Clumpy jets from black hole–massive star binaries as engines of fast radio bursts

Shu-Xu Yi †, 1,2† K. S. Cheng 1 and Rui Luo ‡, 3, 4

1 Department of Physics, The University of Hong Kong, Pokfulam Road, Hong Kong
2 Department of Astrophysics, Radboud University Nijmegen, PO Box 9010, NL-6500 GL Nijmegen, the Netherlands
3 Department of Astronomy, School of Physics, Peking University, Beijing 100871, China
4 Kavli Institute for Astronomy and Astrophysics, Peking University, Beijing 100871, China

Accepted 2018 November 26. Received 2018 November 12; in original form 2018 August 29

ABSTRACT

We propose a new model of fast radio bursts (FRBs) based on stellar-mass black hole–massive star binaries. We argue that the inhomogeneity of the circumstellar materials or/and the time varying wind activities of the stellar companion will cause the black hole to accrete at a transient super-Eddington rate. The collision among the clumpy ejecta in the resulted jet could trigger plasma instability. As a result, the plasma in the jet will emit coherent curvature radiation. When the jet cone aims toward the observer, the apparent luminosity can be $10^{51}–10^{52}$ erg s$^{-1}$. The duration of the resulted flare is $\sim$ millisecond. The high event rate of the observed non-repeating FRBs can be explained. A similar scenario in the vicinity of a supermassive black hole can be used to explain the interval distribution of the repeating source FRB 121102 qualitatively.

Key words: black hole physics – radiation mechanisms: general – binaries: general.

1 INTRODUCTION

High time-resolution Universe contains a lot of unknowns to be revealed. As a new class of astronomical transients, fast radio bursts (FRBs), exhibits basic observational features with short duration ($\sim$0.1–10 ms), large flux density (0.1–100 Jy), and prominent dispersion. From its first discovery (Lorimer et al. 2007) to present, over 50 such flashes have been reported as detections by 2018 October, which are nearly isotropically distributed in the full sky (see Fig. 1, of which the data come from frbcat; † Petroff et al. 2016).

FRBs are believed to have extragalactic or cosmological origin because of their large dispersion measure (DM; from about 170 to 2600 cm$^{-3}$pc). Because of remarkable flux observed, the intrinsic luminosities are estimated to be very high with a broad range ($10^{51}–10^{54}$ erg s$^{-1}$; Luo et al. 2018).

Although there are a substantial number of FRBs reported, the nature of FRBs is still a mystery. So far, theoretical models with number much larger than FRBs themselves have been proposed, related to a wide range of astronomical objects, such as pulsars (Connor, Sievers & Pen 2016; Dai et al. 2016), magnetars (Popov & Postnov 2013; Pen & Connor 2015; Beloborodov 2017; Metzger, Berger & Margalit 2017), neutron stars (Totani 2015; Falcke & Rezzolla 2014; Zhang 2014, 2017; Cordes & Wasserman 2016), quark stars (Shand et al. 2016; Wang et al. 2018), white dwarfs (Kashiyama, Ioka & Mészáros 2013; Gu et al. 2016), black holes (BHs; Liu et al. 2016; Romero, del Valle & Vieyro 2016; Katz 2017), etc.

The only repeating FRB, FRB 121102 (Spitler et al. 2016), draws many attentions owing to continuous observational progresses. Its host galaxy was identified as a dwarf galaxy at a redshift of 0.193 with the Very Large Array (VLA; Chatterjee et al. 2017; Tendulkar et al. 2017) and a persistent radio source is found to be spatially associated with these bursts (Marcote et al. 2017). At one time, people tended to think the persistent radio source could be pulsar wind nebula (Beloborodov 2017; Dai, Wang & Yu 2017) and emits via synchrotron radiation (Waxman 2017). However, new observations on the repeater revealed its huge Faraday rotation measure ($>10^{5}$ rad m$^{-2}$), which suggested that the highly magnetized environment is compatible with those of an accreting massive BH in the galaxy centre (Michilli et al. 2018). The FRB progenitor is proposed to be a neutron star orbiting the central BH (Zhang 2018) or a young millisecond magnetar in the supernova remnant (G50, Metzger et al. 2017).

In this paper, we focus on another possible mechanism related to a much larger population: stellar-mass BH–massive star binaries. When the mass transfer rate from the stellar companion suddenly increases, a transient super-Eddington accretion will occur, analogous to the process in the tidal disruption event (TDE; Dai et al. 2018). A clumpy jet could be thus launched. We find that collision among the ejecta and coherent curvature radiation of the plasma in the jet can produce radio flares that coincide with the observational characteristics of FRBs.
accretion rate: the energy converting efficiency from the accretion to the jet. The efficiency from the accretion to the jet. The typical dimension of the clumps corresponds to the height of the accretion flow at the inner edge, $h$. Therefore the mass of the clump can be approximated as

$$\delta M \approx h^3 \rho_0,$$

where $\rho_0$ is the density of the material at the inner edge of the accretion flow. The accretion rate is related to the properties of the accretion flow as

$$\dot{M} = 4\pi \rho_0 v_r h,$$

where $v$ is the inflow velocity of the materials at the inner edge $v_r$. $v$ can be approximated with the free-falling velocity:

$$v = \sqrt{\frac{2GM_s}{r_w}},$$

where $M_s$ is the mass of the BH. We use the radius of the innermost stable circular orbit of the BH, $r_w = 3r_s$, where $r_s$ is the Schwarzschild radius of the BH. As a result, $v = c/\sqrt{3}$, where $c$ is the speed of light.

For the estimation of $\gamma$, we do not need the explicit formula of $v$. We use the size of the clump $h$ as the average separation, thus the interval between ejecta is scaled with $\delta t \sim h/v$.

Taking equations (3),(4), and (6) into equation (1), we obtain that

$$\gamma \sim \frac{2\pi \rho_0 v_r \delta t}{h},$$

which is independent with the mass and the accretion rate of the BH. We denote the dimensionless $h/r_w$ as $\bar{h}$ in the following texts for simplicity. From equation (7) we expect the $\gamma$ to take value from $\sim 10$ to $\sim 100$. Since equation (7) is an approximated equation, we only take equation (7) as a rough hint of the range of possible $\gamma$ and still treat $\gamma$ as an independent parameter in the following of the model.

Since the accretion flow is inhomogeneous, the velocities among the ejecta are expected to be non-uniform. In a case where a slower clump is ejected earlier than a faster one, the latter clump will collide with the earlier clump at a catch-up distance $l_{cat}$:

$$l_{cat} \approx c\gamma^2 \delta t.$$

This paper is organized as follows. We present our model in Section 2, and we give discussion in Section 3.

## 2 THE MODEL

We focus our interests on the situation where the materials from a massive star are being accreted onto the BH before a steady state accretion disc established. Such a situation is analogous to the transient accretion in TDEs. The materials are accreted at a nearly free-falling rate that is super-Eddington (McKinney, Dai & Avara 2015). The super-Eddington accretion could trigger a jet via Blandford–Znajek mechanism (Blandford & Znajek 1977). Since the accretion flow is not in a steady state, the ejecta in the jet are expected to be inhomogeneous, or in other words, clumpy (McKinney, Tchekhovskoy & Blandford 2012; Dai et al. 2018). When two clumps of ejecta collide with each other, plasma oscillation is activated and charge-separated bunches are formed. These bunches slide along the spiral magnetic field lines in the jet and radiate via curvature radiation. When the frequency of the curvature radiation matches the plasma frequency, the two-stream instability will grow and the charge bunch will emit coherently in a short time. Fig. 2 is an illustration for the model.

### 2.1 Collision between clumpy ejecta in the jet

We start with study of the collision between the successive clumps in the jet.

The Lorentz factor of the clumpy ejecta in the jet can be estimated in the following way. The energy of ejecta with the mass $\delta M$ is

$$\gamma \delta M c^2 = \epsilon M c^2 \delta t,$$

where $\delta t$ is the interval between the successive ejecta, $M$ is the accretion rate onto the BH, and $\epsilon$ is the energy converting efficiency from the accretion to the jet. $M$ is scaled with the Eddington accretion rate:

$$\dot{M} = \eta \dot{M}_{Edd},$$

where $\eta$ is the interval between the successive ejecta, $\delta t$, $\dot{M}$ is the accretion rate from the accretion to the jet. $\dot{M}$ is scaled with the Eddington accretion rate:

$$\dot{M} = \eta \dot{M}_{Edd},$$

The typical dimension of the clumps corresponds to the height of the accretion flow at the inner edge, $h$. Therefore the mass of the clump can be approximated as

$$\delta M = h^3 \rho_0,$$
The ejecta slide along the spiral magnetic field lines, and emit electromagnetic waves via curvature radiation. The frequency of curvature radiation in the rest frame $\nu_{\text{cur}}$ is determined by the local curvature radius of the magnetic field lines and the Lorentz factor of the plasma. Throughout the paper, we assume for simplicity that the plasma remains cold, i.e. the microscopic motion is negligible and we only consider the bulk motion. Since the magnetic field lines are highly spiral in the jet, the curvature radius of the magnetic field lines can be approximated as the radius of the jet cone (see the illustration in Fig. 2). The radius of the jet cone is denoted as $s(l)$ at $l$.

\[ \nu_{\text{cur}}(l) = 2\gamma_\perp \gamma_\parallel^3 c/s(l), \]

where $\gamma_\parallel$ is the Lorentz factor corresponding to the sliding of the plasma along the magnetic field lines, $\gamma_\perp$ corresponds to the bulk velocity along the line of sight (in a case where the jet cone is towards the observer). For simplicity we use $\gamma_\perp \sim \gamma_\parallel \sim \gamma$. The frequency of the curvature radiation as function of $l$ is calculated as

\[ \nu_{\text{cur}}(l) = 3.8 h^{-1} \frac{\gamma_\parallel m}{l} \frac{l_{\text{cur}}}{l} \text{ GHz}, \]

where $m$ is the mass of the BH in units of $M_\odot$, $\gamma_{100} \equiv \gamma/100$. When calculating equation (10), we use equation (8) and with the assumption that the opening angle of the jet cone is 0.1, i.e.

\[ s(l) = 0.1l. \]

\subsection{2.2 Coherent curvature radiation}

The collision between the successive clumps triggers the plasma oscillation, and the charges in the plasma are displaced with the plasma frequency $\nu_{\text{pls}}$. The charge-separated plasma acts like a bunch of charged particles, which moves across the spiralled magnetic field lines and radiates via curvature radiation. When the condition is satisfied such that $\nu_{\text{pls}} \approx \nu_{\text{cur}}$, the charged bunch will radiate coherently.

The plasma frequency in the observer’s frame is

\[ \nu_{\text{pls}}(l) = 2 \sqrt{\frac{\gamma_\parallel e^2 n_e(l)}{\pi m_e}}, \]

where $e$ and $n_e$ are the charge and the mass of the electron, $n_e$ is the number density of the electrons, which is

\[ n_e(l) = 2 \rho(l)/m_p, \]

where $m_p$ is the mass of proton.

Since the dimension of the clump expands along the jet with increasing radius of the jet cone $s(l)$, the density of the plasma decreases accordingly as

\[ \rho(l) = \rho_0 \left( \frac{h}{s(l)} \right)^3, \]

and from equations (2) and (4):

\[ \rho_0 = \frac{\eta M_{\text{Edd}}}{2\pi \nu_{\text{pls}} h}. \]

The Eddington rate is explicitly expressed as

\[ M_{\text{Edd}} = 1.26 \times 10^{33} \frac{m_{\text{BH}}}{\epsilon c^2} \text{ erg s}^{-1}. \]

From the above equations, we obtain that

\[ \nu_{\text{pls}}(l) = 3.45 \sqrt{\frac{\eta}{m_pc h}} \gamma_{100}^{2.5} \left( \frac{l_{\text{cur}}}{l} \right)^{1.5} \text{ GHz}. \]

\[ \text{Figure 3. } \nu_{\text{cur}} \text{ and } \nu_{\text{pls}} \text{ as functions of } l. \text{ Here we use } m = 10, \gamma = 100, \eta = 5, \epsilon = 0.2, \text{ and } h = 0.05. \]

Note that $\nu_{\text{pls}}$ decreases faster than $\nu_{\text{cur}}$ as $l$ increases (see Fig. 3). Therefore as long as $\nu_{\text{pls}} > \nu_{\text{cur}}$ at $l = l_{\text{cat}}$, the condition that $\nu_{\text{pls}} = \nu_{\text{cur}}$ can always meet at some distance $l > l_{\text{cat}}$. In Fig. 3, we plot an example when $m = 10, \gamma = 100, \eta = 5, \epsilon = 0.2$, and $h = 0.05$. The corresponding frequency of the coherent radiation is $\sim 1$ GHz.

Now we will estimate the lifetime of the curvature radiation. Let $Ze$ be the net charge in the bunched plasma, the size of which is $L$. When $\nu_p \approx \nu_{\text{cur}} = 1$ GHz and $\gamma = 100$,

\[ L \sim \epsilon/\nu_p^3 \sim 2c\gamma/\nu_p \sim 10^3 \text{ cm}. \]

The estimation of $Z$ follows the practice of Ruderman & Sutherland (1975):

\[ Z E_p = (Ze)^2/L, \]

where $E_p$ is the rest energy for each plasma particle, $m_p c^2 = 1.5 \times 10^{-3}$ erg. $Z$ is estimated to be $\sim 10^9$. The lifetime of the curvature radiation is

\[ \tau = \frac{Z^2 m_p c^2}{4(Z^2 e^2/c^3)^{1/2}(2e^2/s)^2} \sim 10^9 \mu s, \]

which corresponds to the smallest temporal structure of the FRB. It is essential that $\tau$ is larger than the time-scale of plasma instability growth, $t_g = 1/\nu_p$ ns. Otherwise the plasma cannot be significantly bunched. We note from equations (14) and (15) that $\tau$ is inverse proportional to $t_g$. As a result, the frequency of coherent radiation should be limited to be larger than $\sim 10$ MHz. We see from equation (17) that the emission can be up to a few GHz.

The above argument sets a necessary condition for the coherent radio emission:

\[ \nu_{\text{cur}}(l) > \nu_{\text{pls}}(l) > 10 \text{ MHz}, \quad \text{at } l > l_{\text{cat}}. \]

In Fig. 4, we illustrate the parameter space of $\tilde{h}$ and $\gamma$ corresponding to equation (21), given $m = 10, \epsilon = 0.2$, and $\eta = 5$.

\subsection{2.3 Duration and the luminosity of the flare}

The time-scale of the flare is determined by the duration of the super-Eddington accretion of the transient accretion disc, which corresponds to the free-falling time-scale near the BH:

\[ \tau_{\text{dur}} \sim \tau_{\text{ff}}/c. \]

For a BH with $10 M_\odot$, $\tau_{\text{dur}} \approx 0.3$ ms. This time-scale is in accordance with the millisecond duration of FRBs.

The apparent luminosity is

\[ L = \frac{2\pi}{\Delta \Omega} \epsilon M c^2, \]

Downloaded from https://academic.oup.com/mnras/article-abstract/483/3/4197/5232379 by Radboud University user on 31 January 2019
Considering equation (24), the luminosity distance is

\[ D_L = 8\pi m_\eta \times 10^{40} \text{ erg s}^{-1}. \]  

With typical masses of stellar BHs and super-Eddington accretion rate, \( L \) can be \( 10^{41} - 10^{42} \text{ erg s}^{-1} \). As shown in equation (20), the efficiency of the coherent radio emission is very high. Therefore, the radio luminosity is approximately equal to total luminosity.

### 2.4 Event rate

With a flux density limit at 1 Jy, the radio flare can be detected up to a luminosity distance of \( D_{1\text{Jy}} \), where

\[ \frac{L}{4\pi D_{1\text{Jy}}^2} \approx 1 \text{ GHz} \times 1 \text{ Jy}. \]  

Considering equation (24), the luminosity distance is

\[ D_{1\text{Jy}} \approx 0.3 \sqrt{\frac{2\pi m_\eta}{\pi}} \text{ Gpc}. \]  

An estimation of the detecting rate of the radio emission from the above-mentioned scenario is

\[ \mathcal{R} = \frac{n_G N_{\text{BH}} \Delta \Omega}{T} \frac{\epsilon m_\eta}{4\pi} V, \]  

where \( N_{\text{BH}} \) is the average number of BH–massive star binaries per galaxy, \( n_G \) is the number density of galaxies, \( T \) is the average recurrence time-scale of the radio flares, and \( V \) is the comoving volume within which the radio emission flux density are larger than the detectable limit, which is approximately \( \sim \text{Gpc}^3 \). The factor 2 in equation (27) accounts for the double sides of the jet cone.

We use \( n_G = 0.1 \text{ Mpc}^{-3} \) as an approximation in the low-redshift universe (Conselice et al. 2016; Corral-Santana et al. 2016) estimated a total population of \( \sim 1200 \) BH transients in the Milky Way. As discussed above, we expect to see the violent variation of mass transfer in wind accreting BH binaries with high-mass companion. Therefore, we use \( N_{\text{BH}} = 100 \), i.e. 10 per cent of the total estimated population for the evaluation of the event rate.

The recurrence of the radio flare depends on a fast increasing of mass transfer from the donor companion. This circumstance can occur when the BH is crossing the dense stellar disc of the companion, as in the cases of \( \gamma \)-ray binaries with Be stars (Dubus 2013). In this case, the accretion rate from the circumstellar materials will increase rapidly when the BH is inside the stellar disc. The recurrence time-scales of the radio flares are thus corresponding to the orbital period of the binaries, which are typically a few years. Besides, many wind-accretion binaries have been observed to have superorbital variability (Corbet & Krimm 2013). The superorbital periodicity is believed to related with the modulation on the mass-loss rate from the stellar companion (Koenigsberger et al. 2006; Farrell et al. 2008). A boost of the mass-loss rate from the donor can also cause the increasing of the accretion rate onto the BH. Note that the parameters \((R, \gamma, \epsilon, \eta)\) must fall in certain region given \( m \), in order to satisfy the necessary condition of the coherent radio emission as discussed in Section 2. Therefore, the radio flare might not appear in every orbital or superorbital period, but will recur after several periods. We use \( T = 10 \text{ yr} \) for a rough estimation of the recurrence time-scale.

Taking \( V, N_{\text{BH}}, n_G, \text{and } T \) into equation (27), the event rate is evaluated to be \( \sim 10^4 \text{ sky}^{-1} \text{ d}^{-1} \), which is consistent with the statistic studies of FRBs. Recently, FRBs are observed in a new low-frequency domain 400–800 MHz with CHIME/FRB (Boyle & Chime/Frb Collaboration 2018). Together with the other observations, e.g. 4–8 GHz observation of FRB 121102 (Gajjar et al. 2018; Shannon et al. 2018), these new observations indicate that FRB occurs in spectral islands that move around in frequency, therefore the event rate may be higher than the value estimated previously.

### 3 DISCUSSION

#### 3.1 FRB 121102

Oppermann, Yu & Pen (2018) found the intervals between the successive bursts of FRB 121102 present the tendency of clustering around the time-scale of \( 10^3 \text{ s} \). Although the conclusion needs further confirmation with larger data samples, this work may provide some insight of the possible underlying physical mechanism. More recently Gajjar et al. (2018) observed 23 bursts from this source in a continuous observation of 6 h, 21 bursts of which occurred in the first 60 min, and 18 bursts occurred in the first 30 min. Therefore the highest bursts rate of this source is \( 1/100 \text{ s}^{-1} \). We think that the mechanism of this source is different with above-mentioned stellar-mass BH–massive star model since the latter cannot produce such a high bursts rate. Existing models include the millisecond-magnetar interpretation (G50; Metzger et al. 2017; Margalit et al. 2018). With the hint that FRB 121102 was localized to the centre of its host galaxy, we propose that the repeating bursts are from the stellar-mass BH near the supermassive BH (SMBH) in the galactic centre. The stellar-mass BH orbits across the clumpy inner region of the accretion disc around the SMBH. The inhomogeneity could arise from the instability in the accretion disc. Each time when the stellar BH crosses a gas clump, a transient accreting process occurs. Unlike the stellar-mass BH–massive star binaries, the accreted materials have no angular momentum. If the stellar BH is a Kerr BH, a Blandford–Znajek jet can also be launched even in this case. As a result, the coherent radio emission can be triggered similarly. After all, the luminosity of the persistent source that coincides with FRB 121102 is consistent with a low luminous accreting SMBH (Chatterjee et al. 2017), and the rotation measure of the bursts also agrees with this scenario (Michilli et al. 2018).

Such interpretation of the repeating source implies several observational consequences. The short intervals of \( \sim 100–1000 \text{ s} \) of the

\[ \text{The variability with time-scale longer than the orbital period.} \]
bursts corresponds to the separation between clumps. If the orbit of the stellar BH around the SMBH is highly elliptical, we expect two quiescent periods of the FRB in each orbit. When the BH is outside the accretion disc of the SMBH and around the periastron, the source undergoes a shorter quiescent period; the orbital phases outside the accretion disc and around the apastron corresponds to a longer quiescent period. Another major prediction on the repeating source is that the outbursts of the sources could be found to clustered periodically, corresponding to the orbital period of the BH, after enough data accumulated.

3.2 The compact companion

It is possible for a neutron star to accrete from its massive companion at a super-Eddington rate, as were found in the ultraluminous X-ray pulsars (Bachetti et al. 2014; Fürst et al. 2016; Israel et al. 2017a,b). However, since a neutron star is highly magnetized, the accretion flow is truncated at the Alfvén radius where the magnetic pressure of the neutron star balances the ram pressure of the infalling materials. The typical Alfvén radius is $\sim 10^8$ cm, which is many orders of magnitude larger than the radius of a neutron star. As a result, the conditions of millisecond duration of the model cannot be satisfied with a neutron star companion.

3.3 Distribution in the host galaxies

In this paper, we propose that FRBs originate from stellar-mass BH–massive star binaries. Since massive stars are short lived, we expect such systems are more populated among active star-forming regions. As a result, our model predicts that FRBs should statistically concentrate towards star-forming galaxies. Furthermore, the sources should distribute close to the plane of disc galaxies.

ACKNOWLEDGEMENTS

The authors appreciate the helpful discussion about TDE accretion with Dr L. X. Dai. KSC and S-XY are supported by a GRF grant under 17310916.

REFERENCES

Boyle P. C., Chime/Frb Collaboration, 2018, Astron. Telegram, 11901
Chatterjee S. et al., 2017, Nature, 541, 58

This paper has been typeset from a TeX/LaTeX file prepared by the author.