Flow fluctuations in Pb+Pb collisions at $\sqrt{s_{NN}} = 5.02$ TeV with the ATLAS detector

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Abstract
Measurements of four-particle cumulants $c_n\{4\}$ for $n = 1, 2, 3, 4$ are presented using 470 $\mu$b$^{-1}$ of Pb+Pb collisions at $\sqrt{s_{NN}} = 5.02$ TeV with the ATLAS detector at the LHC. These cumulants provide information on the event-by-event fluctuations of single harmonics $p(v_n)$. For the first time, a negative $c_1\{4\}$ is observed. The $c_4\{4\}$ is found to be negative in central collisions but changes sign around 20–25% centrality. This behavior is consistent with a nonlinear contribution to $v_4$ that is proportional to $v_2^2$. $c_2\{4\}$ and $c_3\{4\}$ are calculated using two reference event classes in order to investigate the influence of volume fluctuations. Over most of the centrality range, $c_2\{4\}$ and $c_3\{4\}$ are found to be negative, while in the ultra-central collisions, $c_2\{4\}$ changes sign and becomes positive, suggesting a deviation from Gaussian behavior in the event-by-event fluctuation of $v_2$. The magnitudes of the sign change are also found to be dependent of the event class definition.

Keywords: Multi-Particle Correlation, Cumulants, Heavy-ion, Flow Fluctuation

1. Introduction
Heavy-ion collisions at RHIC and the LHC create hot, dense matter whose space-time evolution is well described by relativistic viscous hydrodynamics [1]. Owing to strong event-by-event density fluctuations in the initial state, the distributions of the final-state particles also fluctuate event by event. These fluctuations lead to harmonic modulation of the particle densities in the azimuthal angle $\phi$, characterized by a Fourier expansion $dN/d\phi \propto 1 + 2 \sum_{n=1}^{\infty} v_n \cos n(\phi - \Phi_n)$, where $v_n$ and $\Phi_n$ represent the magnitude and event-plane angle of the $n$th-order harmonic flow.

One important observable for studying the initial condition and final state dynamics of the medium is the probability density distribution $p(v_n)$ for events selected with similar centrality. They are directly related to event-by-event fluctuations of the eccentricities $p(\epsilon_n)$, where $\epsilon_n$ describes the $n$th-order shape component in the initial state. In order to study the $p(v_n)$, multi-particle azimuthal correlations within the cumulant framework has been applied [3]. The $p(v_n)$ distribution can be inferred from $2k$-particle cumulants $c_n\{2k\}$.
which are related to the moments of the $p(v_n)$. Most models of the initial state of A+A collisions predict a 
$p(v_n)$ whose shape is close to Gaussian, and that the four-particle cumulants $c_4[4]$ are zero or negative [4].

In heavy-ion collisions, $v_n$ coefficients are often calculated for events with similar activity, defined as the 
particle multiplicity in a fixed pseudorapidity range. Due to fluctuations in the particle production process, 
the centrality for events selected to have the same particle multiplicity fluctuates from event to event. Since 
the $v_n$ coefficients change with centrality, fluctuation of centrality may lead to additional fluctuations of 
$v_n$, which broaden the underlying $p(v_n)$ distribution. These centrality fluctuations, more commonly known 
as volume fluctuations, have been shown to contribute significantly to the event-by-event fluctuation of 
conserved quantities [5]. In this measurement, two reference event classes are used in the calculation of 
cumulants to study the influence of volume fluctuations on the flow cumulants.

2. Analysis details

This analysis uses 470 $\mu b^{-1}$ of Pb+Pb data at $\sqrt{s_{NN}} = 5.02$ TeV collected by ATLAS [6]. The mea-

suresments are performed using the inner detector, the forward calorimeters (FCal), and the zero-degree 
calorimeters. To increase the number of recorded events from very central Pb+Pb collisions, a dedicated 
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calorimeters. To increase the number of recorded events from very central Pb+Pb collisions, a dedicated 
measurement is also applied to quantify the residual non-flow contributions [7].

The $c_n[4]$ for $n = 1, 2, 3, 4$ are calculated using the Q-cumulant method for charged particles in $|\eta| < 2.5$.

The method calculates 2$k$-particle azimuthal correlations $\langle\{2k\}_n\rangle$, and 2$k$-particle cumulants, $c_n[2k]$, for the 
$n^{th}$-order flow harmonics. The two- and four-particle correlations in one event are obtained as:

$$\langle\{2\}_n\rangle = \langle e^{i\phi_1 - \phi_2}\rangle, \langle\{4\}_n\rangle = \langle e^{i(\phi_1 + \phi_2 - \phi_3 - \phi_4)}\rangle$$  \hspace{1cm} (1)

where "$\langle\rangle$" denotes a single-event average over all pairs or quadruplets, respectively. The averages from 
Eq. 1 can be expressed in terms of per-particle normalized flow vectors $q_{nj}$ with $l = 1, 2...$ in each event:

$\overline{q}_{nj} = \sum_j w_j^n e^{i\phi_j} / \sum_j w_j^n$, where the sum runs over all $M$ particles in the event and $w_j$ is a weight assigned to the 
$j^{th}$ particle.

The two- and four-particle cumulants are obtained from the azimuthal correlations as:

$$c_n[2] = \langle\langle\{2\}_n\rangle\rangle, c_n[4] = \langle\langle\{4\}_n\rangle\rangle - 2\langle\langle\{2\}_n\rangle\rangle^2$$  \hspace{1cm} (2)

where "$\langle\langle\rangle\rangle$" represents a weighted average of $\langle\{2k\}_n\rangle$ over an event ensemble, defined as events in either a 
narrow interval of $\Sigma E_T$ or a narrow interval of $N_{ch}^{rec}$, the number of reconstructed charged particles in $0.5 < 
$p_T < 5$ GeV. The $c_n[4]$ is then calculated separately for the two types of reference event classes, denoted 
as $c_n[4, \Sigma E_T]$ and $c_n[4, N_{ch}^{rec}]$, respectively. Furthermore, the recently proposed three-subevent cumulant 
method is also applied to quantify the residual non-flow contributions [7].

3. Results and discussions

Figure 1 shows the centrality dependence of $c_1[4]$ in several $p_T$ ranges, obtained from the reference 
event class based on $\Sigma E_T$. In the hydrodynamic picture, $c_1[4]$ is sensitive to event-by-event fluctuations 
of the dipolar eccentricity $\epsilon_1$ associated with initial-state geometry. Previously ATLAS measured $v_1$ using 
two-particle correlation method in Pb+Pb collisions at 2.76 TeV [8]: the $v_1[2]$ is observed to be negative at 
low $p_T$, change sign at $p_T \approx 1.2$ GeV, and increase quickly towards higher $p_T$. Therefore, it is naturally 
expected that a $c_1[4]$ signal is larger and therefore easier to measure at higher $p_T$. Furthermore, $c_1[4]$ are 
oberved to be consistent in both the standard and three-subevent cumulant methods, suggesting that the 
influence of non-flow correlations is small.

Figure 2 shows the centrality dependence of $c_4[4]$ in several $p_T$ ranges. The $c_4[4]$ values are negative 
in central collisions but change sign in the 25 – 30% centrality range. The centrality value at which the 
sign change occurs shifts towards more peripheral collisions as the $p_T$ of the particles increases. It is well 
established that the $v_4$ in Pb+Pb collisions contains a linear contribution associated with initial geometry and
a mode-mixing contribution from lower-order harmonics due to nonlinear hydrodynamic response [10] \( v_4 = v_{4L} + \beta v_2^2 \), where the linear component \( v_{4L} \) is driven by the corresponding eccentricity in the initial geometry, and \( \beta \) is a constant. Therefore this sign-change reflects the interplay between these two contributions: in central collisions, \( c_4(4) \) is dominated by the negative contribution from \( p(v_{4L}) \), while in peripheral collisions \( c_4(4) \) is dominated by the positive contribution from \( p(v_2^2) \), even though the four-particle cumulant for \( p(v_2^2) \) is negative. The change of the crossing point with \( p_T \) suggests that the relative contributions from these two sources are also a function of \( p_T \).

Figure 3 compare the \( c_2(4) \) and \( c_3(4) \) obtained for the \( \sum E_T \) reference event class with those obtained for the \( N_{\text{ch}}^{\text{rec}} \) reference event class. They are obtained using the standard cumulant method. Events with the same \( N_{\text{ch}}^{\text{rec}} \) may have different \( \sum E_T \), therefore the \( c_4(4) \) values depend on the exact definition of reference event class used for averaging, due to a change in \( p(v_n) \) associated with each reference event class. This comparison can shed light on the fine details of flow fluctuations and how they are correlated with centrality definition [5]. The figures show that the trends of the centrality dependence are very similar in both cases. However, the \( c_3(4,N_{\text{ch}}^{\text{rec}}) \) values are significantly larger than the \( c_3(4,\sum E_T) \) values.

The insert panels of Figure 3 show the trend of \( c_2(4) \) and \( c_3(4) \) in the ultra central collision range of 0 – 4.5%. The \( c_2(4,N_{\text{ch}}^{\text{rec}}) \) values are significantly larger than \( c_2(4,\sum E_T) \), and both quantities change sign and become positive toward more central collisions. In contrast, the \( c_3(4,N_{\text{ch}}^{\text{rec}}) \) values suggest a change of sign in the same centrality range, although the \( c_3(4,\sum E_T) \) always remains negative. All these observations indicate that volume fluctuation plays an important role in the flow cumulant measurement.
4. Summary

Measurements of four-particle cumulants \( c_n^{(4)} \) are presented using 470 \( \mu b^{-1} \) of Pb+Pb collisions at \( \sqrt{s_{NN}} = 5.02 \) TeV with the ATLAS detector at the LHC. This proceedings provide the first measurement of a negative \( c_1^{(4)} \), which sheds light on the nature of the dipolar eccentricity fluctuation in the initial-state geometry. The values of \( c_4^{(4)} \) are found to be negative in central collisions but change sign around 20 – 25% centrality and increase quickly for more peripheral collisions. This behavior is consistent with a nonlinear contribution to \( v_4 \) that is proportional to \( v_2^2 \). In the ultra-central collisions, \( c_2^{(4)} \) changes sign and becomes positive. It also depends on the choice of the reference event class, suggesting the volume fluctuation should be considered in future flow cumulant measurement. These results provide new insights on the fluctuations of the initial-state geometry, especially in the ultra-central collisions, as well as the final-state dynamical evolution of the medium.

This research is supported by NSF under grant numbers PHY-1305037 and PHY-1613294.

References