The effect of stellar-mass black holes on the central kinematics of $\omega$ Cen: a cautionary tale for IMBH interpretations

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ABSTRACT
The search for intermediate-mass black holes (IMBHs) in the centre of globular clusters is often based on the observation of a central cusp in the surface brightness profile and a rise towards the centre in the velocity dispersion profiles. Similar signatures, however, could result from other effects, that need to be taken into account in order to determine the presence (or the absence) of an IMBH in these stellar systems. Following our previous exploration of the role of radial anisotropy in shaping these observational signatures, we analyse here the effects produced by the presence of a population of centrally concentrated stellar-mass black holes. We fit dynamical models to $\omega$ Cen data, and we show that models with $\sim5$ percent of their mass in black holes (consistent with $\sim100$ percent retention fraction after natal kicks) can reproduce the data. When simultaneously considering both radial anisotropy and mass segregation, the best-fit model includes a smaller population of remnants, and a less extreme degree of anisotropy with respect to the models that include only one of these features. These results underline that before conclusions about putative IMBHs can be made, the effects of stellar-mass black holes and radial anisotropy need to be properly accounted for.

Key words: methods: numerical, stars: kinematics and dynamics, globular clusters: general, globular clusters: individual: $\omega$ – Centauri (NGC 5139), galaxies: star clusters: general.

1 INTRODUCTION
Intermediate-mass black holes (IMBHs) could provide the missing link to understand the origin of supermassive black holes and of their host galaxies (Ebisuzaki et al. 2001). It has been suggested that IMBHs could form via a runaway stellar collision process in young ($\lesssim2$ Myr) massive star clusters (Portegies Zwart et al. 2004; Gieles et al. 2018), and great observational effort has been devoted to finding them in dense stellar systems like globular clusters (see, e.g. Lu & Kong 2011; Lützgendorf et al. 2011; Strader et al. 2012; Feldmeier et al. 2013; Haggard et al. 2013; Lützgendorf et al. 2013). The difficulty is that several other factors could cause observational signatures compatible with the presence of an IMBH (van der Marel & Anderson 2010; Vesperini & Trenti 2010). It is therefore important to determine the effect of these alternative ingredients on the quantities that are usually observed for these systems, in order to establish if an IMBH is indeed present or not.

The most common observational signature used to infer the presence of an IMBH in globular clusters is a rise towards the centre in the velocity dispersion profiles. Baumgardt et al. (2004) carried out numerical simulations of star clusters with a central IMBH and with a realistic mass function, taking also into account stellar evolution. They showed that the presence of the IMBH produces a cusp in the velocity dispersion profile in the innermost region of the cluster (within $\sim0.01$ half-mass radii, $r_h$, in their models), and causes the velocity dispersion profile to be larger than what can be explained by the stars over a radius of about $0.1r_h$. This is also observed by Baumgardt (2017) in the case of the best-fit model obtained for the globular cluster $\omega$ Cen (see their Fig. 6). In a recent work (Zocchi, Gieles & Hénault-Brunet 2017), we showed that radially anisotropic models reproduce the observational profiles of $\omega$ Cen well, and describe the central kinematics as derived from Hubble Space Telescope (HST) proper motions without the need for an IMBH. In this paper, we consider another factor that could affect the central velocity dispersion in a similar way as an IMBH, namely a centrally concentrated population of stellar-mass black holes (BHs). We point out that both radial anisotropy and the presence of a population of BHs produce an increase in the central...
projected velocity dispersion without generating a cusp like the one expected from the presence of an IMBH, but the data available at the moment does not allow to discriminate between these effects.

The possibility that old globular clusters host stellar-mass BHs has historically received little attention. First, this is, because BHs are believed to experience a natal kick at their formation in the supernova explosion, which could bring them to a velocity larger than the escape velocity. However, little is known about the magnitude of the corresponding kick velocity, because constraining this empirically has proven challenging. Recent efforts have taken advantage of the distribution in the Milky Way of X-ray binaries that contain black holes (BH-XRBs; Repetto, Davies & Sigurdsson 2012; Repetto & Nelemans 2015; Mandel 2016; Repetto, Igoshev & Nelemans 2017): the analyses based on the sample of observed BH-XRBs reveal that some systems could be explained with no or small natal kicks, but some others are better described when considering a relatively large natal kick. However, these analyses admittedly do not account for the fact that the presence of BH-XRBs found at higher Galactic latitude could be explained by considering the possibility that a few systems have been formed in the halo, or that they could have been ejected from globular clusters by dynamical interactions.

Secondly, the (unknown) fraction of BHs that is retained after supernova kicks was believed to be ejected quickly due to dynamical interactions. Spitzer (1969) showed that for a stellar system composed of two stellar populations with masses $m_1$ and $m_2$, where $m_1 < m_2$, and $M_1$ and $M_2$ the total mass of the two populations, with $M_1 \gg M_2$, equipartition is only possible if:

$$M_2 < 0.16M_1 \left( \frac{m_1}{m_2} \right)^{3/2} \tag{1}$$

(see also Watters, Joshi & Rasio 2000). If this condition is not satisfied, heavy objects (e.g. BHs) become self-gravitating before equipartition is achieved: they form a compact subsystem in the centre, dynamically separated from the rest of the cluster, and they interact only with each other. Due to the short two-body relaxation time-scale of such a subsystem, dynamical ejections are very efficient. Therefore, it was often assumed that BHs quickly eject each other from the cluster, until a single BH-binary is left.

The interest in the dynamical behaviour of a BH subsystem in globular clusters was recently reignited by the discovery of BH candidates in several globular clusters with radio (Strader et al. 2012; Chomiuk et al. 2013; Miller-Jones et al. 2015) and X-ray observations (Maccarone et al. 2007). Breen & Heggie (2013) showed that the dynamical ejection rate of BHs is lower than what was generally assumed (see also Morscher et al. 2013, 2015). The $N$-body models presented by Breen & Heggie (2013) demonstrate that a BH subsystem can survive as long as $\sim 10\tau_{\text{rh}}$, where $\tau_{\text{rh}}$ is the half-mass radius relaxation time. From a comparison of multicomponent dynamical models to $N$-body models, Peuten et al. (2017) showed that the BHs do not achieve equipartition with the stars. This means that if natal kicks are low enough for BHs to be retained by the cluster, and the initial half-mass radius relaxation time is long enough, a BH population is expected to be present in stellar systems as old as globular clusters. In fact, Breen & Heggie (2013) suggest that the collapse of the visible core coincides with the moment when all BHs have escaped the system. Given that only $\sim 20$ per cent of the Milky Way globular clusters are classified as core collapsed (Djorgovski & King 1986), this may mean that a fraction as high as 80 per cent of Galactic globular clusters still contain a population of BHs.

With this in mind, it is worth considering what the effects are of a BH population on the rest of the stars. Merritt et al. (2004) showed that a population of heavy dark remnants inflates the core radius ($R_c$) measured from the visible stars in the cluster. Mackey et al. (2008) suggested that the observed increase of $R_c$ with age in clusters in the Large Magellanic Cloud can be explained by a large retention fraction of BHs (i.e. low kick velocities). Finally, Peuten et al. (2016) showed that the distribution of stars of different masses in the Galactic globular cluster NGC 6101, which displays a surprising lack of mass segregation (Dalessandro et al. 2015), can be reproduced by $N$-body models and dynamical multimass models in which $\gtrsim 50$ per cent of the BHs are retained after supernova explosions (see also Alessandrini et al. 2016).

$\omega$ Cen is a likely candidate to host a BH population at the present day. Because of its large mass, it had a large escape velocity at the time BHs formed. Its present half-mass radius relaxation time is $\tau_{\text{rh}} \sim 20\text{Gyr}$, longer than its age. The relaxation time must have been shorter in the past, because of some expansion following stellar mass loss, so the dynamical age of $\omega$ Cen just falls short of one $\tau_{\text{rh}}$. During this time, we expect $\lesssim 10$ per cent of the BHs retained after supernova kicks to be ejected dynamically (Breen & Heggie 2013). For the metallicity of $\omega$ Cen, the stellar evolution models of Hurley, Pols & Tout (2000), SSE, predict that about 5 per cent of the present day mass is in the form of stellar-mass BHs for a Kroupa, Aarseth & Hurley (2001) stellar initial mass function (IMF) between $0.1M_\odot$ and $100M_\odot$. If a third of those are lost in supernova kicks and dynamical ejections (Morscher et al. 2015), we estimate that $\omega$ Cen hosts $\sim 2 \times 10^4$ stellar-mass BHs (for BHs with a mass of $5M_\odot$ and a mass for $\omega$ Cen of $\sim 3 \times 10^4M_\odot$, as estimated in Zocchi et al. 2017). Spera, Mapelli & Bressan (2015) combined recent stellar evolutionary tracks with models for supernova explosion, and predicted the mass distribution of compact remnants. They compared their results with those obtained by other codes, and found that, interestingly, the fraction of BHs produced from an IMF is remarkably similar across all the codes they compare and almost independent of metallicity. However, there are significant differences when focusing on the massive BHs: at low metallicity ($Z \lesssim 0.002$, applicable to most globular clusters), they find significantly larger maximum BH masses compared to previous predictions (e.g. from SSE), and five to six times more massive ($\gtrsim 25M_\odot$) black holes compared to SSE. The typical mass of BHs in $\omega$ Cen may therefore be larger than $5M_\odot$. Moreover, Shanahan & Gieles (2015) showed that the total mass in BHs with respect to the total mass of the cluster also depends on metallicity: they found that for $Z = Z_\odot$ the BHs account for 4 per cent of the total mass, while for $Z = 0.01Z_\odot$ they make up 7 per cent of the total mass.

Despite the young dynamical age of $\omega$ Cen, the BHs should have already segregated to the centre of the cluster. The equipartition time-scale of a two-component system depends on $\tau_{\text{rh}}$ as $\tau_{\text{eq}} \simeq (m_1/m_2)^2 \tau_{\text{rh}}$ (Spitzer 1969). Because stellar-mass BHs are an order of magnitude more massive than the stars, it only takes $0.1\tau_{\text{rh}}$ for the BHs to reach the centre, i.e. enough time given the dynamical age of $\sim 1\tau_{\text{rh}}$ estimated for $\omega$ Cen. A mild mass segregation has been observed among the visible stars of this cluster (Anderson 2002; Bellini et al. 2018) and by means of an analysis of blue straggler stars (Ferraro et al. 2006), consistent with its current state of partial relaxation (Giersz & Heggie 2003).

The work we are presenting provides information on the presence of stellar mass BHs in $\omega$ Cen and on their masses from a dynamical point of view. We use here dynamical models with two mass

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1This condition was later generalized for a continuous mass spectrum by Vishniac (1978).
components, to account for the different dynamics of stars and BHs in the presence of mass segregation. This allows us to estimate the amount of mass contained in the invisible BH component, and to determine the effect this has on the observed signatures that are often related to the presence of an IMBH in its centre. The fact that the visible stars are only mildly segregated justifies the choice of considering them all as part of the same component. In addition, by means of numerical simulations, Peuten et al. (2017) showed that in dynamically evolved systems with BHs, mass segregation among the stars is strongly suppressed, and the dynamics of stars, white dwarfs, and neutron stars are very similar to each other, further justifying the approximation by a single component for the stars and low-mass remnants, with visible stars used as “tracers” of a larger population.

This paper is organized as follows: in Section 2, we present the dynamical models we use, and in Section 3, we describe the data and the fitting procedure we adopt. We present and discuss our results in Section 4, and draw our conclusions in Section 5.

2 MODELS

To determine the effect of the presence of a population of dark remnants on the observable quantities used to study the dynamics of globular clusters, we use the LIMEPY family of models introduced by Gieles & Zocchi (2015), by considering its formulation with multiple mass components. For these models, it is possible to compute several quantities, of the cluster as a whole, and for each component separately.

These models can describe stellar systems with isotropic or anisotropic velocity distributions. The anisotropic version of these models describes systems that are isotropic in the centre, radially anisotropic in their intermediate part, and isotropic again at the truncation. Multiple components can be introduced, each one tracing a population of stars with a given mass, making up a certain fraction of the total mass of the system. The dynamics of each component is determined by the mean mass of the objects it represents, and these models can describe systems with different degrees of mass segregation.

In this study, we approximate ω Cen by two component models: a low-mass component (in the following also called Avisible component) representing the stars and lower mass stellar remnants (white dwarfs and neutron stars) and a high-mass component (in the following also called Adark component) representing the BHs. These models require only two additional parameters with respect to single-component models, and allow us to isolate the role of BHs in determining the dynamics of the other stars.

2.1 Distribution function

The LIMEPY family of models is a generalization of the formulation proposed by Gomez-Leyton & Velazquez (2014), with multiple mass components included as suggested by Da Costa & Freeman (1976) and Gunn & Griffin (1979). When considering \( N_{\text{comp}} \) mass components, the models are defined by the sum of \( N_{\text{comp}} \) distribution functions, each describing a different mass component, and defined as a function of the specific energy \( E \) and angular momentum \( J \) (Gieles & Zocchi 2015):

\[
f_j(E, J^2) = A_j \exp \left( -\frac{J^2}{2 \sigma_j^2} \right)\frac{E}{\sigma_j^2}
\]

for \( E < \phi(r_i) \) and zero otherwise, where \( \phi \) is the specific potential, and \( r_i \) is the truncation radius. The parameters \( s_j \) and \( r_{\sigma,j} \) indicate the velocity scale and the anisotropy radius for the \( j \)-th component; \( A_j \) is a normalization constant. The exponential function introduced in equation (2) is defined as

\[
E_\gamma(a, x) = \begin{cases} 
\exp(x), & a = 0, \\
\exp(x) \frac{\gamma(a, x)}{\Gamma(a)}, & a > 0.
\end{cases}
\]

where \( \gamma(a, x) \) is the lower incomplete gamma function, and \( \Gamma(a) \) is the gamma function.

The models are solved by computing the potential from the Poisson equation:

\[
\nabla^2 \phi = 4\pi G \sum_j \rho_j,
\]

where

\[
\rho_j = \int f_j d^3v
\]

is the mass density of the \( j \)-th component.

2.2 Model parameters

A model in the family is identified by specifying the values of three parameters. The concentration parameter \( W_0 \) represents the central dimensionless potential; it is a boundary condition for solving the Poisson equation, and determines the shape of the radial profiles of some relevant quantities. The truncation parameter \( g \) imposes the sharpness of the truncation in energy (Gomez-Leyton & Velazquez 2014): models with large \( g \) are more extended, and their truncation is less abrupt. The anisotropy radius \( r_\alpha \) sets the amount of anisotropy in the system, by including it in the same way as in Michie (1963) models: the larger it is, the less radially anisotropic is the model, and when \( r_\alpha \) is large with respect to the truncation radius \( r_i \), the model is everywhere isotropic. In this paper, we will often refer to the dimensionless anisotropy radius \( \hat{r}_\alpha \), defined as the ratio of the anisotropy radius to the scale radius.

The models are solved in dimensionless units (for a definition, see Section 2.1.2 of Gieles & Zocchi 2015). To describe every property of the model in the desired set of units, it is necessary to define the velocity, radial, and mass scales. These scales are related through the gravitational constant \( G \), so that it is enough to specify two scales to completely determine the set of units to use. We consider a mass scale and a radial scale, as these are intuitive quantities to use when fitting the models to data. In particular, these scales are adopted to define the total mass of the cluster, \( M \), and the half-mass radius, \( r_\text{h} \).

To include multiple mass components, several additional parameters are needed. Each component is defined by setting the value of the mean mass of the stars it describes, \( m_j \), and the value of their total mass, \( M_j \). In this paper, we consider only two components, one

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2The LIMEPY (Lowered Isothermal Model Explorer in PYthon) code is available from https://github.com/mgieles/limepy.

3To further clarify the role of this parameter, we point out that for isotropic models, by setting \( g = 0, 1 \) and 2, we respectively obtain the Woolley (1954), King (1966) and (isotropic, non-rotating) Wilson (1975) models, which have all been used to describe globular clusters.
accounting for visible stars and low-mass remnants ($j = 1$), and the other for a population of black holes ($j = 2$); these components are set up by specifying the values of two dimensionless parameters. The first parameter represents the ratio between the mean mass of the dark and visible component, $f_{2,1} = m_2/m_1$, and it is used to determine the mean mass of the dark component as $m_2 = m_1 \times f_{2,1}$. In order to have an estimate of the mean mass of each component expressed in solar masses, we assume $m_1 = 0.3 M_\odot$. However, the value assumed for $m_1$ has no role in the calculation of the model, and can be easily changed to any other value without affecting the fitting results. The total mass of each component is expressed with respect to the total mass of the cluster: $F_1 = M_1/M$. Because $F_1 + F_2 = 1$ and $M$ is defined as one of the two scale parameters (see above), $F_2$ is the second parameter needed to set up the mass function of the models.

The models have two additional parameters, $\delta$ and $\eta$, which set the mass dependence of the velocity scale $s_j$ and of the anisotropy radius of each component $r_{a,j}$ (in equation 2) with respect to their global values $s$ and $r_a$:

\[ s_j = s \left( \frac{m_j}{\bar{m}} \right)^{-\delta}, \]
\[ r_{a,j} = r_a \left( \frac{m_j}{\bar{m}} \right)^{\eta}, \]

where $\bar{m}$ is the mean mass of the stars in the system. We note that our choice for $\bar{m}$ is different from the one proposed by Da Costa & Freeman (1976), Gunn & Griffin (1979), and Gieles & Zocchi (2015), where $\bar{m}$ equals the central density weighted mean mass. Peuten et al. (2017) used the same definition used here, with the mean mass calculated simply as the mean mass of all the stars in the model, without any additional weight. In the following, we indicate with $W_0$ the concentration parameter computed by using a global mean mass for the stars, while the alternative parameter $W_0^*$ is obtained when considering a central density weighted mass for the objects in the cluster. The mass segregation parameter $\delta$ sets the dependence of the velocity scale $s_j$ of each component on the mean mass of its stars. A positive value of this parameter means that more massive stars have smaller velocity scales. Based on the comparison of the LIMEPY models with numerical simulations of clusters with black holes presented by Peuten et al. (2017), we set the value of this parameter to $\delta = 0.35$; in particular, we note that this value is appropriate for clusters that still contain a large population of BHs. The anisotropy parameter $\eta$ allows to modify the anisotropy for the different components. Here, we do not explore the role of this parameter, and we simply fix its value to $\eta = 0$, consistent with what was found in the numerical simulations of Peuten et al. (2017) for relatively unevolved systems, which correspond roughly to the dynamical age we estimated for $\omega$ Cen. We notice that the choice of $\eta = 0$ does not imply that the different mass components have the same anisotropy.

We notice that the Spitzer (1969) criterion (equation 1) can be expressed with our parameters as:

\[ \frac{F_2}{1 - F_2} < 0.16 f_{2,1}^{-3/2}. \]

When this criterion is not satisfied, equipartition in the cluster is impossible to achieve (Bianchini et al. 2016; Spera, Mapelli & Jeffries 2016). Almost all the models considered here violate this criterion, justifying our choice $\delta < 0.5$ (see also Peuten et al. 2017).

3 FITTING PROCEDURE AND RESULTS

Our goal is to show what the effect is of the presence of a population of heavy remnants on the observable quantities, and, in particular, to show how this affects the velocity dispersion profile, which is the main observable used to infer the presence of IMBHs in globular clusters. All the observational quantities are compared with the profiles of the visible component of the models; the other component is never directly compared with data. In this section, we describe the fitting procedures we adopted.

We first carry out a two-step fit: the first step involves a fit of models with a given mass function to the surface brightness profile to determine the structural parameters and the scales, and the second step a fit determining the vertical scaling of the line-of-sight velocity dispersion profile, defined by means of the mass-to-light ratio. In our previous analysis (Zocchi et al. 2017) of $\omega$ Cen with anisotropic models, we decided to carry out a two-step fitting in order to follow a procedure as close as possible to the one used in analyses based on the Jeans equation (e.g. see Noyola et al. 2010; van der Marel & Anderson 2010; Watkins et al. 2013). Indeed, with the Jeans approach, the first step is a fit to the surface brightness profile, which is subsequently deprojected to obtain the 3d velocity distribution.

Then, a certain MIL and an anisotropy profile are chosen, and the Jeans equation is solved to obtain a 3d velocity dispersion, which is projected to be compared to the data; this second step is repeated until the models match the observed profiles. Here, we are using the same two-step fitting procedure (see Section 3.1) because it allows us to explore the dynamics of models with different amounts of BHs reproducing equally well the surface brightness profile of $\omega$ Cen, enabling thus a more direct comparison of models predicting different kinematics for the visible stars (see Section 3.1).

In addition, we also carry out a one-step fit to determine the best model to reproduce all the observational profiles available for this cluster: in this case, nine fitting parameters are determined at once by fitting the models to all the profiles (see Section 3.2).

We used the surface brightness profile and the line-of-sight and proper motions velocity dispersion profiles of $\omega$ Cen. For a detailed description of these profiles, we refer the reader to section 3 of Zocchi et al. (2017), as we use the same set of data for the present analysis. The surface brightness profile is composed of data from Trager, King & Djorgovski (1995) and Noyola et al. (2008); line-of-sight velocities of single stars are taken from Reijns et al. (2006) and Pancino et al. (2007); ground-based proper motions are from van Leeuwen et al. (2000), and HST data from Anderson & van der Marel (2010).

We carry out the fits by using emcee (Foreman-Mackey et al. 2013), a PYTHON implementation of Goodman and Weare’s affine invariant Markov chain Monte Carlo ensemble sampler.\(^4\)

3.1 Two-step fitting

In order to understand the effect of the presence of the dark population on the visible component, we carry out fits of models with different mass functions, by varying the values of the parameters $f_{2,1}$ and $F_2$. To do this, we select several values for $f_{2,1}$ and $F_2$ to explore a large range of possible scenarios. With the values chosen for these parameters, the mean mass of objects in the dark component is $3 \leq f_{2,1} \leq 30$ (this means that, when considering $m_1 = 0.3 M_\odot$, $m_2$ ranges from $0.9 M_\odot$ to $9 M_\odot$), and the total mass they account

\(^4\)EMCEE is available at https://github.com/dfm/emcee.
for ranges from 0.1 per cent to 10 per cent of the total mass of the cluster. We deliberately chose extreme values for the boundaries of the grid of values to fully probe the parameter space. The distance to ω Cen is fixed to 5 kpc, as in Zocchi et al. (2017). In order to determine the importance of remnants independently from radial anisotropy, in this section, we consider isotropic models.

As in Zocchi et al. (2017), we first determine the model structural parameters (\(W_0\) and \(g\)) and the scales (the luminosity \(L\), and the half-mass radius \(r_h\)) by fitting the models to the surface brightness profile alone: this ensures that the models we find are able to accurately represent the distribution of visible stars in the cluster. In this first step, we determine the best-fit values of the four fitting parameters by maximizing the log-likelihood function:

\[
\lambda \propto -\frac{\chi^2}{2},
\]

i.e. by minimizing the following quantity:

\[
\chi^2 = \sum_{i=1}^{N_{SB}} \frac{(\bar{S}_i - \lambda_{SB}(R_i))^2}{\delta S^2_i},
\]

where \(l_i\) and \(\delta l_i\) are the surface luminosity and luminosity error at the radial position \(R_i\) for each of the \(N_{SB}\) points in the surface brightness profile; \(\lambda_{SB}\) is the projected luminosity density of the visible component of the model, its shape determined by the values of all the fitting parameters. For the parameters, we adopt uniform priors over the following ranges: 1 < \(W_0\) < 30, 0.1 < \(g\) < 3.5, 0.1 < \(L\) < 50 in units of \(10^6\) \(L_\odot\), 0.1 < \(r_h\) < 50 in units of pc.

The best-fit value for each parameter is obtained as the median of the correspondent marginalized posterior probability distribution, and the errors correspond to the 16 and 84 per cent percentiles.

Then, in the second step, the mass-to-light ratio \(M/L\) is obtained by determining the scaling of the line-of-sight velocity dispersion profile, by minimizing the following quantity:

\[
\chi^2 = \sum_{i=1}^{N_{VDOS}} \frac{(\sigma_{los,i} - \sigma_{LOS,0})^2}{\delta\sigma_{los,i}^2},
\]

where \(\sigma_{los,i}\) and \(\delta\sigma_{los,i}\) are the line-of-sight velocity dispersion and its error at the position \(R_i\), for each of the \(N_{VDOS}\) points in the velocity dispersion profile; \(\sigma_{LOS}\) is the velocity dispersion profile of the model, projected along the line of sight and normalized with respect to its central value, and \(\delta\sigma_{LOS}\) is the vertical scaling needed to match the model to the data, depending on the value of the mass-to-light ratio \(M/L\).

The best-fit parameters obtained with the two-step fitting procedure are indicated in Table 1. Fig. 1 reproduces the surface brightness profile and the line-of-sight, radial and tangential proper motion velocity dispersion profiles of some of the considered models; each line in these figures represents a system with a certain mass function, different from the others, as indicated by the label in the top left-hand panel.

In particular, two sets of models are represented here: the blue solid lines represent the best-fit models obtained when considering \(F_2 = 5\) per cent, and the red dashed lines represent the best-fit models obtained when considering \(F_2 = 1\) per cent (i.e. \(m_2 = 1.5\) \(M_\odot\) when adopting \(m_1 = 0.3\) \(M_\odot\)). The set of red lines, therefore, can be used to inspect the effect of considering different values for the fraction of total mass in the dark component, while the set of blue lines shows the effect of assuming different values for the mean mass of objects in the dark component.

All the models reproduce the observed surface brightness profile equally well. We recall that only the line-of-sight velocity dispersion profiles are involved in the fit determining the mass-to-light ratio of the cluster. The kinematic profiles are always better described by models including a large fraction of dark remnants with large mass (darkest blue and red lines in the plot), because of their larger velocity dispersion in the centre. We point out that Fig. 1 shows that models with a very different mass function reproduce the surface brightness profile of the cluster equally well but are different from each other when considering the velocity dispersion profiles: this is a clear indication of the need of kinematical data in order to truly assess the dynamics of these stellar systems and their composition.

### 3.2 One-step fitting

In this section, we include the parameters defining the mass function of the model \((f_2, 1)\) and \((F_2, 2)\) in a fit to all the observational profiles at the same time. Indeed, while the two-step procedure allows us to clearly illustrate variations in the kinematics caused by changes in the mean and total masses of BHs, this one-step procedure gives the values of the parameters that best describe all the profiles considered simultaneously. Moreover, we also fit on the distance \(d\), and on the dimensionless anisotropy radius \(r_a\), which sets the amount of anisotropy of the model, allowing us to explore possible degeneracy between radial anisotropy and stellar-mass BHs. We have a total of nine fitting parameters, and we determine their best-fit values by minimizing the following quantity:

\[
\chi^2 = \chi^2_{\Delta M} + \chi^2_{\Delta \sigma} + \chi^2_{\Delta f_2} + \chi^2_{\Delta r_a},
\]

where each of the terms on the right-hand side is in the form:

\[
\chi^2 = \sum_{i=1}^{N_S} \frac{(x_i - X_i(R_i))^2}{\delta x_i^2} + \sum_{i=1}^{N_{VDOS}} \frac{(\sigma_{los,i} - \sigma_{LOS,0})^2}{\delta\sigma_{los,i}^2},
\]

where \(x_i\) and \(\delta x_i\) represent the observational quantity and its error at the radial position \(R_i\), and \(X_i\) is the corresponding model profile for the visible component. The four terms appearing on the right-hand side of equation (12) correspond to the surface brightness profile, line-of-sight velocity dispersion profile, and radial and tangential proper motion velocity dispersion profiles, respectively.

For the nine fitting parameters, we adopt uniform priors over the following ranges: 1 < \(W_0\) < 30, 0.1 < \(g\) < 3.5, 0.1 < \(M\) < 50 in units of \(10^6\) \(M_\odot\), 0.1 < \(r_h\) < 50 in units of pc, \(-3 < \log F_2 < -0.9, 2 < f_2 < 15, 1 < M/L < 5\) in solar units, \(1 < d < 10\) in units of kpc, \(-4 < \log r_a < 1.3\) (we consider \(\log F_2\) and \(\log r_a\) as fitting parameters instead of \(F_2\) and \(f_2\) to have an uninformative prior, because they can span several orders of magnitude).

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5Because the model profiles are defined in terms of masses and not luminosities, here we consider \(M/L = 1\) to perform the fit; when the best-fit value of \(M/L\) is then recovered from the second step in the fitting procedure, the value of \(L\) is updated accordingly.
We also carry out a fit to determine what is the best isotropic model to fit the data. In this case, we only have eight parameters ($r_0$ is not required).

Fig. 2 shows the surface brightness, line-of-sight velocity dispersion, and radial and tangential proper motion velocity dispersion profiles of ω Cen. In these plots, the black solid lines represent the anisotropic best-fit model, the dashed blue lines the isotropic one. The best-fit parameters obtained with the one-step fitting procedure for the isotropic and anisotropic models are indicated in Table 2. In the table, we also indicate the errors on the parameters, which, in some cases, appear to be quite large: this is probably due to the large number of parameters we consider in this fit, and to the large errors on the data. Another reason for the large errors is the fact that we consider as fitting parameters $f_{z1}$ and $f_{z2}$: because they have a very important role in determining the shape of the model profiles, by changing them slightly a large spread is obtained in the values of $W_0$ in order to reproduce the observed profiles.

To illustrate how different the definition of the concentration parameter is in the case of multiple components with respect to the single-component case, we also include in Table 2 (as well as in Table 1) the values of this parameter obtained when considering a different definition for the mean mass of the stars in the system (see Section 2.2). By inspecting the tables, it is clear that the best-fit values of $W_0$ are smaller than the ones generally obtained with King models for this cluster, while the values of its alternative definition, $W_0^∗$, are much larger. When considering King (1966) models, large values of concentration indicate a core-collapsed cluster, but for the multimass models we consider here this is not to be true, and, in general, it is not trivial to have a general criterion to indicate whether a cluster is core-collapsed or not.

We notice that the best-fit values of the total mass and of the half-mass radius obtained with these two models are consistent with each other (and with those of best-fit models obtained with the two-step procedure). The distance obtained for the isotropic model is very close to the one assumed in the two-step fitting procedure, while the one inferred with the anisotropic model is a bit larger, but they are all consistent within 1σ.

The best-fit anisotropic model reproduces the observed profiles better than the isotropic one, suggesting that, as expected, anisotropic models are more indicated to describe ω Cen. This conclusion is supported by Fig. 3, which reproduces the anisotropy profiles (calculated as the ratio of tangential to radial proper motions velocity dispersion profiles, $\sigma_t/\sigma_r$; $\sigma_t/\sigma_r < 1$ indicates radial anisotropy, $\sigma_t/\sigma_r > 1$ indicates tangential anisotropy, and $\sigma_t/\sigma_r = 1$ indicates isotropy) of the best-fit models obtained with the one-step fitting procedure in this paper for multimass models and in Zocchi et al. (2017) for single-mass models. In this plot, the dashed green and solid blue lines indicate the single-mass and multimass isotropic best-fit models, and the dashed red and solid black lines the anisotropic single-mass and multimass best-fit models. Anisotropic models better reproduce the shape of the observed profile (especially the HST data) with respect to isotropic models. A discrepancy is seen between the models and the ground-based anisotropy data at large distances from the centre, but the large
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Figure 1. From top left, proceeding clockwise: surface brightness profile, line-of-sight velocity dispersion profile, tangential and radial proper motion velocity dispersion profiles for ω Cen. Red dashed lines represent the best-fit models obtained when considering $f_{2,1} = 5$ (i.e. $m_2 = 1.5 \, M_\odot$), and different values of $F_2$; blue lines represent the best-fit models obtained when considering $F_2 = 5$ per cent, and different values of $f_{2,1}$ (see labels and Table 1). The surface brightness profile is from Trager et al. (1995) and Noyola et al. (2008). The line-of-sight velocity dispersion is calculated from velocities by Pancino et al. (2007) and Reijns et al. (2006). The proper motions velocity dispersion profiles are calculated from data by van Leeuwen et al. (2000) and Anderson & van der Marel (2010).

scatter of these data prevents us from drawing any firm conclusion from this. With the forthcoming Gaia proper motions data it will be possible to extend the profile currently available to even larger radii, up to the edge of the cluster, and to investigate this further. If the tendency towards tangential anisotropy will be confirmed, different models will need to be considered in order to reproduce the profile (such as, for example, those by Varri & Bertin 2012).

For the anisotropic best-fit model, we compute the anisotropy profiles for the two components, to understand how radial anisotropy is distributed in each component. The anisotropy profile for the dark component has a deeper minimum (i.e. it is more radially anisotropic), $\min (\sigma_T/\sigma_R) \sim 0.4$, than the visible component, $\min (\sigma_T/\sigma_R) \sim 0.7$ (see black line in Fig. 3). However, the BHs are more concentrated in the innermost part of the cluster, in a region where these profiles are similar to each other, and where their value is $\sigma_T/\sigma_R \sim 1$, which indicates isotropy. Therefore, the invisible component is not characterized by strong radial anisotropy. This is confirmed by computing the anisotropy parameter $\kappa = 2K_r/K_t$, defined as the ratio between the radial and tangential components of the kinetic energy (Polyachenko & Shukhman 1981; Fridman et al. 1984): $\kappa > 1$ for radially anisotropic systems, $\kappa < 1$ for tangentially anisotropic systems, and $\kappa = 1$ for isotropic systems. The value of this parameter for the system as a whole is given in Table 2; when considering each component separately, we obtain $\kappa_1 = 1.12$, and $\kappa_2 = 1.06$, confirming that the light stars are more anisotropic.

In the top right panel of Fig. 2 we also show the velocity dispersion profile calculated from integrated spectra obtained by Noyola et al. (2010) in the inner region of the cluster. The black dots reproduce the profile provided by Noyola et al. (2010) when considering their kinematical centre, the green square the profile obtained when considering the centre by Noyola et al. (2008), and the red pentagons the one with the centre by Anderson & van der Marel (2010). In addition, we overplot the velocity dispersion profile recently calculated from data obtained with MUSE observations by Kamann et al. (2018); this profile is represented here with yellow triangles. By inspecting the figure we see that, even though the best-fit models have been calculated without using these data, the best-fit two-component models obtained here can partially reproduce their behaviour; in particular, the Kamann et al. (2018) profile is well represented by our best-fit models, with the only exception of the innermost data point, which is $\sim 2\sigma$ away from our models. The MUSE data was kindly made available to us by Sebastian Kamann and the first data point in the velocity profile is sensitive to the selection criteria of the stars used to compute it. In Kamann et al. (2018) the first data point is computed by including also the stars that were observed only once; by
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Figure 2. From top left, proceeding clockwise: surface brightness profile, line-of-sight velocity dispersion profile, tangential and radial proper motion velocity dispersion profiles for $\omega$ Cen. Solid black lines and dashed blue lines reproduce respectively the radial profiles of the anisotropic and isotropic best-fit model obtained with the one-step fitting procedure. The shaded and dashed areas represent respectively the anisotropic and isotropic models that occupy a 1$\sigma$ region around the maximum likelihood, as identified by EMCEE. The data profiles are the same as in Fig. 1. In addition, in the top right-hand panel, we also show the velocity dispersion profiles calculated from integrated spectra: the black dots reproduce the profile provided by Noyola et al. (2010) when considering their kinematical centre, the green squares the profile they obtained when considering the centre by Noyola, Gebhardt & Bergmann (2008), and the red pentagons the one with the centre by Anderson & van der Marel (2010). Moreover, the yellow triangles reproduce the profile by Kamann et al. (2018), derived from MUSE data.

4 DISCUSSION

4.1 Central line-of-sight velocity dispersion

Among the observational features that can be linked to the presence of an IMBH in the centre of globular clusters, one of the most widely sought-after is a rise in the line-of-sight velocity dispersion profile towards the centre. Zocchi et al. (2017) showed that the increase of the velocity dispersion towards the centre of the cluster can be partially accounted for by the presence of radial anisotropy in the system, therefore limiting the room for the presence of a massive IMBH.

Here, we explore the effect of the presence of a centrally concentrated population of dark remnants on this observable. In globular clusters, two-body encounters bring the systems towards a state of partial energy equipartition (Spitzer 1987; Trenti & van der Marel 2013; Bianchini et al. 2016; Peute et al. 2017): massive stars tend to lose kinetic energy in the encounters, and sink in the centre of the cluster, while low-mass stars gain kinetic energy and move towards the outer parts. This process induces mass segregation and causes the system to have mass-dependent kinematics, with fast low-mass stars and slow massive stars. Therefore, in a globular cluster containing a large number of remnants, we expect to observe a larger velocity dispersion for visible stars, with respect to the one we would measure in a cluster in which the red giant stars are the most massive ones. We investigate the magnitude of this effect by using the results of the fits on $\omega$ Cen.

Fig. 4 shows the values of the central line-of-sight velocity dispersion $\sigma_0$ obtained for the visible component for each model as a function of the mean mass of BHs. Coloured circles correspond to the values found for the isotropic models obtained with the two-step fitting procedure described in Section 3.1 (see also Table 1 for a full

excluding those and by determining the velocity dispersion of the 100 stars nearest to the centre and having a probability of being variable lower than 0.8, we obtained $\sigma(R = 3.2'') = 20.36^{+1.67}_{-1.01}$ km/s.
The effect of stellar-mass black holes on the central kinematics of ω Cen

Table 2. Best-fit parameters for ω Cen, obtained with the one-step fitting procedure. The columns refer to the anisotropic and isotropic models. For each model, we provide the values of the concentration parameter $W_0$ and of its alternative definition $W_0^*$, the truncation parameter $g$, the mass $M$ in units of $10^6 \, M_\odot$, the half-mass radius $r_h$ in units of pc, the fractional mass of the cluster contained in the dark component $F_2$, the fractional mean mass of the dark to visible components $f_2,1$, the mass-to-light ratio M/L in solar units, the distance $d$ in kpc, the dimensionless anisotropy radius $\kappa$, and the anisotropy parameter $\chi$. The uncertainties are indicated for all the fitting parameters. The last four lines of the table list the values of the reduced chi-squared for the various parts of the fit introduced in equations (12) and (13).

<table>
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<tr>
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<th>Anisotropic</th>
<th>Isotropic</th>
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<tr>
<td>$W_0$</td>
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<td>$3.64^{+0.74}_{-0.72}$</td>
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<td>$W_0^*$</td>
<td>$9.55^{+1.10}_{-0.23}$</td>
<td>$8.66^{+2.81}_{-1.40}$</td>
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<td>$g$</td>
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<td>$2.020^{+0.33}_{-0.26}$</td>
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<tr>
<td>$M$</td>
<td>$3.01^{+0.49}_{-0.39}$</td>
<td>$2.91^{+0.49}_{-0.44}$</td>
</tr>
<tr>
<td>$r_h$</td>
<td>$8.52^{+0.61}_{-0.62}$</td>
<td>$8.28^{+0.62}_{-0.63}$</td>
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<tr>
<td>$F_2$</td>
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<td>$0.052^{+0.029}_{-0.031}$</td>
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<td>$7.92^{+1.45}_{-2.12}$</td>
</tr>
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<td>M/L</td>
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<td>$2.59^{+0.34}_{-0.27}$</td>
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<tr>
<td>$d$</td>
<td>$5.14^{+0.25}_{-0.24}$</td>
<td>$5.01^{+0.24}_{-0.24}$</td>
</tr>
<tr>
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</tr>
<tr>
<td>$\chi_{SB}$</td>
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<tr>
<td>$\chi_{FM,T}$</td>
<td>$4.00$</td>
<td>$5.49$</td>
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Figure 3. Anisotropy profile $\sigma_1/\sigma_2$ of ω Cen, calculated as the ratio of the tangential to radial components of the proper motions velocity dispersion profiles. Black dots represent the anisotropy calculated by HST data from Anderson & van der Marel (2010), white circles the anisotropy calculated by ground-based data from van Leeuwen et al. (2000). The dashed green and red lines indicate the isotropic and anisotropic single-mass best-fit models obtained by Zocchi et al. (2017); the solid blue and black lines represent the isotropic and anisotropic multimass best-fit models described in Section 3.2. The shaded and dashed areas represent, respectively, the anisotropic multimass and single-mass models that occupy a 1σ region around the maximum likelihood, as identified by EMCEE.

Figure 4. Central line-of-sight velocity dispersion as a function of the fraction of mean mass of stars in the dark component to mean mass of stars in the visible component, $f_{2,1}$; the mean mass of stars in the dark component, $m_2$, is also indicated in the top, as obtained when assuming $m_1 = 0.3 \, M_\odot$. Coloured circles correspond to the values found for the two-steps fitting procedure, for the isotropic models listed in Table 1; each colour indicates a different value of the fraction of the total mass of the cluster contained in the dark component, $F_2$, as indicated by the label. The black square and the black star correspond to the values found for the one-step fit described in Section 3.2 for isotropic and anisotropic models, respectively. The dashed line marks the value of $\sigma_0$ obtained in Zocchi et al. (2017), and the shaded grey area represents the error on this value.

In Fig. 4, we also show the values found for the one-step fit (see Section 3.2) for isotropic and anisotropic models, indicated with the black square and the black star, respectively. The dashed line marks the value of $\sigma_0$ obtained in Zocchi et al. (2017), and the shaded grey area represents the error on this value. From the plot, we see that the largest value of $\sigma_{0,1}$ is obtained, for isotropic models, when considering the presence of a very large population of massive dark remnants ($F_2 = 10$ per cent and $f_{2,1} = 30$, i.e. $m_2 = 9 \, M_\odot$ when assuming $m_1 = 0.3 \, M_\odot$). Zocchi et al. (2017) showed that a similar value is reached for the most radially anisotropic model without mass segregation they consider ($\kappa = 1.3$, see their Fig. 7). However, when adopting the one-step fitting procedure and allowing the models to be both radially anisotropic and mass segregated, it is possible to obtain the same value of $\sigma_{0,1} \sim 18.6 \, \text{km} \, \text{s}^{-1}$ with a smaller population of remnants ($F_2 = 4.5$ per cent), and with a less extreme degree of anisotropy ($\kappa = 1.13$).
4.2 Comparison with previous works

In Table 3, we list the values obtained with different models for the mass, mass-to-light ratio, and distance of ω Cen; we compare the results in the literature with those we present here. The values of the mass and mass-to-light ratio we obtain for ω Cen are compatible within 2σ with all the previous estimates, except for those proposed by Meylan et al. (1995). As for the distance, our estimate is larger than those by Watkins et al. (2013) and Bianchini et al. (2013), but it is compatible with all the others within 2σ.

The only other work in the literature adopting dynamical models with two mass components (one visible, describing stars, and the other invisible, describing remnants) to reproduce this cluster is the one by de Vita, Bertin & Zocchi (2016). The authors impose a value of f2,1 = 3 and F2 = 0.33 to set up the models, and they find a best-fit total mass for invisible component of $7.5 \times 10^4 \, M_\odot$. In this work, we find a mass of $1.35 \times 10^5 \, M_\odot$ for the invisible component ($F_2 \sim 4.5$ per cent). Even though the mass function of these works is different, the total mass obtained for the cluster is remarkably similar, and the value of the mass-to-light ratio is compatible within 2σ. An additional comparison is possible with the work presented by de Vita et al. (2016), as they present the mass-to-light ratio radial profile of their best-fit models (see the right-hand panel of their Fig. 12). The profile they obtained for models having an invisible heavy component decreases from $M/L \sim 2.8$ in the centre to $M/L \gtrsim 2$ at about 30 pc from the centre. The mass-to-light ratio profile of our anisotropic best-fit model is also decreasing, but more steeply: we find $M/L \sim 4.5$ in the centre and $M/L \sim 2.5$ at about 7 pc from the centre; interestingly, we find the same behaviour also for our isotropic best-fit model. The difference in the values of $M/L$ that we find here with respect to those by de Vita et al. (2016) is in line with the difference among the global values of $M/L$ listed in Table 3.

Arca-Sedda (2016) proposed an analysis of numerical simulations showing that the excess of mass in the centre of a cluster could be due to the presence of a subsystem of heavy remnants orbitally segregated, and not to an IMBH. In particular, for the globular cluster ω Cen they estimate a mass of $(1.45 \pm 0.03) \times 10^4 \, M_\odot$ for the central component of massive remnants, assuming a total mass of $2.5 \times 10^5 \, M_\odot$ for the cluster. Our models predict a larger value for the mass of the dark component, but in our case this is not completely segregated in the centre, extending up to about the half-mass radius. We note that with our choice of δ for the models, motivated by N-body models (Peuten et al. 2017), the distribution of the massive objects is not a choice, but is constrained by the definition of the distribution function, whereas with other methods there is no constraint in this regard. It is however interesting to note that for the dark component in our best-fit models (see Table 2) the mass contained within the central 0.2 pc equals $1.4 \times 10^3 \, M_\odot$, in agreement with the estimate by Arca-Sedda (2016).

4.3 Implications on the presence of an IMBH

The presence of a central IMBH is accounted for by the analyses carried out by van der Marel & Anderson (2010) and Baumgardt (2017). van der Marel & Anderson (2010) find an upper limit to the presence of an IMBH in the centre of ω Cen of $<1.2 \times 10^4 \, M_\odot$, which corresponds to 0.4 per cent of the total mass they estimate for the cluster. The best-fit model proposed by Baumgardt (2017) includes an IMBH amounting to $4.1 \times 10^4 \, M_\odot$, i.e. $\sim 1.4$ per cent of the mass of the cluster. The invisible mass accounted for by these objects is smaller than the one we find for the population of BHs, but much more concentrated.

Fig. 5 shows a comparison between the best-fit models obtained here and some models proposed in the literature including a central IMBH. Even though these models were obtained by fitting to different data, it is interesting to compare them, because they are all describing ω Cen. The blue solid line in the figure represents the best-fit model by Baumgardt (2017), which includes a central IMBH of mass $4.1 \times 10^4 \, M_\odot$; this model has been obtained by comparing a suite of N-body simulations to the observed profiles of the cluster, and it is shown to provide a good fit to the data. In their Fig. 7, van der Marel & Anderson (2010) show several models for ω Cen, and we reproduce three of these in Fig. 5, considering only the ones obtained by including the presence of a cusp in the density profile of the cluster: the red long-dashed line is the best-fit isotropic model including an IMBH of $4 \times 10^4 \, M_\odot$, as reported by Noyola et al. (2008); the orange dot-dashed line is the isotropic model including an IMBH of mass $1.8 \times 10^4 \, M_\odot$, and the green dashed line the anisotropic model including an IMBH with mass $8.7 \times 10^4 \, M_\odot$.

By comparing these models with the ones proposed here, and reproduced in the background of Fig. 5, we see that a discrepancy is visible in the innermost region of the cluster. The isotropic model by van der Marel & Anderson (2010), indicated with the dot-dashed orange line in the figure, is above the 1σ region of our best-fit two-components models only within $\sim 1$″ from the centre, the profile by Baumgardt (2017) is above the 1σ region within $\sim 3$″ from the centre: it is remarkable that our models, which do not include an IMBH, produce a projected velocity dispersion profile that is indeed very similar to these ones, except for the innermost region, where data are not available. This is an illustration of the partial degeneracy between the signatures produced by an IMBH and by a population of centrally concentrated BHs, and suggests that to firmly assess whether an IMBH is indeed hosted in this system, more data are necessary in the very centre of the cluster.

A larger discrepancy is found when considering the model including the IMBH as suggested by Noyola et al. (2008), which appears to be above the 1σ region within $\sim 8$″ from the cluster centre. We point out that, however, this model accounts for a mass of the central IMBH which is basically the same as the model by Baumgardt (2017), even though the respective profiles look different. Another discrepancy is visible in the intermediate part of the cluster, between $\sim 30$ and 200″, where the models from the literature appear to be below our best-fit models (but still within the 1σ region of the isotropic model we presented). This is probably due to the different set of data we considered in the fitting procedure.

5 CONCLUSIONS

One of the expected signatures of the presence of an IMBH in the centre of globular clusters is a central cusp in the velocity dispersion profiles (Noyola et al. 2010; Anderson & van der Marel 2010), and a general increase of the projected velocity dispersion over a region of about an order of magnitude larger than the radius of influence of the IMBH (Baumgardt et al. 2004). A similar feature, however, is also obtained in radially anisotropic stellar systems or in systems having a population of dark heavy remnants. We explored the effect of the first of these alternatives in a previous work (Zocchi et al. 2017), and here we investigated the second.

Stellar-mass BH candidates have been detected in globular clusters (Strader et al. 2012; Chomiuk et al. 2013; Miller-Jones et al. 2015). From a theoretical point of view, they are also expected to be found in these systems (Breen & Heggie 2013; Sippel & Hurley 2013; Morscher et al. 2015). For many aspects, the effect of
In particular, their presence quenches mass segregation among the visible stars (Peuten et al. 2016; Gill et al. 2008), and clusters containing these objects are expected to have a large core (Heggie et al. 2007; Peuten et al. 2017). Moreover, their presence also affects the central velocity dispersion, causing it to be larger than in systems where they do not play a role. Therefore, it is necessary to understand the role of a population of BHs in shaping the dynamics of visible stars, before being able to determine whether or not an IMBH is present in the centre of these systems.

Here, we explore this issue by using \( \omega \) Cen as a test case. We describe this cluster by means of LIMEPY dynamical models (Gieles & Zocchi 2015) with two mass components: a low-mass component representing the stars and low-mass stellar remnants (white dwarfs and neutron stars) and a high-mass component representing a population of BHs segregated towards the centre. BHs are assumed to be on average more massive than the visible stars, but their total mass is smaller than that of stars. We compare observational profiles to those predicted by the models for the visible component: the dark component has no direct role in the comparison to observations, but its presence influences the dynamics and modifies the shape of these kinematic and structural profiles.

In order to explore this, we carried out a two-step fitting procedure by considering models with a given mass function, with the values of the mean and total mass of stars in each component chosen to fully explore the parameter space. The first step consists in a fit to the surface brightness profile of \( \omega \) Cen as a test case. We describe this cluster by means of LIMEPY dynamical models (Gieles & Zocchi 2015) with two mass components: a low-mass component representing the stars and low-mass stellar remnants (white dwarfs and neutron stars) and a high-mass component representing a population of BHs segregated towards the centre. BHs are assumed to be on average more massive than the visible stars, but their total mass is smaller than that of stars. We compare observational profiles to those predicted by the models for the visible component: the dark component has no direct role in the comparison to observations, but its presence influences the dynamics and modifies the shape of these kinematic and structural profiles.

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to the projected anisotropy profile measured by proper motions (see Fig. 3).

The innermost part of the line-of-sight velocity dispersion profile (Noyola et al. 2010) has been used to claim the presence of an IMBH in the centre of this cluster. The best-fit models we obtained with the one-step fitting procedure (and also some of those obtained with the two-step procedure, when considering a large population of heavy BHs) are partially able to reproduce this behaviour. Particularly interesting is the fact that anisotropic single-mass models and isotropic multimass models predict a very similar value for the central velocity dispersion; when combining anisotropy and multiple mass components, again, it is possible to obtain the same value for $\sigma_{0,1}$, but with less extreme mass functions and milder anisotropy. The discrepancy between these best-fit models and the central cusp prevents us from excluding the presence of a central IMBH, but significantly reduces the expected mass, with respect to the one predicted when using single-mass isotropic models (see also Zocchi et al. 2017). We are currently developing a new version of the models proposed here, including the presence of a central IMBH, in order to provide a global description of the dynamics of the stars in GCs, and to estimate the mass of IMBHs that could reside in their centre.

Upcoming measurements of proper motions by the Gaia mission and measurements of line-of-sight velocities by ground-based facilities will soon enable us to study the kinematics of many Galactic globular clusters in great detail and up to their outermost regions, which are currently not explored because data are not available (for $\omega$ Cen, for example, Gaia data will provide proper motions of stars located beyond ~100 arcsec from the centre, thus complementing HST data). This will enable a more detailed exploration of the kinematics of stars in these systems, and will provide us with information on their invisible components. In particular, the expected errors on proper motions (in Gaia Data Release 2, proper motions for individual stars with $V \leq 18$ mag in $\omega$ Cen have errors $\lesssim 3$ km s$^{-1}$) guarantee that Gaia data will enable us to quantify anisotropy in the outer parts of Galactic globular clusters, lifting part of the degeneracy between anisotropy and heavy remnants.

Both radial anisotropy and the presence of a population of black holes have an important effect on the dynamics of clusters and on their observational properties. In order to provide an accurate estimate for the mass of a central IMBH, it is therefore crucial to take these ingredients into account.

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