The intergalactic magnetic field probed by a giant radio galaxy


(Affiliations can be found after the references)

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ABSTRACT

Cosmological simulations predict that an intergalactic magnetic field (IGMF) pervades the large scale structure (LSS) of the Universe. Measuring the IGMF is important to determine its origin (i.e. primordial or otherwise). Using data from the LOFAR Two Metre Sky Survey (LoTSS), we present the Faraday rotation measure (RM) and depolarisation properties of the giant radio galaxy J1235+5317, at a redshift of $z = 0.34$ and $3.38$ Mpc in size. We find a mean RM difference between the lobes of $2.5 \pm 0.1$ rad m$^{-2}$, in addition to small scale RM variations of $\sim 0.1$ rad m$^{-2}$. From a catalogue of LSS filaments based on optical spectroscopic observations in the local universe, we find an excess of filaments intersecting the line of sight to only one of the lobes. Associating the entire RM difference to these LSS filaments leads to a gas density-weighted IGMF strength of $\sim 0.3 \mu$G. However, direct comparison with cosmological simulations of the RM contribution from LSS filaments gives a low probability ($\sim 5\%$) for an RM contribution as large as $2.5$ rad m$^{-2}$, for the case of IGMF strengths of $10$ to $50$ nG. It is likely that variations in the RM from the Milky Way (on 11 scales) contribute significantly to the mean RM difference, and a denser RM grid is required to better constrain this contribution. In general, this work demonstrates the potential of the LOFAR telescope to probe the weak signature of the IGMF. Future studies, with thousands of sources of high quality RM data from LoTSS, will enable more stringent constraints on the nature of the IGMF.

Key words. radio continuum: galaxies – galaxies: magnetic fields – galaxies: active – galaxies: jets – techniques: polarimetric – galaxies: individual (J1235+5317)

1. Introduction

Diffuse gas is expected to permeate the large-scale structure (LSS) of the Universe away from galaxy groups and clusters. Detecting and characterising this intergalactic gas is challenging due to the expected low particle number density ($\sim 10^{-5}$ to $10^{-6}$ cm$^{-3}$) and temperature ($10^4$ to $10^7$ K). Although diffuse, this warm-hot intergalactic medium (WHIM) [Dave et al. 2001; Cen & Ostriker 2006] potentially contains half the total baryon content of the local Universe [Bregman 2007; Nicastro et al. 2018]. In addition, accretion shocks along these LSS filaments are predicted to accelerate particles to relativistic energies and to amplify magnetic fields. Thus, detecting this filamentary structure in synchrotron emission using radio telescopes is a promising avenue for studying the WHIM (e.g. Vazza et al. 2015a). Recent statistical studies based on the cross-correlation of diffuse radio synchrotron emission and the underlying galaxy distribution have derived upper limits on the magnetisation of filaments of the order of $0.1 \mu$G [Vernstrom et al. 2017; Brown et al. 2017]. Furthermore, Vacca et al. (2018) found a faint population of sources which might be the tip of the iceberg of a class of diffuse large-scale synchrotron sources associated with the WHIM connected to a large-scale filament of the cosmic web. An alternative approach is to measure the Faraday rotation properties of the magnetised WHIM using many bright, polarised, background radio sources (e.g. Stasyszyn et al. 2010; Akahori et al. 2014; Vacca et al. 2016).

From simulations, the field strength of the intergalactic magnetic field (IGMF) is expected to be in the range of 1 to 100 nG (e.g. Dolag et al. 1999; Brüggen et al. 2005; Ryu et al. 2008; Vazza et al. 2017a). It is important to constrain the magnetic field in the WHIM in order to determine the unknown origin of the large scale magnetic field in the Universe [Zweibel 2006]. While large scale fields are commonly detected in galaxies and galaxy clusters, the strong modification of these fields erases the signature of their origin (e.g. Vazza et al. 2015b). This may not be the case in the WHIM, as the amplification of primordial magnetic fields in these filamentary regions are likely primarily due to compressive and shearing gas motions, in addition to small-scale shocks, such that the observed level of magnetisation could be connected to the seeding process (e.g. Ryu et al. 2008; Vazza et al. 2014a). The AGN and star formation activity in galaxies can also drive powerful outflows that may significantly magnify the intergalactic medium on large scales (e.g. Furlanetto & Loeb 2001; Donnert et al. 2009; Beck et al. 2013). Therefore, distinguishing between a primordial origin and a later injection of magnetic field that was initially generated on smaller scales by galaxies and stars is a key goal for studies of the IGMF (see Akahori et al. 2018 and references therein).

It has also been proposed to study the WHIM using large or ‘giant’ radio galaxies (GRGs) whose linear size can extend beyond 1 Mpc, with the largest such example being 4.7 Mpc in extent (Machalski et al. 2008). GRGs are usually FRII type radio galaxies (e.g. Dabhade et al. 2017), although some giant FRI also exist (e.g. Heesen et al. 2018; Horellou et al. 2018), that extend well beyond their host galaxy and local environments, into the surrounding intergalactic medium. Asymmetries in the GRG morphology can be used as a probe of the ambient gas density (Subramanayan et al. 2008; Safouri et al. 2009; Pirya et al. 2012; Malarecki et al. 2015) and the Faraday rotation properties...
of the polarised emission from the lobes can be used to study the magnetic field properties of the surrounding gas on Mpc scales (Xu et al. 2006; O’Sullivan et al. 2018). Another potential approach to studying the magnetised WHIM in cluster outskirts is by using Faraday rotation observations of the highly polarised emission from radio relics (e.g. Kierdorf et al. 2017; Loi et al. 2017).

The effect of Faraday rotation is measured through its influence on the linear polarisation vector as a function of wavelength-squared. The observed Faraday rotation measure, \( RM \) [rad m\(^{-2}\)], depends on the line-of-sight magnetic field, \( B \) [\( \mu \)G], threading a region of ionised gas with electron density, \( n_e \) [cm\(^{-3}\)], along a path length, \( l \) [pc], following

\[
RM = 0.812 \int_{\text{source}} n_e B_\phi \, dl \text{ rad m}^{-2}. \tag{1}
\]

In this paper, we present an analysis of the linear polarisation and Faraday rotation properties of an FRII radio galaxy (J1235+5317) with a linear size of 3.4 Mpc. The observations were done with the Low Frequency Array (LOFAR; van Haarlem et al. 2013) which provides excellent sensitivity to diffuse extended structures due to the presence of numerous short base-line and exceptional Faraday rotation measure (RM) accuracy, which depends on the total coverage in wavelength-squared. While low frequency radio telescopes provide the best RM accuracy, the observed Faraday rotation measure, \( RM \), depends on the line-of-sight magnetic field, \( B \), threading a region of ionised gas with electron density, \( n_e \) [cm\(^{-3}\)], along a path length, \( l \) [pc], following

\[
RM = 0.812 \int_{\text{source}} n_e B_\phi \, dl \text{ rad m}^{-2}. \tag{1}
\]

The target source J1235+5317 was discovered to be polarised at 144 MHz by Van Eck et al. (2018), in LOFAR Two-Metre Sky Survey (LoTSS; Shimwell et al. 2017), which is observing the whole northern sky with the LOFAR High-Band Antenna (HBA) from 120 to 168 MHz. The data relevant to our target were observed in full polarisation for 8 hours on 26 June 2014, as part of the observing program LC2_038 and with a pointing centre of J2000 12\( ^{h}\)38\( ^{m}\)06.71, +52\( ^{\circ}\)07\( ^{\prime}\)19\( ^{\prime\prime}\). This gives a distance of \( \sim 1.26 \) of the target J1235+5317 from the pointing centre (the FWHM of the primary beam is \( \sim 4\)'). Direction-independent calibration was performed using the \texttt{prefactor} pipeline\(^1\) as described in detail in Shimwell et al. (2017) and de Gasperin et al. (2018), which includes the ionospheric RM correction using \texttt{RMextact}\(^2\). Residual ionospheric RM correction errors of \( \sim 0.05 \) rad m\(^{-2}\) are estimated between observations (Van Eck et al. 2018), while slightly larger errors of \( \sim 0.1 \) to 0.3 rad m\(^{-2}\) are estimated across a single 8-hour observation (Sotomayor-Beltran et al. 2013).

The resulting measurement set, after the \texttt{prefactor} pipeline, has a time resolution of 8 s and a frequency resolution of 97.6 kHz. The direction-independent calibrated data are used throughout for the polarisation and rotation measure analysis, while the direction-dependent calibrated total intensity image (Shimwell et al. 2018) is used to determine the source morphological properties with high precision and for the identification of the host galaxy location. Analysis of polarisation and rotation measure data products after direction-dependent calibration will be presented in future work.

2. Observations & Data Analysis

2.1. Radio observations

The target source J1235+5317 was observed as part of the LOFAR Two-Metre Sky Survey (LoTSS; Shimwell et al. 2017), which is observing the whole northern sky with the LOFAR High-Band Antenna (HBA) from 120 to 168 MHz. The data relevant to our target were observed in full polarisation for 8 hours on 26 June 2014, as part of the observing program LC2_038 and with a pointing centre of J2000 12\( ^{h}\)38\( ^{m}\)06.71, +52\( ^{\circ}\)07\( ^{\prime}\)19\( ^{\prime\prime}\). This gives a distance of \( \sim 1.26 \) of the target J1235+5317 from the pointing centre (the FWHM of the primary beam is \( \sim 4\)'). Direction-independent calibration was performed using the \texttt{prefactor} pipeline\(^1\) as described in detail in Shimwell et al. (2017) and de Gasperin et al. (2018), which includes the ionospheric RM correction using \texttt{RMextact}\(^2\). Residual ionospheric RM correction errors of \( \sim 0.05 \) rad m\(^{-2}\) are estimated between observations (Van Eck et al. 2018), while slightly larger errors of \( \sim 0.1 \) to 0.3 rad m\(^{-2}\) are estimated across a single 8-hour observation (Sotomayor-Beltran et al. 2013).

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2.2. Polarisation and Faraday rotation imaging

To analyse the polarisation and Faraday rotation properties of the target, we phase-shifted the calibrated uv-data to the coordinates of the host galaxy (12\( ^{h}\)35\( ^{m}\)01.5, +53\( ^{\circ}\)17\'55\"), which lies almost at the centre of the extended emission. We calibrated the data for short-timescale phase variations caused by the ionosphere, then averaged to 32 s to reduce the data size and to help speed up the subsequent imaging, while avoiding any significant time smearing (e.g. Neld et al. 2018). Both the phase-shifting and time-averaging were done using NDPPP (Van Diepen 2011\(^3\)).

\(^1\) https://github.com/lofar-astron/prefactor
\(^2\) https://github.com/lofar-astron/RMextact
\(^3\) https://support.astron.nl/LOFARImagingCookbook/
The imaging software **wscclean**\(^4\) was used to create \(I, Q, U, V\) channel images at 97.6 kHz resolution, for a 25' field of view (~twice the linear size of J1235+5317). A minimum uv-range of 150 \(\lambda\) was used to avoid sensitivity to Galactic polarised emission on scales of \(\geq 25'\). The maximum uv-range was set to 18 k\(\lambda\), and combined with a Briggs weighting of 0, resulted in a beam size of 26' x 18', sampled with 3' x 3' pixels. The differential beam correction per channel was applied using **wscclean**, as the correction for the LOFAR beam gain at the pointing centre was already applied during the initial calibration of the data. All channel images with \(Q\) or \(U\) noise higher than five times the average noise level were removed from subsequent analysis, leaving a total of 404 images covering 120 to 167 MHz (with a central frequency of 143.5 MHz).

**RM synthesis and rmclean**\(^5\)\(^5\)\(^\) were then applied to the \(Q\) and \(U\) images using **pyrmsynth**. The data have an RM resolution of 1.16 rad m\(^{-2}\), are sensitive to polarised emission from Faraday thick regions up to \(\sim 0.98\) rad m\(^{-2}\), and [RM] values for Faraday thin regions as high as 450 rad m\(^{-2}\) can be detected. An RM cube with a Faraday depth (\(\phi\)) axis covering \(\pm 500\) rad m\(^{-2}\) and sampled at 0.5 rad m\(^{-2}\) intervals was constructed for initial inspection of the data. The concept of Faraday depth (Burn 1966) can be useful to introduce here to describe regions with complicated distributions of Faraday rotation along the line of sight, such as multiple distinct regions of polarised emission experiencing different amounts of Faraday rotation, which could be identified through multiple peaks in a Faraday depth spectrum or Faraday dispersion function (FDF). As no significant emission was found at large Faraday depths, the final RM and polarisation images were constructed from FDFs with a range of \(\pm 150\) rad m\(^{-2}\), sampled at 0.15 rad m\(^{-2}\). To identify peaks in the FDF, a threshold of \(8\sigma_{\text{QU}}\) was used, where \(\sigma_{\text{QU}}\) is calculated from the outer 20% of the Faraday depth range in the \texttt{rmclean} \(Q\) and \(U\) spectra. The mean \(\sigma_{\text{QU}}\) across the field was \(\sim 90\) \(\mu\)Jy beam\(^{-1}\). Since no correction was made for the instrumental polarisation, peaks in the Faraday dispersion function appear near \(\phi \sim 0\) rad m\(^{-2}\) at a typical level of \(\sim 1.5\%\) of the Stokes \(I\) emission. This instrumental polarisation signal is also smeared out by the ionospheric RM correction making it difficult to identify real polarised emission at low Faraday depths (\(\leq 3\) rad m\(^{-2}\)). Thus, when identifying real polarised emission peaks in the FDF, the range \(\pm 3\) rad m\(^{-2}\) is excluded. RM and polarised intensity images are created from the brightest, real polarised peak above \(8\sigma_{\text{QU}}\) at each pixel, after fitting a parabola around the peak to obtain the best-fitting RM and polarised intensity. In the case of the polarised intensity image, a correction for the polarisation bias was also made following (George et al. 2012). The error in the RM at each pixel was calculated in the standard way as the RM resolution divided by twice the signal to noise ratio of the detection (Brentjens & de Bruyn 2005).

A full-band Stokes \(I\) image was made using the same image parameters as the channel images specified above, with multi-scale cleaning applied for an automatic threshold of \(3\sigma\) and deeper cleaning (to \(0.3\sigma\)) within an automatic masked region created from the clean components. The degree-of-polarisation image was created by dividing the band-averaged polarised intensity image from RM synthesis (with a cutoff at \(8\sigma_{\text{QU}}\)) by the full-band Stokes \(I\) image (with a cutoff at 3 times the local noise level).

\(^4\) https://sourceforge.net/projects/wscclean

\(^5\) https://github.com/mrbell/pyrmsynth

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**SDSS J123501.52+531755.0** was observed with the Nordic Optical Telescope on March 25 and March 26 2018 for a total integration time of 5400 sec. We used the Andalucia Faint Object Spectrograph and Camera (AIFOSC) and a 1.3 arcsec wide longslit and grism 4 with 300 rules per millimetre providing a spectral resolution of 280 and a useful spectral range of 3800 to 9100 Å. The slit was placed at a parallactic angle of 60 degrees east of north on both nights at the onset of integration. The airmass ranged from 1.20 to 1.15. The observing conditions were poor with a variable seeing above 2 arcsec and with passing
clouds. Despite this we clearly detected several emission lines (Figure 1) consistent with a mean redshift of 0.3448 ± 0.0003 (1-sigma error). The [O\textsc{ii}] and [O\textsc{iii}] images have a peculiar morphology extending away from the continuum source to the northern side of the galaxy. In particular [O\textsc{ii}], +5008 Å can be traced over 4 arcseconds below the continuum trace (20 kpc at $z = 0.34$). This indicates the presence of an extended emission line region.

3. Results

3.1. Radio morphology of J1235+5317

Figure 2 shows the total intensity image at 6″ resolution from the LoTSS direction-dependent calibrated data (Shimwell et al. 2018). This provides the best radio image to date for this source, enabling an unambiguous host galaxy identification with SDSS J123501.52+531755.0. The noise level in the image ranges from $\sim 70 \mu$Jy beam$^{-1}$ in areas away from bright sources to $\sim 100 \mu$Jy beam$^{-1}$ near the hotspots/lobes.

The core of this FRII radio galaxy, located at J2000 12$^h$35$^m$01$^s$.53$^s$+53$^\circ$17′.55″, has an integrated flux density of $\sim$1.1 mJy at 144 MHz and 1.4 GHz (FIRST; Becker et al. 1995) suggesting a flat spectrum. However, the core is also detected in the VLASS Quick-Look (QL) image at 3 GHz ($\sim$2.9 mJy) and the 9C catalogue (Waldram et al. 2010) at 15 GHz ($\sim$4 mJy) indicating an inverted spectral index of $\alpha_{core} \approx +0.3$ when combined with the LoTSS core flux density. As the LoTSS, VLASS and 9C observations are closest in time, we consider the core to have an inverted spectral index, with time variability explaining the lower than expected flux density from FIRST at 1.4 GHz. There is also a faint hint of a jet connecting the host with the south-east (SE) lobe. If this is real, then it suggests that the SE jet and lobe are oriented slightly towards us on the sky.

Using the 3σ contour to define the lobe edges, we find the lobes have a width of $\sim 83^\prime$ and $\sim 94^\prime$, giving an axial ratio of $\sim 4.4$ for the north-west (NW) lobe and $\sim 3.3$ for the SE lobe, respectively. This is consistent with the typical axial ratios from 2 to 7 for the lobes of most (smaller) FRGs (e.g. Machalski et al. 2006). In Table 1 we compile the integrated flux densities of the NW and SE lobes and hotspots from both current and archival data. The integrated flux densities of the NW lobe and hotspot are slightly higher than the SE lobe and hotspot at 144 MHz, with both having spectral index values of $\alpha_{lobe} \sim -0.8$. The NW hotspot is resolved into primary and secondary hotspot regions in the VLASS at 3 GHz (2.4″×2.1″ beam), while the SE hotspot maintains a single component.

The straight-line distance from the core to the NW hotspot is $\sim 365′$ (1.84 Mpc), compared to $\sim 311′$ (1.56 Mpc) from the core to the SE hotspot, giving a lobe length ratio of 1.17. The inferred jet-misalignment (from co-linearity) of $\sim 13.6^\circ$ is most likely due to bending of the NW and/or SE jets on large scales, as is sometimes observed in other FRII radio sources (Blair et al. 1992). We expect that the lobe-length asymmetry and jet-misalignment are caused by interactions between the jet and the external environment on large scales, as opposed to light travel time effects (Longair & Riley 1979). Asymmetries in the jet and lobe lengths of FRGs are often attributed to interactions with the large scale structure environment (Pirya et al. 2012 Malarecki et al. 2015). The advancing NW jet may be influenced by a nearby filament (see Section 4.4.1 and the filament in the $z \sim 0.335$ slice), although deeper optical spectroscopic observations would be required to determine whether or not this filament is indeed close enough in redshift to that of the host galaxy to have an influence.

3.2. Faraday rotation measure distribution

Figure 3 shows the RM distribution for J1235+5317, using an $8\sigma_{RM}$ threshold, overlaid by Stokes I contours at the same angular resolution. The Faraday dispersion functions for the brightest pixel in polarised intensity in each lobe are also shown, with a red cross marking the peak polarisation at which the RM was found. Other peaks in the spectrum are either noise peaks or related to the instrumental polarisation near RM $\sim 0$ rad m$^{-2}$. The RM distributions of each lobe are shown in Figure 4. The mean and standard deviation of the RM are $+7.42$ rad m$^{-2}$ and 0.07 rad m$^{-2}$ for the NW lobe, and $+9.92$ rad m$^{-2}$ and 0.11 rad m$^{-2}$ for the SE lobe, respectively. The median RM errors for the NW and SE lobe regions are 0.04 rad m$^{-2}$ and 0.06 rad m$^{-2}$. The mean RM difference between the lobes of 2.5 ± 0.1 rad m$^{-2}$ is thus highly significant. At the angular separation of the lobes (11′), systematic errors in the ionospheric RM correction would affect both lobes equally and thus do not contribute to the RM difference between the lobes. We can estimate the significance of the small RM variations within each lobe accounting for the number of pixels in each synthesised beam following Leahy et al. (1986), where a reduced-chi-squared of $\sim 1$ is expected if noise errors dominate the RM fluctuations. We find no evidence for the detection of significant RM variations across the NW lobe, with a reduced-chi-squared of 1.1. However, a reduced-chi-squared of $\sim 1.8$ provides evidence, at a level of $\sim 1.35\sigma$, for RM variations across the SE lobe of $\sim 0.1$ rad m$^{-2}$.

3.3. Faraday depolarisation

The polarised intensity and degree of polarisation distributions are shown in Figure 3. The NW lobe is much brighter with a peak polarised intensity of 6.5 mJy beam$^{-1}$ (coincident with the hotspot) and a degree of polarisation of 4.9% at that location (ranging from 1.2% to 5.1% across the detected emission). The SE lobe is fainter with a peak polarised intensity of 1.1 mJy beam$^{-1}$. The degree of polarisation at that location is 2.8%, and it ranges from 1.1 to 3.3% across the lobe. The non-detection of polarised emission from the SE hotspot is likely due to intrinsic non-uniform field structures and Faraday depolarisation on scales smaller than the resolution of our observations. The fainter, extended lobe emission would have to be $\geq 10\%$ polarised to be detected in these observations.

In order to estimate the amount of depolarisation between 1.4 GHz and 144 MHz, the LoTSS data were compared with those of the NRAO VLA Sky Survey (NVSS; Condon et al. 1998). To determine the degree of polarisation at the same angular resolution as the NVSS survey, the RM pipeline was re-applied to the LoTSS data imaged at a lower angular resolution of $\sim 45′$.

At the peak polarised intensity location in the NW lobe of the LOFAR image, matched to the NVSS resolution, the degree of polarisation is 4.0 ± 0.3%. At the same location in the NVSS image at 1.4 GHz, the degree of polarisation is 7.3 ± 0.4%. This gives a depolarisation factor of DP$^{144\text{GHz}}_{1400\text{MHz}} \sim 0.6$, where DP$^{144\text{GHz}}_{1400\text{MHz}}$ is the degree of polarisation at 144 MHz divided by the degree of polarisation at 1.4 GHz. Assuming the commonly used external Faraday dispersion model for depolarisation, $p(\lambda) \propto e^{-\sigma_{RM}^2/\sigma_{RM}^2}$ (Burn 1966), provides a value of $\sigma_{RM} \sim 0.1$ rad m$^{-2}$. 
Fig. 3. Left image: Main image: Faraday rotation measure distribution (colour scale) of the north-west (NW) and south-east (SE) lobe regions that are detected above the threshold of $8\sigma_{\nu}$, overlaid by the total intensity contours starting at 5 mJy beam$^{-1}$ and increasing in factors of two. Insets: The absolute value of the $\text{RMCLEAN}$ Faraday dispersion function for the brightest polarised pixel in the NW lobe (top) and SE lobe (bottom). Right image: Main image: polarized intensity greyscale, in mJy beam$^{-1}$, overlaid by the total intensity contours. Insets: degree of polarisation colourscale (in per cent) from zoomed in regions of the NW and SE lobes.

For the SE lobe, the degree of polarisation at the peak polarised intensity at 144 MHz is $1.8 \pm 0.7\%$ (at 45$''$ resolution) and $10.1 \pm 2.1\%$ at the same location at 1.4 GHz. This gives $\text{DP}_{144}^{1.4} \sim 0.2$, corresponding to larger amounts of depolarisation than in the NW lobe. In the case of external Faraday dispersion, this corresponds to $\sigma_{\text{RM}} \sim 0.2$ rad m$^{-2}$.

The observed difference in depolarisation between the NW and SE lobes may be due to the different location within each lobe from which the polarised emission arises. In the case of the NW lobe, the peak polarised emission is coincident with the hotspot location, whereas in the SE lobe, the peak polarised emission is significantly offset from the hotspot ($\sim 40''$ away, in the bridge emission, with the offset also present in the NVSS images). Furthermore, from the non-detection of polarisation in the SE hotspot at 144 MHz, with a degree of polarisation $< 0.35\%$, we can place a lower limit on the Faraday depolarisation at this location of $\sigma_{\text{RM}} \sim 0.25$ rad m$^{-2}$, based on comparison with the NVSS degree of polarisation of $\sim 5\%$ at this location.

From inspection of the VLASS QL image at 3 GHz, the physical extent of the NW hotspot ($\sim 2.4''$) is smaller compared to the SE lobe region (of order $20''$ in size) and thus less affected by depolarisation caused by RM variations within the synthesised beam at 144 MHz. Since the amount of depolarisation scales roughly as the square-root of the number of Faraday rotation cells, this could reasonably explain the difference in the observed depolarisation between the lobes. However, the enhanced depolarisation at the location of the SE hotspot is more difficult to explain and may indicate a significant interaction between the hotspot/lobe magnetic field and the ambient medium. This warrants further investigation with more sensitive observations at low frequencies.

Overall, given the small amount of observed Faraday depolarisation, it is important to consider the accuracy of the correction for Faraday rotation from the ionosphere. Van Eck et al. (2018) estimate a residual error in the ionosphere RM correction between observations of 0.05 rad m$^{-2}$. As the ionosphere RM corrections across an observation (i.e. 8 hours) are linearly interpolated in time between direct estimates every 2 hours, a rough...
Table 1. Archival and measured flux densities, as well as the best-fit flux densities (in the self-consistent, s.c., fits) for the north-west and south-east lobes of J1235+5317.

<table>
<thead>
<tr>
<th>Freq. (MHz)</th>
<th>Entire Lobe [mJy]</th>
<th>N-lobe Hotspots [mJy]</th>
<th>s.c. fit</th>
<th>Entire Lobe [mJy]</th>
<th>N-lobe Hotspots [mJy]</th>
<th>s.c. fit</th>
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<td>378±40</td>
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<td>358±52</td>
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<td>320±52</td>
<td>333.3</td>
<td></td>
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<tr>
<td>151(2)</td>
<td>375±32</td>
<td>344</td>
<td>302±31</td>
<td>333.3</td>
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<td></td>
</tr>
<tr>
<td>325(3)</td>
<td>177±36</td>
<td>193.0</td>
<td>149±36</td>
<td>185.1</td>
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<td></td>
</tr>
<tr>
<td>325(4)</td>
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<td>153±58</td>
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<tr>
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<td>145±34</td>
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<td>(6.6±2)</td>
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</tr>
</tbody>
</table>

References. (1) 6C (Hales et al. 1990), (2) 7Cn (Riley et al. 1999), (3) WENSS (Rengelink et al. 1997), (4) B3 (Pedani & Greff 1999), (5) NVSS (Condon et al. 1998), (6) GB6 (Gregory et al. 1998), (7) VLASS (Lacy et al. in prepr.), (8) 9Cc (Waldram et al. 2019), (9) this paper.

3.4. Dynamical modelling

In order to decouple the properties of the electron density and magnetic field along the line of sight in the measured Faraday rotation and depolarisation, additional information is required on the physical characteristics of J1235+5317 (i.e. the magnetic field strength of the emission region) and the properties of its surrounding environment (i.e. the ambient gas density). These properties can be estimated through dynamical modelling of the radio lobes, while simultaneously accounting for energy losses of relativistic particles (electrons and positrons) injected into the expanding lobes by the relativistic jets (e.g. Machalski et al. [2011, 2016] and references therein). This is important because we lack X-ray data that could constrain the properties of the external medium (e.g. Ineson et al. 2017) and/or the magnetic field strength of the hotspot and lobes, without the need for the assumption of equipartition between the radiating particles and magnetic field (e.g. Mingo et al. 2017). Therefore, here we apply the evolutionary DYNA GE code of Machalski et al. (2007) to the radio lobes of J1235+5317, primarily to obtain an estimate of the external gas density, as well as estimates for the magnetic field strength of the lobes. The fitting procedure is performed separately for each lobe using the observational data given in Section 3.1 together with the radio luminosities calculated from the flux densities listed in Table 1. The input model parameters that are assumed are given in Table 2.

Characteristic of almost all FRII sources is a modest asymmetry in the length and radio luminosity of the lobes. Therefore, as might be expected, the DYNA GE results for the jet power $Q_j$, the central density of the external medium $\rho_0$, and other physical parameters can appear different for the two lobes of the same source. This aspect has been analysed by Machalski et al. (2009) and Machalski et al. (2011) for a sample of thirty GRGs. While some of the differences were within the uncertainties of the fitted values for the model parameters, significant differences were possible in cases where the evolution of the magnetic field and/or various energy losses and acceleration processes of the relativistic particles are different at the hotspots of the opposite lobes. Alternatively, such differences, especially in GRGs, may reflect different external conditions well beyond the host galaxy and cluster/group environment.

Following Machalski et al. (2009), we averaged the values of $Q_j$ and $\rho_0$ initially found in the ‘independent solution’ and treated them as fixed parameters in the ‘self-consistent’ model, $(Q_j)$ and $(\rho_0)$, respectively. New values of the slope of the ambient density distribution ($\beta$) and the age ($t_c$) for the NW and SE lobes, are denoted as $\beta_{nc}$ and $t_{nc}$ (Table 3). The DYNA GE fits to the observed data points are shown with solid lines in Figure 5. Table 3 presents the derived physical properties of the lobes, including a minimum-energy magnetic field strength in the lobes of $B_{min} \sim 1 \mu G$ and an external density of $n_e \sim 10^{-7} \mathrm{cm}^{-3}$ (i.e. $n_e \sim 10^{-7} \mathrm{cm}^{-3}$). This density is similar to the mean density of the Universe assuming half the baryons are in the WHIM (Machalski et al. 2011), and implies that the radio lobes are likely propagating into a low-density region of the Universe.

We also used the synchrotron minimum energy (equipartition) magnetic field formulation in Worrall & Birkinshaw (2006) to estimate the lobe magnetic field strength. From this we find an equipartition magnetic field strength that is 2.6 times higher than the $1 \mu G$ derived from the dynamical modelling (for $\gamma_{min} = 10$). When calculated in this manner the lobe equipartition field strength is usually found to be overestimated, by a factor of 2 to 3, compared to that found from X-ray Inverse Compton observa-

Figure 5. DYNA GE fits (solid lines) to the total intensity spectra of the north-west and south-east lobes (open circles), and the spectral points of the hotspot regions (filled dots; not used in the fits). Note that the north-west lobe flux density scale is shifted one decade up in relation to the given ordinate scale.

The residuals can be made for the residual error within the observation of $-0.05 \sqrt{4} \sim 0.1 \ \mathrm{rad\ m^{-2}}$. This means that most (or all) of the observed depolarisation in the NW hotspot is possibly due to residual errors in the ionospheric RM correction. However, the difference in depolarisation between the NW hotspot and SE lobe cannot be explained by ionosphere RM errors. Therefore, a $\sigma_{RM}$ of at least $-0.1 \ \mathrm{rad\ m^{-2}}$ in the SE lobe can be considered astrophysically meaningful. This is comparable to the RM variations across the SE lobe of $\sim 0.1 \ \mathrm{rad\ m^{-2}}$ found in Section 3.2.
The diadiabatic expansion and age of the lobes. takes into account more physical e
netic field strength obtained from the dynamical modelling as it
tition magnetic field strengths in radio galaxies (e.g. Beck &
4. Interpretation

tions of lobes (e.g. Ineson et al. 2017, Mingozzi et al. 2017). This highlights some of the uncertainties in the calculation of equipar
tition magnetic field strengths in radio galaxies (e.g. Beck &
4.2. Local environment RM contribution

2. D. O’Sullivan et al.: The intergalactic magnetic field probed by a giant radio galaxy

<table>
<thead>
<tr>
<th>Parameter</th>
<th>Symbol</th>
<th>Value</th>
<th>Value</th>
</tr>
</thead>
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<tr>
<td>Jet power [$10^{39}\text{erg s}^{-1}$]</td>
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<tr>
<td>Core density [$10^{-27}\text{cm}^{-3}$]</td>
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<td>1.61±0.3</td>
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<tr>
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<tr>
<td>Lobe pressure [$10^{-13}\text{dyn cm}^{-2}$]</td>
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<tr>
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<td>$v_{\text{par}}$</td>
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</tbody>
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4.4. Local environment RM contribution

The hot gas in rich groups and clusters is magneto
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ground radio sources (see Carilli & Taylor 2002 and references therein). For radio galaxy lobes that have not expanded signifi

tion of the GRM and its variation across the extent of J1235+5317.

4. Interpretation

The difference in the mean RM between the NW and SE lobes is 2.5 ± 0.1 rad m^{-2}. This may be due to variations in the Galactic RM (GRM) on scales of ~11', differences in the magnetoiono
tic material of the intergalactic medium on large scales, and/or line

<table>
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<tr>
<td>Adiabatic index of the lobes’ material</td>
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<tr>
<td>Adiabatic index of the ambient medium</td>
<td>$\Gamma_\text{a}$</td>
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</tr>
<tr>
<td>Adiabatic index of the lobes’ magnetic field</td>
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<tr>
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<td>Maximum electron Lorentz factor (injected)</td>
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<tr>
<td>Jet viewing angle</td>
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Table 3. Fitted values of the model free-parameters in the ‘self-consistent’ dynamical modelling solution

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<th>Value for S-lobe</th>
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The hot gas in rich groups and clusters is magneto
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ground radio sources (see Carilli & Taylor 2002 and references therein). For radio galaxy lobes that have not expanded signifi

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4.4. Local environment RM contribution

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An appropriate gas density profile, \( n(r) \), for a galaxy group or cluster is a “beta-profile”, where \( n(r) = n_0 (1 + r^2/r_c^2)^{-3/2} \). We assume that the magnetic field strength scales linearly with the gas density, \( B(r) = B_0 n(r)/n_0 \), where \( B_0 \) is the central magnetic field strength (e.g. Dole et al. 2001; Laing et al. 2006; Vaccarino et al. 2012; Govoni et al. 2017). Values of \( r_c \sim 10^{-3} \text{ cm} \), \( r_c \sim 100 \text{ kpc} \) and \( \beta \sim 0.5 \) are not unreasonable for a poor cluster (e.g. Laing et al. 2008; Bonafede et al. 2010; Guidetti et al. 2012). The choice of these parameters is arbitrary given our limited information about the environment of the host galaxy (Section 2.2) but we use them simply as a plausible example. Following Murgia et al. (2004, eqn. 15), we find a Faraday dispersion of \( \sigma_{\text{RM}} \sim 0.1 \text{ rad m}^{-2} \) at \( r \sim 1.5 \text{ Mpc} \), which requires \( B_0 \sim 5 \mu \text{G} \) with a magnetic field correlation length of \( \sim 25 \text{ kpc} \). This implies an ambient density of \( \sim 1.7 \times 10^{-3} \text{ cm}^{-3} \) and field strength \( B \sim 0.09 \mu \text{G} \) at the location of the hotspots. Using these values and a large outer scale for the magnetic field fluctuations of 500 kpc (Vaccarino et al. 2010) gives a mean RM of \( -0.4 \text{ rad m}^{-2} \). Therefore, we can reasonably explain \( \sigma_{\text{RM}} \sim 0.1 \text{ rad m}^{-2} \) at \( r \sim 1.5 \text{ Mpc} \), we cannot self-consistently explain the large mean RM excess of \( \sim 2.5 \text{ rad m}^{-2} \), even for a large outer scale of turbulence in the magnetic field power spectrum (Enßlin & Vogt 2003; Murgia et al. 2004). Note that the outer scale is mainly responsible for the observed mean RM and the inner scale for the value of \( \sigma_{\text{RM}} \). We used a large outer scale here to show that this model cannot self-consistently explain both \( \sigma_{\text{RM}} \) and the mean RM.

Draping of the ambient field in addition to compression of the ambient magnetoionic gas could enhance the mean RM near the surface of the lobes (Guidetti et al. 2011, 2012), and may also help explain the higher depolarisation of \( \sigma_{\text{RM}} \gtrsim 0.15 \text{ rad m}^{-2} \) at the location of the SE hotspot. Enhancements in the field strength and gas density by factors of 4 over a path length of \( \sim 50 \text{ kpc} \) outside the lobes could produce an additional [RM] of \( -0.5 \text{ rad m}^{-2} \). More sensitive observations at high angular resolution are required to determine if such ordered field structures are indeed present.

We note that the external gas density used here is two orders of magnitude higher than estimated from the dynamical modelling. This means that either the observed depolarisation does not occur in the external medium local to the source or that the dynamical modelling is severely underestimating the external density. Such low density gas may be challenging to detect in X-rays, but extrapolation of an X-ray profile from the inner region would be very instructive. In general, comparison with simulations of the propagation of large scale jets within a realistic cosmological environment may provide the best avenue for progress in this area (e.g. Huarte-Espinosa et al. 2011; Hardcastle & Krause 2014; Turner & Shabala 2015; English et al. 2016; Vazza et al. 2017a).

### 4.3. Internal Faraday depolarisation

Our observations are insensitive to polarised emission from RM structures broader than \( \sim 1 \text{ rad m}^{-2} \) (Section 2.2). Therefore, the large amounts of internal Faraday rotation required to explain the mean RM excess are ruled out. However, it is worth considering if the small amount of Faraday depolarisation

\[ (\sigma_{\text{RM}} \sim 0.1 \text{ rad m}^{-2}) \] can be explained by Faraday rotating material mixed with the synchrotron emitting material in the lobes.

One of the most commonly used magnetic field models for the lobes of extragalactic sources is one where the field is highly tangled on small scales, with the observed appreciable degrees of polarisation produced due to stretching and compression (Laing 1990). Given the equipartition magnetic field strength of \( \sim 1 \mu \text{G} \) within the lobes (Section 3.4), and as an illustrative example, we choose a thermal gas density internal to the lobes of \( n_e \sim 10^{-3} \text{ cm}^{-3} \), with 500 field reversals through a lobe depth of \( \sim 500 \text{ kpc} \), to produce \( \sigma_{\text{RM}} \sim 0.1 \text{ rad m}^{-2} \) (using Eqn. 1 and assuming \( B_0 = B/\sqrt{3} \) ). Observations at even lower frequencies would be required to resolve a Faraday depth width of \( 0.1 \text{ rad m}^{-2} \) in the Faraday spectrum (e.g. using LOFAR observations down to at least 30 MHz, in combination with the data in this paper). In addition, broadband polarisation modelling would be needed to distinguish between internal and external Faraday depolarisation scenarios (e.g. Anderson et al. 2018; O’Sullivan et al. 2018). Using the LOFAR international baselines to obtain sub-arcssecond resolution would further enhance the ability to isolate different contributions by resolving the external RM variations across the emission region.

For now, we can assess the likelihood of this scenario in terms of the implied energetics. For expected internal thermal gas temperatures of \( \gtrsim 10 \text{ keV} \) (Gitti et al. 2007), the lobe thermal gas pressure is \( p_e \sim 2n_e kT \sim 3 \times 10^{18} \text{ dyn cm}^{-2} \), which is an order of magnitude larger than the pressure from the synchrotron-emitting plasma in the lobes (\( p_0 \) in Table 5). This is inconsistent with expectations from studies of other FRII lobes (Croston et al. 2005; Ineson et al. 2017), and thus unlikely, unless the internal thermal gas is much cooler than assumed here.

### 4.4. RM contribution from large-scale structure

Significant asymmetries in the magnetoionic material in the foreground IGM, far from the local source environment, could also contribute to the observed mean RM difference between the lobes. Such variations could be caused by the magnetised component of the large scale structure (LSS) at redshift, as Ryu et al. (2008), Cho & Ryu (2009) and Akahori & Ryu (2010) predict a root-mean-square RM (\( \sigma_{\text{RM}} \)) through LSS filaments of order 1 rad m\(^{-2}\). In our case, the polarised emission of one lobe needs to pass through more foreground filaments than the other to explain the observed RM difference of 2.5 rad m\(^{-2}\). Therefore, information is required on the location of LSS filaments with respect to the lines of sight probed by the polarised emission from the lobes of J1235+5317.

#### 4.4.1. Location of large scale structure filaments

The catalogue of Chen et al. (2015, 2016) provides a cosmic filament reconstruction from the SDSS data for 130 redshift slices in the range \( 0.5 < z < 0.7 \). In Figure 6, we plot the location of the filaments that are in the foreground of J1235+5317 (i.e. at \( z < 0.34 \)). There are five filaments identified in different foreground redshift slices that pass through the field. We assign a thickness of 1 Mpc to each filament (Vazza et al. 2015c) to determine which filaments most likely intersect lines of sight towards the polarized lobes (Figure 9). For a thickness of 1 Mpc, there are four filaments that cover the NW lobe and one filament that covers the SE lobe. Therefore, we estimate that there is an excess of three filaments covering the NW lobe. Considering different filament thicknesses results in different numbers of
filaments covering each lobe, with an excess of filaments covering the NW lobe remaining for filaments up to a thickness of ~3.8 Mpc (i.e. the thickness above which the same number of filaments cover both lobes). In light of this result, we consider if the RM difference between the lobes can be explained by magnetised gas in these filaments. We note that there is no evidence of an individual intervening galaxy in the SDSS images that could explain the RM difference.

4.4.2. Magnetic field strength in filaments

To explain the RM difference between the lobes, an RM excess of ~2.5 rad m⁻² must be provided by the three extra filaments covering the NW lobe. Simulations suggest that the electron number density of LSS filaments can vary from 10⁻⁶ to 10⁻⁴ cm⁻³ (Cen & Ostriker 2006; Ryu et al. 2008; Cho & Ryu 2009; Akahori & Ryu 2010; Vazza et al. 2015c). Thus, we adopt a mean electron density of 10⁻⁵ cm⁻³. Akahori & Ryu (2011) found a peak in the RM power spectrum, due to their simulated IGMF in filaments, on scales corresponding to a proper length of ~3 Mpc, which they expect to correspond to the typical line-of-sight path through LSS filaments. Therefore, using a path length (L) of 3 Mpc and a coherence length (l) of 300 kpc (Cho & Ryu 2009) leads to a magnetic field strength in the filaments (B_{LSS}) of approximately

\[
B_{LSS} \sim 0.3 \left( \frac{n_e}{10^{-5} \text{cm}^{-3}} \right)^{-1} \left( \frac{L}{3(3 \text{ Mpc})} \right) \left( \frac{l}{300 \text{ kpc}} \right)^{-1/2} \mu \text{G},
\]

for \( B_0 = B_{LSS} / \sqrt{3} \). This estimate of the density-weighted IGMF strength of ~0.3 \( \mu \text{G} \) has significant uncertainty given our limited knowledge of the particle number density of the gas in these filaments, as well as the observationally unconstrained coherence length of the field and the path length though each filament. Furthermore, this estimate cannot be treated as an upper limit as a large Galactic RM variation across the source (Section 4.1) could make the difference in RM between the lobes even larger (since the RM can be positive or negative). Furthermore, much larger RM variations are observed across radio relics which cannot be explained by Galactic RM variations, indicating the presence of large scale ordered fields in the outskirts of galaxy clusters (e.g. Kierdorf et al. [2017], Loi et al. [2017]).

Therefore, a better approach may be to compare directly with cosmological simulations of the RM contribution from such LSS filaments. These simulations suggest that the magnetic field strength in filaments could range somewhere from ~1 to 10 nG (e.g. Vazza et al. 2015c). Early hydrodynamic simulations by Ryu et al. (2008) used a prescription to produce magnetic fields from the kinetic energy of turbulent gas flows (guided by expectations from small-scale magnetic dynamo simulations), which produced average IGMF strengths of ~10 nG. Subsequent work by Cho & Ryu (2009) and Akahori & Ryu (2010, 2011), using the results of these simulations, provided estimates of the "typical" RM contribution from LSS filaments. The most relevant number for Faraday rotation is the gas density (\( \rho \)) weighted average of the strength of the magnetic field through the filaments, i.e. \( (\rho B^2)^{1/2}/(\rho^2)^{1/2} \), which gave a few \( \times 0.1 \mu \text{G} \) in the above simulations. From this, it was found that the root-mean-square RM (RM_{rms}) through the filaments scales with the number of filaments (\( N_f \)) as RM_{rms} \sim 1.5 \mu \text{G} \text{ rad m}^{-2}, up to a saturation point that corresponds to ~25 filaments for \( z > 1 \). In the case of three filaments, the predicted RM_{rms} \sim 2.6 \mu \text{G} \text{ rad m}^{-2}, which is consistent with our observations (where we have an RM difference of 2.5 rad m⁻² between only two lines of sight, in which one passes through three additional filaments). Therefore, it can be argued that our results are consistent with the expected Faraday rotation signature from an average magnetic field strength in LSS filaments of ~10 nG.

We further investigated the above findings by direct comparison with recent MHD cosmological simulations, as described in Vazza et al. (2014b). In particular, we analysed the RM distribution in the warm-hot gas simulated in a cosmic volume of 50³ Mpc³, at a spatial resolution of 20 kpc (comoving). To better compare with our observations, we generated a long integration cone for this volume, stacking several randomly oriented, mirrored replicas of the volume, covering the comoving distance out to \( z = 0.34 \). In this way, we could measure the probability of having a contribution as large as 2.5 rad m⁻² from LSS filaments for the J1235+5317 observations at \( z = 0.34 \). We found that this occurred in only 5% of cases, for typical magnetisation values of ~10 to 50 nG, amplified from an initial magnetic field strength of 1 nG, which was seeded at an early cosmological epoch and is in line with the upper limits given by the Planck satellite (Planck Collaboration et al. 2016a). The probability was negligible for a significantly smaller seed field of 0.1 nG.

Lower limits on the primordial field strength of \( \sim 10^{-16} \) G (Neronov & Vovk 2010) and \( \sim 10^{-20} \) G (Takahashi et al. 2013), imply that the true value may indeed be much lower. However, this is not the only possible scenario, as the LSS can be magnetised by a more "astrophysical" mechanism, such as galaxy feedback (e.g. Vazza et al. 2017b, for a recent review), or produced by a more efficient dynamo amplification of primordial fields (Ryu et al. 2008) than is found in current MHD simulations. Therefore, from comparison with the MHD simulations, we consider it unlikely that the true RM contribution from the IGMF is as large as 2.5 rad m⁻², and that the observed RM excess is possibly dominated by other contributions along the line of sight, such as small scale GRM variations (Section 4.1).
5. Conclusions

We have presented a linear polarisation and Faraday rotation study of a giant FRII radio galaxy, J1235+5317, using data from the LOFAR Two-Metre Sky Survey (Shimwell et al. 2018). After obtaining the spectroscopic redshift of the host galaxy (SDSS J123501.52+531755.0, z = 0.3448 ± 0.0003), we find that the radio galaxy has a projected linear extent of 3.4 Mpc. Both lobes are detected in polarisation with a mean RM difference between the lobes of 2.5 ± 0.1 rad m⁻². Small amounts of Faraday depolarisation (∼ 0.1 rad m⁻²) are also detected. In the absence of direct tracers of the gas density on large scales, we employ dynamical modelling of the advancing hotspots to infer a particle number density of the ambient gas of ne ~ 10⁻⁷ cm⁻³. This implies that the radio galaxy is expanding into an underdense region of the Universe. However, explaining the observed Faraday depolarisation (that most likely occurs in the environment local to the source) requires ne ~ 10⁻⁵ cm⁻³ in combination with a turbulent magnetic field strength of ∼ 0.09 μG at a distance of ~ 1.5 Mpc from the host galaxy. Therefore, either the dynamical modelling is underestimating the density of the external medium or the depolarisation does not occur in the local source environment. Simulations of the propagation of FRII jets to large scales within a realistic cosmological environment may help distinguish between these scenarios. In general, the estimated magnetic field strength is unable to account for the observed mean Faraday rotation difference of 2.5 rad m⁻² between the two lobes.

Using a catalogue of large scale structure (LSS) filaments in the local universe derived from optical spectroscopic observations, we find an excess of filaments intersecting lines of sight towards the polarised emission of the NW lobe. Assuming that magnetised gas in these LSS filaments is responsible for the RM difference between the lobes, gives a density-weighted magnetic field strength of 0.3 μG (assuming ne ~ 10⁻⁵ cm⁻³, a line-of-sight path length through each filament of 3 Mpc, and a magnetic field coherence length of 300 kpc). However, we find that predictions from cosmological simulations of the RM contribution from LSS filaments gives a low probability (~ 5%) for an RM contribution as large as 2.5 rad m⁻². This probability applies to the case of magnetic field strengths in the LSS filaments of 10 to 50 nG, which are amplified from primordial magnetic fields close to current upper limits from the CMB of ~ 1 nG (the probability decreases to ~ 0% for weaker fields). Extrapolation of the observed variations in the Milky Way RM to 11° scales (i.e. the angular size of J1235+5317) indicates that this likely contributes significantly to the mean RM difference, however, further observations are required to obtain better constraints.

In the near future, large samples of RMSs from radio galaxies with known redshifts will allow more advanced statistical analysis techniques to be used, such as RM structure function analyses (e.g. Akahori et al. 2014) and cross-correlation with other tracers of LSS (e.g. Stasyszyn et al. 2010, Vernstrom et al. 2017, Brown et al. 2017). This will enable a better separation of the Faraday rotation due to our Galaxy (e.g. Haverkorn et al. 2004, Sun & Reich 2009, Mao et al. 2010, Stil et al. 2011) from that due to the cosmic web, and put stronger constraints on the strength and structure of the intergalactic magnetic field.

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