Collision-Induced Absorption between O₂-CO₂ for the $a^1\Delta_g (v = 1) \leftrightarrow X^3\Sigma_g^- (v = 0)$ transition of molecular oxygen at 1060 nm

Agniva Banerjee, Julien Mandon, Frans Harren, and David H. Parker

Collision-induced absorption between O₂ and CO₂ molecules associated with the $a^1\Delta_g (v = 1) \leftrightarrow X^3\Sigma_g^- (v = 0)$ band of oxygen around 1060 nm was measured using cavity ring-down spectroscopy. The lineshape for this transition is measured for the first time, and the integrated cross-section is found to be smaller than the only previous report. For pure oxygen, we find an integrated absorption value of $(2.10 \pm 0.31) \times 10^{-4}$ cm²amg⁻² which is in good agreement with the previous reported values. For O₂-CO₂ collisions we report an integrated value of $(6.37 \pm 1.09) \times 10^{-4}$ cm²amg⁻² which is small but still significant and not accounted for by theory.

1. Introduction

Absorption of sunlight by atmospheric constituents is a complex phenomenon where the efficiency depends on the quantum nature of the molecules together with the details of collisions taking place among them. Collision-induced phenomena¹ can be considered as resulting from a transient complex formed during collision where the absorption efficiency differs from those of the individual constituents. Due to the very short complex lifetime (≈ $10^{-13}$s), collision-induced absorption (CIA) is small compared to normal line absorption, and relevant only at atmospheric pressures or higher.

Carbon dioxide, CO₂, is the most abundant greenhouse gas on Earth² and industrial progress has resulted in a significant rise in CO₂ concentration³ which causes increased surface warming, affecting Earth’s climate. Reports of local yearly average CO₂ concentrations at Mauna Loa Observatory, Hawaii, for example, indicated values of 407.98 ppm in January 2018, 406.13 ppm in January 2017 and 402.52 ppm in January 2016.⁴ A better understanding of the sources and sinks of carbon cycles is thus important.

High precision satellite measurements of the local concentration of CO₂ by ESA’s Environmental Satellite (ENVISAT), and NASA’s Orbiting Carbon Observatory (OCO-2) provide important new data for this quest.⁵ 6 ⁷ However, clouds and aerosols complicate accurate determination of CO₂ concentration,⁸ and for these satellites, calibration methods are also needed.⁹ ¹⁰

Molecular oxygen, O₂, is often used for calibration as it is abundant and has a well-known spectrum.¹¹ ¹² ¹³ O₂ is unusual in having many bound electronic states below the first dissociation limit, but all of the transitions from the ground electronic state in the infrared, visible, and ultraviolet region below the allowed VUV Schumann-Runge transition are optically forbidden. Very weak magnetic dipole and/or electric quadrupole transitions from the ground state to the lower excited electronic states are possible, along with transitions induced by weak spin-orbit coupling, which can increase significantly during a collision. Under Earth’s atmospheric conditions, light absorption is often governed by collision-induced absorption. When one oxygen molecule collides with other atmospheric species such as O₂, N₂, or CO₂, a transition moment can be induced, therefore lifting up the symmetry restrictions slightly,¹⁴ the efficiency of this phenomenon depends on the quantum character of the collision partner. The probability of CIA is also strongly dependent on the vibrational level of the O₂ excited electronic state reached by CIA, where vertical excitation ($\Delta v=0$) should be favoured for the lower vibrational states of oxygen.

In this paper, we study the O₂ transition from $X^3\Sigma_g^- (v = 0)$ to $a^1\Delta_g (v = 1)$, which lies around 1060nm. Mixing by spin-orbit coupling of the $X^3\Sigma_g^-$ ground state with the higher lying $d^1\Pi_g$ and/or $C^3\Pi_g$ Rydberg states gives this transition magnetic dipole allowed character.¹⁵ While a strong decrease in the magnetic dipole transition for vibrational levels $a (v > 0)$ due to unfavourable Frank-Condon factors is predicted,¹⁶ the collision induced absorption coefficient was found to be surprisingly large.¹⁷ ¹⁸ Literature values for integrated O₂-O₂ CIA cross sections in cm²amg⁻² for the near infrared bands of oxygen are listed in Table 1.¹⁹ ²⁰ ²¹ ²²

In a recent paper, Karman et al.²³ reported ab-initio calculations and experimental measurements of CIA between O₂-O₂ and O₂-N₂ for the $X^3\Sigma_g^- (v = 0) \rightarrow a^1\Delta_g (v' = 0,1,2)$ and $b^1\Sigma_g^+ (v=0,1)$ transitions in details. Two mechanisms were found to be important: spin-orbit coupling which enhances only the
Δv=0 transition, and for O₂-O₂ (two paramagnetic molecules) an exchange mechanism involving the total electron spin of the collision complex in which total spin remains conserved while one O₂ monomer changes its spin state. The spin exchange mechanism was found to also enhance Δv>0 transitions. Near quantitative agreement was found between ab-initio theory and experiment for these two collision pairs.

From fundamental interest, but also due to the importance of O₂ in exoplanet atmospheres, it is useful to compare CIA of O₂-O₂ and O₂-N₂ with that of O₂-CO₂. Vangvichith et al. reported an integrated CIA strength for O₂-CO₂ for the 0(v=0) to a(v=0) and a(v=1) transition. Fraser et al. obtained a value of 2.13×10⁻⁴ cm⁻²·amg⁻², significantly higher than the value from Vangvichith for the (v=0) transition. We also note that Hidemori and co-workers reported a 2-3 times increase in emission intensity with the addition of a heavy atom/molecule for the a(v=0) to X(v=0) O₂-O₂ collision-induced emission transition, which they suggested as being due to an increase in the spin-orbit mixing of the O₂ molecule. The only measurement of the CIA for the O₂-CO₂ X 3Σ⁻(v=0) to a 1Δ(g) (v = 1) transition, Ref. 22, reported only the integrated cross section, i.e., without line-shape information. The limited availability of data, together with the discrepancy in cross section values motivated the present study of the X(v=0) → a(v=1) transition for O₂-CO₂.

### 2. Experimental section

Figure 1 shows a schematic overview of our cavity ringdown set-up used for measurement, which is similar to that of Spiering et al., with some modifications. An optical cavity was created by placing two highly reflecting cavity mirrors (Layertec, reflectivity 99.993% between 9100-9900 cm⁻¹, the radius of curvature 8000 mm) separated at 350 mm distance in between a high-pressure cell (max. pressure 10 bar). This creates an effective path length of ~5 km. A continuous wave grating-stabilized diode laser (Toptica DL100) which consists of AR coated diode with the power of 170 mW in 9200 -9500 cm⁻¹ spectral region was used as the light source. The laser includes an optical isolator to prevent any reflection feedback. The line-width of the laser is much smaller than the free spectral range of cavity (0.0143 cm⁻¹). A small portion (2%) of light was reflected through a glass plate to a wavelength meter (Ångström HighFinesse WS/6). The rest of the light was guided through silver mirrors, a convex lens (f=25 cm) placed with a distance of 13 cm from the cavity cell and finally to the cavity cell respectively. Mode matching between the laser and cavity was obtained by tuning the mirror positions with an external controller and also by small adjustment of diode current. The addition of the lens helped in mode matching of the cavity as well as to excite only the lowest transverse mode. This procedure incorporates an uncertainty in the wavelength measurement of about half the free spectral range of the cavity (0.007 cm⁻¹). The light leaking out of the cavity was detected using a Si-avalanche photodiode (Licel, 500-1100 nm). The pressure inside the cell was monitored with a diaphragm pressure gauge (Pfeiffer Vacuum D-35614, accuracy 0.3%). The controlled flow (200-250 ml/min) of high purity oxygen (Linde gas, 99.99999% purity) and high purity carbon dioxide (Linde gas, 99.9993% purity) were passed to the cell using two different digital thermal mass flow controllers (El-Flow, Bronkhorst high tech). The flow rate set in the controllers determine the percentage of the resultant gas mixture in the pressure cell. Each measurement started with emptying out the cell using a...
membrane pump before gas filling. The signals of the pressure gauge and photodiode were sent to NI-SI133 data acquisition device (National Instruments, 50 MHz Bandwidth, 100 MS/s, 2-Channel, 8-Bit), and the photodiode signal was sent to a home-built switch controller. When the light intensity of the photodiode reaches a pre-defined threshold value, a pulse (4V, 200 µs) is used shut the laser off which occurs in the timescale of ns, so that the light in the cavity can decay exponentially. The decay time of an empty cavity was about 28-29 µs. For actual measurements, both pressure and decay signal were recorded simultaneously and the signals are sent to a computer for further analysis using a LabVIEW routine. The rate of measurement was kept constant at ~3 decay signals per second either by changing the threshold value or increasing the sensitivity by changing the detector gain. This process was repeated for other wavelengths as well. Rayleigh Scattering (RS) contributes also to our extinction values. Measuring extinction as a function of pressure allowed us to differentiate RS from CIA due to different scaling in absorption with density. All the measurements were performed at 293 K. From the HITRAN database, it is clear that there are absorptions in our wavelength range due to O$_2$, H$_2$O, and CO$_2$. To reduce their effect, the gas tubing along with the pressure cell were heated and the chamber was flushed with pure N$_2$ or Ar for a long time. Wavelengths without line absorption of carbon dioxide and water were selected as much as possible.

3. Analysis

Collision-induced absorption (CIA) in an O$_2$-CO$_2$ mixture can be expressed by the following empirical formula (1),

$$
\varepsilon (v) = N^2 \left[ \rho_{O_2}^2 a_{O_2O_2}(v) + \rho_{O_2} \rho_{CO_2} a_{O_2CO_2}(v) \right] + N L_s \left[ \rho_{O_2} \sigma_{O_2}(v) + \rho_{CO_2} \sigma_{CO_2}(v) \right] + C(v), \hspace{1cm} (1)
$$

where $\varepsilon$ stands for extinction, $N$ is the particle density, $\rho_{O_2}$ the partial pressure of oxygen, $\rho_{CO_2}$ the partial pressure of carbon dioxide, $a_{O_2O_2}$ the collision induced absorption cross-section coming from O$_2$-O$_2$ collisions and $a_{O_2CO_2}$ the collision induced absorption cross-section coming from O$_2$-CO$_2$ collisions, $L_s$ is Loschmidt constant, $\sigma$ values are the corresponding Rayleigh scattering cross-sections for both O$_2$ and CO$_2$, $C$ is a constant representing mirror loss. All $a$, $\sigma$ and $C$ values are wavenumber ($v$) dependent. The analysis of the data includes fitting each measured ring-down time signal with an exponential decay for different pressure during the pressure ramp. Finally, a set of extinction values for corresponding pressure values at a particular laser wavelength were obtained. The same procedure was carried out for each wavelength between 9200 to 9500 cm$^{-1}$ (within the diode laser range) for both O$_2$-O$_2$ and O$_2$-CO$_2$ mixtures. The whole procedure was repeated several times.

The constant value $C$ was obtained from the empty cavity ring-down time at the measured laser wavelength. The Rayleigh scattering values for O$_2$ were taken from Bates$^{32}$ and for CO$_2$ were taken from Bideau-Mehu$^{33}$ (which produce values within the error bar) and subtracted from our measured extinction values. The resultant absorption values were fitted with a quadratic equation in order to extract the CIA coefficients at different wavenumbers. The fitting procedure with resultant absorption values for different gas mixtures is shown below in figure 2.

![Fig. 2: Density ramps for different mixtures of O$_2$-CO$_2$ used in this study at 9380.685 cm$^{-1}$. 1) Green: 100% O$_2$-0% CO$_2$, 2) Pink: 60% O$_2$-40% CO$_2$, 3) Blue: 50% O$_2$-50% CO$_2$, 4) Red: 30% O$_2$-70% CO$_2$, 5) Yellow: 100% CO$_2$. For most of our measurements we used 100% O$_2$ & 50% O$_2$ – 50% CO$_2$ mixtures, mixtures correspond to the pink, red and yellow lines were used only for confirmation.](image-url)

This whole procedure was repeated for both pure O$_2$ and O$_2$/CO$_2$ (1:1 mixture) for all wavelengths. The CIA coefficient values obtained for pure O$_2$ were lowered with a factor of (0.50$^\circ$) or 0.25 because in the mixture only 50% O$_2$ is present and CIA is quadratic in nature. The resultant scaled coefficient values originating from O$_2$-O$_2$ collisions were subtracted from the CIA coefficient values obtained from a (1:1) O$_2$-CO$_2$ mixture, which contains all contributions according to their relative partial pressures, so that this correction results in a CIA coefficient originating only due to O$_2$-CO$_2$ collisions.

In order to extract the CIA contribution arising from pure CO$_2$-CO$_2$ collisions (if this is measurable), the same procedure was carried out for pure CO$_2$ gas. Line absorption of CO$_2$ was taken from the HITRAN database$^{34}$, corrected for the corresponding pressure values and subtracted from the measured extinction values. The remaining CO$_2$-CO$_2$ absorption signal was very low as was the magnitude of its CIA coefficient when fit with a quadratic equation. Our system may not be sensitive enough to quantify such very low CIA values, as discussed later in this article. In the following analysis, we neglected the contribution arising from CO$_2$-CO$_2$ collisions.
4. Results and discussions

Quadratic fitting \( y = ax^2 + bx + c \) of the measured extinction values with respect to density results in two coefficients, one which depends on the square of density (a), one which linearly depends on density (b) and (c) being the intercept. The first coefficient corresponds to CIA and the second to Rayleigh Scattering (RS). For pure O\(_2\), we see a quadratic dependence on density and from simple fitting it was possible to extract the RS coefficients, although the values obtained from measurements had large error (\( \pm50\% \)) and deviated from the theoretical values provided by Bates.\(^{22}\) For CO\(_2\), the very weak extinction values did not show a clear quadratic or linear dependence and it was difficult to use for a proper fitting in order to extract coefficients. This can be due to very low absorption or scattering by CO\(_2\) in this wavelength region, or to a limitation within our system itself. Theoretical RS values were used instead of obtained values.

The HITRAN database allows us to identify the most prominent H\(_2\)O line absorption between 9150 - 9350 cm\(^{-1}\). To avoid these absorptions, experimental wavelengths were chosen which fall between water line absorptions. Gases with very high purity and heating of the tubes ensured a water absorption value \(< 10^{-8} \text{ cm}^{-1}\). From figure 3, it is clear that line absorptions of CO\(_2\) are much more pronounced than those of O\(_2\). Although the strongest absorptions for CO\(_2\) occur around 9500 cm\(^{-1}\), our diode could measure only until 9480 cm\(^{-1}\). The CO\(_2\) lines were so dense, it was very difficult to set the laser at a wavelength without line absorption. In addition, when the molecules collide, due to inelastic collisions, there will be a transfer of intensity. Our line mixing program\(^{41}\) takes into account molecular inelastic collisions towards the line shape which results in the intensity transfer between two adjacent rotational lines following an expression by Fano for this effect.\(^{35}\) Later Tonkov\(^{36}\) introduced one more parameter previously defined by Fano, to allow line mixing between transitions between two different branches, called the ABC model. This model was applied for O\(_2\), CO, CO\(_2\), CH\(_3\)F, and CH\(_4\) successfully.\(^{36,37,38,39,40}\) Our line mixing model uses a Voigt convolution of line mixing spectra and Gaussian contributions arising from Doppler effect as described by Spiering and co-workers.\(^{41}\) The computational program determines the line mixing correction on the sum of Voigt line shape spectrums based on the collisional parameters, which includes pressure shifts, for each transition value reported in the HITRAN database.\(^{34}\) Due to molecular collisions, the Lorentzian lines need to be modified with a Gaussian function, which resulted in a Voigt shape profile. The corrected line absorption values for both O\(_2\) and CO\(_2\) were subtracted from the measured extinction. Resulting absorption values when fitted with the square of density, yield the final CIA coefficient values, which are presented in figure 4.

It is clear from figure 4 that the total collision-induced absorption coefficient values from a 1:1 O\(_2\)-CO\(_2\) mixture is higher than the O\(_2\)-O\(_2\) component (considering its 50% contribution), with a maximum value around 9380 cm\(^{-1}\). Since pure CO\(_2\) showed a very weak and noisy absorption profile, another approach was used to evaluate any CO\(_2\)-CO\(_2\) contribution which could underlie the O\(_2\)-CO\(_2\) collisional effect. Different O\(_2\)-CO\(_2\) mixture ratios, as shown in figure 2, were used to re-calculate collision coefficients of the different possible interactions included in equation (1). The wavelength of 9380.685 cm\(^{-1}\) (near the O\(_2\)-O\(_2\) CIA peak) was studied, considering the fact that both O\(_2\)-CO\(_2\) and CO\(_2\)-CO\(_2\) (if contributing at all) components contribute the most at this photon energy. For the five different mixtures used in this study, equation (1) was transformed into five different expressions and by solving these equations, the normalized values obtained for O\(_2\)-O\(_2\), O\(_2\)-CO\(_2\) and CO\(_2\)-CO\(_2\) were (9.65\(\pm0.18\))\(\times10^{-7}\) cm\(^2\)amg\(^{-2}\), (3.83\(\pm0.21\))\(\times10^{-7}\) cm\(^2\)amg\(^{-2}\), (6.50\(\pm0.95\))\(\times10^{-9}\) cm\(^2\)amg\(^{-2}\) respectively. CIA values for O\(_2\)-O\(_2\) and O\(_2\)-CO\(_2\) obtained from (1:1) O\(_2\)-CO\(_2\) mixture around 9380 cm\(^{-1}\), plotted in figure 5, match quite well with the one obtained in this process performed with different mixtures of O\(_2\)-CO\(_2\) at 9380.685 cm\(^{-1}\) and these lie within the error limit. Owing to its low value, we neglected pure CO\(_2\)-CO\(_2\) collision effects for the rest of our calculation. We assume similar behaviour from CO\(_2\) for other wavelengths for this band as well. Figure 5 shows both the normalized O\(_2\)-O\(_2\) and O\(_2\)-CO\(_2\) CIA
The integrated CIA cross section value obtained from an extrapolated Lorentzian fit with FWHM of (97±2) cm\(^{-1}\) was 
\((6.37±1.09) \times 10^{-5}\) cm\(^2\)amg\(^{-2}\). The error in the integrated absorption strength originates from the choice of fitting method, and from statistical fluctuations of the measured data points and also from the extrapolation. The peak was observed at (9384±2) cm\(^{-1}\). Uncertainties in temperature and pressure are smaller than statistical error.

No sharp features were observed in the CIA spectrum. The O\(_2\)-CO\(_2\) CIA spectrum is much narrower than the O\(_2\)-O\(_2\) CIA spectrum, as is clearly visible in figure 5, and its integrated intensity is about 3.3 times lower. The efficiency, which is a measure of the probability for a transition to occur based purely on Franklin-Condon (FC) factors, can be expressed with the following expression

\[
\eta = \frac{A(v_a)}{A(v=0)},
\]

where the A values are for integrated collision-induced absorption at the corresponding vibrational level transitions, the values of which are given in table 2.

The large error associated with \(\eta_{v_a=1}\) for O\(_2\)-CO\(_2\) is due to uncertainty (46%) associated with the determination of the integrated CIA values. Our cross section for the X \((v=0)\) \(\rightarrow\) a \((v=1)\) transition is a factor of almost three smaller than the only previous literature value for this process.\(^{22}\) A possible reason for this discrepancy could arise from the extrapolation method and the accuracy of our line-mixing model, which excludes all the line-absorptions arising due to H\(_2\)O, O\(_2\), and CO\(_2\). Among these, the CO\(_2\) monomer makes the most significant contribution to the light absorption process at high pressure.

The relatively large O\(_2\)-CO\(_2\) CIA cross section we find for the X \((v=0)\) \(\rightarrow\) a \((v=1)\) compared to X \((v=0)\) \(\rightarrow\) a \((v=0)\) is not consistent with a recent model of CIA by Karman et al.\(^{23}\) which predicts a very low cross section since CO\(_2\) (as well as N\(_2\)) as discussed in Ref. 23 is diamagnetic and cannot follow thefavoured total spin exchange mechanism. This disagreement is not surprising considering that the isotropic potentials used in Ref. 23 will be less applicable to CO\(_2\). Further analysis is necessary to better understand this effect.

### Table 2: Comparing efficiencies (\(\eta\)) of different transitions, \(\eta = \text{Integrated CIA (v_a)} / \text{Integrated CIA (v0)}\)

<table>
<thead>
<tr>
<th>(v_a)</th>
<th>(\eta_{O_2-O_2})</th>
<th>(\eta_{O_2-CO_2})</th>
</tr>
</thead>
<tbody>
<tr>
<td>0</td>
<td>1</td>
<td>1</td>
</tr>
<tr>
<td>1</td>
<td>0.76±0.10</td>
<td>0.85±0.50</td>
</tr>
</tbody>
</table>

The efficiency values for the optical transition are comparable between O\(_2\)-CO\(_2\) & O\(_2\)-O\(_2\) for the above-mentioned transition, considering the error bar. The efficiencies based on the FC factor for this transition is 0.013.\(^{17}\) A change in the internuclear distance in the excited \(a\)-state from 1.2156 Å to 1.1152 Å is necessary to modify the FC factors in a way that it agrees with the integrated intensity values, within the error bar, for O\(_2\)-O\(_2\) collisions.\(^{20}\) Comparing the measured efficiency values we can suggest that CO\(_2\) deforms the excited \(a\)-state to some extent. Despite having a ground state configuration of \(^3\Sigma^+\), a large electric quadrupole moment and polarizability anisotropy of CO\(_2\) could cause more penetration during a collision with the O\(_2\) molecule, producing a compression in the excited state bond length of O\(_2\).\(^{22}\) Being a larger molecule, CO\(_2\) could further increase spin-orbit coupling between the \(X^3\Sigma^+\) and higher electronic \(d^3\Pi_g\) state compared to O\(_2\).\(^{27}\) We note that this is an oversimplification of the complex processes occur during collisions.

Chagas et al.\(^{17}\) have reported the effect of CIA on the 1060 nm band in the total absorption in our atmosphere. For a mid-latitude summer atmospheric profile with a solar zenith angle of 60\(^\circ\), a surface albedo of 0.1, and a total incoming solar irradiation of 1368 Wm\(^{-2}\), they found that the CIA of O\(_2\)-O\(_2\) at 1060 nm band contributed for 0.30 Wm\(^{-2}\). This value was recalculated for our CIA contributions of O\(_2\)-O\(_2\) and O\(_2\)-CO\(_2\) collisions and we see that the CIA at 1060 nm band adds 0.22% to the short wavelength absorption in our atmosphere. About 0.000118% of this is caused by collisions between CO\(_2\) and O\(_3\).

### Table 3: The effect of CIA on the absorption in our atmosphere at 1060 nm band

<table>
<thead>
<tr>
<th>CIA contributors</th>
<th>O(_2)-O(_2)</th>
<th>O(_2)-CO(_2)</th>
<th>Total</th>
</tr>
</thead>
<tbody>
<tr>
<td>CIA contribution</td>
<td>1.01±0.04 (5.30±0.90)x10(^{-4})</td>
<td>≈ 1.01±0.04</td>
<td></td>
</tr>
<tr>
<td>Sunlight absorption</td>
<td>0.30±0.03 (1.58±0.29)x10(^{-4})</td>
<td>≈ 0.30±0.03</td>
<td></td>
</tr>
<tr>
<td>Short-wave absorption</td>
<td>0.22±0.05 (1.18±0.14)x10(^{-4})</td>
<td>≈ 0.22±0.05</td>
<td></td>
</tr>
</tbody>
</table>
At sunrise or sunset when longest path lengths are present the absorption process should become most significant. Due to the very low absolute concentration of CO₂ gas present in our atmosphere, the O₂-CO₂ CIA coefficients are very small and it is probably not possible to measure this induced absorption process in Earth’s atmosphere.

5. Conclusion

By the use of cavity ring-down spectroscopy, we have characterized collision-induced absorption of two important atmospheric gas molecules, CO₂ collisions with O₂ for the O₂ a 1Δg ← X 3Σg⁻ transition. The very small amount of CO₂ present in the air makes this CIA process less significant, although the amount of CO₂ is increasing at present. Collisional effects between O₂-CO₂ have not been studied in detail so far for this O₂ transition. Assuming the profile to be Lorentzian, we were able to determine the CIA contribution which make the profile to be Lorentzian, we were able to determine the CIA contribution which remains the most dominant. A proper accounting for this small but significant CIA contribution remains a challenge for theory.

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References


