Narrow-band search for gravitational waves from known pulsars using the second LIGO observing run

B. P. Abbott et al.*

(LIGO Scientific Collaboration and Virgo Collaboration)

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Isolated spinning neutron stars, asymmetric with respect to their rotation axis, are expected to be sources of continuous gravitational waves. The most sensitive searches for these sources are based on accurate matched filtering techniques that assume the continuous wave to be phase locked with the pulsar beamed emission. While matched filtering maximizes the search sensitivity, a significant signal-to-noise ratio loss will happen in the case of a mismatch between the assumed and the true signal phase evolution. Narrow-band algorithms allow for a small mismatch in the frequency and spin-down values of the pulsar while coherently integrating the entire dataset. In this paper, we describe a narrow-band search using LIGO O2 data for the continuous wave emission of 33 pulsars. No evidence of a continuous wave signal is found, and upper limits on the gravitational wave amplitude over the analyzed frequency and spin-down ranges are computed for each of the targets. In this search, we surpass the spin-down limit, namely, the maximum rotational energy loss due to gravitational waves emission for some of the pulsars already present in the LIGO O1 narrow-band search, such as J1400−6325, J1813−1246, J1833−1034, J1952+3252, and for new targets such as J0940−5428 and J1747−2809. For J1400−6325, J1833−1034, and J1747−2809, this is the first time the spin-down limit is surpassed.

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I. INTRODUCTION

Eleven gravitational wave (GW) signals have so far been detected by the LIGO [1,2] and Virgo GW interferometers [3] in their first and second observing runs (O1 and O2, respectively) [4]. All the signals detected so far come from the coalescence of two compact objects. These signals belong to the class of transient signals, since they are observed only within a short time window during the observing run. Ten detections of binary black hole mergers [4–9] and a detection from a binary neutron star (NS) merger [10] have been accomplished during the first and second observing runs.

Another class of GW signals potentially observable by the LIGO and Virgo detectors is the so-called continuous wave (CW). CWs could potentially be present during the entire data-taking period of the GW detectors. Potential sources of CWs are isolated spinning NSs asymmetric with respect to their rotation axis. In the case of an oblate NS, CWs are emitted at a frequency that is 2 times its rotational frequency.

Different types of CW searches can be performed according to the astrophysical scenario in which the NS is observed. If the NS is a pulsar, an accurate ephemeris may be available and matched filtering techniques can be employed to reach, ideally, the best possible sensitivity by using waveform templates that cover the entire observing run. These types of searches are referred to as targeted searches. The LIGO and Virgo Collaborations have already searched for this type of emission from known pulsars (both isolated and some in binaries) [11–19], for which accurate ephemerides were available. While for NSs observed as a central compact object of a supernova remnant or in a binary system, usually accurate ephemerides are not available. In this case, we can pinpoint the source and look for the CW signal over a wide frequency range using semicoherent analysis, e.g., dividing the observing run in several data chunks and looking for a waveform template in each of them. Such searches are called “directed” and offer the possibility to explore a large number of templates at the price of a lower sensitivity with respect to targeted searches [20–24]. Recently, there has also been a study for a possible deviation of CW signals from the general relativity model [25] by including nontensorial modes.

Between targeted and directed searches, we find the narrow-band searches. Such pipelines are based on algorithms which allow us to make a full coherent search, and, at the same time, we are able to deal with a frequency mismatch between the CW signal and the electromagnetic inferred value of the order of 500 mHz [14,26,27]. Usually, this will correspond to the evaluation of millions of waveform templates for each pulsar considered in the analysis.

*Full author list given at the end of the article.
Hence, narrow-band searches offer a sensitivity comparable to the one of targeted searches while relaxing the phase-lock assumption of the CW signal with the NS rotation. The CW phase locking is indeed a strong assumption that may prevent the detection of a CW signal. In fact, a coherent (or targeted) CW search that uses one year of data has a frequency resolution of about $3 \times 10^{-8}$ Hz. A mismatch between the rotational frequency inferred from the ephemeris and the CW signal frequency of this size or larger is enough to drastically reduce the chance of detection.

A small frequency mismatch may arise for several physical reasons that usually are parametrized in a frequency mismatch of the form $\Delta f_{\text{gw}} \sim f_{\text{gw}}(1 + \delta)$ [14]. In the case of a differential rotation between the GW engine and the electromagnetic pulse engine, the factor $\delta$ will be proportional to the timescale of some torque which enforces correlation between the two engines. Another possibility is that the NS is freely precessing. In this scenario, the $\delta$ factor will be proportional to the angle between the star symmetry axis and the star rotation axis [28]. In some of the previous narrow-band searches [14,26], we used a value of $\delta \sim 10^{-4}$, which can accommodate the previous theoretical models. However starting from the first narrow-band search with advanced detector data [27], we explore a frequency/spin-down range corresponding to $\delta \sim 10^{-3}$.

Another possibility is that the pulsar ephemerides provided are not accurate enough to carry on targeted searches with the required resolution, or they are not available during the observing time of our detectors. That is the case for many low-frequency and energetic pulsars observed in the x- and $\gamma$-ray bands, such as J1833 – 1034 and J1813 – 1749. For these reasons, along with targeted searches, we search for CWs also with narrow-band searches.

In this paper, we present the narrow-band search for CWs from 33 known pulsars using LIGO O2 data. In Sec. II, we provide a brief background on the CW signal model and the algorithm used. In Sec. III, we summarize the main features of the O2 narrow-band analysis, while in Sec. IV, we introduce the pulsars that we have selected for this search. The results of the search followed by the upper limits on the signal strain amplitude are discussed in Sec. V. Finally, in Sec. VI we draw the conclusion of this work.

II. BACKGROUND

A. The signal

The GW signal emitted by an asymmetric spinning NS can be written at the detector frame using the formalism introduced in [29] as the real part of

$$h(t) = H_0(H^+(\eta, \psi)\Lambda_+ (t) + H^x(\eta, \psi)\Lambda_x (t))e^{2\pi if_{\text{gw}}(t)t + i\phi_0},$$

(1)

where $f_{\text{gw}}(t)$ is the GW frequency (which incorporates all the modulation of the signal at the detector frame) and $\phi_0$ an initial phase. The polarization amplitudes $H^+(\eta, \psi), H^x(\eta, \psi)$ are functions of the ratio of the polarization ellipse semiminor to semimajor axis $\eta$ and the polarization angle $\psi$. The functions $\Lambda_+(t), \Lambda_x(t)$ are the detector responses to the two wave polarizations. These two functions depend on the detector geographical location and the $0, \pm 1, \pm 2$ harmonics of the sidereal rotational frequency of Earth $F_{\text{sid}}$ (the inverse of the sidereal day); see [29] for more details. In Eq. (1), the amplitude of the GW $H_0$ is related to the canonical strain amplitude $h_0$ given the angle between the line of sight and the star rotation axis $t$:

$$H_0 = h_0\sqrt{\frac{1 + 6\cos^2 t + \cos^4 t}{4}}$$

(2)

and

$$h_0 = \frac{14\pi^2 G}{d} c^5 I_{zz} f_{\text{gw}}^2 \epsilon,$$

(3)

with $d, I_{zz}$, and $\epsilon$ the star distance, moment of inertia with respect to the rotation axis, and ellipticity. The ellipticity measures the degree of asymmetry of the star with respect to its rotation axis. In the detector reference frame, the signal is modulated by several effects, the most important being the R"omer delay (also called the barycentric correction) due to the detector motion given by Earth’s orbital motion and rotation, with respect to the GW source. Moreover, the GW signal is also modulated by the source’s intrinsic spin-down due to the rotational energy loss from the source. Given a measure of the pulsar rotational frequency $f_{\text{rot}}$, its derivative $\dot{f}_{\text{rot}}$, and distance $d$, the GW signal amplitude can be constrained, assuming that all the star’s rotational energy is lost via gravitational radiation. This theoretical value, which is an upper limit on the rotational energy that can be emitted in GWs, is called the spin-down limit and is given by [30]

$$h_{\text{sd}} = 8.06 \times 10^{-19} f_{\text{rot}}^{1/2} \left[ \frac{1 \text{ kpc}}{d} \right] \left[ \frac{f_{\text{rot}}}{\text{Hz/s}} \right]^{1/2} \left[ \frac{\text{Hz}}{f_{\text{rot}}} \right]^{1/2},$$

(4)

where $I_{38}$ is the star’s moment of inertia in units of $10^{38}$ kg m$^2$. Different values of the moment of inertia are possible according to the NS equation of state, mass, and spin [31]; however, in this work we will assume its canonical value to be $I = 10^{38}$ kg m$^2$. The corresponding spin-down limit on the star’s equatorial fiducial ellipticity can be obtained from Eq. (3),

$$\epsilon_{\text{sd}} = 1.91 \times 10^5 I_{38}^{-1/2} \left[ \frac{f_{\text{rot}}}{\text{Hz/s}} \right]^{1/2} \left[ \frac{\text{Hz}}{f_{\text{rot}}} \right]^{5/2},$$

(5)

which does not depend on the star’s distance.
B. The five-vector narrow-band pipeline

The narrow-band pipeline uses the five-vector method [32] and, in particular, its latest implementation for narrow-band searches described in [33].

The pipeline explores a range of frequency and spin-down values by applying barycentric and spin-down corrections to the data and then identifies the GW signal using its characteristic frequency components.

The pipeline first removes the modulations given by the barycentric corrections and intrinsic source spin-down. The barycentric corrections are applied using a frequency-independent nonuniform resampling [33]. The spin-down is removed by applying a phase correction on the data time series. Also, the Einstein delay is corrected in the time domain.

Once we have removed the barycentric and spin-down modulations of a possible signal, the GW signal power is spread among five frequencies given by the coupling of the signal frequency and the detector sidereal responses $A_+(t), A_{x}(t)$. These frequency components are $f_{\text{gw}} - 2F_{\text{sid}}, f_{\text{gw}} - F_{\text{sid}}, f_{\text{gw}} + F_{\text{sid}}, f_{\text{gw}} + 2F_{\text{sid}}$, and $f_{\text{gw}} + 3F_{\text{sid}}$, where $F_{\text{sid}}$ is the frequency corresponding to the Earth sidereal day.

Hence, a pair of matched filters, one for each sidereal response function, is computed for each point of the explored parameter space. This is done using a frequency grid which allows us to compute the matched filters simultaneously over the whole analyzed frequency band. These steps are done separately for each detector. Then, the output of the matched filters at each point of the parameter space are combined, taking into account the phase shift$^1$ between the two datasets in order to build a detection statistic.

The next step consists of selecting the maximum of the detection statistic for every $10^{-4}$ Hz interval and over the whole spin-down range. Within this set, points in the parameter space with a $p$ value below a 0.1% threshold (taking into account the number of trials) or smaller. In the previous O1 search, we used a threshold of 1% due to the fact that the data quality of LHO and LLO was significantly different at lower frequencies; see Appendix B for more details.

III. THE ANALYSIS

The LIGO second observing run O2 started on November 30, 2016 16:00:00 UTC and ended on August 25, 2017 22:00:00 UTC, while Virgo joined the run later on August 1, 2017 12:00:00 UTC and ended on August 25, 2017 22:00:00 UTC. The narrow-band search can be performed jointly between different detectors if the datasets cover the same observing time. Since Virgo O2 data covered just approximately one month at the end of O2 and was characterized by a lower sensitivity with respect to LIGO data, we have decided to exclude it from the analysis. For this analysis, we have used the second version of calibrated LIGO data (C02) [34]. We jointly analyzed LIGO Hanford (LHO) and LIGO Livingston (LLO) data over the period between January 4, 2017 00:00:00 UTC and August 25, 2017 22:00:00 UTC. LLO data between the beginning of the run and December 22, 2016 have been excluded due to bad spectral contamination, while both detectors underwent a commissioning break between December 22, 2016 and January 4, 2017. The observing time $T_{\text{obs}}$ was $\sim$232 days, implying frequency and spin-down bins of, respectively, $\delta f = 5 \times 10^{-8}$ Hz and $\delta \dot{f} = 2.5 \times 10^{-15}$ Hz/s. LHO and LLO duty cycles were about 45% and 56% and corresponded to an effective observing time of 104 and 129 days, respectively.$^2$ The sensitivity of the O2 search is reported in Fig. 1, where we also show O1 sensitivity. While at lower frequency, only O2 LLO seems to be much better than O1, at higher frequencies the sensitivity is significantly better for both detectors. In order to validate the analysis, we have looked for four hardware injections in the data, checking if their parameters were recovered correctly; see Appendix A.

The explored frequency and spin-down ranges were set to 0.4% of the pulsar rotational frequency and spin-down reported in the ephemeris. Since in this analysis we subsampled data at 1 Hz, the explored frequency region of some pulsars has been chosen manually in order to avoid a possible signal aliasing.

We have decided to select as outliers for the follow-up the points in the parameter space with a value of the detection statistic corresponding to a $p$ value of 0.1% (taking into account the number of trials) or smaller. In the previous O1 search, we used a threshold of 1% due to the fact that the data quality of LHO and LLO was significantly different at lower frequencies; see Appendix B for more details.

IV. SELECTED TARGETS

In our O2 analysis, we have selected as an initial set of targets all the pulsars present in the O1 narrow-band search [27]. Then, we have enlarged it, deciding to analyze all the pulsars with rotation frequency of 10 and 350 Hz with spin-down limit given in Eq. (4) within a factor of 10 from the optimal sensitivity of the search of O2 LLO (in most cases). This choice has been driven by the fact that available pulsar distances can be affected by a large error. The spin-down limit has been computed according to the most recent estimation of the distance given in the ATNF catalog [35] (v1.58) and extrapolating the rotational frequency and spin-down rate at the O2 epoch. For the pulsars J1028 $-5819$, J1112 $-6103$, J1813 $-1246$, and J2043 $+2740$, we have checked that the extrapolated rotational parameters together with the ranges explored in the narrow-band search cover

$^1$This is given by the fact that the data sampling usually does not begin at the exact same time for different detectors.

$^2$With the exception of pulsars that have glitched during the analysis. For those, we have performed two independent analyses before and after the glitch.
the values reported by the updated ephemeris during the O2 epoch in [19]. For the pulsars J0835−4510, J0940−5428, J1105−6107, J1410−6132, J1420−6048, J1531−5610, J1718−3825, J1809−1917, and J1838−0655, the extrapolated spin-down rate resulted off range with respect to the one reported in [19], and for this reason, the searched parameter space has been adjusted in such a way to cover the updated values. For the pulsars J0205 + 6449, J0534 + 2200, J1913 + 1011, J1952 + 3252, and J2229 + 6114, we have used updated ephemerides provided by the telescopes at Jodrell Bank (UK). For the remaining pulsars, no monitoring is present during the O2 run. Even though we are aware that an extrapolation from outdated ephemerides might bring a GW search which does not cover the actual pulsar rotational parameters during O2, we have decided to carry on the analysis in such a way to exploit the possibility that the actual pulsar rotational parameters were covered even partially by the narrow-band search.

Table I reports the spin-down limit on amplitude $h_0$ and ellipticity $\epsilon$ for each target, given their distance estimation and uncertainty. Hereafter, the distance uncertainties are propagated to the derived quantities (such as the spin-down limit) assuming normal distributions, namely,

$$
\sigma_Y^2 = \left( \frac{\partial Y}{\partial d} \right)^2 \sigma_d^2,
$$

with $Y$ being a function of the distance and $\sigma^2$ the distribution variance.

The spin-down limits are compared to the estimated narrow-band search sensitivity in Fig. 1. The analysis covers the 11 targets that we have already analyzed for O1 plus 22 new targets. Based on the estimated sensitivity, we expected to surpass the spin-down limit in the O2 analysis for nine of the 11 O1 targets. The exceptions are J2043 + 2740 and J2229 + 6114, for which the current distance estimation has been increased with respect to the ATNF catalog v1.54 (the catalog used for O1 [27]).
TABLE I. Properties of analyzed pulsars. The second column reports the distance as provided by the ephemerides based on the dispersion measure and the galactic electron density model of [36]. If the pulsar distance is estimated according to an independent measure, we refer to it next to the name entry. The distance uncertainty refers to 1σ confidence level and is assumed to have a normal distribution. In the third and fourth columns, the spin-down limit \( h_{\text{sd}} \) and the corresponding ellipticity \( \epsilon_{\text{sd}} \) are computed using Eqs. (4) and (5).

<table>
<thead>
<tr>
<th>Name</th>
<th>( d ) (kpc)</th>
<th>( h_{\text{sd}} )</th>
<th>( \epsilon_{\text{sd}} )</th>
</tr>
</thead>
<tbody>
<tr>
<td>J0205 + 6449</td>
<td>2.0 ± 0.3</td>
<td>((6.9 ± 1.1) \times 10^{-25})</td>
<td>(1.42 \times 10^{-3})</td>
</tr>
<tr>
<td>J0534 + 2200</td>
<td>2.0 ± 0.5</td>
<td>((1.4 ± 0.4) \times 10^{-24})</td>
<td>(7.56 \times 10^{-4})</td>
</tr>
<tr>
<td>J0537 − 6910</td>
<td>49.7 ± 0.2</td>
<td>((2.91 ± 0.02) \times 10^{-26})</td>
<td>(8.90 \times 10^{-5})</td>
</tr>
<tr>
<td>J0540 − 6919</td>
<td>49.7 ± 0.2</td>
<td>((4.99 ± 0.02) \times 10^{-26})</td>
<td>(1.50 \times 10^{-3})</td>
</tr>
<tr>
<td>J0835 − 4510</td>
<td>0.28 ± 0.02</td>
<td>((3.4 ± 0.3) \times 10^{-24})</td>
<td>(1.80 \times 10^{-3})</td>
</tr>
<tr>
<td>J0940 − 5428</td>
<td>0.2 ± 0.2</td>
<td>((1.3 ± 0.5) \times 10^{-24})</td>
<td>(8.97 \times 10^{-4})</td>
</tr>
<tr>
<td>J1028 − 5819</td>
<td>1.4 ± 0.6</td>
<td>((2.4 ± 1.0) \times 10^{-25})</td>
<td>(6.70 \times 10^{-4})</td>
</tr>
<tr>
<td>J1105 − 6107</td>
<td>2.4 ± 0.9</td>
<td>((1.7 ± 0.7) \times 10^{-25})</td>
<td>(3.82 \times 10^{-4})</td>
</tr>
<tr>
<td>J1112 − 6103</td>
<td>4.5 ± 1.8</td>
<td>((1.3 ± 0.5) \times 10^{-25})</td>
<td>(5.61 \times 10^{-4})</td>
</tr>
<tr>
<td>J1300 + 1240</td>
<td>0.7 ± 0.2</td>
<td>((5.3 ± 1.3) \times 10^{-27})</td>
<td>(3.17 \times 10^{-8})</td>
</tr>
<tr>
<td>J1302 − 6350</td>
<td>2.3 ± 0.9</td>
<td>((7.6 ± 3.0) \times 10^{-26})</td>
<td>(9.52 \times 10^{-5})</td>
</tr>
<tr>
<td>J1400 − 6325</td>
<td>0.9 ± 0.3</td>
<td>((1.0 ± 0.3) \times 10^{-24})</td>
<td>(2.07 \times 10^{-4})</td>
</tr>
<tr>
<td>J1410 − 6132</td>
<td>13.5 ± 5.3</td>
<td>((4.8 ± 1.9) \times 10^{-26})</td>
<td>(3.83 \times 10^{-4})</td>
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<tr>
<td>J1420 − 6048</td>
<td>5.6 ± 2.2</td>
<td>((1.6 ± 0.7) \times 10^{-25})</td>
<td>(9.81 \times 10^{-4})</td>
</tr>
<tr>
<td>J1524 − 5625</td>
<td>3.4 ± 1.3</td>
<td>((1.7 ± 0.7) \times 10^{-25})</td>
<td>(8.25 \times 10^{-4})</td>
</tr>
<tr>
<td>J1531 − 5610</td>
<td>2.8 ± 1.1</td>
<td>((1.2 ± 0.5) \times 10^{-25})</td>
<td>(5.47 \times 10^{-4})</td>
</tr>
<tr>
<td>J1617 − 5055</td>
<td>4.7 ± 1.9</td>
<td>((2.4 ± 1.0) \times 10^{-25})</td>
<td>(1.28 \times 10^{-3})</td>
</tr>
<tr>
<td>J1718 − 3825</td>
<td>3.5 ± 1.4</td>
<td>((9.7 ± 3.8) \times 10^{-26})</td>
<td>(4.48 \times 10^{-4})</td>
</tr>
<tr>
<td>J1747 − 2809</td>
<td>8.2 ± 3.2</td>
<td>((1.7 ± 0.7) \times 10^{-25})</td>
<td>(8.97 \times 10^{-4})</td>
</tr>
<tr>
<td>J1747 − 2958</td>
<td>2.5 ± 1.0</td>
<td>((2.5 ± 1.0) \times 10^{-25})</td>
<td>(1.47 \times 10^{-3})</td>
</tr>
<tr>
<td>J1809 − 1917</td>
<td>3.3 ± 1.3</td>
<td>((1.4 ± 0.6) \times 10^{-25})</td>
<td>(7.27 \times 10^{-4})</td>
</tr>
<tr>
<td>J1811 − 1925</td>
<td>5.0 ± 2.0</td>
<td>((1.3 ± 0.6) \times 10^{-25})</td>
<td>(6.59 \times 10^{-4})</td>
</tr>
<tr>
<td>J1813 − 1246</td>
<td>&gt; 2.5</td>
<td>(&lt; 1.9 \times 10^{-25})</td>
<td>(2.67 \times 10^{-4})</td>
</tr>
<tr>
<td>J1813 − 1749</td>
<td>4.7 ± 0.8</td>
<td>((2.9 ± 0.5) \times 10^{-25})</td>
<td>(6.42 \times 10^{-4})</td>
</tr>
<tr>
<td>J1831 − 0952</td>
<td>3.7 ± 1.5</td>
<td>((7.7 ± 3.0) \times 10^{-26})</td>
<td>(3.04 \times 10^{-4})</td>
</tr>
<tr>
<td>J1833 − 1034</td>
<td>4.1 ± 0.3</td>
<td>((3.6 ± 0.3) \times 10^{-25})</td>
<td>(1.32 \times 10^{-3})</td>
</tr>
<tr>
<td>J1838 − 0655</td>
<td>6.6 ± 0.9</td>
<td>((1.0 ± 0.2) \times 10^{-25})</td>
<td>(7.94 \times 10^{-4})</td>
</tr>
<tr>
<td>J1913 + 1011</td>
<td>4.6 ± 1.8</td>
<td>((5.4 ± 2.1) \times 10^{-26})</td>
<td>(7.54 \times 10^{-5})</td>
</tr>
<tr>
<td>J1952 + 3252</td>
<td>3.0 ± 2.0</td>
<td>((1.0 ± 0.7) \times 10^{-25})</td>
<td>(1.15 \times 10^{-4})</td>
</tr>
<tr>
<td>J2022 + 3842</td>
<td>10.0 ± 2.0</td>
<td>((1.1 ± 0.3) \times 10^{-25})</td>
<td>(6.00 \times 10^{-4})</td>
</tr>
<tr>
<td>J2043 + 2740</td>
<td>1.5 ± 0.6</td>
<td>((6.3 ± 2.5) \times 10^{-26})</td>
<td>(2.03 \times 10^{-4})</td>
</tr>
<tr>
<td>J2124 − 3358</td>
<td>0.4 ± 0.1</td>
<td>((4.3 ± 1.0) \times 10^{-27})</td>
<td>(9.49 \times 10^{-9})</td>
</tr>
<tr>
<td>J2229 + 6114</td>
<td>3.0 ± 2.0</td>
<td>((3.3 ± 2.3) \times 10^{-25})</td>
<td>(6.27 \times 10^{-4})</td>
</tr>
</tbody>
</table>

The new O2 targets mainly consist of pulsars with rotational frequencies within 10 and 20 Hz with spin-down rate \( < 10^{-12}\) Hz/s, but there are also a few millisecond pulsars, for which we can approach the spin-down limit. Among these, there is the millisecond pulsar J2124 + 3358, for which we expect to barely approach the spin-down limit with targeted searches. One of these millisecond pulsars J1300 + 1240 is located in a binary system. However, according to the orbital parameters in the ephemeris, the intrinsic binary orbital modulation on a possible CW signal would be of the order of \( \Delta f_{\text{bin}} \approx 10^{-10}\) Hz, which is below our frequency resolution and hence can be neglected. 3

3The frequency shift due to the binary motion has been computed using [50].

Millisecond pulsars are characterized by a low rotational spin-down value \( \dot{f}_{\text{rot}} \) together with a high rotational frequency \( f_{\text{rot}} \), hence, according to Eq. (4), their spin-down limit will also be harder to surpass our search sensitivities. Although the narrow-band search is currently not sensitive enough for the millisecond pulsars, we have decided to perform the search in order to test the capabilities of the pipeline at higher frequencies. Furthermore, pulsars J0205 + 6449, J0534 + 2200, J0835 − 4510, J1028 − 5819, and J1718 − 3825 had a glitch during O2. J0205 + 6449 glitched on May 27, 2017, J0534 + 2200 glitched on March 27, 2017, J0835 − 4510 had a glitch on December 16, 2016 [51], J1028 − 5819 glitched on May 29, 2017, and J1718 − 3825 glitched on May 1 July 2017 [19]. For these pulsars, we have performed two independent analyses, one before and one after the glitch, excluding...
the day in which the glitch was present. For J0835 – 4510 and J1718 – 3825, only the analysis after or before the glitch was done, since few data were available before or after the two glitches.

Table II reports the frequency/spin-down regions that we have analyzed for each of the 33 targets. The reference time for the rotational parameters of the pulsars is December 1, 2016 00:00:00 UTC.

V. RESULTS

The search has produced a total of 49 outliers for 15 of the 33 targets. Every outlier underwent a chain of follow-up steps aimed to test its nature, namely, (i) check for the presence of known instrumental noise lines, (ii) compare the SNR GW amplitude estimation among several detectors, and (iii) study the outlier significance with software injections. The outliers are given in Table III together with the follow-up step where we excluded them.

The narrow-band search carried out in the past on O1 data [27] produced two interesting outliers for J0835 – 4510 and 1833 – 1034. In order to confirm or reject them, the data from the first four months of O2 (available with calibration version C01 at the time) were used and no evidence of a signal was found. The full O2 analysis discussed in this paper confirms those findings. No outlier
TABLE III. This table summarizes the outliers found in the O2 narrow-band search. The first column reports the name of the pulsar for which we have found outliers. The second column gives the central frequency of the pulsar search band, and the third column the p value of the least significant outlier. The last column reports the step of the follow-up in which we have vetoed the outliers. For a description of the follow-up steps, refer to the main text.

<table>
<thead>
<tr>
<th>Name</th>
<th>f</th>
<th>Number of outliers</th>
<th>p value</th>
<th>Step</th>
</tr>
</thead>
<tbody>
<tr>
<td>J1105 – 6107</td>
<td>31.64</td>
<td>16</td>
<td>4.23 × 10^{-4}</td>
<td>i,ii</td>
</tr>
<tr>
<td>J1112 – 6103</td>
<td>30.78</td>
<td>1</td>
<td>1.83 × 10^{-4}</td>
<td>ii</td>
</tr>
<tr>
<td>J1300 + 1240</td>
<td>321.62</td>
<td>1</td>
<td>7.80 × 10^{-4}</td>
<td>iii</td>
</tr>
<tr>
<td>J1302 – 6350</td>
<td>41.87</td>
<td>4</td>
<td>7.79 × 10^{-4}</td>
<td>ii</td>
</tr>
<tr>
<td>J1420 – 6048</td>
<td>29.32</td>
<td>11</td>
<td>9.82 × 10^{-4}</td>
<td>i,ii</td>
</tr>
<tr>
<td>J1531 – 5610</td>
<td>23.75</td>
<td>1</td>
<td>4.65 × 10^{-4}</td>
<td>ii</td>
</tr>
<tr>
<td>J1617 – 5055</td>
<td>28.80</td>
<td>2</td>
<td>7.80 × 10^{-4}</td>
<td>i,ii</td>
</tr>
<tr>
<td>J1747 – 2809</td>
<td>38.32</td>
<td>1</td>
<td>9.68 × 10^{-4}</td>
<td>ii</td>
</tr>
<tr>
<td>J1811 – 1925</td>
<td>30.91</td>
<td>1</td>
<td>3.30 × 10^{-4}</td>
<td>ii</td>
</tr>
<tr>
<td>J1813 – 1246</td>
<td>41.60</td>
<td>2</td>
<td>6.73 × 10^{-4}</td>
<td>ii,iii</td>
</tr>
<tr>
<td>J1831 – 0952</td>
<td>29.73</td>
<td>1</td>
<td>2.15 × 10^{-4}</td>
<td>ii</td>
</tr>
<tr>
<td>J1833 – 1034</td>
<td>32.29</td>
<td>1</td>
<td>9.33 × 10^{-4}</td>
<td>ii</td>
</tr>
<tr>
<td>J1952 + 3252</td>
<td>50.59</td>
<td>4</td>
<td>4.48 × 10^{-4}</td>
<td>i,ii</td>
</tr>
<tr>
<td>J2124 – 3358</td>
<td>405.59</td>
<td>2</td>
<td>5.61 × 10^{-4}</td>
<td>i,ii</td>
</tr>
<tr>
<td>J2229 + 6114</td>
<td>38.71</td>
<td>1</td>
<td>9.66 × 10^{-4}</td>
<td>ii</td>
</tr>
</tbody>
</table>

*a Most vetoed since they are close to the comb line of the 0.987925 Hz comb in LLO and the comb line of 2.109223 Hz in LHO.

*b Various unidentified lines around 35.51 Hz.

*c Unidentified noise disturbance in LHO at 41.8838 Hz.

*d Combin. of 1.945501 Hz in LHO.

*e Unidentified combed line disturbance at 41.654–41.660 Hz.

*f Combin. of 2.109223 Hz in LHO, comb. of 1.9455045 Hz in LHO, comb. of 1.945437 Hz in LHO.

*g Combin. of 0.9967943 Hz in LLO.

has been found for J0835 – 4510, while an outlier has been found for J1833 – 1034, at a slightly different frequency which, however, as discussed in the next section, has been vetoed.

A. Outliers follow-up

The first step of the follow-up was to check if a known instrumental noise line was present in one of the two detectors [52]. This ruled out most of the candidates for the pulsars J1105 – 6107 and J2121 – 3358; see Appendix C for more details.

The second step of the follow-up was to study the evolution of the recovered signal-to-noise ratio (SNR) and amplitude $h_0$ with respect to the fraction of data samples that we were integrating. We expect the SNR to increase as the square root of the integration time and the amplitude $h_0$ to be nearly constant. We have performed this type of test in a LHO, LLO, and joint search for different integration times, checking if the SNR and $h_0$ estimation were compatible across the different cases.

Many outliers at frequencies <100 Hz have been classified as LHO disturbances since they have been observed only in LHO (see Appendix C). Some of these are in proximity of unidentified noise lines (lines which are confidently classified as detector disturbances but whose origin is unknown). That is the case of the outliers from J1112 – 6103, J1302 – 6350, and J1813 – 1246. Other outliers at low frequency were not in proximity to unidentified noise lines but have been vetoed as the signal-to-noise ratio is bigger than 8 only in LHO data, which has a sensitivity 2 to 3 times worse than LLO, thus, being incompatible with a true CW signal.

Only three outliers survived up to the third step of the follow-up, namely, from pulsars J1300 + 1240, J1617 – 5055, and J2124 – 3358. For all these pulsars, we cannot approach the theoretical spin-down limit with our current search sensitivity, and this is a strong hint of the noise origin of these outliers. The last step of the follow-up consisted of studying the SNR and recovered CW amplitude $h_0$ with software injections with an amplitude $h_0$ fixed to that estimated for the outlier. The evolution of the SNR and $h_0$ for the outlier are then compared to the distributions derived from the injections. If they are compatible among the three different analyses, LHO, LLO, and joint combination, the outlier is subject to more dedicated studies. The two remaining outliers for the millisecond pulsars were ruled out since they were present in just one detector, while the injections predicted that they would be visible in both detectors. The J1617 – 5055 remaining outlier was also ruled out, as the injections show that they were likely driven by a LHO disturbance. Refer to Appendix C for more details on the last steps of this follow-up.

B. Upper limits

Since there was no evidence of the presence of a CW signal, we have computed upper limits (ULs) on the CW amplitude $h_0$. The ULs have been produced using the same procedure as in the O1 narrow-band search [27], which consists of injecting nonoverlapping GW signals with fixed amplitude $h_0$ in data every $10^{-4}$ Hz intervals. When 95% of injections produce a value of the detection statistic higher than the one used for the outlier selection, we set the upper limit to the injected amplitude value.

Figure 1 shows the median value of the UL for each of the 33 targets. The ULs are driven at lower frequencies by LLO sensitivity since it is the most sensitive detector in that frequency region. On the other hand, at higher frequencies, the ULs lie close to the sensitivity of the two detectors, which are indeed similar.

Table IV summarizes our results of the O2 narrow-band search. The table reports the median value of the UL on the strain amplitude $h_0$ and the corresponding ellipticity computed using Eq. (5). We consider the spin-down limit surpassed for a given pulsar if the ULs are lower than the spin-down limit over the entire frequency band.

The most stringent ULs have been set for the three pulsars J0537 – 6910, J1300 + 1240, and J2124 – 3358.
and are of the order of $5.5 \times 10^{-26}$ which, however, are above the spin-down limit. The lowest ellipticity UL has been set for J1300 + 1240, of about $3.3 \times 10^{-7}$. We have been able to surpass the spin-down limit for the pulsars J0205 + 6449, J0534 + 2200 (Crab), J0835 − 4510 (Vela), J1400 − 6325, J1813 − 1246 (assuming the lower bound for the distance), J1813 − 1749, J1833 − 1034, and J2229 + 6114. For J0940 − 5428, while the median value
of the UL is below the spin-down limit, a small fraction of the individual results are above. For J1747 – 2809 and J1952 + 3252, we are close to surpassing the spin-down limit, see Table IV. For all the pulsars for which we have surpassed the spin-down limit, we have computed the upper limit on the ratio of the GW to the rotational energy loss. The lower ULs on the GW energy loss are for J0534 + 2200 and J1400 – 6325 corresponding to a fraction of about 0.8%. The lowest ULs on the GW amplitude and ellipticity among the pulsars for which we have surpassed the spin-down limit are, respectively, 8.29 × 10^{-26} and 1.78 × 10^{-5} for J1400 – 6325. For a canonical pulsar with a radius of about 10 km, this number would correspond to a maximum surface deformation of about 5 cm.

For the remaining 22 targets, we were not able to surpass the spin-down limit. Table IV roughly suggests to us that an improvement in sensitivity of a factor 3 is needed for most of the low-frequency pulsars. It must be considered, however, that the spin-down limits have been computed assuming a canonical value for the moment of inertia of 10^{38} kg m^2. In fact, it could be significantly larger, depending on the NS equation of state, up to ≈ 3 x 10^{38} kg m^2, implying a spin-down limit ∼ √(3) times larger.

VI. CONCLUSION

Overall, the narrow-band search over O2 data has brought an improvement with respect to previous searches in terms of ULs. On the other hand, ULs are similar to those found in O1 for pulsars with rotation frequency below 30 Hz. For instance, the UL on the Vela Pulsar (around 22 Hz) has improved by 10%, while the UL on J0205 + 6449 has improved by about 22%. On the other hand, for pulsars with expected GW frequencies >30 Hz, the UL is improved even by a factor 2. The UL on J0534 + 2200 did not improve, since in O2 we split the analysis in two different chunks due to the presence of the glitch. For this reason, the UL both before and after the glitch is comparable to the one found in the O1 analysis. We have also been able to surpass the spin-down limit for two pulsars that were not analyzed in O1, J0940 – 5428, J1747 – 2809.

We still have not been able to surpass the spin-down limit for the millisecond pulsars and for low-frequency pulsars with spin-down below ∼ 10^{-12} Hz/s. However, we have been able to surpass the spin-down limit for low-frequency and high energetic pulsars (such as Crab or J1833 – 1034) or for low-frequency pulsars that are close to Earth.

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4Excluding a frequency band heavily contaminated by noise.
5Please note that the spin-down limit of this pulsar has been computed using two different distances in O1 and O2. For O1, we used 2.0 kpc [54], while for O2 the nominal ephemeris value was 3.2 kpc.
define the relative error on the CW amplitude recovery as estimating the accuracy of the recovered parameters. We have looked for four hardware injections in LIGO data to validate the efficiency of the pipeline used in this paper, monitored and their injected parameters are known. In order to validate the efficiency of the pipeline used in this paper, we have looked for four hardware injections in LIGO data studying the accuracy of the recovered parameters. We define the relative error on the CW amplitude recovery as 

\[ \epsilon_{h_0} = 1 - \frac{h_{0,\text{est}}}{h_{0,\text{inj}}} \]

where \( h_{0,\text{inj}} \) is the injected CW amplitude and \( h_{0,\text{est}} \) is the recovered value, whereas we define the relative error on the angular parameters \( \eta \) as 

\[ \epsilon_\eta = \frac{|\eta_{\text{inj}} - \eta_{\text{est}}|}{90 \deg} \]

and \( \epsilon_\psi = \frac{|\psi_{\text{inj}} - \psi_{\text{est}}|}{2} \). Table V reports the errors on the parameter estimation for the validation tests performed with the O2 hardware injections.

**APPENDIX A: VALIDATION WITH HARDWARE INJECTIONS**

Hardware injections are simulated signals in LIGO-Virgo data for testing purposes. These artificial signals are injected by a control system which acts on the mirror and simulates a CW signal. The hardware injections are continuously monitored and their injected parameters are known. In order to validate the efficiency of the pipeline used in this paper, we have looked for four hardware injections in LIGO data studying the accuracy of the recovered parameters. We define the relative error on the CW amplitude recovery as 

\[ \epsilon_{h_0} = 1 - \frac{h_{0,\text{est}}}{h_{0,\text{inj}}} \]

where \( h_{0,\text{inj}} \) is the injected CW amplitude and \( h_{0,\text{est}} \) is the recovered value, whereas we define the relative error on the angular parameters \( \eta \) as 

\[ \epsilon_\eta = \frac{|\eta_{\text{inj}} - \eta_{\text{est}}|}{90 \deg} \]

and \( \epsilon_\psi = \frac{|\psi_{\text{inj}} - \psi_{\text{est}}|}{2} \). Table V reports the errors on the parameter estimation for the validation tests performed with the O2 hardware injections.

**APPENDIX B: VALIDATION OF THE THRESHOLD**

The narrow-band search is based on the five-vector method [29] that was implemented originally for targeted searches. In that context, just one template is explored for each detector, and an overall threshold on the p value of, say, 1% for the candidate selection, is sufficient to efficiently recover 95% of injected signals with SNR = 8. However, in narrow-band searches, we are exploring a large number of templates in a frequency region of about 0.04 Hz or more, using two detectors that have different data quality, i.e., different level of noise and duty cycle. The threshold in this case is computed by using as noise background the values of the statistic excluded from the local maxima selection and then extrapolating the long tails of the distribution. By definition, these excluded points are representative of the noise level in the given frequency bands. This means that, if the noise level in the 10^{-4} Hz wide frequency subband that we are analyzing is slightly higher than the noise level in the overall frequency region from which we are generating noise backgrounds, then close-to-threshold outliers will occur. These close-to-threshold outliers may not be completely distinguishable from the actual noise. As an example, we have generated 200 software injections with amplitude \( h_0 \) fixed to the one that generated a 1% p-value outlier in the postglitch analysis of pulsar J0534 + 2200. We have estimated the recovered signal-to-noise ratio of the injections by integrating coherently more and more data from LHO and LLO. If the injections are distinguishable from the noise, we expect 95% of the injections to have a recovered signal-to-noise ratio greater than 8. However, it is shown by Fig. 2 that this is not the case. For a full coherent LHO-LLO search, the distribution of the recovered SNR is below 8. We have also performed the same test by injecting fake signals with an amplitude \( h_0 \) that would correspond to a 0.1% outlier. In this case, as shown in Fig. 2, the recovered SNR of the injections is higher than 8, confirming that the 0.1% p-value threshold represents a more conservative choice while recovering CW signals.

**APPENDIX C: FOLLOW-UP TEST CASES**

We report in this Appendix some explanatory plots of the analysis steps used for outliers follow-up. The first step

![FIG. 2. Vertical axis: Fraction of injections recovered with a SNR equal to or higher than the one indicated on the horizontal axis. The different line colors indicate a set of software injections that would produce an outlier at 1% and 0.1% according to the evaluation of the noise-only distribution of the detection statistic. The red dashed vertical line indicates the SNR = 8 threshold that is commonly used to distinguish the signal from the noise.](image)

![FIG. 3. Top: LHO spectrum around the expected frequency of J1105 − 6107. Bottom: LLO spectrum around the expected signal frequency of J1105 − 6107. In both detectors, we see the contribution of various noise lines which are known combs with fundamental frequency 0.987925 Hz in LLO and 2.109223 Hz in LHO.](image)
consisted of checking if a known noise line was present in the proximity of the outlier. We considered an outlier consistent with a known noise disturbance if it was found in a frequency region covered by the frequency variation of the noise line due to the Doppler and spin-down corrections.

Many of the outliers found in the case of the pulsar J1105 − 6107 and J1952 + 3252 originated from vetoed combs in one or both of the detectors. Figures 3 and 4 show the spectra of the time series obtained for the J1105 − 6107 and J1952 + 3252 outliers. In the first case, noise combs pollute both LLO and LHO, while in the second case, different noise combs contribute to the same noise disturbance at 50.58 Hz in the LHO data.

The second step of the follow-up chain was to study the evolution of the recovered CW amplitude $h_0$ and the recovered SNR of the outlier with respect to the integration time. In Fig. 5, we report the recovered SNR for different integration times. In this frequency region, the LHO noise floor is about 2 times higher than the LLO noise floor. Hence, in the presence of a reliable CW outlier, we would expect the recovered SNR to be higher in LLO and the joint analysis. As shown in Fig. 5, this is not the case, and the outlier is probably due to an unknown noise disturbance in LHO.

The last step of the follow-up consisted of studying the noise properties with software injections around the candidates. The software injections had amplitude $h_0$ equal to the one recovered from the most sensitive search. This corresponds to LLO for most of the frequencies <40 Hz, while it is the joint search if the noise floor of the two detectors is comparable. The recovered distribution of the CW amplitude and SNR for the software injections is then plotted with respect to the integration time of the analysis and compared with the recovered CW amplitude and SNR for the outlier. Figure 6 shows the distributions of the recovered SNR and CW amplitude for 200 software injections with an amplitude fixed at $h_0 = 3.9 \times 10^{-26}$, which is the one recovered for the outlier of the millisecond pulsar J1300 + 1240 in the joint search. The software injections have a frequency at least $10^{-3}$ Hz away from the actual outlier, in such a way as to not interfere with the

![Figure 4](image1.png)

**FIG. 4.** Top: LHO spectrum around the expected frequency of J1952 + 3252. Bottom: LLO spectrum around the expected frequency of J1952 + 3252. In LHO we see the contribution of various noise lines due to combs with fundamental frequencies 2.109223, 1.9455045, and 1.945437 Hz in LHO.

![Figure 5](image2.png)

**FIG. 5.** Example of the first stage follow-up for one of the candidates of J1105 + 6107 that were not vetoed. The recovered SNR of the outlier is on the vertical axis, while the horizontal axis indicates the fraction of data samples that we are integrating with the matched filter. The outlier is visible only in LHO and propagates to the joint analysis.

![Figure 6](image3.png)

**FIG. 6.** These plots show the distribution of the recovered CW amplitude $h_0$ and SNR for 200 software injections in the frequency region around the outlier of the millisecond pulsar J1300 + 1240. The black dashed line indicates the observed estimator for the outlier. First and second rows of plots: Recovered CW amplitude and SNR. First, second, and third columns of plots: Joint, LLO, and LHO searches.
outlier. From Fig. 6 we can see that the outlier seems to be compatible with the results of the software injections in LLO data, but on the other hand, it is not compatible with the joint and LHO analysis. In this frequency region, LLO data, but on the other hand, it is not compatible with the results of the software injections in outlier. From Fig. 6 we can see that the outlier seems to be comparable results for the LLO and LHO analysis.


1LIGO, California Institute of Technology, Pasadena, California 91125, USA
2Louisiana State University, Baton Rouge, Louisiana 70803, USA
3Inter-University Centre for Astronomy and Astrophysics, Pune 411007, India
4Università di Salerno, Fisciano, I-84084 Salerno, Italy
5INFN, Sezione di Napoli, Complesso Universitario di Monte S.Angelo, I-80126 Napoli, Italy
6OzGrav, School of Physics & Astronomy, Monash University, Clayton 3800, Victoria, Australia
7LIGO Livingston Observatory, Livingston, Louisiana 70754, USA
8Max Planck Institute for Gravitational Physics (Albert Einstein Institute), D-30167 Hannover, Germany
9Leibniz Universität Hannover, D-30167 Hannover, Germany
10University of Cambridge, Cambridge CB2 1TN, United Kingdom
11University of Birmingham, Birmingham B15 2TT, United Kingdom
12LIGO, Massachusetts Institute of Technology, Cambridge, Massachusetts 02139, USA
13Instituto Nacional de Pesquisas Espaciais, 12227-010 São José dos Campos, São Paulo, Brazil
14Gran Sasso Science Institute (GSSI), I-67100‘Aquila, Italy
15INFN, Laboratori Nazionali del Gran Sasso, I-67100 Assergi, Italy
16International Centre for Theoretical Sciences, Tata Institute of Fundamental Research, Bengaluru 560089, India
17NCSA, University of Illinois at Urbana-Champaign, Urbana, Illinois 61801, USA
18Università di Pisa, I-56127 Pisa, Italy
19INFN, Sezione di Pisa, I-56127 Pisa, Italy
20Departamento de Astronomia y Astrofísica, Universitat de València, E-46100 Burjassot, València, Spain
21OzGrav, Australian National University, Canberra, Australian Capital Territory 0200, Australia
22Laboratoire des Matériaux Avancés (LMA), CNRS/IN2P3, F-69622 Villeurbanne, France
23University of Wisconsin-Milwaukee, Milwaukee, Wisconsin 53201, USA
24SUPA, University of Strathclyde, Glasgow G1 1XQ, United Kingdom
25LAL, Univ. Paris-Sud, CNRS/IN2P3, Université Paris-Saclay, F-91898 Orsay, France
26California State University Fullerton, Fullerton, California 92831, USA
27APC, AstroParticule et Cosmologie, Université Paris Diderot, CNRS/IN2P3, Observatoire de Paris, Sorbonne Paris Cité, F-75205 Paris Cedex 13, France
28European Gravitational Observatory (EGO), I-56021 Cascina, Pisa, Italy
29Università di Roma Tor Vergata, I-00133 Roma, Italy
30INFN, Sezione di Roma Tor Vergata, I-00133 Roma, Italy
31INFN, Sezione di Roma, I-00185 Roma, Italy
32Laboratoire d’Annecy de Physique des Particules (LAPP), Univ. Grenoble Alpes, University Savoie Mont Blanc, CNRS/IN2P3, F-74941 Annecy, France
33Embry-Riddle Aeronautical University, Prescott, Arizona 86301, USA
34Montclair State University, Montclair, New Jersey 07043, USA
35Max Planck Institute for Gravitational Physics (Albert Einstein Institute), D-14476 Potsdam-Golm, Germany
36Nikhef, Science Park 105, 1098 XG Amsterdam, Netherlands
37Korea Institute of Science and Technology Information, Daejeon 34141, South Korea
38West Virginia University, Morgantown, West Virginia 26506, USA
39Università di Perugia, I-06123 Perugia, Italy
40INFN, Sezione di Perugia, I-06123 Perugia, Italy
41Syracuse University, Syracuse, New York 13244, USA
42University of Minnesota, Minneapolis, Minnesota 55455, USA
43SUPA, University of Glasgow, Glasgow G12 8QQ, United Kingdom
44LIGO Hanford Observatory, Richland, Washington, D.C. 99352, USA
45Caltech CaRT, Pasadena, California 91125, USA
46Wigner RCP, RMKI, H-1121 Budapest, Konkoly Thege Mikhó út 29-33, Hungary
47University of Florida, Gainesville, Florida 32611, USA
48Stanford University, Stanford, California 94305, USA
49Università di Camerino, Dipartimento di Fisica, I-62032 Camerino, Italy
50Università di Padova, Dipartimento di Fisica e Astronomia, I-35131 Padova, Italy
51INFN, Sezione di Padova, I-35131 Padova, Italy
52Montana State University, Bozeman, Montana 59717, USA
53Nicolaus Copernicus Astronomical Center, Polish Academy of Sciences, 00-716, Warsaw, Poland
54OzGrav, University of Adelaide, Adelaide, South Australia 5005, Australia
55Theoretisch-Physikalisches Institut, Friedrich-Schiller-Universität Jena, D-07743 Jena, Germany
56INFN, Sezione di Milano Bicocca, Gruppo Collegato di Parma, I-43124 Parma, Italy
109 Dipartimento di Scienze Matematiche, Fisiche e Informatiche, Università di Parma, P-43124 Parma, Italy

110 California State University, Los Angeles, 5151 State University Drive, Los Angeles, California 90032, USA

111 Universität di Trento, Dipartimento di Fisica, I-38123 Povo, Trento, Italy

112 Università di Roma ‘La Sapienza,’ I-00185 Roma, Italy

113 Colorado State University, Fort Collins, Colorado 80523, USA

114 Kenyon College, Gambier, Ohio 43022, USA

115 Christopher Newport University, Newport News, Virginia 23606, USA

116 National Astronomical Observatory of Japan, 2-21-1 Osawa, Mitaka, Tokyo 181-8588, Japan

117 Canadian Institute for Theoretical Astrophysics, University of Toronto, Toronto, Ontario M5S 3H8, Canada

118 Observatori Astronòmic, Universitat de València, E-46980 Paterna, València, Spain

119 School of Mathematics, University of Edinburgh, Edinburgh EH9 3FD, United Kingdom

120 Institute for Advanced Research, Gandhinagar 382426, India

121 Indian Institute of Technology Bombay, Powai, Mumbai 400 076, India

122 University of Szeged, Dóm tér 9, Szeged 6720, Hungary

123 Tata Institute of Fundamental Research, Mumbai 400005, India

124 INAF, Osservatorio Astronomico di Capodimonte, I-80131, Napoli, Italy

125 University of Michigan, Ann Arbor, Michigan 48109, USA

126 American University, Washington, D.C. 20016, USA

127 GRAPPA, Anton Pannekoek Institute for Astronomy and Institute of High-Energy Physics, University of Amsterdam, Science Park 904, 1098 XH Amsterdam, Netherlands

128 Delta Institute for Theoretical Physics, Science Park 904, 1090 GL Amsterdam, Netherlands

129 Directorate of Construction, Services & Estate Management, Mumbai 400094 India

130 University of Białystok, 15-424 Białystok, Poland

131 King’s College London, University of London, London WC2R 2LS, United Kingdom

132 University of Southampton, Southampton SO17 1BJ, United Kingdom

133 University of Washington Bothell, Bothell, Washington, D.C. 98011, USA

134 Institute of Applied Physics, Nizhny Novgorod, 603950, Russia

135 Ewha Womans University, Seoul 03760, South Korea

136 Inje University Gumi, South Gyeongsang 50834, South Korea

137 National Institute for Mathematical Sciences, Daejeon 34047, South Korea

138 Ulsan National Institute of Science and Technology, Ulsan 44919, South Korea

139 Universität Hamburg, D-22761 Hamburg, Germany

140 Maastricht University, P.O. Box 616, 6200 MD Maastricht, Netherlands

141 Chennai Mathematical Institute, Chennai 603103, India

142 NCBJ, 05-400 Świerk-Otwock, Poland

143 Institute of Mathematics, Polish Academy of Sciences, 00656 Warsaw, Poland

144 Cornell University, Ithaca, New York 14850, USA

145 Hillsdale College, Hillsdale, Michigan 49242, USA

146 Hanyang University, Seoul 04763, South Korea

147 Korea Astronomy and Space Science Institute, Daejeon 34055, South Korea

148 NASA Marshall Space Flight Center, Huntsville, Alabama 35811, USA

149 Dipartimento di Matematica e Fisica, Università degli Studi Roma Tre, I-00146 Roma, Italy

150 INFN, Sezione di Roma Tre, I-00146 Roma, Italy

151 ESPCI, CNRS, F-75005 Paris, France

152 OzGrav, Swinburne University of Technology, Hawthorn VIC 3122, Australia

153 University of Portsmouth, Portsmouth, PO1 3FX, United Kingdom

154 Southern University and A&M College, Baton Rouge, Louisiana 70813, USA

155 College of William and Mary, Williamsburg, Virginia 23187, USA

156 Centre Scientifique de Monaco, 8 quai Antoine Ier, MC-98000, Monaco

157 Indian Institute of Technology Madras, Chennai 600036, India

158 INFN Sezione di Torino, Via P. Giuria 1, I-10125 Torino, Italy

159 Institut des Hautes Etudes Scientifiques, F-91440 Bures-sur-Yvette, France

160 IISER-Kolkata, Mohanpur, West Bengal 741252, India

161 Whitman College, 345 Boyer Avenue, Walla Walla, Washington, D.C. 99362 USA

162 Université de Lyon, F-69361 Lyon, France

163 Hobart and William Smith Colleges, Geneva, New York 14456, USA

164 Janusz Gil Institute of Astronomy, University of Zielona Góra, 65-265 Zielona Góra, Poland