Probing Crust Meltdown in Inspiring Binary Neutron Stars

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Thanks to recent measurements of tidal deformability and radius, the nuclear equation of state and structure of neutron stars are now better understood. Here, we show that through resonant tidal excitations in a binary inspiral, the neutron crust generically undergoes elastic-to-plastic transition, which leads to crust heating and eventually meltdown. This process could induce $\sim \mathcal{O}(0.1)$ phase shift in the gravitational waveform. Detecting the timing and induced phase shift of this crust meltdown will shed light on the crust structure, such as the core-crust transition density, which previous measurements are insensitive to. A direct search using GW170817 data has not found this signal, possibly due to limited signal-to-noise ratio. We predict that such a signal may be observable with Advanced LIGO Plus and more likely with third-generation gravitational-wave detectors such as the Einstein Telescope and Cosmic Explorer.

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Introduction.—Inspiring neutron stars deform under mutual tidal interactions. In the adiabatic limit, the star's induced quadrupole moment is directly proportional to the tidal gravitational field, with the proportionality constant given by the tidal Love number. Deformed neutron stars orbit each other differently from black holes with the same masses, and the phase difference can be used to measure the tidal Love number [1], as shown in the analysis of GW170817 [2]. Together with neutron star radius measurements [3], maximum mass estimates [4] and possibly post-merger electromagnetic signals [5], the star's equation of state (EOS) is now better constrained.

In addition to adiabatic tides, tidal interaction can excite internal modes of neutron stars as the binary sweeps through the inspiral frequency range. The pressure (p) and fundamental (f) modes [6] will not be fully excited as their frequencies are generally higher than the inspiral frequency, although it has been suggested that early excitation of f modes may be observed in the late inspiral stage [7]. Gravity modes may be fully excited, but their couplings to tidal gravitational fields are so small that the induced phase shifts are $\mathcal{O}(10^{-3})$ or smaller [8,9]. Resonance of rotational modes has also been investigated assuming a rotational frequency of a few $\times 10^2$ Hz [10–13], whereas the fastest rotating pulsar known in a binary neutron star system has a frequency of ~ 60 Hz [14,15].

The interface (i) modes [16,17], excited at the interface of the fluid core and solid crust, have frequencies around several tens to a few hundred Hertz, depending on the star's equation of state and prescription of the crust. The resonance of i modes was proposed to explain precursors

of short gamma-ray bursts due to possible crust failures [18]. We observe that through excitation of i modes, the crustal material actually reaches its elastic limit well before the mode resonance. After reaching this threshold the crust undergoes an elastic-to-plastic transition and the tidal driving starts to heat up the crust. The whole process ends with the meltdown of the crust in tens of cycles.

Crust heating up and melting down.—The outer part of the crust is commonly described by a Coulomb lattice with shear modulus μ [19]. The inner crust may have nonuniform structures associated with the “nuclear pasta” phase [20,21], which is not considered in this study. Simulations of molecular dynamics [22] have shown that the lattice responds elastically under small applied stress; once the induced strain exceeds the breaking strain ($\epsilon_b \sim 0.1$), plastic deformation starts to develop. Assuming an applied stress σ , the plastic deformation rate $\dot{\epsilon}_{\text{pl}}$ is exponentially small if $\sigma < \sigma_b = \mu\epsilon_b$, and becomes exponentially large if $\sigma > \sigma_b$. Mathematically, it is well approximated by [22]

$$\dot{\epsilon}_{\text{pl}} = \frac{n_i Z^2 e^2}{a} \frac{\omega_p}{\mu \bar{N} \Gamma} e^{(-18.5 \bar{\sigma}_b + \bar{\sigma} \bar{N}) \Gamma}, \quad (1)$$

where the dot denotes a time derivative, ω_p is the plasma frequency, $\bar{N} = 500/(\Gamma - 149) + 18.5$, $\bar{\sigma} = \sigma/(n_i Z^2 e^2/a)$ and $\Gamma = Z^2 e^2/aT$ is the melting parameter with e the electron charge, Ze the total charge per ion, a the lattice spacing, n_i the ion density, and T the temperature. The elastic part of the strain ϵ_{el} satisfies $\sigma = \mu\epsilon_{\text{el}}$ and the total strain is simply $\epsilon = \epsilon_{\text{el}} + \epsilon_{\text{pl}}$.

With the plastic deformation, mode energy dissipates into thermal energy, heating up the crust with a rate [23]

$$n_i \dot{e}_i = \sigma \dot{\epsilon}_{\text{pl}}(\sigma, T), \quad (2)$$

where n_i is the ion number density, e_i is the thermal energy per ion, and $de_i = c_V dT$ with c_V the specific heat capacity for $T < T_{\text{melt}}$ [24]. Once the melting temperature T_{melt} is reached, the crustal material still needs an extra amount of latent heat ($\sim kT_{\text{melt}}$ per ion) to be melted [25]. As a result, the total energy per ion needed to melt the crust from its initial cold state is roughly $e_{\text{melt}} = \int_0^{T_{\text{melt}}} c_V dT + kT_{\text{melt}}$. In this work we have ignored contributions from dripped neutrons as their specific heat may be suppressed by superfluidity.

Mode analysis.—In the linear approximation, the stellar response to the tidal force is specified by the Lagrangian displacement $\xi(\mathbf{r}, t)$ of a fluid element from its equilibrium position. The displacement can be decomposed into eigenmodes, $\xi(\mathbf{r}, t) = \sum_{\alpha} a_{\alpha}(t) \xi_{\alpha}(\mathbf{r})$, where α denotes the quantum number of an eigenmode. In the context of this Letter, we only consider i modes driven by the leading quadrupole term of the tidal force, so that $\xi_m(\mathbf{r}) = [U(r)\hat{r} + rV(r)\nabla]Y_{2m}(\theta, \phi)$, where $Y_{2m}(\theta, \phi)$ is the $l = 2$ spherical harmonic. The displacement behavior is governed by the linear pulsation equation [16,17]

$$[\mathcal{L}(r; \mu) - \omega_0^2] \xi_m = 0, \quad (3)$$

with $\mathcal{L}$ being an operator specifying the restoring force inside the star (see Supplemental Material [26] for the explicit expression).

For the example star with $M_{\star} = 1.3 M_{\odot}$, $R_{\star} = 11.7$ km assuming SLy4 EoS [27,28] and a core-crust baryon transition density $n_{b,\text{cc}} = 0.065 \text{ fm}^{-3}$, we obtain an i -mode frequency $f_0 = \omega_0/2\pi = 190$ Hz [17,18] and the tidal coupling coefficient (a measure quantifying the overlap between the waveform and the tidal field)

$$Q = \frac{1}{M_{\star} R_{\star}^2} \int d^3x \rho \xi_m^* \cdot \nabla [r^2 Y_{2m}(\theta, \phi)] = 0.018, \quad (4)$$

with the normalization $\langle \xi_m | \xi_{m'} \rangle := \int d^3x \rho \xi_m^* \cdot \xi_{m'} = \delta_{mm'} M_{\star} R_{\star}^2$, where ρ is the mass density [29].

The evolution of the mode amplitude $a_m(t)$ is governed by [8]

$$\ddot{a}_m + \gamma(t) \dot{a}_m + \omega_0^2(t) a_m = \frac{GM' W_{2m} Q}{D^3} e^{-im\Phi(t)}, \quad (5)$$

where the right-hand side is the leading quadrupole term of the tidal driving force with $M' = qM_{\star}$ the companion star mass, D the binary separation, $\Phi(t)$ the orbital phase, and W_{2m} is a coefficient of $\mathcal{O}(1)$ [see Eq. (2.4) in Ref. [8]]. On the left-hand side, $\gamma(t) \dot{a}_m$ is a damping term capturing the

plastic deformation induced dissipation with $\gamma(t)$ defined as the ratio between the mode energy dissipation rate and two times the mode kinetic energy, i.e.,

$$\gamma(t) = \frac{\int_{\text{crust}} n_i \dot{e}_i d^3x}{M_{\star} R_{\star}^2 \sum_m |\dot{a}_m|^2}, \quad (6)$$

where the numerator is the crust heating rate (which is equal to the mode energy dissipation rate), and the mode kinetic energy is $\frac{1}{2} \int d^3x \rho \dot{\xi}(\mathbf{r}, t) \cdot \dot{\xi}^*(\mathbf{r}, t) = \frac{1}{2} M_{\star} R_{\star}^2 \sum_m |\dot{a}_m|^2$. The mode frequency $\omega_0(t)$ to leading order is determined by [see Eq. (3)]

$$\omega_0^2(t) = \frac{\langle \xi_m | \mathcal{L}(r; \mu_{\text{avg}}) \xi_m \rangle}{\langle \xi_m | \xi_m \rangle}, \quad (7)$$

where μ_{avg} is the average shear modulus which decreases as the crust is heated and we find the mode frequency is roughly proportional to the square root of the average shear modulus [30].

Given the mode amplitude $a_m(t)$, it is straightforward to calculate the fluid element displacement $\xi(\mathbf{r}, t) = \sum_m a_m(t) \xi_m(\mathbf{r})$ and the corresponding strain ϵ_{el} . From Eq. (1), the plastic deformation rate $\dot{\epsilon}_{\text{pl}}$ has an exponential dependence on the local strain ϵ_{el} for $\epsilon_{\text{el}} \gtrsim 0.1$, so does the energy dissipation rate $\sigma \dot{\epsilon}_{\text{pl}}$. Physically, the dissipated energy comes from the local elastic energy, therefore the energy dissipation rate cannot exceed its replenishment rate $(\mathcal{A}/2) \mu \epsilon_{\text{el}}^2 f_{\text{GW}}$, where f_{GW} is the frequency of both the tidal force and the GW emission and $\mathcal{A}$ is a coefficient of $\mathcal{O}(1)$. Here we take $\mathcal{A} = 2$ as an example. As for the initial condition, we choose $T_i = 0.02 T_{\text{melt}}$, where $T_{\text{melt}} \sim 1$ MeV is the melting temperature of the ion crystal at the crust base [19]. Using the 4th-order Runge-Kutta scheme, we evolve Eqs. (1), (2), (5) on the two-dimensional surface of the crust base, i.e., we only trace the thermal evolution of the crust base considering its dominant role in the crust heat capacity.

As the neutron star binary spirals inward, the tidal field increases and so does the i -mode amplitude $a_{m=0,\pm 2}$, as shown in Fig. 1. At a certain binary separation (with corresponding gravitational wave frequency $f_{\text{GW,melt}} < f_0$), part of the crust reaches the yield limit ϵ_b due to the i -mode excitation and plastic deformation starts. Heating first takes place at the equator where the strain maximizes. As the crust heats up, it softens so that i -mode frequency f_0 decreases and the mode amplitude a_m increases. As a result, the crust yields on larger and larger areas, extending from the equator to the poles, and finally the whole crust is melted. The crust melting takes about 20 orbit periods and a total amount of energy $E_{\text{melt}} \simeq 1.1 \times 10^{47}$ ergs. Notice that this mode treatment is approximate once the plastic motion turns on, where a more accurate description requires three-dimensional dynamical modeling of crustal motions. A two-dimensional

FIG. 1. Left three panels are the heat maps e_i/e_{melt} of the neutron star crust (within a $1.3 M_\odot + 1.3 M_\odot$ binary) at binary separations $D = 12.0/11.6/11.4 R_*$, respectively. In the rightmost panel, dashed lines denote the evolution of the i -mode frequency f_0 and the gravitational wave (GW) frequency f_{GW} , and solid lines denote the evolution of mode amplitude a_m with $m = \pm 2, 0$.

consistent evolution was implemented in Ref. [23] to reveal yield patterns of magnetar crust under strong magnetic stress.

Waveform signature.—After the melting process, part of the binary orbital energy is converted to the mode and thermal energy resulting in a phase shift of the gravitational waveform. Similar to the discussion in Refs. [8,9,31] for mode resonances, for the binary neutron star waveform $h(f) = A(f)e^{i\Psi(f)}$, its phase is modified as

$$\begin{aligned} \delta\Psi(f) &= \sum_{i=1,2} \delta\phi_i \left(1 - \frac{f}{f_i}\right) \Theta(f - f_i) \\ &\approx \delta\phi_a \left(1 - \frac{f}{f_a}\right) \Theta(f - f_a), \end{aligned} \quad (8)$$

where Θ is the Heaviside function and f_i is the melting frequency of each star. Therefore the search and forecast presented below for crust melting apply equally for generic mode resonances, and we will use “mode resonance signature” and “crust melting signature” interchangeably. The melting process decreases the coalescence phase by $\delta\phi_i$ and the coalescence time by $\delta\phi_i/2\pi f_i$. In the second line we introduced $\delta\phi_a = \sum_i \delta\phi_i$ and $\delta\phi_a/f_a = \sum_i \delta\phi_i/f_i$ to reduce the number of extra parameters in this model, which simplifies the parameter estimation process. Notice that if energy transfers from the orbit to the mode (or heat in this case) during resonance, $\delta\phi$ is positive; if energy transfers from the mode to the orbit, as expected in some of the r -mode resonances [12], $\delta\phi$ is negative.

For each neutron star, $\delta\phi$ depends on its mass M_* , the mass ratio of the companion q (with the companion mass being qM_*), the melting energy E_{melt} and the melting frequency $f_{\text{GW,melt}}$ as follows [8]

$$\delta\phi = \frac{2\omega_{\text{orb}} E_{\text{melt}}}{P_{\text{GW}}} \simeq \frac{0.1}{q^2} \left(\frac{1+q}{2}\right)^{2/3} E_{47} M_{1.3}^{-10/3} f_{70}^{-7/3}, \quad (9)$$

where $\omega_{\text{orb}} = \pi f_{\text{GW,melt}}$ is the orbital angular frequency, P_{GW} is the energy loss rate due to GW emission, and $E_{47} = E_{\text{melt}}/10^{47}$ ergs, $M_{1.3} = M_*/1.3 M_\odot$, $f_{70} = f_{\text{GW,melt}}/70$ Hz. From Eq. (9), we immediately see that the phase shift increases if the melting process happens earlier (lower

$f_{\text{GW,melt}}$) in the inspiral phase. In Fig. 2, we show the total phase change $\delta\phi_a$ for an equal-mass binary neutron star (BNS) merger with $M_* = 1.3 M_\odot$, where $\delta\phi_a$ varies from 0.03 to 0.6 depending on the star’s EOS and the core-crust transition baryon density $n_{b,\text{cc}}$. The melting energy increases substantially with increasing $n_{b,\text{cc}}$ (commonly assumed to be within $0.06\text{--}0.1 \text{ fm}^{-3}$ [32–34]), whereas the i -mode frequency and the associated melting frequency are nonmonotonic functions of $n_{b,\text{cc}}$. We also note that since the mode calculation presented here is Newtonian with the Cowling approximation [35], the fully relativistic mode frequencies may be different (for examples, the frequencies of p and f modes are smaller with the metric perturbation included [36,37]). If there are also more unpaired neutrons present within the star, as suggested by the cooling measurement in Ref. [38], the melting energy may be significantly boosted and the internal mode spectrum may be modified as well.

FIG. 2. The crust melting induced phase change $\delta\phi_a$ in GWs of a BNS merger with each star of $M_* = 1.3 M_\odot$ and $R_* = 12.5/11.3/11.7/12.7$ km for the EOS SkI6/APR4/SLy4/MPA1, respectively, which are not ruled out by the LIGO tidal measurement with GW170817. Note that the core-crust transition density $n_{b,\text{cc}}$ is subject to a large uncertainty in each EOS instead of being an accurately predicted value, so we take the transition density as a free parameter.

FIG. 3. Posterior distribution of chirp mass $\mathcal{M}$, phase shift $\delta\phi_a$ and melting frequency f_a obtained with PyCBC, where the prior for f_a is set to be $[30, 300]$ Hz and $[0, 2]$ for $\delta\phi_a$. Left plot: the search using data from GW170817. Right plot: a search obtained assuming LIGO A+ sensitivity and an mode resonance injection at $f_a = 60$ Hz and $\delta\phi_a = 0.3$.

Therefore the search of mode resonance signatures may also help probe the superfluid composition of neutron stars. The effects of nuclear pastas on the melting energy budget and the mode frequency determination also need to be better understood. Nevertheless, the measurement of f_a and $\delta\phi_a$ will convey useful information about the core-crust transition density and the star's EOS around that density.

Search with GW170817.—We now present the first search for mode resonance effects (including crust melting) in binary neutron star systems with data from GW170817 with Eq. (8) implemented. A similar search for tidal- p - g instability is discussed in Ref. [39] using different $\delta\Psi(f)$. The Markov-chain Monte Carlo (MCMC) parameter estimation is performed with PyCBC [40], for which we assume the source distance and sky location are known as the electromagnetic counterpart of this source has been identified [41]. We use the TaylorF2 waveform [42] as the background binary neutron waveform. We present the posterior distributions of chirp mass $\mathcal{M}$, $\delta\phi_a$ and f_a in Fig. 3. The marginal distribution of ϕ_a indicates that there is no evidence for mode resonance in GW170817, as $\delta\phi_a < 1.5$ at 95% confidence level. A similar conclusion can be drawn from a Bayesian model comparison framework. We denote $\mathcal{H}_a$ as the hypothesis with mode resonance and $\mathcal{H}_0$ as the one without, the Bayes factor can be defined as

$$B_0^a = \frac{P(\text{GW170817}|\mathcal{H}_a)}{P(\text{GW170817}|\mathcal{H}_0)}, \quad (10)$$

which measures the relative probability of these two hypotheses. We have computed the Bayes factor using both the method of thermodynamic integration [43] and the Savage-Dickey density ratio method [44], which both suggest consistent values of $\log B_0^a$ in the range of

$[-0.6, -0.3]$. This means that these two hypotheses are essentially indistinguishable with this set of gravitational wave data [45].

It is natural to expect observations with higher signal-to-noise ratios as the sensitivity of gravitational wave detectors improves. In the mid-2020s the upgrade of Advanced LIGO, LIGO A+, is expected to start its construction [46]. Assuming LIGO A+ design sensitivity for all three detectors at Hanford/Livingston/India, and Advanced Virgo with its full sensitivity, we may observe GW170817-like events with signal-to-noise ratios beyond 100. In the right panel of Fig. 3, we present a sample search with an injected signal with $\delta\phi_a = 0.3$, $f_a = 60$ Hz (for a GW170817-type system with star masses $m_1 = 1.47 M_\odot$, $m_2 = 1.28 M_\odot$, tidal Love numbers $\Lambda_1 = 210.6$, $\Lambda_2 = 525.6$, zero star spins and nearly face-on orientation with inclination angle $\iota = 0.2$ rad) into simulated detector noises consistent with the aforementioned LIGO A+ network sensitivity. We find the mock signal will be detected with $\text{SNR} = 197$ and a MCMC analysis of the mock data successfully recovers the injected values of f_a and ϕ_a with small uncertainties. So it is possible that we observe the crust melting signature in gravitational waves with LIGO A+.

Stacking different events may also improve detectability, as is the case for subdominant modes in black hole ringdowns [47]. However, we have no prior information on $\delta\phi_a$ and f_a , which are distinct for each binary neutron star system. If we have an underlying or phenomenological model that predicts or characterizes $\delta\phi_a$, f_a as a function of star mass, core-crust transition density and star compactness (which depends on the EOS), the hyperparameters in this model may be constrained from different events. Certainly, the posterior distribution of the hyperparameters from different events can be multiple together to form the

joint probability distribution. This is something worth pursuing in future studies.

If a mode resonance signature is indeed detected (i.e., preferred over the null hypothesis), it is still necessary to compare to other possible origins, such as tidal- p - g coupling [39], dynamical scalarization and vectorization [48,49], scalar modes associated to certain GR extensions [50] and extensions to standard particle physics [51], that predict different $\delta\Psi(f)$. Since the crust melting is nearly instant (Fig. 1), its impact on the waveform boils down to shifting the coalescence time and the coalescence phase, i.e., $\delta\Psi(f) = \delta\phi_a(1 - f/f_a)$ with $\delta\phi_a$ being a constant. For other processes with continuous orbital energy draining, e.g., the tidal- p - g coupling extending the whole frequency range once the nonlinear instability is turned on, the waveform signature can be formulated in a similar way except with a frequency dependent phase shift $\delta\phi_a(f)$ which encodes the details of orbital energy draining. To simulate this, we inject a mode resonance signal ($\delta\phi_a = 0.3$, $f_a = 60$ Hz) into detector noise corresponding to the LIGO A+ network, and perform the Bayesian model selection between our model resonance waveform and the tidal- p - g waveform. We find a Bayes factor $\log \mathcal{B}_{\text{pg}}^a = 2.7 \pm 0.3$, suggesting that it is also possible to determine the correct model if a positive detection occurs (see Supplemental Material [26] for more details of the Bayesian analysis). The comparison will be much sharper with third-generation gravitational wave detectors. Similarly for the scalarized neutron stars proposed in scalar tensor theories or other particle physics considerations, there are also effects, such as dipole scalar radiation, that will be effective during the whole frequency range once turned on [51]. We also perform a model selection between the mode resonance and an example model of BNSs with scalar dipole radiation using the same mock data above, and we find the Bayes factor is $\log \mathcal{B}_{\text{dipole}}^a = 11.7 \pm 2.2$ (see Supplemental Material [26]).

Discussion.—Resonant tidal excitations in a neutron star binary induce a phase shift $\delta\phi_a$ in the gravitational wave signal by melting its crust. In calculating the crust heating rate, we have used the fitting formula $\dot{\epsilon}_{\text{pl}}(\sigma)$ [Eq. (1)], which is a result of molecular dynamics simulations [22]. If this simulation result does not accurately apply to the NS crust with a breaking strain ϵ_b different from 0.1, the crust melting frequency $f_{\text{GW,melt}}$ will also change. For a smaller breaking strain $\epsilon_b = 0.05$, we find the melting frequency $f_{\text{GW,melt}}$ decreases by $\sim 25\%$ and the phase shift $\delta\phi_a$ increases by a factor ~ 2 . All the predicted phase shifts corresponding to different EOSs are still well consistent with the constraint $\delta\phi_a < 1.5$ (95% confidence level) from GW170817. LIGO A+ may already be able to detect such induced phase shifts. A 3rd-generation detector network with Cosmic Explorer [52] sensitivity at the LIGO detectors and Einstein Telescope [53] sensitivity at the Virgo detector is able to limit $\delta\phi_a$ with uncertainty ~ 0.01 and f_a below 1%. This will not only allow high-confidence

detection of the crust melting effect, but also precisely measure crustal and EOS properties as shown in Fig. 2.

We do not expect significant energy release to the neutron star magnetosphere associated with crustal failure, as the magnetic fields ($\sim 10^{12}$ G) assumed are too weak to efficiently transfer energy by sending out Alfvén waves. However, if the star is a magnetar with field $\sim 10^{15}$ G, this emission mechanism may excite star magnetospheres and power precursor gamma-ray bursts [23,54,55]. Interestingly, the recent LIGO observation of a heavy neutron-star binary (GW190425 [56]) may indicate the existence of a fast-merging channel to form binary neutron stars. Such systems may have short-enough lifetime $\sim 10^4$ years to allow active magnetars in the binary coalescence stage [57].

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