Measurement of the ratio of cross sections for inclusive isolated-photon production in $pp$ collisions at $\sqrt{s} = 13$ and 8 TeV with the ATLAS detector

The ATLAS collaboration

E-mail: atlas.publications@cern.ch

Abstract: The ratio of the cross sections for inclusive isolated-photon production in $pp$ collisions at centre-of-mass energies of 13 and 8 TeV is measured using the ATLAS detector at the LHC. The integrated luminosities of the 13 TeV and 8 TeV datasets are 3.2 fb$^{-1}$ and 20.2 fb$^{-1}$, respectively. The ratio is measured as a function of the photon transverse energy in different regions of the photon pseudorapidity. The predictions from next-to-leading-order perturbative QCD calculations are compared with the measured ratio. The experimental systematic uncertainties as well as the uncertainties affecting the predictions are evaluated taking into account the correlations between the two centre-of-mass energies, resulting in a reduction of up to a factor of 2.5 (5) in the experimental (theoretical) systematic uncertainties. The predictions based on several parameterisations of the proton parton distribution functions agree with the data within the reduced experimental and theoretical uncertainties. In addition, this ratio to that of the fiducial cross sections for $Z$ boson production at 13 and 8 TeV using the decay channels $Z \rightarrow e^+e^-$ and $Z \rightarrow \mu^+\mu^-$ is made and compared with the theoretical predictions. In this double ratio, a further reduction of the experimental uncertainty is obtained because the uncertainties arising from the luminosity measurement cancel out. The predictions describe the measurements of the double ratio within the theoretical and experimental uncertainties.

Keywords: Hadron-Hadron scattering (experiments), Photon production, QCD

ArXiv ePrint: 1901.10075

https://doi.org/10.1007/JHEP04(2019)093
1 Introduction

The production of prompt photons in proton-proton collisions, \( pp \rightarrow \gamma + X \), provides a means of testing perturbative QCD (pQCD) with a hard colourless probe. Since the dominant production mechanism in \( pp \) collisions at the LHC proceeds via the \( qg \rightarrow q\gamma \) process, measurements of prompt-photon\(^1\) production are sensitive to the gluon density in the proton \([1, 2]\). These measurements can also be used to tune Monte Carlo (MC) models to improve our understanding of prompt-photon production and aid those analyses for which events containing photons are an important background.

\(^1\)All photons produced in \( pp \) collisions that are not secondaries from hadron decays are considered to be “prompt”.

---

\[ \text{JHEP04(2019)093} \]
At leading order (LO) in pQCD, two processes contribute to prompt-photon production: the direct-photon process, in which the photon originates directly from the hard interaction, and the fragmentation-photon process, in which the photon is emitted in the fragmentation of a high transverse momentum ($p_T$) parton \cite{3, 4}.

Measurements of prompt-photon production at a hadron collider necessitate an isolation requirement to reduce the large contribution of photons from hadron decays and the fragmentation component in which the emitted photon is close to a jet. The production of isolated photons in $pp$ collisions has been measured previously by the ATLAS \cite{5-9} and CMS \cite{10, 11} collaborations at centre-of-mass energies ($\sqrt{s}$) of 7, 8 and 13 TeV.

Comparisons of measurements of prompt-photon production and pQCD predictions are usually limited by the theoretical uncertainties associated with the missing higher-order terms in the perturbative expansion. The measurements of inclusive isolated-photon cross sections performed by ATLAS at 13 TeV \cite{9} and 8 TeV \cite{8} were compared with the predictions of pQCD at next-to-leading order (NLO) \cite{12, 13}. At both centre-of-mass energies, the uncertainties affecting the predictions are dominated by terms beyond NLO and are larger than those of experimental nature, preventing a more precise test of the theory. An avenue to reach a more stringent test is the inclusion of next-to-next-to-leading-order (NNLO) QCD corrections in the calculations \cite{14}. Another avenue is to make measurements of the ratio of cross sections for inclusive isolated-photon production at 13 and 8 TeV ($R_{13/8}$) and compare them with the predictions \cite{15, 16}. The impact of the experimental systematic uncertainties and theoretical uncertainties on the ratio of the cross sections is reduced, allowing a more precise comparison between data and theory. This is achieved by accounting for inter-$\sqrt{s}$ correlations in the experimental systematic uncertainties affecting the measurements and in the uncertainties of the theory predictions.

A further reduction of the experimental uncertainty can be achieved by measuring a double ratio: the ratio of $R_{13/8}$ to the ratio of the fiducial cross sections for $Z$ boson production at 13 TeV and 8 TeV ($R_{13/8}^Z \equiv \sigma_Z^{13/8}(13 \text{ TeV})/\sigma_Z^{13/8}(8 \text{ TeV})$) presented in ref. \cite{17}. The measurements of the fiducial cross sections for $Z$ boson production use the decay channels $Z \rightarrow e^+e^-$ and $Z \rightarrow \mu^+\mu^-$. This observable, $D_{13/8}^{\gamma/Z} \equiv R_{13/8}^\gamma/R_{13/8}^Z$, can be viewed as the increase of the cross section for isolated-photon production as a function of $\sqrt{s}$ normalised to the increase for $Z$ boson production as a function of $\sqrt{s}$. Measuring $D_{13/8}^{\gamma/Z}$ is beneficial because the uncertainties from the luminosity measurement cancel out, and $D_{13/8}^{\gamma/Z}$ has only a slightly larger theory uncertainty than $R_{13/8}^\gamma$.

This paper presents measurements of the ratio of cross sections for isolated-photon production in $pp$ collisions at $\sqrt{s} = 13$ TeV and 8 TeV with the ATLAS detector at the LHC. The phase-space region is given by the overlap of the ATLAS measurements at $\sqrt{s} = 13$ and 8 TeV, defined by the photon transverse energy\footnote{ATLAS uses a right-handed coordinate system with its origin at the nominal interaction point (IP) in the centre of the detector and the z-axis along the beam pipe. The x-axis points from the IP to the centre of the LHC ring, and the y-axis points upwards. Cylindrical coordinates ($r, \phi$) are used in the transverse plane, $\phi$ being the azimuthal angle around the z-axis. The pseudorapidity is defined in terms of the polar angle $\theta$ as $\eta = -\ln \tan(\theta/2)$.} ($E_T$) in the range $E_T > 125$ GeV and the photon pseudorapidity ($\eta$) in the region $|\eta| < 2.37$, excluding
the region $1.37 < |\eta| < 1.56$. The photon is isolated by requiring that the transverse energy inside a cone of size $\Delta R \equiv \sqrt{(\Delta \eta)^2 + (\Delta \phi)^2} = 0.4$ in the $\eta$-$\phi$ plane around the photon direction, $E_T^{\text{iso}}$, is smaller than $E_T^{\text{iso, cut}} \equiv 4.2 \cdot 10^{-3} \cdot E_T^\gamma + 4.8$ GeV \cite{8, 9}. Non-isolated prompt photons are not considered as signal. The measurements of the ratios are based on the ATLAS measurements at 13 TeV \cite{9} and 8 TeV \cite{8} and a detailed study of the correlations of the experimental systematic uncertainties between the two centre-of-mass energies is presented here. The measurement of the ratios is presented as a function of $E_T^\gamma$ in different regions of $\eta$, namely $|\eta| < 0.6$, $0.6 < |\eta| < 1.37$, $1.56 < |\eta| < 1.81$ and $1.81 < |\eta| < 2.37$. Next-to-leading-order pQCD predictions for the ratio are compared with the measurements. In addition, measurements of $D_{13/8}^\gamma/Z$ are presented using the ATLAS results for $R_{13/8}^Z$ \cite{17}; the measurements are compared with available theory predictions.

The paper is organised as follows: the ATLAS detector is described in section 2. The analysis strategy is summarised in section 3. Fixed-order QCD predictions and their uncertainties are discussed in section 4. Section 5 is devoted to the description of the experimental uncertainties. The results are reported in section 6. A summary is given in section 7.

2 ATLAS detector

The ATLAS experiment \cite{18} at the LHC uses a multipurpose particle detector with a forward-backward symmetric cylindrical geometry and a near $4\pi$ coverage in solid angle. It consists of an inner tracking detector, electromagnetic (EM) and hadronic calorimeters, and a muon spectrometer. The inner detector is surrounded by a thin superconducting solenoid and includes silicon detectors, which provide precision tracking in the pseudorapidity range $|\eta| < 2.5$, and a transition-radiation tracker providing additional tracking and electron identification information for $|\eta| < 2.0$. For the $\sqrt{s} = 13$ TeV data-taking period, the inner detector also includes a silicon-pixel insertable B-layer \cite{19, 20}, providing an additional layer of tracking information close to the interaction point. The calorimeter system covers the range $|\eta| < 4.9$. Within the region $|\eta| < 3.2$, EM calorimetry is provided by barrel and endcap high-granularity lead/liquid-argon (LAr) EM calorimeters, with an additional thin LAr presampler covering $|\eta| < 1.8$ to correct for energy loss in material upstream of the calorimeters; for $|\eta| < 2.5$ the LAr calorimeters are divided into three layers in depth. Hadronic calorimetry is provided by a steel/scintillator-tile calorimeter for $|\eta| < 1.7$ and two copper/LAr hadronic endcap calorimeters for $1.5 < |\eta| < 3.2$. The forward region is covered by additional coarser-granularity LAr calorimeters up to $|\eta| = 4.9$. The muon spectrometer consists of three large superconducting toroidal magnets, one barrel and two endcaps, each containing eight coils, precision tracking chambers covering the region $|\eta| < 2.7$, and separate trigger chambers up to $|\eta| = 2.4$. For the data taken at 8 TeV, a three-level trigger system was used. The first-level trigger was implemented in hardware and used a subset of the detector information. This was followed by two software-based trigger levels that together reduce the accepted event rate to approximately 400 Hz. For the data taken at 13 TeV, the trigger was changed \cite{21} to a two-level system, using custom hardware.
followed by a software-based level which runs offline reconstruction software, reducing the event rate to approximately 1 kHz.

3 Analysis strategy

The measurements of ratios of cross sections presented in this paper are based on the measurements presented in previous ATLAS publications [8, 9, 17], where details of the analyses are given. The strategies followed for the measurement of the ratios and for the theoretical predictions are described below.

3.1 Analysis strategy for $R_{13/8}$

The measurements of $d\sigma/dE_T^{\gamma}$ at $\sqrt{s} = 8$ TeV (13 TeV) used in the measurement of $R_{13/8}$ are based on an integrated luminosity of $20.2 \pm 0.4 \text{ fb}^{-1}$ ($3.16 \pm 0.07 \text{ fb}^{-1}$). The measurement of the ratio covers the range $E_T^{\gamma} > 125 \text{ GeV}$ and is performed separately in the four regions of $\eta^{\gamma}$ defined in section 1. A summary of the analyses leading to the measurements of the differential cross sections for inclusive isolated-photon production at $\sqrt{s} = 13$ and 8 TeV is given below.

Photon candidates are reconstructed from clusters of energy deposited in the EM calorimeter. Candidates without a matching track or reconstructed conversion vertex in the inner detector are classified as unconverted photons, while those with a matching reconstructed conversion vertex or a matching track consistent with originating from a photon conversion are classified as converted photons [22]. The photon identification is based primarily on shower shapes in the calorimeter [22]. It uses information from the hadronic calorimeter, the lateral shower shape in the second layer of the EM calorimeter and the shower shapes in the finely segmented first EM calorimeter layer to ensure the compatibility of the measured shower profile with that originating from a single photon impacting the calorimeter. The photon energy measurement is made using calorimeter and, when available, tracking information. An energy calibration [23] is applied to the candidates to account for upstream energy loss and both lateral and longitudinal leakage. Events with at least one photon candidate with calibrated $E_T^{\gamma} > 125 \text{ GeV}$ and $|\eta^{\gamma}| < 2.37$ excluding the region $1.37 < |\eta^{\gamma}| < 1.56$ are selected. The isolation transverse energy $E_{T,\text{iso}}^{\gamma}$ is corrected for leakage of the photon energy into the isolation cone and the estimated contributions from the underlying event (UE) and additional inelastic $pp$ interactions (pile-up). The latter two corrections are computed simultaneously on an event-by-event basis using the jet-area method [24, 25]. After these corrections, isolated photons are selected by requiring $E_{T,\text{iso}}^{\gamma}$ to be lower than $E_{T,\text{cut}}^{\gamma}$. A small background contribution still remains after imposing the photon identification and isolation requirements and is subtracted using a data-driven method based on background control regions [8, 9]. The selected samples of events are used to unfold the distribution in $E_T^{\gamma}$ for each $|\eta^{\gamma}|$ region to a phase-space region close to that used for event selection.

The phase-space region at particle level uses particles with a decay length $c\tau > 10 \text{ mm}$; these particles are referred to as “stable”. The particle-level isolation requirement for the photon is built by summing the transverse energy of all stable particles, except for muons
and neutrinos, in a cone of size $\Delta R = 0.4$ around the photon direction after the contribution from the UE is subtracted; the same subtraction procedure and isolation requirement used on data are applied at the particle level.

An important part of this analysis is the evaluation of the experimental systematic uncertainties in the ratio of the cross sections at 13 and 8 TeV taking into account correlations. This study is described in section 5. Given the dominance of the systematic uncertainty arising from the photon energy scale when measuring the cross sections, it is necessary to carefully study this source of uncertainty. This source of systematic uncertainty is decomposed into independent components [23] and the treatment of the correlations of these components between the measurements at 13 and 8 TeV results in a reduction of the systematic uncertainty of the ratio.

The measurements of the ratio of cross sections are compared with NLO pQCD predictions for which a proper evaluation of the theoretical uncertainties is also of importance. The theoretical uncertainties in the predictions for the cross sections are $\mathcal{O}(10–15\%)$ for both centre-of-mass energies and are dominated by contributions from terms beyond NLO. These uncertainties are much larger than those of experimental nature and limit how precisely the predictions can be tested. The study of the theoretical uncertainties in the ratio is described in section 4. As is the case for the experimental systematic uncertainties, it is imperative that for each source of theoretical uncertainty the degree of correlation between the two centre-of-mass energies is taken into account. As a result, the theoretical uncertainty is reduced in the ratio, thus allowing a more stringent test of the predictions.

3.2 Analysis strategy for $D_{13/8}^{\gamma/Z}$

The measurement of the double ratio $D_{13/8}^{\gamma/Z}$ is based on the measurement of $R_{13/8}^{\gamma}$ described above as well as on the measurement of $R_{13/8}^{Z}$. It should be noted that $R_{13/8}^{\gamma}$ is measured as a function of $E_T^{\gamma}$ in different ranges of $\eta^{\gamma}$, while $R_{13/8}^{Z}$ is a single number. The measurement of $R_{13/8}^{Z}$ used here is the one reported in ref. [17]. The fiducial cross section at a given $\sqrt{s}$, $\sigma_{\text{fid}}^{Z}(\sqrt{s})$, is defined as the production cross section of a $Z$ boson times the branching ratio of the decay into a lepton pair of flavour $\ell^+\ell^- = e^+e^-$ or $\mu^+\mu^-$ within the following phase space: the lepton transverse momentum $p_T^{\ell} > 25$ GeV, the lepton pseudorapidity $|\eta_{\ell}| < 2.5$ and the dilepton invariant mass $66 < m_{\ell\ell} < 116$ GeV. The measurement at $\sqrt{s} = 13$ TeV was performed in the aforementioned phase space while the measurement at $\sqrt{s} = 8$ TeV was extrapolated to the same phase space as described in ref. [17]. Measurements of the fiducial cross sections were made using the decay channels $Z \rightarrow e^+e^-$ and $Z \rightarrow \mu^+\mu^-$, and combined for the final result. The measured $R_{13/8}^{Z}$ is $1.537 \pm 0.001$ (stat.) $\pm 0.010$ (syst.) $\pm 0.044$ (lumi.) [17], where “stat.” denotes the statistical uncertainty, “syst.” denotes the systematic uncertainty and “lumi.” denotes the uncertainty due to the ratio of the integrated luminosities. The evaluation of the systematic uncertainty in the ratio takes into account correlations of systematic uncertainties across channels and $\sqrt{s}$ as described in ref. [17].

The predictions for $D_{13/8}^{\gamma/Z}$ are obtained from NLO pQCD calculations for $R_{13/8}^{\gamma}$ [12, 13] and NNLO pQCD calculations for $R_{13/8}^{Z}$ [26, 27]. The evaluation of the uncertainties affecting
the predictions for $D_{13/8}^{\gamma/Z}$ requires considerations that account for the correlations arising from the parton distribution functions (PDFs) and the strong coupling constant, $\alpha_s(m_Z)$.

4 Fixed-order QCD predictions

The theoretical predictions for the ratios of cross sections are obtained using fixed-order QCD calculations. Details of the generators and of the estimations of the theoretical uncertainties are given below, especially emphasising the correlations between the two centre-of-mass energies.

4.1 Theoretical predictions for $R_{13/8}^{\gamma}$

The theoretical predictions for $R_{13/8}^{\gamma}$ presented here are based on NLO QCD calculations computed using the program Jetphox 1.3.1.2 [12, 13]. This program includes a full NLO QCD treatment of both the direct- and fragmentation-photon contributions to the cross section for the $pp \rightarrow \gamma + X$ reaction. The number of quark flavours is set to five. The renormalisation ($\mu_R$), factorisation ($\mu_F$) and fragmentation ($\mu_t$) scales are chosen to be $\mu_R = \mu_F = \mu_t = E_T^\gamma$. The calculations are performed using various parameterisations of the proton PDFs and the BFG set II of parton-to-photon fragmentation functions at NLO [28]. The nominal calculation is based on the MMHT2014 PDF set [29]. Predictions are also obtained with other PDFs, namely CT14 [30], HERAPDF2.0 [31], NNPDF3.0 [32] and ABMP16 [33]. For MMHT2014, CT14, HERAPDF2.0 and NNPDF3.0 parameterisations of the PDFs, the sets determined at NLO are used. For ABMP16, the set at NNLO is used. The strong coupling constant $\alpha_s(m_Z)$ is set to the value assumed in the fit to determine the PDFs; as an example, in the case of MMHT2014 PDFs, $\alpha_s(m_Z)$ is set to the value 0.120.

The calculations are performed using a parton-level isolation criterion for the photon, which requires a total transverse energy of the partons inside a cone of radius $R = 0.4$ around the photon direction below $E_{T_{\text{cut}}}^{\gamma}$. The predictions from Jetphox are at parton level, while the measurements are at particle level. Corrections for the non-perturbative (NP) effects of hadronisation and the UE are estimated using samples from Pythia 8.186 [34] as described below. First, a correction factor ($C_{NP}^{\gamma}$) is derived for the isolated-photon cross section at each centre-of-mass energy as the ratio of the cross section at particle level for a Pythia sample with UE effects to the Pythia cross section at parton level without UE effects. Second, the ratio of the correction factor for $\sqrt{s} = 13$ TeV to that for $\sqrt{s} = 8$ TeV, $C_{NP}^{\gamma} = C_{NP}^{13}/C_{NP}^{8}$, is evaluated. The ratio of correction factors is obtained using the ATLAS set of tuned parameters A14 [35] with the LO NNPDF2.3 PDF set [36]. The ratio of correction factors for non-perturbative effects applied to the ratio predictions from Jetphox is $C_{NP}^{\gamma} = 0.9964 \pm 0.0020$.

The following sources of uncertainty in the theoretical predictions are considered:

- The uncertainty in the NLO QCD predictions due to terms beyond NLO is estimated by repeating the calculations using values of $\mu_R$, $\mu_F$ and $\mu_t$ scaled by the factors 0.5 and 2. The three scales are either varied simultaneously or individually; in addition,
configurations in which one scale is fixed and the other two are varied simultaneously are also considered. In all cases, the condition $0.5 \leq \mu_A/\mu_B \leq 2$ is imposed, where $A, B = R, F, f$. The final uncertainty is taken as the largest deviation from the nominal value among the 14 possible variations.

- The uncertainty in the NLO QCD predictions related to the proton PDFs is estimated by repeating the calculations using the 50 additional sets from the MMHT2014 error analysis.

- The uncertainty in the NLO QCD predictions related to the value of $\alpha_s(m_Z)$ is estimated by repeating the calculations using two additional sets of proton PDFs from the MMHT2014 analysis for which different values of $\alpha_s(m_Z)$ were assumed in the fits, namely $\alpha_s(m_Z) = 0.118$ and 0.122 [37].

- The impact of the beam energy uncertainty is estimated by repeating the calculations with $\sqrt{s}$ varied by its uncertainty of 0.1% [38].

- The uncertainty in the corrections for non-perturbative effects is estimated by comparing the results of using variations of the A14 tune in which the parameter settings related to the modelling of the UE are changed [35].

For the individual differential cross sections and for both centre-of-mass energies, the dominant theoretical uncertainty arises from the estimate of contributions from terms beyond NLO [8, 9].

The predictions for $R_{13/8}$ are obtained by calculating the ratio of the individual differential cross sections at each centre-of-mass energy. To estimate the theoretical uncertainty in $R_{13/8}$, the correlation between the two centre-of-mass energies for each source listed above needs to be considered. The uncertainties due to the PDFs, $\alpha_s(m_Z)$, beam energy and non-perturbative effects are fully correlated between the two centre-of-mass energies. The relative uncertainties in $R_{13/8}$ due to the uncertainties in $\alpha_s(m_Z)$, the PDFs and the beam energy exhibit a significant degree of cancellation with respect to the individual predictions. However, for the scale uncertainties, the correlation is a priori unknown. In the standard approach, varying the scales coherently or incoherently at both centre-of-mass energies leads to very different theoretical uncertainties:

- In the coherent case, there are large cancellations in the uncertainties in the predictions for $R_{13/8}$, particularly in the variation of $\mu_R$, which is $\mathcal{O}(10\%)$ for the individual predictions and below 1% for $R_{13/8}$. The envelope of the scale variations for $R_{13/8}$ shrinks in comparison with the envelopes for the individual predictions: from $\mathcal{O}(10\%)$ for the individual predictions to below 2% for $R_{13/8}$ across most of the range in $E_T$.

- In the incoherent case, the envelope of the scale variations for $R_{13/8}$ is $\mathcal{O}(14\%)$ in all regions of phase space.

A second approach is also investigated, which is free from ambiguity in the correlation. It consists of considering the difference between the LO and NLO predictions for $R_{13/8}$. The LO predictions are obtained with JETPHOX using the same parameter settings and PDF set.
as the baseline NLO predictions. The LO and NLO predictions for $R_{13}^{7}$ are compared and the differences are up to 3.5%, which are similar to the estimates based on the standard approach with coherent variations at the two centre-of-mass energies. Thus, the results of this second approach support the use of the standard approach with a coherent variation of the scales; an incoherent variation of the scales clearly leads to an overestimation of the theoretical uncertainty.

Figure 1 shows an overview of the theoretical uncertainties in $R_{13}^{7}$. The total relative uncertainty is below 2% (4%) at low (high) $E_T$ in all regions of $|\eta^\gamma|$. The uncertainty due to the variation of the scales is dominant everywhere. At high $E_T$ for $|\eta^\gamma| < 0.6$ and $0.6 < |\eta^\gamma| < 1.37$, the uncertainty due to the PDFs can be as large as the contribution from the scale variations.

The NLO pQCD predictions of Jetphox for $R_{13}^{7}$ based on the MMHT2014 parameterisations of the proton PDFs are about 2 at $E_T = 125$ GeV and increase as $E_T$ increases, to about 10 for $E_T = 1300$ (1000) GeV for $|\eta^\gamma| < 0.6$ ($0.6 < |\eta^\gamma| < 1.37$). For $1.56 < |\eta^\gamma| < 1.81$ ($1.81 < |\eta^\gamma| < 2.37$), the predicted $R_{13}^{7}$ increases from about 2 at $E_T = 125$ GeV to around 10 (25) at $E_T = 600$ GeV. The increase is greater for the forward regions than for the central regions. Predictions based on different parameterisations of the proton PDFs are compared. Those based on MMHT2014, NNPDF3.0 and CT14 are found to be similar in all $\eta^\gamma$ and $E_T$ regions. The predictions of $R_{13}^{7}$ based on HERAPDF2.0 and ABMP16 show some differences from the predictions based on the other PDFs in some regions of phase space, especially at high $E_T$ (see section 6).

4.2 Theoretical predictions for $D_{13}^{Z}$

The theoretical predictions for $D_{13}^{Z}$ presented here are based on NNLO QCD calculations for the predictions of $R_{13}^{Z}$ computed using the program Dyturbo, which is an optimised version of the DYNNLO program [26, 27], and NLO QCD calculations for the predictions of $R_{13}^{7}$ using Jetphox with the procedure described in section 4.1.

The calculations using Dyturbo are based on sets of PDFs extracted using NNLO QCD fits, namely MMHT2014nnlo, CT14nnlo, HERAPDF2.0nnlo and NNPDF3.0nnlo. The strong coupling constant $\alpha_s(m_Z)$ is set to the value assumed in the fit to determine the PDFs. In the case of MMHT2014nnlo PDFs, $\alpha_s(m_Z)$ is set to the value 0.118.

For consistency, and to properly take into account the correlations in the PDF uncertainties, the calculations of Jetphox for $R_{13}^{7}$ are repeated using the NNLO PDF sets mentioned above. It is consistent to use NLO matrix elements convolved with PDF sets determined at NNLO. The resulting predictions include partially NNLO corrections and, therefore, are understood to still have NLO accuracy. For these additional calculations, the same parameter settings for the number of flavours, scales and fragmentation functions mentioned in section 4.1 are used. The change in the predictions for $R_{13}^{7}$ based on MMHT2014nnlo relative to those using MMHT2014nnlo is $\sim 0.5\%$ at low $E_T$. At high $E_T$, the change depends on the $|\eta^\gamma|$ region: for $|\eta^\gamma| < 0.6$ the change is below 2% for $E_T < 750$ GeV and increases to 6% in the highest-$E_T$ measured point; for $0.6 < |\eta^\gamma| < 1.37$ ($1.56 < |\eta^\gamma| < 1.81$) the change is below 2% (1.3%) for the entire measured range; for
Figure 1. Relative theoretical uncertainty in $R_{13/8}^\gamma$ as a function of $E_T^\gamma$ for different $\eta^\gamma$ regions arising from the scale variations (shaded area), the value of $\alpha_s$ (dashed lines), the PDF (dotted lines) and the beam energy (dot-dashed lines). The total theoretical uncertainty is shown as the solid line.

1.81 < $|\eta^\gamma|$ < 2.37 the change is below 2% for $E_T^\gamma < 550$ GeV and increases to 2.7% in the highest-$E_T^\gamma$ measured point.

The sources of uncertainty in the theoretical predictions based on MMHT2014nnlo are the same as those described in section 4.1. The uncertainty related to the beam energy is neglected, due to the small size of its effect on $R_{13/8}^\gamma$. The uncertainties in the prediction of $R_{13/8}^Z$ due to the scale variations, the PDFs and $\alpha_s(m_Z)$ are $+0.02\%$, $+0.9\%$ and $-0.03\%$, respectively. For the predictions of $D_{13/8}^{\gamma/Z}$, the uncertainties have been estimated as follows:

- The scale variations are considered uncorrelated between $Z$ boson production and isolated-photon production since they are different processes.
• The PDF uncertainties are considered fully correlated between $Z$ boson production and isolated-photon production.

• The $\alpha_s(m_Z)$ uncertainties are considered fully correlated between $Z$ boson production and isolated-photon production. The uncertainty in the predictions due to that in $\alpha_s(m_Z)$ is estimated by using PDF sets in which $\alpha_s(m_Z)$ was fixed at $0.116$ or $0.120$.

In what follows, the resulting uncertainties in the predictions of $D_{13/8}^{\gamma/Z}$ are described. In the region $|\eta^\gamma| < 0.6$ (0.6 < $|\eta^\gamma|$ < 1.37), the total relative uncertainty is below 2% for $125 \leq E_T^\gamma \leq 650$ (650) GeV and it rises to $\approx 4.5\%$ (3.3\%) for $E_T^\gamma = 1300$ (1000) GeV. In both $\eta^\gamma$ regions, the total uncertainty is mostly dominated by the variation of the scales. For $|\eta^\gamma| < 0.6$ and $E_T^\gamma \gtrsim 300$ GeV, the uncertainties in the PDFs are dominant, and for $0.6 < |\eta^\gamma| < 1.37$ and $E_T^\gamma \gtrsim 750$ GeV, the contributions from the scale variations and the PDFs are equally large. In the region $1.56 < |\eta^\gamma| < 1.81$ (1.81 < $|\eta^\gamma|$ < 2.37), the total relative uncertainty is below 2\% (3\%) for $125 \leq E_T^\gamma \leq 350$ (470) GeV and it rises to $\approx 3\%$ (3.6\%) for $E_T^\gamma = 600$ GeV. For $1.56 < |\eta^\gamma| < 1.81$, the uncertainty due to the variation of the scales is dominant, but for $1.81 < |\eta^\gamma| < 2.37$ and $E_T^\gamma \gtrsim 550$ GeV, the contributions from the scale variations and the PDFs are equally important.

The theoretical predictions based on the MMHT2014nnlo parameterisations of the proton PDFs for $D_{13/8}^{\gamma/Z}$ are about 1.4 at $E_T^\gamma = 125$ GeV and increase as $E_T^\gamma$ increases, to 6–17 at the high end of the spectrum, depending on the $\eta^\gamma$ region. The increase is larger for the forward regions than for the central regions. Predictions based on different parameterisations of the proton PDFs are compared; those based on MMHT2014nnlo, NNPDF3.0nnlo and CT14nnlo are found to be similar in all $\eta^\gamma$ and $E_T^\gamma$ regions. The predictions of $D_{13/8}^{\gamma/Z}$ based on HERAPDF2.0nnlo show some differences from the predictions based on the other PDFs in some regions of phase space, especially at high $E_T^\gamma$ (see section 6).

5 Experimental uncertainties

The sources of systematic uncertainties that affect the measurements of the photon differential cross sections at $\sqrt{s} = 8$ and 13 TeV are detailed in refs. [8] and [9], respectively. A proper estimation of the systematic uncertainties in this measurement of cross-section ratios requires taking into account inter-$\sqrt{s}$ correlations for each source of systematic uncertainty. Assuming no correlation provides a conservative estimate and full correlation is used only when justified. The estimation of the systematic uncertainties in the ratio has to take into account the changes in the data-taking conditions as well as changes in the detector conditions. The measurements at $\sqrt{s} = 8$ (13) TeV are based on data taken when the LHC operated with a bunch spacing of 50 (25) ns. During the data-taking period at $\sqrt{s} = 8$ (13) TeV there were on average 20.7 (13.5) proton-proton interactions per bunch crossing. Furthermore, the addition of the silicon-pixel insertable B-layer leads to extra material upstream of the calorimeters for data-taking at $\sqrt{s} = 13$ TeV. The procedures used to account for the impact of each source of systematic uncertainty on the ratio $R_{13/8}^{\gamma}$ are described below.
5.1 Photon energy scale

The systematic uncertainties associated with the photon energy scale and resolution represent the dominant experimental uncertainties in the measurements of the differential cross sections for inclusive isolated-photon production at both centre-of-mass energies. The uncertainty arising from the photon energy scale ($\gamma$ES) in $R_{13/8}^\gamma$ is estimated by decomposing it into uncorrelated sources for both the 8 TeV and 13 TeV measurements. A total of 22 individual components [23] influencing the energy scale and resolution of the photon are considered. Twenty of these components are common to both centre-of-mass energies. For some of the components the uncertainty is separated into a part which is correlated between the two centre-of-mass energies and another part which is specific to 13 TeV data and which is treated as uncorrelated (see below). These components include the uncertainties in: the overall energy scale adjustment using $Z \rightarrow e^+e^-$ events; the non-linearity of the energy measurement at the cell level; the relative calibration of the different calorimeter layers; the amount of material in front of the calorimeter; the modelling of the reconstruction of photon conversions; the modelling of the lateral shower shape; the modelling of the sampling term; and the measurement of the constant term in $Z$ boson decays. The uncertainties depend on $E_T^\gamma$ as well as on $|\eta^\gamma|$ and are larger in the region $1.56 < |\eta^\gamma| < 1.81$ due to the presence of more material than in other $|\eta^\gamma|$ regions. The remaining two components are specific to the 13 TeV measurement and take into account the differences in the configuration of the ATLAS detector between 2012 and 2015, namely changes in the LAr temperature, in the stability of the layer intercalibration and in the material in front of the calorimeters between Run 1 and Run 2 [39].

The procedure used to estimate the systematic uncertainty in $R_{13/8}^\gamma$ is as follows: all the uncertainty components described above are taken as fully correlated except for the uncertainty in the overall energy scale adjustment using $Z \rightarrow e^+e^-$ events, which for 2015 includes the effects of the changes in the configuration of the ATLAS detector mentioned above, and the uncertainties specific to the 13 TeV measurement. Calibration differences due to a change of optimal filtering coefficients and LAr timing samples between Run 1 and Run 2 are considered as a source of uncertainty in $R_{13/8}^\gamma$. The uncertainties in the photon energy scale due to pile-up are small enough compared to other uncertainties that the specific treatment of the correlation does not impact the results. The uncertainties due the photon energy resolution are treated as uncorrelated between $\sqrt{s} = 13$ TeV and 8 TeV since they include the effects of pile-up, which was different in the 2012 and 2015 data-taking periods.

The relative uncertainty due to the correlated components of the photon energy scale in $R_{13/8}^\gamma$ as a function of $E_T^\gamma$ is shown in figure 2 for each region in $\eta^\gamma$. For illustration purposes, the result of estimating that part of the systematic uncertainty assuming no correlation is also shown in this figure: the results obtained using the complete correlation model exhibit a large reduction in comparison with those in which the correlations are ignored. This demonstrates that a proper treatment of the inter-$\sqrt{s}$ correlations in the

---

4 The relative energy resolution is parameterised as $\sigma(E)/E = a/\sqrt{E} + c$, where $a$ is the sampling term and $c$ is the constant term.
Figure 2. Relative systematic uncertainty in $R_{13/8}^\gamma$ as a function of $E_T^\gamma$ for different $\eta^\gamma$ regions due to the $\gamma$ES correlated components (dashed lines). For comparison, the results of considering the components as uncorrelated are also shown (dotted lines) to illustrate the reduction in the size of the systematic uncertainty when the proper treatment is applied. The relative uncertainty due to the uncorrelated components of the photon energy scale and the components specific to 2015 is also shown (solid lines).

5.2 Other sources of experimental uncertainty

The other sources of experimental uncertainty affecting the measurements are treated as listed below. For several of these sources, the uncertainties in the measurements at
$\sqrt{s} = 13$ TeV and 8 TeV are treated conservatively as uncorrelated since their impact is small.

- **Statistical uncertainties.** The statistical uncertainties in both the data and the Monte Carlo simulations at $\sqrt{s} = 13$ and 8 TeV are treated as uncorrelated.

- **Luminosity uncertainty.** The luminosity uncertainties associated to the measurements of the photon cross sections at $\sqrt{s} = 8$ TeV and 13 TeV are dominated by effects that are uncorrelated between different centre-of-mass energies and data-taking periods. The resulting relative uncertainty in $R_{13/8}^{\gamma}$ amounts to $\pm 2.8\%$.

- **Trigger uncertainty.** The uncertainties in the trigger efficiency are treated as uncorrelated for data at different $\sqrt{s}$. Different trigger requirements were used during 2012 and 2015. In addition, during 2012 a three-level trigger system was used to select events while in 2015 a two-level system was employed.

- **Photon-identification uncertainty.** In both measurements, the photon identification is based primarily on shower shapes in the EM calorimeter. These uncertainties are treated as uncorrelated since different methods are used at $\sqrt{s} = 13$ TeV [40] and 8 TeV [22] to estimate the uncertainties; in addition, the photon identification criteria are re-optimised for data taken at 13 TeV.

- **Modelling of the photon isolation in Monte Carlo.** In both measurements, the photon candidate is required to be isolated. The in-time (out-of-time) pile-up, which is due to additional $pp$ collisions in the same (earlier or later than) bunch crossing as the event of interest, was different in 2012 and 2015 due to the different LHC conditions, namely the instantaneous luminosity and the bunch spacing. For simulated events, data-driven corrections to $E_{iso}^{T}$ are applied such that the peak position in the $E_{iso}^{T}$ distribution coincides in data and simulation. These uncertainties are treated as uncorrelated since different methods are used at $\sqrt{s} = 13$ and 8 TeV for the corrections and uncertainties.

- **Choice of background control regions.** The background subtraction is performed using a data-driven two-dimensional sideband technique based on background control regions. A plane is formed by the variable $E_{iso}^{T}$ and a binary variable that encapsulates the photon identification ("tight" vs. "non-tight"). A photon candidate is classified as "non-tight" if it fails at least one of four requirements on the shower-shape variables computed from the energy deposits in the first layer of the EM calorimeter, but satisfies the tight requirement on the total lateral shower width in the first layer and all the other tight identification criteria in other layers [22]. The plane is divided into four regions: region A for tight isolated photons, region B for tight non-isolated photons, region C for non-tight isolated photons and region D for non-tight non-isolated photons. The background control regions B, C and D are specified by lower and upper limits on $E_{iso}^{T}$ as well as by the definition of "non-tight" photon candidates. Variations of the limits and alternative definitions of the "non-tight" condition are used to estimate
the uncertainties due to the choice of background control regions. These uncertainties are treated as uncorrelated since, as mentioned above, the photon-identification requirements are re-optimised for data-taking at 13 TeV.

- **Photon identification and isolation correlation in the background.** In the background subtraction method described above, the photon isolation and identification variables are assumed to be uncorrelated for background events. Uncertainties due to this assumption are estimated by using validation regions, which are dominated by background. These uncertainties are treated as uncorrelated since, as mentioned above, the photon-identification requirements are re-optimised for data-taking at 13 TeV.

- **Signal modelling.** MC simulations of signal processes are used to estimate the signal leakage fractions in the background control regions and to compute the unfolding corrections. For both measurements, at $\sqrt{s} = 13$ and 8 TeV, the PYTHIA [34] generator is used for the nominal results and the SHERPA [41] generator for studies of systematic uncertainties related to the model dependence. The uncertainty due to the mixture of direct and fragmentation processes in the simulations is estimated using the MC simulations of PYTHIA. These uncertainties are treated as uncorrelated since different methods and versions of the generators are used at $\sqrt{s} = 13$ TeV and 8 TeV to estimate the uncertainties. For $\sqrt{s} = 13$ (8) TeV, PYTHIA 8.186 with the A14 tune (PYTHIA 8.165 with the AU2 tune) and SHERPA 2.1.1 (SHERPA 1.4.0) with the CT10 tune are used. For the 8 TeV analysis the results of using the default admixture of direct and fragmentation contributions in PYTHIA are compared with those using an optimal admixture obtained by fitting the two components to the data; for the 13 TeV analysis the results of enhancing the fragmentation contribution by a factor of two or removing it completely are compared with those using the default admixture.

- **QCD-cascade and hadronisation model dependence.** These uncertainties are treated as uncorrelated since different versions and tunes of the Monte Carlo generators PYTHIA and SHERPA are used at $\sqrt{s} = 13$ and 8 TeV.

- **Pile-up uncertainties.** The in-time and out-of-time pile-up in the 2012 and 2015 data-taking periods were different. Conservatively and given the fact that the impact is rather small, these uncertainties are treated as uncorrelated.

### 5.3 Total experimental uncertainties in $R_{13/8}^\gamma$

Using the prescription for the treatment of the correlations between the measurements described in the previous sections, the systematic uncertainties in $R_{13/8}^\gamma$ are evaluated. Figure 3 shows the relative uncertainties in $R_{13/8}^\gamma$ due to (i) the photon energy scale, which includes the correlated and uncorrelated contributions as well as the additional ones associated with 2015 data, (ii) the remaining sources of systematic uncertainty excluding that in the luminosity measurements and (iii) the sum in quadrature of the non-$\gamma$ES uncertainties and the uncertainty due to the luminosity determination. The uncertainty due to the photon energy scale increases as $E_T^\gamma$ increases and is larger for the region
Figure 3. Relative systematic uncertainty in $R_{13/8}$ as a function of $E_T$ for different $\eta^\gamma$ regions due to different sources: $\gamma$ES uncertainties (solid lines), non-$\gamma$ES uncertainties excluding the luminosity uncertainty (dashed lines) and non-$\gamma$ES and luminosity uncertainties added in quadrature (dotted lines).

1.56 < $|\eta^\gamma|$ < 1.81 due to more material in front of the calorimeters than in the other regions. From figure 3 it is concluded that the relative uncertainty in $R_{13/8}$ due to the photon energy scale is no longer the dominant uncertainty, except for $E_T > 300$ GeV in the regions 0.6 < $|\eta^\gamma|$ < 1.37 and 1.56 < $|\eta^\gamma|$ < 1.81.

The total relative experimental systematic uncertainty in $R_{13/8}$ is shown in figure 4, as is its sum in quadrature with the relative statistical uncertainty. In all pseudo-rapidity regions, the systematic uncertainty is dominant compared to the statistical uncertainty up to $E_T \sim 300$ GeV, while the measurement becomes statistically limited for $E_T \gtrsim 600$ GeV.
Figure 4. Total relative systematic uncertainty in $R_{\gamma}^{13/8}$ as a function of $E_T^{\gamma}$ for different $\eta^{\gamma}$ regions (shaded band) and the sum in quadrature of the total relative systematic and statistical uncertainties (solid line).

There are significant correlations in the systematic uncertainties across bins in $E_T^{\gamma}$; the uncertainty in the luminosity measurement is one of the major contributions and is fully correlated for all bins in $E_T^{\gamma}$ and all $\eta^{\gamma}$ regions.

5.4 Total experimental uncertainties in $D_{\gamma}^{7/Z}$

The total relative experimental uncertainty in $D_{\gamma}^{7/Z}$ is obtained as follows:

- The uncertainty in $R_{\gamma}^{13/8}$ as presented in section 5.2, not including the contribution from the luminosity, is used. The uncertainty in the luminosity measurement cancels out in $D_{\gamma}^{7/Z}$ since the measurements of $R_{\gamma}^{13/8}$ and $R_{Z}^{13/8}$ are performed using data taken during the same periods of 2012 and 2015.
The statistical (0.1%) and systematic (0.7%) uncertainties in $R_{13/8}^Z$ are added in quadrature to the total uncertainty in $R_{13/8}^\gamma$ (see section 5.3). The systematic uncertainty in $R_{13/8}^Z$ is dominated by the uncertainty in the lepton reconstruction and efficiency; the correlation between the small contribution due to the electron energy scale and the photon energy scale in $D_{13/8}^\gamma$ can be safely neglected.

The relative total systematic uncertainty in the measured $D_{13/8}^\gamma$ as a function of $E_T$ is shown for each $\eta^\gamma$ region in figure 5. For comparison, the relative total systematic uncertainty in $R_{13/8}^\gamma$ is also shown. Since the total systematic uncertainty in $R_{13/8}^\gamma$ is at least a factor of three smaller than the total systematic uncertainty in $R_{13/8}^\gamma$, the effect of adding in quadrature such a contribution has a small impact. On the other hand, the luminosity uncertainty, which amounts to 2.8% for $R_{13/8}^\gamma$, cancels out in $D_{13/8}^\gamma$ and this has a significant impact except at high $E_T^\gamma$, where the statistical uncertainty dominates.

6 Results

The measurements of the ratios of cross sections are presented and the main features exhibited by the data are described. The theoretical predictions are compared with the experimental results for both $R_{13/8}^\gamma$ and $D_{13/8}^\gamma$.

6.1 Results for $R_{13/8}^\gamma$

The measured $R_{13/8}^\gamma$ as a function of $E_T^\gamma$ in different regions of $|\eta^\gamma|$ is shown in figures 6 and 7 and table 1. The measured $R_{13/8}^\gamma$ increases with $E_T^\gamma$ from approximately 2 at $E_T^\gamma = 125$ GeV to approximately 8–29 at the high end of the spectrum. In the forward regions the increase of $R_{13/8}^\gamma$ with $E_T^\gamma$ is larger than in the central regions. At a fixed value of $E_T^\gamma$, the measured ratio increases as $|\eta^\gamma|$ increases.

The NLO QCD predictions based on the MMHT2014 PDFs are compared with the measured $R_{13/8}^\gamma$ in figures 6 and 7. Even though there is a tendency for the predictions to underestimate the data, the measurements and the theory are consistent within the uncertainties; in particular, the increase as $E_T^\gamma$ increases and the dependence on $\eta^\gamma$ are reproduced by the predictions. To study in more detail the description of the measured $R_{13/8}^\gamma$ by the NLO QCD predictions, the ratio of the predictions to the data is shown in figures 6 and 7. In these figures, the predictions based on different PDFs, namely MMHT2014, CT14, NNPDF3.0, HERAPDF2.0 and ABMP16 are included to ascertain the sensitivity of $R_{13/8}^\gamma$ to the proton PDFs. The predictions generally agree with the measured $R_{13/8}^\gamma$ within the experimental and theoretical uncertainties for all PDFs considered within the measured range.

The comparison of the NLO QCD predictions for $d\sigma/dE_T^\gamma$ and the measured differential cross sections in the ATLAS analyses at 8 and 13 TeV is limited by the theoretical uncertainties, which are larger than those of experimental nature and dominated by the uncertainties due to the terms beyond NLO. The theoretical uncertainties in $d\sigma/dE_T^\gamma$ are 10–15%; in contrast, the theoretical uncertainties for $R_{13/8}^\gamma$ are below 2% for most of the phase space considered and smaller than the experimental uncertainties. The experimental
uncertainties in $R_{13/8}^7$ also benefit from a significant reduction since the systematic uncertainties partially cancel out, in particular those related to the photon energy scale, which is dominant in the measurement of $d\sigma/dE_T^\gamma$. The total systematic uncertainty in $R_{13/8}^7$ is below 5% for most of the phase space considered. Thus, the significant reduction of the experimental and theoretical uncertainties in $R_{13/8}^7$ allows a more stringent test of NLO QCD. The overall level of agreement between data and the NLO QCD predictions based on several parameterisations of the proton PDFs within these reduced uncertainties validates the description of the evolution of isolated-photon production in $pp$ collisions with the centre-of-mass energy.
<table>
<thead>
<tr>
<th>$E_T^* [\text{GeV}]$</th>
<th>$R_{13/8}^*$ ± statistical uncertainty ± systematic uncertainty</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td>$</td>
</tr>
<tr>
<td>125–150</td>
<td>$2.08 \pm 0.01 \pm 0.09$</td>
</tr>
<tr>
<td>150–175</td>
<td>$2.12 \pm 0.01 \pm 0.08$</td>
</tr>
<tr>
<td>175–200</td>
<td>$2.23 \pm 0.02 \pm 0.09$</td>
</tr>
<tr>
<td>200–250</td>
<td>$2.28 \pm 0.02 \pm 0.09$</td>
</tr>
<tr>
<td>250–300</td>
<td>$2.42 \pm 0.03 \pm 0.09$</td>
</tr>
<tr>
<td>300–350</td>
<td>$2.53 \pm 0.04 \pm 0.10$</td>
</tr>
<tr>
<td>350–400</td>
<td>$2.64 \pm 0.07 \pm 0.11$</td>
</tr>
<tr>
<td>400–470</td>
<td>$2.83 \pm 0.09 \pm 0.11$</td>
</tr>
<tr>
<td>470–550</td>
<td>$3.11 \pm 0.14 \pm 0.13$</td>
</tr>
<tr>
<td>550–650</td>
<td>$3.28 \pm 0.21 \pm 0.14$</td>
</tr>
<tr>
<td>650–750</td>
<td>$4.00 \pm 0.42 \pm 0.18$</td>
</tr>
<tr>
<td>750–900</td>
<td>$5.20 \pm 0.75 \pm 0.25$</td>
</tr>
<tr>
<td>900–1100</td>
<td>$9.9 \pm 2.3 \pm 0.5$</td>
</tr>
<tr>
<td>1100–1500</td>
<td>$13.9 \pm 9.8 \pm 0.8$</td>
</tr>
</tbody>
</table>

**Table 1.** The measured $R_{13/8}^*$ as a function of $E_T^*$ together with the statistical uncertainty and total systematic uncertainty in different regions of $|\eta^*|$. 
Figure 6. The measured $R_{13/8}$ (dots) as a function of $E_T^\gamma$ in different regions of $|\eta^\gamma|$. The NLO QCD predictions based on the MMHT2014 PDFs (black lines) are also shown. The inner (outer) error bars represent the statistical (total) uncertainties. The shaded band represents the theoretical uncertainty in the predictions. For most of the points, the error bars are smaller than the marker size and, thus, not visible. The lower part of the figures shows the ratio of the NLO QCD predictions based on the MMHT2014 PDFs to the measured $R_{13/8}$ (black lines). The ratios of the NLO QCD predictions based on different PDF sets to the measured $R_{13/8}$ are also included.
Figure 7. The measured $R'_{13/8}$ (dots) as a function of $E_T^\gamma$ in different regions of $|\eta|$. The NLO QCD predictions based on the MMHT2014 PDFs (black lines) are also shown. The inner (outer) error bars represent the statistical (total) uncertainties. The shaded band represents the theoretical uncertainty in the predictions. For most of the points, the error bars are smaller than the marker size and, thus, not visible. The lower part of the figures shows the ratio of the NLO QCD predictions based on the MMHT2014 PDFs to the measured $R'_{13/8}$ (black lines). The ratios of the NLO QCD predictions based on different PDF sets to the measured $R'_{13/8}$ are also included.
<table>
<thead>
<tr>
<th>$E_T^\gamma$ [GeV]</th>
<th>$D_{13/8}^{\gamma/Z}$ ± statistical uncertainty ± systematic uncertainty</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td>$</td>
</tr>
<tr>
<td>125–150</td>
<td>$1.35 \pm 0.01 \pm 0.04$</td>
</tr>
<tr>
<td>150–175</td>
<td>$1.38 \pm 0.01 \pm 0.04$</td>
</tr>
<tr>
<td>175–200</td>
<td>$1.45 \pm 0.01 \pm 0.04$</td>
</tr>
<tr>
<td>200–250</td>
<td>$1.49 \pm 0.01 \pm 0.04$</td>
</tr>
<tr>
<td>250–300</td>
<td>$1.57 \pm 0.02 \pm 0.04$</td>
</tr>
<tr>
<td>300–350</td>
<td>$1.65 \pm 0.03 \pm 0.05$</td>
</tr>
<tr>
<td>350–400</td>
<td>$1.72 \pm 0.04 \pm 0.05$</td>
</tr>
<tr>
<td>400–470</td>
<td>$1.84 \pm 0.06 \pm 0.05$</td>
</tr>
<tr>
<td>470–550</td>
<td>$2.02 \pm 0.09 \pm 0.06$</td>
</tr>
<tr>
<td>550–650</td>
<td>$2.13 \pm 0.14 \pm 0.07$</td>
</tr>
<tr>
<td>650–750</td>
<td>$2.60 \pm 0.27 \pm 0.09$</td>
</tr>
<tr>
<td>750–900</td>
<td>$3.39 \pm 0.49 \pm 0.14$</td>
</tr>
<tr>
<td>900–1100</td>
<td>$6.4 \pm 1.5 \pm 0.3$</td>
</tr>
<tr>
<td>1100–1500</td>
<td>$9.1 \pm 6.4 \pm 0.5$</td>
</tr>
</tbody>
</table>

Table 2. The measured $D_{13/8}^{\gamma/Z}$ as a function of $E_T^\gamma$ together with the statistical and total systematic uncertainty in different regions of $|\eta^\gamma|$.  

### 6.2 Results for $D_{13/8}^{\gamma/Z}$

The measurements of $D_{13/8}^{\gamma/Z}$ as a function of $E_T^\gamma$ in different regions of $|\eta^\gamma|$ are shown in figures 8 and 9 and table 2. The measured $D_{13/8}^{\gamma/Z}$ increases with $E_T^\gamma$ from approximately 1.4 at $E_T^\gamma = 125$ GeV to approximately 5–19 at the high end of the spectrum. At a fixed value of $E_T^\gamma$, the measured ratio increases as $|\eta^\gamma|$ increases.

The theoretical predictions based on the MMHT2014nnlo PDFs are compared with the measured $D_{13/8}^{\gamma/Z}$ in figures 8 and 9. The predictions are in agreement with the measured $D_{13/8}^{\gamma/Z}$; in particular, the increase as $E_T^\gamma$ increases and the dependence on $\eta^\gamma$ are reproduced by the predictions. As an example, the measured value of $D_{13/8}^{\gamma/Z}$ at the lowest-$E_T^\gamma$ point for $|\eta^\gamma| < 0.6$ is $1.35 \pm 0.04$ while the prediction using MMHT2014 is $1.31 \pm 0.02$. The tendency of the predictions to underestimate the data observed in $R_{13/8}^\gamma$ is also present in $D_{13/8}^{\gamma/Z}$; nevertheless, they are still consistent with each other within the uncertainties. To study in more detail the description of the measured $D_{13/8}^{\gamma/Z}$ by the theoretical predictions, the ratio of the predictions to the data is shown in figures 8 and 9. In these figures, the predictions based on different PDFs, namely MMHT2014nnlo, CT14nnlo, NNPDF3.0nnlo and HERAPDF2.0nnlo are included to estimate the sensitivity of $D_{13/8}^{\gamma/Z}$ to the proton PDFs. The predictions generally agree with the measured $D_{13/8}^{\gamma/Z}$ within the experimental and theoretical uncertainties for all PDFs considered within the measured range.
Figure 8. The measured $D_{13/8}^{\gamma/Z}$ (dots) as a function of $E_T^\gamma$ in different regions of $|\eta|^\gamma$. The pQCD predictions based on the MMHT2014nnlo PDFs (black lines) are also shown. The inner (outer) error bars represent the statistical (total) uncertainties. The shaded band represents the theoretical uncertainty in the predictions. For most of the points, the error bars are smaller than the marker size and, thus, not visible. The lower part of the figures shows the ratio of the pQCD predictions based on the MMHT2014nnlo PDFs to the measured $D_{13/8}^{\gamma/Z}$ (black lines). The ratios of the pQCD predictions based on different PDF sets to the measured $D_{13/8}^{\gamma/Z}$ are also included.
Figure 9. The measured $D_{13/8}^{\gamma/Z}$ (dots) as a function of $E_T^\gamma$ in different regions of $|\eta|$. The pQCD predictions based on the MMHT2014nnlo PDFs (black lines) are also shown. The inner (outer) error bars represent the statistical (total) uncertainties. The shaded band represents the theoretical uncertainty in the predictions. For most of the points, the error bars are smaller than the marker size and, thus, not visible. The lower part of the figures shows the ratio of the pQCD predictions based on the MMHT2014nnlo PDFs to the measured $D_{13/8}^{\gamma/Z}$ (black lines). The ratios of the pQCD predictions based on different PDF sets to the measured $D_{13/8}^{\gamma/Z}$ are also included.
7 Summary and conclusions

The ratio of cross sections for inclusive isolated-photon production in pp collisions at $\sqrt{s} = 13$ and 8 TeV ($R_{13/8}^\gamma$) is measured using the ATLAS detector at the LHC. The integrated luminosities of the 13 TeV and 8 TeV datasets are 3.2 fb$^{-1}$ and 20.2 fb$^{-1}$, respectively. The ratio of differential cross sections as a function of $|\eta^\gamma|$ for photons with $125 < E_T^\gamma < 1500$ GeV and $|\eta^\gamma| < 2.37$, excluding the region $1.37 < |\eta^\gamma| < 1.56$. In the estimation of the experimental systematic uncertainties for $R_{13/8}^\gamma$, the correlations between the measurements at the two centre-of-mass energies are taken into account. The systematic uncertainty arising from the photon energy scale, which is dominant for the individual cross sections, is reduced significantly in $R_{13/8}^\gamma$ and no longer the dominant uncertainty. The total systematic uncertainty for $R_{13/8}^\gamma$ is below 5% in most of the phase space of the measurement. The measurements can be useful for tuning models of prompt-photon production in pp collisions.

The predictions from NLO QCD calculations are compared with the measured $R_{13/8}^\gamma$. The theoretical uncertainties affecting these predictions are also evaluated taking into account the correlations between the two centre-of-mass energies, resulting in a significant reduction in the uncertainty of the predicted $R_{13/8}^\gamma$. The theoretical uncertainties in $R_{13/8}^\gamma$ are below 2% for most of the phase space of the measurement, in contrast with those in the individual cross-section predictions, which have approximately 10–15% uncertainties. Thus, the comparison of the predictions with the measured $R_{13/8}^\gamma$ represents a stringent test of the pQCD calculations. Within these reduced experimental and theoretical uncertainties, the NLO QCD predictions based on several parameterisations of the proton PDFs agree with the data. Even though there is a tendency of the predictions to underestimate the data, the measurements and the theory are consistent within the uncertainties. The level of agreement achieved validates the description of the evolution of isolated-photon production in pp collisions from $\sqrt{s} = 8$ to 13 TeV.

A double ratio of cross sections is also measured: the ratio of $R_{13/8}^\gamma$ to the ratio of the fiducial cross sections for Z boson production at 13 and 8 TeV ($R_{13/8}^Z$). In $R_{13/8}^{\gamma/Z} \equiv R_{13/8}^\gamma/R_{13/8}^Z$, the uncertainty due to the luminosity cancels out at the expense of a small increase in the systematic uncertainty from all other sources, leading to a more precise measurement of the evolution of the inclusive-photon cross section with the centre-of-mass energy normalised to the evolution of the Z boson cross section. The theoretical prediction, based on NNLO (NLO) QCD calculations for Z boson (inclusive-photon) production, describes the measurements within the theoretical uncertainties and the reduced experimental uncertainties.

Acknowledgments

We thank CERN for the very successful operation of the LHC, as well as the support staff from our institutions without whom ATLAS could not be operated efficiently.

We acknowledge the support of ANPCyT, Argentina; YerPhI, Armenia; ARC, Australia; BMWFW and FWF, Austria; ANAS, Azerbaijan; SSTC, Belarus; CNPq and FAPESP,
Brazil; NSERC, NRC and CFI, Canada; CERN; CONICYT, Chile; CAS, MOST and NSFC, China; COLCIENCIAS, Colombia; MSMT CR, MPO CR and VSC CR, Czech Republic; DNRF and DNSRC, Denmark; IN2P3-CNRS, CEA-DRF/IRFU, France; SRNSFG, Georgia; BMBF, HGF, and MPG, Germany; GSRT, Greece; RGC, Hong Kong SAR, China; ISF and Benoziyo Center, Israel; INFN, Italy; MEXT and JSPS, Japan; CNRST, Morocco; NWO, Netherlands; RCN, Norway; MNiSW and NCN, Poland; FCT, Portugal; MNE/IFA, Romania; MES of Russia and NRC KI, Russian Federation; JINR; MESTD, Serbia; MSSR, Slovakia; ARRS and MIZŠ, Slovenia; DST/NRF, South Africa; MINECO, Spain; SRC and Wallenberg Foundation, Sweden; SERI, SNSF and Cantons of Bern and Geneva, Switzerland; MOST, Taiwan; TAEK, Turkey; STFC, United Kingdom; DOE and NSF, United States of America. In addition, individual groups and members have received support from BCKDF, CANARIE, CRC and Compute Canada, Canada; COST, ERC, ERDF, Horizon 2020, and Marie Skłodowska-Curie Actions, European Union; Investissements d’ Avenir Labex and Idex, ANR, France; DFG and AvH Foundation, Germany; Herakleitos, Thales and Aristeia programmes co-financed by EU-ESF and the Greek NSRF, Greece; BSF-NSF and GIF, Israel; CERCA Programme Generalitat de Catalunya, Spain; The Royal Society and Leverhulme Trust, United Kingdom.

The crucial computing support from all WLCG partners is acknowledged gratefully, in particular from CERN, the ATLAS Tier-1 facilities at TRIUMF (Canada), NDGF (Denmark, Norway, Sweden), CC-IN2P3 (France), KIT/GridKA (Germany), INFN-CNAF (Italy), NL-T1 (Netherlands), PIC (Spain), ASGC (Taiwan), RAL (U.K.) and BNL (U.S.A.), the Tier-2 facilities worldwide and large non-WLCG resource providers. Major contributors of computing resources are listed in ref. [42].

Open Access. This article is distributed under the terms of the Creative Commons Attribution License (CC-BY 4.0), which permits any use, distribution and reproduction in any medium, provided the original author(s) and source are credited.

References


23 (a) INFN Bologna and Universita’ di Bologna, Dipartimento di Fisica; (b) INFN Sezione di Bologna; Italy.
24 Physikalisches Institut, Universitat Bonn, Bonn; Germany.
25 Department of Physics, Boston University, Boston MA; United States of America.
26 Department of Physics, Brandeis University, Waltham MA; United States of America.
27 (a) Transilvania University of Brasov, Brasov; (b) Horia Hulubei National Institute of Physics and Nuclear Engineering, Bucharest; (c) Department of Physics, Alexandru Ioan Cuza University of Iasi, Iasi; (d) National Institute for Research and Development of Isotopic and Molecular Technologies, Physics Department, Cluj-Napoca; (e) University Politehnica Bucharest, Bucharest; (f) West University in Timisoara, Timisoara; Romania.
28 (a) Faculty of Mathematics, Physics and Informatics, Comenius University, Bratislava; (b) Department of Subnuclear Physics, Institute of Experimental Physics of the Slovak Academy of Sciences, Kosice; Slovak Republic.
29 Physics Department, Brookhaven National Laboratory, Upton NY; United States of America.
30 Departamento de Fisica, Universidad de Buenos Aires, Buenos Aires; Argentina.
31 California State University, CA; United States of America.
32 Cavendish Laboratory, University of Cambridge, Cambridge; United Kingdom.
33 (a) Department of Physics, University of Cape Town, Cape Town; (b) Department of Mechanical Engineering Science, University of Johannesburg, Johannesburg; (c) School of Physics, University of the Witwatersrand, Johannesburg; South Africa.
34 Department of Physics, Carleton University, Ottawa ON; Canada.
35 (a) Faculté des Sciences Ain Chock, Réseau Universitaire de Physique des Hautes Énergies — Université Hassan II, Casablanca; (b) Faculté des Sciences, Université Ibn-Tofail, Kénitra; (c) Faculté des Sciences Semlalia, Université Cadi Ayyad, LPHEA-Marrakech; (d) Faculté des Sciences, Université Mohamed Premier and LPTPM, Oujda; (e) Faculté des sciences, Université Mohammed V, Rabat; Morocco.
36 CERN, Geneva; Switzerland.
37 Enrico Fermi Institute, University of Chicago, Chicago IL; United States of America.
38 LPC, Université Clermont Auvergne, CNRS/IN2P3, Clermont-Ferrand; France.
39 Nevis Laboratory, Columbia University, Irvington NY; United States of America.
40 Physics Department, Southern Methodist University, Dallas TX; United States of America.
41 (a) Dipartimento di Fisica, Università della Calabria, Rende; (b) INFN Gruppo Collegato di Cosenza, Laboratori Nazionali di Frascati; Italy.
42 Physics Department, Southern Methodist University, Dallas TX; United States of America.
43 Physics Department, University of Texas at Dallas, Richardson TX; United States of America.
44 National Centre for Scientific Research “Demokritos”, Agia Paraskevi; Greece.
45 (a) Department of Physics, Stockholm University; (b) Oskar Klein Centre, Stockholm; Sweden.
46 Deutsches Elektronen-Synchrotron DESY, Hamburg and Zeuthen; Germany.
47 Lehrstuhl für Experimentelle Physik IV, Technische Universität Dortmund, Dortmund; Germany.
48 Institut für Kern- und Teilchenphysik, Technische Universität Dresden, Dresden; Germany.
49 Department of Physics, Duke University, Durham NC; United States of America.
50 SUPA — School of Physics and Astronomy, University of Edinburgh, Edinburgh; United Kingdom.
51 INFN e Laboratori Nazionali di Frascati, Frascati; Italy.
52 Physikalisches Institut, Albert-Ludwigs-Universität Freiburg, Freiburg; Germany.
53 II. Physikalisches Institut, Georg-August-Universität Göttingen, Göttingen; Germany.
54 Département de Physique Nucléaire et Corpusculaire, Université de Genève, Genève; Switzerland.
55 (a) Dipartimento di Fisica, Università di Genova, Genova; (b) INFN Sezione di Genova; Italy.
56 II. Physikalisches Institut, Justus-Liebig-Universität Giessen, Giessen; Germany.
57 SUPA — School of Physics and Astronomy, University of Glasgow, Glasgow; United Kingdom.
58 LPSC, Université Grenoble Alpes, CNRS/IN2P3, Grenoble INP, Grenoble; France.
59 Laboratory for Particle Physics and Cosmology, Harvard University, Cambridge MA; United States of America.
Department of Physics, University of Pennsylvania, Philadelphia PA; United States of America.
Konstantinov Nuclear Physics Institute of National Research Centre "Kurchatov Institute", PNPI, St. Petersburg; Russia.
Department of Physics and Astronomy, University of Pittsburgh, Pittsburgh PA; United States of America.

(a) Laboratório de Instrumentação e Física Experimental de Partículas — LIP; (b) Departamento de Física, Faculdade de Ciências, Universidade de Lisboa, Lisboa; (c) Departamento de Física, Universidade de Coimbra, Coimbra; (d) Centro de Física Nuclear da Universidade de Lisboa, Lisboa; (e) Departamento de Física, Universidade do Minho, Braga; (f) Universidad de Granada, Granada (Spain); (g) Dep Física and CEFITEC of Faculdade de Ciências e Tecnologia, Universidade Nova de Lisboa, Caparica; Portugal.

Institute of Physics of the Czech Academy of Sciences, Prague; Czech Republic.

Czech Technical University in Prague, Prague; Czech Republic.

Charles University, Faculty of Mathematics and Physics, Prague; Czech Republic.

Particle Physics Department, Rutherford Appleton Laboratory, Didcot; United Kingdom.

IRFU, CEA, Université Paris-Saclay, Gif-sur-Yvette; France.

Santa Cruz Institute for Particle Physics, University of California Santa Cruz, Santa Cruz CA; United States of America.

(1) Departamento de Física, Pontificia Universidad Católica de Chile, Santiago; (2) Departamento de Física, Universidad Técnica Federico Santa María, Valparaíso; Chile.

Department of Physics, University of Washington, Seattle WA; United States of America.

Department of Physics and Astronomy, University of Sheffield, Sheffield; United Kingdom.

Department of Physics, Shinshu University, Nagano; Japan.

Department Physik, Universitäit Siegen, Siegen; Germany.

Department of Physics, Simon Fraser University, Burnaby BC; Canada.

SLAC National Accelerator Laboratory, Stanford CA; United States of America.

Physics Department, Royal Institute of Technology, Stockholm; Sweden.

Departments of Physics and Astronomy, Stony Brook University, Stony Brook NY; United States of America.

Department of Physics and Astronomy, University of Sussex, Brighton; United Kingdom.

School of Physics, University of Sydney, Sydney; Australia.

Institute of Physics, Academia Sinica, Taipei; Taiwan.

(a) E. Andronikashvili Institute of Physics, Iv. Javakhishvili Tbilisi State University, Tbilisi; (b) High Energy Physics Institute, Tbilisi State University, Tbilisi; Georgia.

Department of Physics, Technion, Israel Institute of Technology, Haifa; Israel.

Raymond and Beverly Sackler School of Physics and Astronomy, Tel Aviv University, Tel Aviv; Israel.

Department of Physics, Aristotle University of Thessaloniki, Thessaloniki; Greece.

International Center for Elementary Particle Physics and Department of Physics, University of Tokyo, Tokyo; Japan.

Graduate School of Science and Technology, Tokyo Metropolitan University, Tokyo; Japan.

Department of Physics, Tokyo Institute of Technology, Tokyo; Japan.

Tomsk State University, Tomsk; Russia.

Department of Physics, University of Toronto, Toronto ON; Canada.

(a) TRIUMF, Vancouver BC; (b) Department of Physics and Astronomy, York University, Toronto ON; Canada.

Division of Physics and Tomonaga Center for the History of the Universe, Faculty of Pure and Applied Sciences, University of Tsukuba, Tsukuba; Japan.

Department of Physics and Astronomy, Tufts University, Medford MA; United States of America.

Department of Physics and Astronomy, University of California Irvine, Irvine CA; United States of America.

Department of Physics and Astronomy, University of Uppsala, Uppsala; Sweden.
Also at Institute for Particle and Nuclear Physics, Wigner Research Centre for Physics, Budapest; Hungary.

Also at Institute of Particle Physics (IPP); Canada.

Also at Institute of Physics, Academy Sinica, Taipei; Taiwan.

Also at Institute of Physics, Azerbaijan Academy of Sciences, Baku; Azerbaijan.

Also at Institute of Theoretical Physics, Ilia State University, Tbilisi; Georgia.

Also at Instituto de Fisica Teorica, IFT-UAM/CSIC, Madrid; Spain.

Also at Istanbul University, Dept. of Physics, Istanbul; Turkey.

Also at Joint Institute for Nuclear Research, Dubna; Russia.

Also at LAL, Université Paris-Sud, CNRS/IN2P3, Université Paris-Saclay, Orsay; France.

Also at Louisiana Tech University, Ruston LA; United States of America.

Also at LPNHE, Sorbonne Université, Paris Diderot Sorbonne Paris Cité, CNRS/IN2P3, Paris; France.

Also at Manhattan College, New York NY; United States of America.

Also at Moscow Institute of Physics and Technology State University, Dolgoprudny; Russia.

Also at National Research Nuclear University MEPhI, Moscow; Russia.

Also at Physikalisches Institut, Albert-Ludwigs-Universität Freiburg, Freiburg; Germany.

Also at School of Physics, Sun Yat-sen University, Guangzhou; China.

Also at The City College of New York, New York NY; United States of America.

Also at The Collaborative Innovation Center of Quantum Matter (CICQM), Beijing; China.

Also at Tomsk State University, Tomsk, and Moscow Institute of Physics and Technology State University, Dolgoprudny; Russia.

Also at TRIUMF, Vancouver BC; Canada.

Also at Universita di Napoli Parthenope, Napoli; Italy.

* Deceased