrate) was used in a beam splitter/rejection filters backscattering configuration. The scattered light was dispersed in a FHR1000 (HORIBA) 1 m spectrometer with a 1200 lines/mm grating and registered by a liquid-nitrogen-cooled PyLoN CCD detector [Princeton Instruments].

Temperature-dependent measurements were done using a helium flow cryostat (Oxford Instruments) with temperature stability better than 1 K. Samples were mounted on the cold finger using silver paste. A plan achromatic long working distance objective MSPlan 50× (Olympus) was used both...
to guide the excitation light to the sample and to collect the scattered light.

Low-temperature azimuthal and magnetic field dependences were both measured in a helium bath cryostat with samples in the exchange helium gas at a base temperature of 4.2 K. High-field experiments were performed at the High Field Magnet Laboratory (HFML, Nijmegen) in a 50 mm bore Florida-Bitter magnet with a maximum dc magnetic field of 30 T. A singlet objective (with the numerical aperture of 0.68) with an effective focal length of 3.1 mm and anti-reflective coating suitable for the spectral range of interest was used for both the excitation and collection of scattered light. In all experiments, the same set of achromatic half-wave plates and Glan-Taylor polarizers (Thorlabs) were used to selectively probe specific elements of the Raman tensors. Experimental setups were controlled with the modular PYTHON suite QUDI [30].

IV. LATTICE DYNAMICS

A. Overview

With the known structure [13], the group-theoretical analysis is applied for the determination of the number and symmetry of the possible phonon modes:

\[
\Gamma = 11A_g + 7B_{1g} + 11B_{2g} + 7B_{3g} + 10A_u + 14B_{1u} + 10B_{2u} + 14B_{3u},
\]

where one of the whole set of \( B_{1u}, B_{2u}, \) and \( B_{3u} \) modes is acoustic phonons and all others are optical ones. Since PbMnBO₄ is centrosymmetric, the mutual exclusion principle dictates that even (gerade) modes are observed only in Raman scattering and the odd (ungerade) ones are observed only in the infrared (IR) spectra. In the present Raman experiments, only even modes are probed.

Selection rules are well described with the use of the Raman tensor formalism:

\[
A_g = \begin{pmatrix} \langle a|e^{i\phi} & 0 & 0 \\ 0 & |b|e^{i\phi} & 0 \\ 0 & 0 & |c|e^{i\phi} \end{pmatrix},
\]

\[
B_{1g} = \begin{pmatrix} 0 & |d|e^{i\phi} & 0 \\ |d| & 0 & 0 \\ 0 & 0 & 0 \end{pmatrix},
\]

\[
B_{2g} = \begin{pmatrix} 0 & 0 & |e| \\ 0 & 0 & 0 \\ |e| & 0 & 0 \end{pmatrix},
\]

\[
B_{3g} = \begin{pmatrix} 0 & 0 & 0 \\ 0 & 0 & |f| \\ 0 & |f| & 0 \end{pmatrix}.
\]

It should be noted that in the case of optically anisotropic noncubic crystals which possess birefringence and dichroism for the incident and scattered light and when the polarization deviates from the main crystallographic axes, the Raman tensor elements should have a complex phase factor [31–33]. For the intermediate polarization directions between the main crystallographic axes, the classical formalism (zero phase difference) predicts monotonic dependences for angles between crystallographic axes for parallel \((e_i \parallel e_j)\) configurations. However, when complex phases are taken into account, the intensity behaves differently for the intermediate states of the light polarization; namely, it has additional, but still nonzero, minimum, and the intensity ratios between parallel and crossed configurations are also strongly affected. All these indicators can be directly captured in azimuthally resolved experiments.

Since the crystal structures of PbMnBO₄ and PbFeBO₄ are the same and the atomic masses of the Mn and Fe ions are comparable, one can expect that the phonon spectra of these two crystals should be reasonably similar. Previous studies of the lattice dynamics of PbFeBO₄ using powdered samples [34] and single crystals [23] showed that the whole spectrum can be divided into three main parts: (i) the low-energy part (up to 200 cm⁻¹), which should mainly correspond to phonons involving heavy Pb ions; (ii) the middle-energy part (200–600 cm⁻¹), which is related to transition metal ions; and (iii) the high-energy part (600–1300 cm⁻¹), which involves rigid covalent triangle \([BO_3]\) groups. Mainly in the high-energy part, beginning from about 800 cm⁻¹, a clear contribution of multiphonon scattering can be observed, consisting of broad nonsymmetric bands, additionally confirming the high structural quality of the single crystals.

As can be seen from Fig. 2, polarized Raman spectra of PbMnBO₄ share most of the above-mentioned features observed in PbFeBO₄. The low-energy part of the spectra...
consists of a number of very sharp phonon lines, the lowest one being at 49.4 cm\(^{-1}\), whose linewidths are, in fact, resolution limited. The main focus in our study was placed on the low-energy part of the spectra (\(\sim 20-400\) cm\(^{-1}\)) since we expected to observe spin dynamics exactly in this range. All temperature, polarization, and magnetic field dependences were studied in this low-energy spectral range.

The advantage of the present study of PbMnBO\(_4\) in comparison with the previous study of PbFeBO\(_4\) [23] is the ability to get direct access to all simple crystal faces, namely, (100), (010), and (001). This allowed us to achieve polarization and geometrical conditions consistent with the pure selection rules and thus undoubtedly distinguish the phonons of \(B_{1g}\), \(B_{2g}\), and \(B_{3g}\) symmetries. Moreover, performing azimuthal scans allowed us to further refine the symmetry assignment of overlapping modes.

All Raman lines in the spectra were fitted with the sum of Voigt peaks in order to accommodate for nonintrinsic broadening of the lines using FITKY software [35]. The extracted frequencies are listed in Table I and compared with the experimental values for PbFeBO\(_4\) [23] and DFT calculations [26]. It can be seen that the frequencies of most modes coincide well in PbMnBO\(_4\) and PbFeBO\(_4\) crystals, especially in the low- and middle- to high-energy regions; however, those phonons, the normal modes of which involve strong distortions of the [MnO\(_6\)] octahedra, significantly differ from those for similar modes in the PbFeBO\(_4\) crystal. The high-energy modes are also quite different, probably because they correspond to boron-oxygen groups connecting [MnO\(_5\)] chains and therefore are also distorted. The substantial deviation for modes corresponding to the [MnO\(_6\)] octahedra (see the yellow region in Fig. 3) is remarkable and can be used to verify the hypothesis that specific lengths and angles for the M-O-M bonds are responsible for entirely different ferromagnetic and antiferromagnetic ground states of PbMnBO\(_4\) and PbFeBO\(_4\), respectively, as found in the DFT calculations.

It should be noted that the detailed information on lattice dynamics is exceptionally beneficial for comparison with the results of \textit{ab initio} methods since they combine multiple observables, in this case the frequencies of the 36 even phonon modes, which is way more than in the typical static structural data for cell dimensions and ionic coordinates. Thus, this can lead to models of exceptional precision. Moreover, in most Raman experiments only the frequencies of the phonons are available, with the addition of their symmetries in polarized experiments. By performing azimuthal-resolved measurements we were able to extract Raman tensor elements for each individual phonon. Such elements can be used to
further advance DFT calculations, which in turn could shed light on the subtle aspects of the unique ferromagnetic ground state of PbMnBO4 and unveil fundamental mechanisms of the Jahn-Teller effect and magnetic interaction.

B. Phonon selection rules

The large number of the overlapping phonons with different selection rules, intensities, and half-widths impedes their correct assignment, and thus, a detailed investigation is required to determine the phonon symmetry, the contribution of complex phases, and the reliable determination of Raman tensor elements. In order to fulfill these tasks, full 360° azimuthal scans were performed on the three main crystallographic faces of the PbMnBO4 single-crystal samples, and the results of this study are shown as angular-dependent spectral maps in Fig. 4. All polarization measurements reported in this section were done at T = 4.2 K. Strong anisotropy for the in-plane angular dependences is observed as expected for the low-symmetry PbMnBO4 crystal. Minor leakage of some modes in forbidden configurations was typically less than a few percent in integrated intensity and could be explained by depolarization effects on the optical elements and in the sample itself, as well as by the use of an objective with high numerical aperture, leading to a collection of light deviating from the normal. A small deviation of the sample normal from the main crystallographic axes can also contribute to leakage and cannot be ruled out.

Despite the fact that the mode symmetry can be directly deduced from the maps, it is more informative to extract the integral angular dependence of the phonon intensity for each phonon, as shown in Figs. 5 and 6 for the $A_g$ and the $B_g$ phonons, respectively.

The angular intensity variations [31] are described according to the following equation:

$$I = |\mathbf{e}_i \mathcal{R} \mathbf{e}_s|^2,$$

where $\mathcal{R}$ corresponds to a particular Raman tensor from Eq. (2) and $\mathbf{e}_i$ and $\mathbf{e}_s$ are the polarization vectors of the excitation and scattered radiation, respectively. To describe the observed azimuthal variations, these vectors are simultaneously rotated within the selected plane in parallel ($\mathbf{e}_i \parallel \mathbf{e}_s$) and perpendicular (crossed; $\mathbf{e}_i \perp \mathbf{e}_s$) configurations. Several conclusions can be drawn immediately on the basis of only the angular-dependent polarization measurements and the data fitting using Eq. (3): (i) For most $A_g$ phonons, the Raman tensor elements strongly vary, and in some particular cases, e.g., for the 224.7 and 283.9 cm$^{-1}$ modes, difference becomes so large that azimuthal response looks almost purely two-lobed. (ii) The intensity of the $A_g$ modes in the parallel configuration have well-defined minima for angles between the main crystallographic axes, which cannot be explained assuming only real Raman tensor elements. These results confirm the necessity of taking into account the complex phase formalism [31–33]. (iii) Surprisingly, the $B_{1g}$ modes observed within the $ab$ plane should also have a complex phase between the nondiagonal elements. The effects of such complex phases are shown in the bottom right corner in Fig. 6. Notably, the nonzero phase will lead to a finite intensity in the crossed polarization geometry for angles between the crystallographic axes, which cannot be explained assuming only real Raman tensor elements. The results confirm the necessity of taking into account the complex phase formalism [31–33]. (iii) Surprisingly, the $B_{1g}$ modes observed within the $ab$ plane should also have a complex phase between the nondiagonal elements. The effects of such complex phases are shown in the bottom right corner in Fig. 6. Notably, the nonzero phase will lead to a finite intensity in the crossed polarization geometry for angles between the crystallographic axes, which cannot be explained assuming only real Raman tensor elements. The results confirm the necessity of taking into account the complex phase formalism [31–33].
FIG. 5. Azimuthal plots of the integral phonon intensity for the $A_g$ modes measured at 4.2 K. Each column corresponds to a particular phonon with the energy shown on top, and each row corresponds to a different crystal orientation. Note that the scale within each column is the same. Experimental data are shown as colored circles, and solid black lines show model calculations.

based solely on the Raman scattering study. For any arbitrary crystal orientation, the $R$ tensor in Eq. (3) should be rotated according to a $RR^{-1}$ transformation, where $R$ is the rotation matrix.

C. Temperature effects on phonons

Temperature dependences of phonon excitations in magnetically ordered crystals allow probing the spin-phonon interaction which is typically manifested as hardening or softening of particular modes [36]. As a rule, this interaction can be conveniently described on a phenomenological level by the following equation [37]:

$$\Delta \omega = \lambda \langle S_i S_j \rangle,$$

where the static part of the spin-spin correlation function is proportional to the square of the Brillouin function and $\lambda$ is the spin-phonon coupling coefficient. On the microscopic level,

FIG. 6. Azimuthal dependences of the integral intensity of the $B_g$ phonons at $T = 4.2$ K. In the bottom right corner, the effect of the phase difference on the nondiagonal element of the Raman tensor on the shape of the angular dependence is shown for the four different values of the apparent phase.
the coefficient $\lambda$ should be proportional to the derivative of the exchange interaction on a normal mode coordinate because this contribution to the phonon frequency is based on the modulation of the exchange interaction by a specific phonon mode. However, since normal coordinates are inaccessible, it is impossible to estimate the spin-phonon effect on the mode. However, since normal coordinates are inaccessible, it is impossible to estimate the spin-phonon effect on the mode. However, since normal coordinates are inaccessible, it is impossible to estimate the spin-phonon effect on the mode. However, since normal coordinates are inaccessible, it is impossible to estimate the spin-phonon effect on the mode. However, since normal coordinates are inaccessible, it is impossible to estimate the spin-phonon effect on the mode.

To conclusively extract the spin-phonon contribution it is necessary to disentangle it from the usual anharmonic contributions, which we will describe on a phenomenological level. This contribution affects both the phonon frequency and the half-width (inversely proportional to the lifetime) and is usually understood through three- and four-phonon relaxation processes, which we will describe on a phenomenological level.

Most phonons do not show any noticeable anomalies at the transition temperature [within the resolution of the setup, e.g., see Fig. 7(a)]. However, some of them in the range of 220–430 cm$^{-1}$ demonstrate very pronounced frequency shifts with opposite signs. No FWHM changes could be registered, which points to a spin-phonon/exchange striction mechanism rather than to renormalization due to relaxation processes involving, for example, magnetic excitations.

Since only a small number of phonons are affected, one may assume that the origin of this effect is, indeed, the spin-phonon interaction and not the change in the unit cell volume. Another argument to support this hypothesis is that most of the phonons demonstrating the spin-phonon coupling are directly related to the $[\text{MnO}_6]$ octahedron, and this is in accordance with the DFT results obtained for PbFeBO$_4$ [34].

Pankrats et al. [14] observed an almost complete absence of the magnetodielectric contribution in the ordered phase and concluded that PbMnBO$_4$ has significantly weaker coupling between the lattice and magnetic subsystems in comparison with PbFeBO$_4$ [40]. However, our observation of a pronounced spin-phonon interaction for several phonons and, even more importantly, magnetostriction effects shows the apparent interaction between these two subsystems. It is known that the magnetodielectric contribution to the dielectric susceptibility originates from the odd IR-active phonons [41]. In view of this, we can assume that mostly even Raman-active phonons are experiencing frequency shifts due to magnetic ordering which are not manifested in the susceptibility and that careful measurements of IR-active, odd phonons would be beneficial.

Another interesting aspect is the transformation of the Raman tensor elements relevant to the 224.7 cm$^{-1}$ mode as a function of temperature, in particular when crossing $T_C$ (see Fig. 8). Our azimuthally resolved data at 4.2 K and the temperature dependence of the intensity for a number of selected polarizations, for example, for the $c(aa)c$, $b(aa)b$, $a(aa)a$, and $b(aa)b$ phonons are experiencing frequency shifts due to magnetic ordering which are not manifested in the susceptibility and that careful measurements of IR-active, odd phonons would be beneficial.

FIG. 7. Spin-phonon interaction of different phonon modes observed in the ferromagnetic phase of PbMnBO$_4$. The logarithmic temperature scale was applied to highlight the low-temperature region.

FIG. 8. Temperature (logarithmic scale) dependence of the 224.7 cm$^{-1}$ phonon mode peak intensity in different polarizations. Insets demonstrate transformations of the azimuthal dependences of the Raman tensor elements deep in the ferromagnetic (blue shaded area) and paramagnetic (red shaded area) phases.
related phenomena. The response to static magnetic fields will contribute to better understanding of the spin-phonon interaction and related phenomena.

D. Field-dependent lattice dynamics

It was expected that no effect of a magnetic field on the lattice subsystem would be observed due to rather weak spin-phonon coupling. However, a few modes showed subtle spectral shifts accessible due to the high resolution of the experimental setup. The observed effect is rather weak, making it necessary to mitigate the extrinsic influences such as long-term drift of the setup and slight shifts in the sample position when the field is applied. Thus, the data are presented in the following way:

$$\Delta \omega_i(H) = \omega_i(H) - \omega_i(30\,^\circ\!\text{C}) - \frac{1}{N} \sum_{j \neq i} \omega_j(H),$$

(7)

where $\omega_i(H)$ is the field dependence of the frequency of the selected mode, $\omega_i(30\,^\circ\!\text{C})$ is the frequency of the same mode at 30 T, and the last term is the mean frequency of all other phonons $N$. This normalization allowed us to evaluate and plot the effect of the magnetic field on each sufficiently narrow specific phonon mode, as shown in Fig. 9. Only the 224.7 and 283.9 cm$^{-1}$ modes out of the whole set in the low-energy region (<400 cm$^{-1}$) experience a pronounced continuous shift up to the spin-flip transition when the field is applied along the hard c axis. As for the case with $H \parallel b$ these phonons have an intensity close to zero, as can be seen in Fig. 5, thus making it impossible to conclusively observe the shifts in Faraday geometry.

Surprisingly, these modes are the same ones that show clear spin-phonon coupling [see Figs. 7(b) and 7(c)], namely, the 224.7 cm$^{-1}$ mode with $\lambda = 2.4$ cm$^{-1}$ softens by $\approx 0.4$ cm$^{-1}$, while the 283.9 cm$^{-1}$ mode with $\lambda = -0.26$ cm$^{-1}$ softens by $\approx 0.1$ cm$^{-1}$, suggesting a correspondence between the magnitudes but with an opposite sign. The origin of this effect can be presumably attributed to the magnetostriiction when the applied magnetic field couples with the lattice, resulting in a change in the lattice parameters and, consequently, in a modification of the phonon frequency. However, this scenario seems to be unlikely because only two modes demonstrate such behavior, while the larger part of the phonon spectrum is expected to immediately reflect any change in the crystal lattice parameters with the corresponding Grüneisen parameters.

An alternative hypothesis is similar to the spin-phonon effect, which is phenomenologically described (see Sec. IV C) as an additional contribution to the phonon force constants appearing at the transition from the paramagnetic to the ordered state [e.g., ferromagnetic (FM) or antiferromagnetic (AFM)] due to the presence of magnetic order. Thus, the observed effect can be attributed to a field-dependent contribution to the spin-phonon coupling or a specific exchange-striction affecting only bonds and/or groups, most likely related to the [MnO$_6$] octahedra. However, the complete understanding of the observed effect requires application of additional complementary techniques such as XRD or dilatometry in order to determine the changes in the static parameters, i.e., cell constants, across $T_C$ and spin orientation transitions for hard and intermediate axes. Additionally, it would be nice to add thorough $ab$ initio calculations (the data presented in Sec. IV A) on top of the Grüneisen parameters for further deconvolution of the static and dynamic contributions to the phonon energy renormalization.

V. MAGNETIC DYNAMICS

A. Overview

At $T_C = 31$ K PbMnBO$_4$ undergoes ferromagnetic ordering [14], which necessarily results in hosting well-defined magnetic excitations. The number of branches, which are, within LSWT formalism, purely transverse, equals the number of magnetic ions in the magnetic unit cell; in our case $N = 4$. Only one of the four expected modes, namely, the lowest-in-energy acoustic magnetic excitation or FMR mode, was previously observed [14] with the use of electronic spin resonance at 112 GHz $\approx 3.7$ cm$^{-1}$. In fact, a mode with such a low frequency is nearly the limit of continuous-wave Raman spectroscopy. Despite these experimental challenges we explored both the ultralow- and intermediate-frequency regions and registered the above-mentioned lowest-frequency modes.
mode along with three others. To understand the origin of these modes, we used a complementary approach: First, by measuring full azimuthal dependences on the three main orthogonal faces, we were able to extract Raman tensors, revealing the mode symmetries, which are essentially different from the phonon ones. Second, we analyze the temperature dependences of observables such as frequency, full widths, etc., which also demonstrated strong deviations from the typical phonon behavior. Third, these modes manifest an expected response in an applied magnetic field. Fourth, both the frequency and field dependence of the observed excitations could be well described within a spin-wave theory formalism, as shown in Sec. VE. These observations allowed us to conclude that the four modes observed below $T_C$ originate from one-magnon excitations.

B. Magnon polarization and selection rules

Polarization-dependent measurement of the ultralow-energy part ($-20$–$20$ cm$^{-1}$) at 4.2 K and in zero applied field showed exotic symmetries of the magnetic excitations in both the Stokes (S) and anti-Stokes (AS) regimes, as shown in Fig. 10. While the 12 cm$^{-1}$ optical magnon at 4.2 K in zero field has a diagonal tensor of $A_g$ symmetry similar to phonons, the lowest- and highest-frequency magnons demonstrate very distinct and exotic responses. The intensity variation in the parallel configuration for the FMR mode looks similar to that typical for the $B_g$ modes with minima observed at angles corresponding to the crystal axes and maxima at intermediate angles between them (this behavior can be compared with the phonons in Fig. 6). However, in crossed configurations, instead of the expected four-lobe response, the intensity follows a twofold “dumbbell” shape displaying the intrinsic asymmetry of the Raman tensor. Moreover, the most surprising feature is the response in the crossed configuration, which looks different for the Stokes and anti-Stokes parts of the spectra. For some angles, this leads to a dramatic situation in which this mode has a substantially larger intensity in the anti-Stokes spectral part than in the Stokes one.

Similar deviations from the expected $AS/S$ ratio were previously observed in Raman scattering experiments on the antiferromagnetic system FeF$_2$ for which the main case of the non-Bose intensity ratio was attributed to the contribution of magneto-optical effects such as magnetic linear and circular dichroism and magnetic linear and circular birefringence [46,47]. We note that the observed effect was previously reported in only a few cases and at some selected angles, whereas we demonstrate its complete polarization dependence. A similar observation of AS-S asymmetry was recently found in CrI$_3$ [7]; however, in these experiments circularly polarized light was used, which “averages out” Raman tensor elements. In our study, the use of linear polarization allowed us to directly probe these dependences.

We should note that the asymmetry effect is intrinsically different from that observed in thin ferromagnetic films [48,49], in which it was associated with surface magnons, while in our study it is due to quadratic magneto-optical coupling [50].

Reconstruction of the tensors based on the observed polarization dependences of the integral intensity results in the
following equation [50]:

\[
\frac{I_s}{I_{AS}} = \frac{R}{\Delta \lambda^2} \left( (\Psi_{MLB} \mp \Psi_{MCD})^2 + \left( \frac{1}{2} \Psi_{MLD} \pm \frac{1}{4} \Psi_{MCD} \right)^2 \right),
\]

where \( R = [\eta(\omega) + 1]/[n(\omega)], \) \( n(\omega) = 1/\left( e^{\hbar \omega/k_B T} - 1 \right) \) is the Bose thermal population factor, \( \lambda_{ex} \) is the excitation wavelength, and \( \hbar \) is the optical absorption. MLB, MCB, MLD, and MCD stand for magnetic linear birefringence, magnetic circular birefringence, magnetic linear dichroism, and magnetic circular dichroism, respectively. However, the lack of information on the magneto-optical parameters of PbMnBO\(_4\) seriously limits further progress in the interpretation of the observed effects and calls for further static magneto-optical experiments.

The selection rules of the magnetic excitations and their Raman tensors are inherently different from those for phonons and can be described by nondiagonal asymmetrical tensors with a nonzero complex phase in the following form, adapted from [51]:

\[
M_{A_\ell} = \begin{pmatrix}
|h|e^{i\phi_h} & 0 & 0 \\
0 & |m|e^{i\phi_m} & |p|e^{i\phi_p} \\
0 & |q| & |n|e^{i\phi_n}
\end{pmatrix}
\]

\[
M_{B_{\ell}} = \begin{pmatrix}
0 & |r|e^{i\phi_r} & |s|e^{i\phi_s} \\
|r| & 0 & 0 \\
|u| & 0 & 0
\end{pmatrix}
\]

The main differences from the phononic Raman tensors [Eq. (2)] are the nonsymmetric form and the simultaneous presence of both diagonal and nondiagonal elements for the \( A_\ell \) mode and the occurrence of more than one nondiagonal element for the \( B_{\ell} \) modes. It should be noted that the diagonal and nondiagonal parts of the \( M_{A_\ell} \) tensors were treated separately in such a way that \( I = |e| M_{A_\ell} e |e|^2 + |e| M_{B_{\ell}} e |e|^2 \) following the approach used in [52]; such a separation of the intensity components holds for the large scattering volume, which is the case for our experiments on the bulk crystals and the use of the excitation line in the transparency window of PbMnBO\(_4\).

Tensor elements were determined by fitting the experimental data, as shown in Fig. 10, and the following parameters were obtained:

mode 4S: \( r = 12, t = 5.3, s \approx u \approx 6.5, \)

mode 4AS: \( r = 5.3, t = 12, \)

mode 12S: \( h = 42, m = 29, n = 58, \)

mode 12AS: \( h = 10.5, m = 7.25, n = 14.5, \)

mode 125S: \( h = 23, m = 38, n = 22, p = 40, q = 28, \)

where S and AS stand for the Stokes and anti-Stokes parts of the spectra, respectively. The phase differences between each diagonal Raman tensor element are \( \pi/2 \), while those between nondiagonal elements are different and close to \( 120^\circ \) for the \( M_{B_{\ell}} \) elements and \( 56^\circ \) between nondiagonal elements of the \( M_{A_\ell} \) tensor for the 125 cm\(^{-1}\) optical magnon mode.

The difference in the Raman tensors could be directly linked to the symmetry of the modes itself calculated within the linear spin-wave theory, as shown in Fig. 11. The acoustic mode corresponds to the precession of the total magnetic moment around the easy \( a \) axis and transforms according to the \( B_{\ell} \) representation of the \( mm'm'l' \) magnetic point group, while for all optical magnons there is no precession of the net moment by itself, only changes in their magnitudes.

C. Temperature effects on spin dynamics

The low-energy part of the spectra is dominated by the quasielastic (QE) scattering pronounced above the magnetic transition temperature, and it is strongly suppressed at low temperatures. This is followed by a complete suppression at 4.2 K, down to an observable limit of \( \approx 3 \) cm\(^{-1}\) on both the Stokes and anti-Stokes sides, as can be seen from raw data in Fig. 10. Such an observation reflects the importance of the short-range ordering effects both at and above \( T_C \), which goes along with observations for PbFeBO\(_4\) [23] and is compatible with the hypothesis of the dimensionality crossover proposed in [24], where PbFeBO\(_4\) was considered to be a good three-dimensional antiferromagnet well below \( T_N \). However, it shows low-dimensional features at and above \( T_N \), namely, the presence of an anomalous peak in the magnetic susceptibility [40] and the persistence of the detectable and highly polarized QE scattering up to room temperature.

Magnon energies are proportional to the magnitudes of the magnetic moment, and their temperature changes can be typ-
FIG. 12. Temperature dependences of (a)–(d) the energy (circles) and FWHM (squares) and (e) and (f) integral intensity of the magnetic excitations for the four observed magnetic modes. Frequencies of excitations in (a) and (b) follow a Brillouin function, while the intensity in (e) has a maximum close to a transition and is suppressed at both low and high temperatures, roughly following $\langle SS \rangle_T$ dependence (purple line). Note the logarithmic temperature scale for the $110 \text{ cm}^{-1}$ magnon. As expected, the frequency of the magnon modes is strongly temperature dependent and follows this function, as shown in Fig. 12. In contrast, all excitations have very different field and temperature dependences of the integral intensities; for example, the optical mode at $109 \text{ cm}^{-1}$ is quenched at low temperatures, closely following the $\langle SS \rangle_T$ function. A similar observation was made for another insulating ferromagnet, CrBr$_3$ [53], which was later explained in [54]. This rather sharp increase in the scattering intensity is known as the critical scattering and, according to Moriya [55], is associated with fluctuations developing just below $T_C$. Surprisingly, all other spin-wave modes have a different intensity behavior when the temperature is varied. Namely, the intensity of the $125 \text{ cm}^{-1}$ mode mainly follows a $\langle S_z \rangle^2$ function. Unfortunately, it was impossible to follow the acoustic magnon mode above $\approx 15 \text{ K}$ since it softens below the rejection band of the volume Bragg grating filters ($\approx 3 \text{ cm}^{-1}$). The diversity of the temperature-dependent parameters, specifically the intensities, suggests intricate excitation and relaxation processes, potentially involving lattice dynamics, a complete understanding of which is beyond the scope of this paper.

FIG. 13. Frequencies of the magnetic excitations as a function of magnetic field for the (a)–(c) high- and (d)–(f) low-energy branches. The purple line depicts the calculated field dependence based on the suggested exchange structure.

D. Magnetic field effects on magnons

To gain further insights into the origin of the observed modes, field-dependent measurements were performed, and the results are shown in Fig. 13. The magnetic field applied along the ferromagnetic vector ($a$ axis) leads only to a Zeeman contribution, resulting in the nearly linear increase of the magnon frequency, acoustic and optical alike. However, a field applied perpendicular to this axis leads to a spin orientation phase transition at the field value defined by an effective anisotropy tensor. In our work, the frequencies of the magnetic excitations as a function the magnetic field were tracked, and the abrupt changes were used as markers for the determination of spin orientation transitions. In Fig. 13 such dependences revealed transitions for the intermediate ($b$) and hard ($c$) axes. These observations of spin orientation transitions and the critical field values (2.26 and 4.75 T for the $b$ and $c$ axes, respectively) are fully compatible with the FMR measurements done in [14].

E. Linear spin-wave theory calculations

Even though the energy of the acoustic magnon branch was reliably determined in [14], it was not enough to uniquely estimate the exchange constants of PbMnBO$_4$ since the FMR frequency depends only on the anisotropy field. In contrast, Raman scattering experiments allowed us to detect all four magnetic modes corresponding to one acoustic and three optical branches. Thus, combining these observations, along with the known critical field values for spin orientation transitions, it is possible to reliably evaluate the full set of exchange and effective anisotropy constants of PbMnBO$_4$.

Octahedral coordination of the Mn$^{3+}$ ions, especially the octahedra elongation caused by the Jahn-Teller effect, could potentially lead to site-dependent anisotropy, where the local anisotropy axis follows a particular octahedra tilt. In our model we consider the site-dependent effective (single-ion-like) biaxial anisotropy constant $D$ with the local axis rotated...
by ±15° following rotation of the [MnO₆] octahedra within the ac plane. This step was necessary to simultaneously obtain the correct frequency of the acoustic magnon branch and reproduce the critical fields (see Fig. 13), which was impossible with considering “global” anisotropy.

It is known (and also was demonstrated for PbFeBO₄) that the strongest exchange interaction constant $J₀$ corresponds to the path directed along the chains (b axis) [19,25]. However, even if it is unlikely, according to the phase diagram of the $J₀$-$J₁$-$J₂$ model [24], the ferromagnetic structure can be realized with any of these couplings being the dominating FM interaction. Thus, these will be our assumptions in determining the exchange structure.

Calculations are based on the numerical solution [56,57] of the following Heisenberg Hamiltonian:

$$
\mathcal{H} = \sum_{\langle i,j \rangle} J₀ S_i S_j + \sum_{\langle\langle i,j \rangle\rangle} J₁ S_i S_j + \sum_{\langle\langle\langle i,j \rangle\rangle\rangle} J₂ S_i S_j + \sum_i D(S_i^z)^2 + \mu_B H \sum_i g S_i^z,
$$

where $J₀, J₁,$ and $J₂$ are isotropic exchange constants and $D$ is the effective anisotropy tensor with $z$ along the c axis.

The solution leads to four spin-wave branches nondegenerate at the Γ point, as shown in Fig. 14. By matching the Γ-point energies with those of the experimentally registered magnons shown in Fig. 14, it is possible to derive a unique set of exchange constants, as well as the diagonal components of the anisotropy tensor $D$. The determined constants are $J₀ = -1.680$, $J₁ = 0.025$, and $J₂ = -0.045$ meV and, for the anisotropy $D$ (before the rotation), $D_{x{x}} = -0.20$, $D_{y{y}} = -0.12$, and $D_{z{z}} = 0.0$ meV, where a negative $D$ value stands for the easy-axis type of anisotropy, thus making the $a$ axis an easy axis and the $c$ axis a hard one. These values of the anisotropy tensor nicely reproduce the critical fields of the spin orientation transitions (4.6 T for $H \parallel c$ and 2.5 T for $H \parallel b$; see Fig. 13 and [14]). The full set of the exchange and anisotropy constants fully reproduces the number and the energy of the observed spin-wave branches, the small tilt of the magnetic moments even in zero field observed in [18], and a full set of magnetic field dependences.

It is curious to note that a small AFM exchange $J₁$ was necessary to correctly match the experimentally observed frequencies, introducing a small degree of exchange frustration. Moreover, at least three different exchange interactions are needed to match the experimental data, similar to the case of antiferromagnetic PbFeBO₄ [24], making the proposed Hamiltonian the minimal one. Another interesting fact of the suggested model is that the determined $J₀$ is surprisingly close in magnitude to $J₀$ in PbFeBO₄ [24] but of opposite sign, −1.68 and 1.67 meV, respectively. Thus, in these two crystals we are facing the extremely rare situation when slight structural changes (without breaking the crystallographic symmetry) induced by the Jahn-Teller distortion by Mn³⁺ ions lead to a sign change of the strongest exchange interaction $J₀$.

Symmetrically distinct normal magnon modes obtained from the eigenvectors of the quadratic form [56] of the Hamiltonian (10) are shown in Fig. 11. Slight ellipticity of the precession orbit (not shown) is expected due to the biaxial $(D_{x{x}} \neq D_{y{y}})$ form of the anisotropy tensor. However, it less pronounced in optical modes where the isotropic exchange interactions start to contribute to the energy of the modes. The presence of the large “energy gap” at the Γ point between the two lowest and two highest modes could be easily understood from the proposed exchange structure of PbMnBO₄ shown in Fig. 11 since the lowest modes involve in-phase precession of the moments coupled by the strongest $J₀$ interaction, while for the highest mode the precession is in antiphase. The field dependences are sufficiently well described with $g = 2.00$, suggesting the negligible role of orbital effects in the spin dynamics.

Up to now, there were no exchange constants known directly supported by experiment, e.g., inelastic neutron scattering. Nevertheless, several attempts, both experimental and theoretical, have been made to estimate the exchange structure. A PbMBO₃ family of crystals was introduced in an original work by Park et al. [13] in which the magnetic susceptibility measurements were interpreted with Bonner-Fisher analysis [58] assuming a purely one-dimensional ferromagnetic chain, resulting in $J₀ = −0.948$ meV. Another estimate [15] was based on the experimentally determined $T_C$ and the paramagnetic Curie temperature $θ$ within
Ginzburg-Landau theory, which resulted in $J_0 = -1.74$, $J_1 = -0.19$ meV while ignoring further couplings. This estimate gives a close match in $J_0$ but overestimates $J_1$ and gives the wrong sign for it. Other attempts using *ab initio* calculations should also be mentioned; for example, Koo and Whangbo [19] estimated the set as $J_0 = -3.19$, $J_1 = -0.043$, $J_2 = -0.258$ meV, in which the exchange was strongly overestimated. Xiang et al. obtained [20] somewhat similar values, $J_0 = -2.321$, $J_1 = -0.018$, $J_2 = -0.208$ meV, with all couplings being FM.

Summing up this section, we proposed a minimal Hamiltonian and a consistent exchange model with a set of exchange coupling and effective anisotropy constants of PbMnBO$_4$ based on the frequency and field dependences of the four observed magnetic excitations and the values of critical fields of the two distinct spin orientation phase transitions. In view of the very similar crystal structures of PbMnBO$_4$ and PbFeBO$_4$ with almost equally strong dominating but opposite in sign $J_0$ exchange couplings, these systems can pave the way for manipulation of the exchange interaction [59,60] or coherent control of magnetism through nonlinear phononics [61–63], e.g., through selective excitations of the specific phonon modes (see Sec. IV C) demonstrating strong coupling between lattice and magnetic subsystems.

VI. SUMMARY AND CONCLUSIONS

In summary, a systematic inelastic Raman scattering study of the insulating ferromagnet PbMnBO$_4$ in the wide temperature range of 4–300 K and in a magnetic field up to 30 T was presented. Most of the even Raman phonons, 34 of the symmetry-predicted 36, were registered.

Detailed polarization-dependent measurements allowed us to undoubtedly determine their symmetry and, on the basis of the full $360^\circ$ azimuthal dependences, directly extract the Raman tensor elements and their complex phases. A number of modes demonstrated either softening or hardening below $T_C$, distinctly deviating from the usual anharmonic behavior and thus pointing to an intense spin-phonon coupling. Moreover, a 224.7 cm$^{-1}$ $A_g$ phonon assigned to a particular oxygen mode relevant to [MnO$_6$] octahedra additionally demonstrated pronounced coupling between the lattice and magnetic subsystems, manifesting in both the frequency and Raman tensor renormalization below $T_C$, as well as a noticeable shift in applied magnetic field. These features unravel a peculiar interaction between the Jahn-Teller elongation of the [MnO$_6$] octahedra and the magnetic ordering.

Four magnetic excitations were registered below $T_C$ on the basis of temperature and magnetic field dependences, and they all were assigned to the one-magnon scattering

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**FIG. 15.** Temperature-dependent Raman scattering maps for different polarizations. Observed magnons are marked M1–M4; the anomalous phonon (see Fig. 8) is marked by an asterisk. Note the logarithmic temperature scale to highlight the ferromagnetically ordered state. Horizontal dashed lines mark the PM to FM transition ($T_C$, Curie) temperature.

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processes. Anomalous polarization-dependent Stokes to anti-Stokes intensity ratios of the acoustic magnon (ferromagnetic resonance) were explicitly attributed to the contribution related to magneto-optical effects. A noncontradictory set of exchange and effective anisotropy parameters was obtained based on the experimentally observed frequencies of spin excitations.

Thus, being an extremely rare example of an insulating ferromagnet, PbMnBO₄ demonstrates rich spin dynamics in the subterahertz and terahertz energy range and complex features such as pronounced spin-phonon coupling, interaction of the Jahn-Teller distortion with magnetism, and a direct contribution of the magneto-optical effects to Raman scattering, making this material a rich playground for further studies of both static and dynamic properties and interaction between lattice and magnetic subsystems.

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APPENDIX: RAW TEMPERATURE AND FIELD DEPENDENCE MAPS

Two sets of the non-corrected, raw data (with only cosmic spikes removed) are shown below. Temperature dependence set shown in Fig. 15, and field dependence one in Fig. 16. Note that the different collection optics were used along with a greatly increased distance between the sample and the spectrometer in the latter case resulting in almost complete suppression of the elastic line.

J. Head, P. Manuel, F. Orlandi, M. Jeong, M. R. Lees, R. Li, and C. Greaves, Structural, magnetic, magnetocaloric, and magnetostriuctive properties of Pb$_{1-x}$Sr$_x$MnBO$_4$ ($x = 0, 0.5$, and $1.0$), Chem. Mater. 32, 10184 (2020).


[39] The anharmonic constants obtained through the fitting procedure are $\omega_0 = 187.1$, $A = 0.45$, $B = 0.09$, $\Gamma_0 = 0.35$, $C = 1.09$, $D = 0.17$; $\omega_0 = 226.6$, $A = 4.94$, $B = 0.02$, $\Gamma_0 = 0.01$, $C = 1.78$, $D = 0.55$; $\omega_0 = 285.7$, $A = 1.25$, $B = 0.00$, $\Gamma_0 = 0.01$, $C = 1.68$, $D = 0.30$; $\omega_0 = 355.0$, $A = 0.65$, $B = 0.14$, $\Gamma_0 = 0.01$, $C = 5.05$, $D = 0.42$; $\omega_0 = 359.2$, $A = 4.64$, $B = 0.00$, $\Gamma_0 = 0.01$, $C = 4.27$, $D = 0.49$; $\omega_0 = 426.2$, $A = 0.72$, $B = 0.36$, $\Gamma_0 = 0.01$, $C = 3.29$, $D = 0.23$ for curves (a)–(f) in Fig. 7, respectively.


[42] C. Zhu and R. Zheng, Ultrasonic evidence for magnetoelastic coupling in La$_{0.60}$Y$_{0.17}$Ca$_{0.33}$MnO$_3$ perovskites, Phys. Rev. B 59, 11169 (1999).


