The Size, Shape, and Scattering of Sagittarius A* at 86 GHz: First VLBI with ALMA

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ABSTRACT

The Galactic Center supermassive black hole Sagittarius A* (Sgr A*) is one of the most promising targets to study the dynamics of black hole accretion and outflow via direct imaging with very long baseline interferometry (VLBI). At 3.5 mm (86 GHz), the emission from Sgr A* is resolvable with the Global Millimeter VLBI Array (GMVA). We present the first observations of Sgr A* with the phased Atacama Large Millimeter/submillimeter Array (ALMA) joining the GMVA. Our observations achieve an angular resolution of ~87µas, improving upon previous experiments by a factor of two. We reconstruct a first image of the unscattered source structure of Sgr A* at 3.5 mm, mitigating effects of interstellar scattering. The unscattered source has a major axis size of 120 ± 34µas (12 ± 3.4 Schwarzschild radii), and a symmetrical morphology (axial ratio of 1.21 ± 0.2), which is further supported by closure phases consistent with zero within 3σ. We show that multiple disk-dominated models of Sgr A* match our observational constraints, while the two jet-dominated models considered are constrained to small viewing angles. Our long-baseline detections to ALMA also provide new constraints on the scattering of Sgr A*, and we show that refractive scattering effects are likely to be weak for images of Sgr A* at 1.3 mm with the Event Horizon Telescope. Our results provide the most stringent constraints to date for the intrinsic morphology and refractive scattering of Sgr A*, demonstrating the exceptional contribution of ALMA to millimeter VLBI.

Keywords: accretion – galaxies: individual: Sgr A* – Galaxy: center – techniques: interferometric
1. INTRODUCTION

Supermassive black holes (SMBHs) play a crucial role in shaping our Universe: they evolve symbiotically with their host galaxies and are the cause of extreme environmental changes via accretion, outflows, jets and mergers (e.g., Ferrarese & Merritt 2000; Gebhardt et al. 2000). They are believed to be the origin of the most energetically efficient and powerful processes in the Universe, and yet we are far from fully grasping how these processes are launched and maintained (e.g., Boccardi et al. 2017; Padovani et al. 2017). Several theories have been put forward to explain accretion and jet launching mechanisms of SMBHs, but observational evidence to discriminate among theoretical models remains scarce (e.g., Yuan & Narayan 2014; Fragile 2014).

Sagittarius A* (Sgr A*) is the radio source associated with the closest known SMBH, with a mass $M \sim 4.1 \times 10^6 M_\odot$, located at the center of our Milky Way, at a distance $D \sim 8.1$ kpc (Ghez et al. 2008; Reid 2009; Gillessen et al. 2009; Gravity Collaboration et al. 2018a). The angular size of the Schwarzschild radius for Sgr A* is thus estimated to be $R_{S,sch} = 2GM/c^2 \sim 10\mu$as. Due to its proximity, Sgr A* subtends the largest angle on the sky among all known SMBHs, and is thus the ideal laboratory to study accretion and outflow physics (Goddi et al. 2017).

Theoretical models of the dominating component of the radio emission in Sgr A* fall into two broad classes: a relativistic compact jet model or a radiatively inefficient accretion flow (Narayan et al. 1995; Falcke & Markoff 2000; Özel et al. 2000; Yuan et al. 2003). However, the southern declination and strong interstellar scattering of Sgr A* (see more details in Section 2.2) lead to uncertainty in its intrinsic radio structure, despite decades of centimeter wavelength Very Long Baseline Array (VLBA) observations (e.g., Alberdi et al. 1993; Marcaide et al. 1999; Bower et al. 2004; Shen et al. 2005; Lu et al. 2011a; Bower et al. 2014). Consequently, these observations have so far been unable to decisively constrain the dominating emission model for Sgr A* to either of those two classes. Additional lines of evidence provide support for both models. For instance, frequency-dependent time lags in light-curves of Sgr A* suggest expanding outflows during flares (e.g., Yusef-Zadeh et al. 2006, 2008; Brinkerink et al. 2015). VLBI observations at 7 mm have found evidence for significant intrinsic anisotropy in some epochs (Bower et al. 2014), although the anisotropy is not universally seen for other instruments and epochs (e.g., Zhao et al. 2017), so the anisotropy may be episodic or may be due to limitations in the scattering mitigation or model fitting procedure.

VLBI in the mm-regime can reach the smallest spatial scales in Sgr A*, enabling detection and imaging of the intrinsic structure. At a wavelength of 1.3 mm, observations with the Event Horizon Telescope (EHT) have shown that the radio emission occurs on scales comparable to the event horizon (Doeleman et al. 2008; Fish et al. 2011; Johnson et al. 2015; Fish et al. 2016; Lu et al. 2018). On these scales, general relativistic effects such as the “shadow” cast by the black hole are expected to determine the source morphology (Falcke et al. 2000), limiting the view of the innermost accretion flow. At longer wavelengths, scatter-broadening by the interstellar medium (ISM) strongly hinders any attempt to probe intrinsic structure. Observations at 3.5 mm, where accretion flow kinematics may give rise to an outflow or compact jet and where scatter-broadening becomes sub-dominant to intrinsic structure, can distinguish between the two classes of models via detailed comparisons of observations and simulations, and help understand the fundamental nature of the radio emission from Sgr A*.

The first 3.5 mm VLBI detection of Sgr A*, by Rogers et al. (1994), gave an initial estimate of the scattered source size using a circular Gaussian fit. Krachbaum et al. (1998) used three stations to measure the first closure phases (consistent with zero) at 3.5 mm on a small triangle. Closure phases are a robust observable, since the closed sum of phases in a triangle removes any station-based instrumental effect. A zero value indicates symmetry in the spatial scales probed by the three baselines involved in the closure measurement, a non-zero value implies asymmetry (e.g., Rauch et al. 2016; Thompson et al. 2017). Subsequent observations, with improved sensitivity and baseline coverage, used closure amplitudes for elliptical Gaussian model-fitting, but the minor axis of the scattered source, along the north-south direction, remained difficult to constrain because of predominantly east-west array configurations (Doeleman et al. 2001; Shen et al. 2005; Bower et al. 2006; Lu et al. 2011a).

The addition of the Large Millimeter Telescope Alfonso Serrano (LMT) and the Robert C. Byrd Green Bank Telescope (GBT) enabled more precise estimates of the intrinsic size and shape of Sgr A* and revealed non-zero closure phases, indicating either intrinsic source asymmetry or substructure from interstellar scattering (Ortiz-León et al. 2016; Brinkerink et al. 2016, hereafter O16, B16). Further analysis by Brinkerink et al. (2018, hereafter B18) found a slight excess of flux density (~1% of total flux density) east of the phase center, giving clear deviation from the purely Gaussian geometry that was assumed in model-fitting. Thus, these improved observations support moving beyond simple Gaussian model-fitting to test more complex source models. Imaging is a natural next step, as it does not assume a particular morphological model.

The development of phased-array capability at the Atacama Large Millimeter/submillimeter Array (ALMA) gives unprecedented sensitivity at 3.5 mm (Doeleman
In addition to its sensitivity, the geographical location of ALMA provides long north-south baselines to Northern hemisphere sites, probing regions where scattering is sub-dominant to intrinsic structure. In this paper, we present the first VLBI observations of Sgr A* with phased ALMA joining twelve stations of the Global Millimeter VLBI Array (GMVA). These observations improve north-south resolution by more than a factor of three compared to previous 3.5 mm experiments, and they allow us to reconstruct the first unscattered image of Sgr A* at 3.5 mm.

The organization of the paper is as follows. In Section 2, we give an overview of the relevant background for models of the intrinsic structure and scattering of Sgr A*. After summarizing the observations and data reduction (Section 3) and the imaging (Section 4), we present our GMVA+ALMA image and discuss data- and image-derived properties of the intrinsic source in the context of previous 3.5 mm experiments in Section 5. In Section 6, we discuss our new constraints on theoretical models for Sgr A* and its scattering. We summarize our results in Section 7.

2. BACKGROUND

2.1. Theoretical models for Sgr A* emission

Sgr A* is a bright radio source, with a spectrum that rises with frequency until it peaks near 1 mm (e.g., Falcke et al. 1998; Bower et al. 2015). The long-standing debate on whether the radio/mm emission from Sgr A* is produced by a radiatively inefficient accretion disk or by a relativistic, compact jet present near the black hole (e.g., Narayan et al. 1995; Markoff et al. 2007; Mościbrodzka et al. 2014; Ressler et al. 2015; Connors et al. 2017; Davelaar et al. 2018; Chael et al. 2018a, and references therein) has not been resolved.

Radiative models of Sgr A* based on three-dimensional general relativistic magnetohydrodynamic (GRMHD) simulations of Kerr black hole accretion naturally combine the disk and jet scenarios. Electrons and ions are not in thermal equilibrium in the hot, diffuse Sgr A* accretion flow, therefore simulations with the same gas dynamics (determined by the ions) can have quite different appearances at 3.5 mm depending on electron thermodynamics assumptions. In particular, both the disk and jet emission dominated models can be realized within a single simulation by adopting a specific distribution for electron heating/acceleration in magnetized plasma in post-processing (e.g., Mościbrodzka & Falcke 2013). Alternatively, electron-ion thermodynamics with a specified prescription for the particle heating from dissipation can be incorporated self-consistently with the other variables in a single simulation. In this framework, Ressler et al. (2017) and Chael et al. (2018a) have shown that both jet- and disk-dominated images can be produced at 3.5 mm, depending on the underlying physical model for electron heating evolved in the simulation.

These models are mainly used to predict 1.3 mm EHT observations (e.g., Chan et al. 2015). At 1.3 mm we expect the emission to originate near the event horizon where effects such as gravitational lensing and relativistic Doppler boosting distort any emission into a ring, crescent or a spot-like shape, making any distinction between dominating emission models difficult. At 3.5 mm, we can potentially constrain the geometry and electron micro-physics of the GRMHD simulations by modeling emission maps in which the physics of accretion rather than relativistic effects shapes the source geometry.

2.2. Interstellar Scattering of Sgr A*

The index of refraction of a plasma depends on density, so density inhomogeneities in the ionized ISM lead to multi-path propagation of radio waves. The scattering is chromatic, with scattering angles proportional to the squared wavelength of a propagating wave. Because the scattering arises from density irregularities, scattering properties are stochastic by nature; their statistical properties depend on the power spectrum $Q(q)$ of density variations, where $q$ denotes a wavevector. Along many lines of sight, the scattering is well characterized using a simplified description in which the scattering material is confined within a single thin screen along the line of sight. For background and reviews on interstellar scattering, see Rickett (1990), Narayan (1992), or Thompson et al. (2017).

The line of sight to Sgr A* is particularly heavily scattered, as is evidenced by an image with a Gaussian shape and a size that is proportional to wavelength squared for wavelengths $\lambda \gtrsim 1$ cm (Davies et al. 1976; van Langevelde et al. 1992; Bower et al. 2004; Shen et al. 2005; Bower et al. 2006; Johnson et al. 2018). In addition, the scattering of Sgr A* is anisotropic, with stronger angular broadening along the east-west axis than along the north-south axis (Frail et al. 1994). The angular broadening has a full width at half maximum (FWHM) of $(1.380 \pm 0.013)\lambda^{2}_{\text{cm}}$ mas along the major axis and $(0.703 \pm 0.013)\lambda^{2}_{\text{cm}}$ mas along the minor axis, with the major axis at a position angle $81.9^\circ \pm 0.2^\circ$ east of north (Johnson et al. 2018, hereafter J18). For comparison, the intrinsic source has an angular size of $\sim 0.4\lambda_{\text{cm}}$ mas (J18), so the ratio of intrinsic size to scatter broadening is $\sim 0.3/\lambda_{\text{cm}}$ along the major axis and $\sim 0.6/\lambda_{\text{cm}}$ along the minor axis. Consequently, observations at 3.5 mm are the longest wavelengths with active VLBI for which the intrinsic structure is not sub-dominant to scattering (VLBI observations of Sgr A* at wavelengths between 3.5 mm and 7 mm are very difficult because of atmospheric oxygen absorption).

As discussed by Psaltis et al. (2018) and J18, the $\lambda^{2}$ and Gaussian scattering behavior of Sgr A* are universally expected if 1) the intrinsic source size $\theta_{\text{src}}$ is sub-dominant to the scatter broadening angle $\theta_{\text{scatt}}$, and 2)
the diffractive scale of the scattering $r_{\text{diff}} \sim \lambda/\theta_{\text{scatt}}$ is smaller than the dissipation scale of turbulence in the scattering material. Thus, even though the angular broadening size and shape are measured very precisely for Sgr A* at centimeter wavelengths, the constraints on the overall scattering properties are quite weak. The expected dissipation scale in the ISM is $10^2$\text{--}10^3$ km \cite[e.g.,][]{Spangler1990}, so the expected transition to non-$\lambda^2$ and non-Gaussian scattering \cite[i.e., when the dissipation scale is comparable to the diffractive scale for Sgr A* occurs at wavelengths of a few millimeters. Consequently, the scattering properties of Sgr A* measured at centimeter wavelengths cannot be confidently extrapolated to millimeter wavelengths. The uncertainties can be parameterized using physical models for the scattering material, which typically invoke an anisotropic power-law for the power spectrum of phase fluctuations, with the power-law extending between a maximum scale (the outer scale $r_{\text{out}}$) and a minimum scale (the inner scale $r_{\text{in}}$). In such a generalization, the scattering properties depend on a spectral index $\alpha$, and on the inner scale of the turbulence, $r_{\text{in}}$. In this paper, we use the scattering model presented in \cite{Psaltis2018} with parameters for Sgr A* determined by J18.

The discovery by \cite{Gwinn2014} of scattering-induced substructure in images of Sgr A* at 1.3 cm gives an additional constraint on the scattering properties of Sgr A*\textsuperscript{∗}. This substructure is caused by modes in the scattering material on scales comparable to the image extent (much larger than $r_{\text{diff}}$), so scattering models with identical scatter-broadening may still exhibit strong differences in their scattering substructure. The substructure manifests in the visibility domain as “refractive noise”, which is an additive complex noise component with broad correlation structure across baselines and time \cite[]{Johnson2016}. Using observations of Sgr A* from 1.3 mm to 30 cm, J18 have shown that the combined image broadening and substructure strongly constrains the power spectrum of density fluctuations. However, a degeneracy between $\alpha$ and $r_{\text{in}}$ persists, and extrapolating the strength of refractive effects to millimeter wavelengths is still quite uncertain.

Two scattering models effectively bracket the range of possibilities for Sgr A*. One model (hereafter J18) has a power-law spectral index $\alpha = 1.38$ (near the expected value for 3D Kolmogorov turbulence, $\alpha = 5/3$) and $r_{\text{in}} = 800$ km (near the expected ion gyroradius in the ionized ISM). The second is motivated by \cite{Goldreich2006,GS06}, who proposed that the scattering of Sgr A* could be caused by thin current sheets in the ISM; it has $\alpha = 0$ and $r_{\text{in}} \sim 2 \times 10^8$ km. The inner scale in this latter model is several orders of magnitude larger than originally proposed by GS06, but this larger value is required to produce the refractive noise observed at 1.3 and 3.5 cm. Both the J18 and GS06 models are consistent with all existing measurements of the angular broadening of Sgr A* and with the refractive noise at centimeter wavelengths, but the GS06 model would produce more refractive noise than the J18 model on long baselines at 3.5 mm, with even more pronounced enhancement for EHT observations \cite[by roughly an order of magnitude; see][]{Zhu2018}. While long-baseline measurements at 3.5 mm can discriminate between these possibilities, observations to-date have been inadequate for an unambiguous detection of refractive substructure at this wavelength \cite{O16, B16, B18}. New observations with ALMA joining 3.5 mm VLBI, with unprecedented resolution and sensitivity, give the opportunity for long-baseline detections of refractive noise at millimeter wavelengths that can enable discrimination between the two scattering models.

3. OBSERVATIONS AND DATA REDUCTION

Observations of Sgr A* ($\alpha_{\text{J2000}} = 17^{h}45^{m}40^{s}.0361$, $\delta_{\text{J2000}} = -29^\circ00'28''.168$) were made with the GMVA, composed of the eight Very Long Baseline Array (VLBA) antennas equipped with 86 GHz receivers, the Green Bank Telescope (GB), the Yebes 40-m telescope (YS), the IRAM 30-m telescope (PV), the Effelsberg 100-m telescope (EB), and the ALMA phased array (AA) consisting of 37 phased antennas. The observations were conducted on 3 April 2017 as part of the first offered VLBI session with ALMA (project code MB007). We recorded a total bandwidth of 256 MHz per polarization divided in 4 intermediate frequencies (IFs) of 116 channels each. The 12 h track (4 h with the European sub-array and 8 h with ALMA) included three calibrator sources: J1749+096, NRAO 530, and J1924−2914. The total integration time on Sgr A* with ALMA was 5.76 h.

The data were processed with the VLBI correlator at the Max Planck Institute for Radio Astronomy using DiFX \cite[]{Deller2011}. After correlation, reduction was carried out using the Haystack Observatory Postprocessing System\textsuperscript{1} (HOPS) supported by a suite of auxiliary calibration scripts presented in \cite{Blackburn2018}, with additional validation and cross-checks from the NRAO Astronomical Image Processing System (AIPS; Greisen2003). The HOPS software package in its current form arose out of the development of the Mark IV VLBI Correlator, see \cite{Whitney2004}. During the HOPS reduction, ALMA baselines were used to estimate stable instrumental phase bandpass and delay between right and left circular polarization relative to the other stations. ALMA or GBT baselines (depending on signal-to-noise) were used to remove stochastic differential atmospheric phase within a scan. Because atmospheric phase corrections are required on short (~second) timescales, leading to a large number of free parameters to fit, a round-robin calibration was used to avoid self-tuning: baseline visibility phases on

\textsuperscript{1} https://www.haystack.mit.edu/tech/vlbi/hops.html
derived from a least-squares solution to baseline detections where unconstrained stations were removed from the dataset. No interpolation of these fringe solutions was performed across scans as the solutions were not stable within their necessary tolerance to maintain coherence. After these phase corrections, our data have enough phase coherence to allow longer averaging times.

We performed a-priori amplitude calibration using provided telescope gain information and measured system temperatures during the observations. The heterogeneity of the stations in the GMVA required us to adopt a careful approach to the amplitude calibration. The calibration for ALMA was fully provided by the ALMA quality assurance (QA2) team (Goddi et al. 2018), and system equivalent flux densities (SEFDs) were generated with a high time cadence by PolConvert (Martí-Vidal et al. 2016). Both YS and PV measure effective system temperatures via the chopper wheel method, and thus do not require an additional opacity correction to their SEFDs. However, the rest of the array (VLBA, GB, EB) measures system temperatures via the noise diode method, requiring an additional opacity correction to account for atmospheric attenuation of the visibility amplitudes. Unfortunately, several VLBA stations observed in difficult weather conditions (ice, wind, rain), leading to limited detections on baselines to Owens Valley (OV), North Liberty (NL) and Pie Town (PT) stations. Additionally, observations at PV suffered from phase coherence losses in the signal chain during the observations, leading to poor quality data and lower visibility amplitudes on those baselines, which cannot be rescaled with a-priori calibration information. Figure 1 shows the detections and non-detections for Sgr A* (top panel) and corresponding signal-to-noise ratio of scan-averaged visibilities for Sgr A* detections. All detections beyond ∼1 Gλ are on baselines to ALMA. After a-priori calibration, we can proceed with imaging routines to determine the morphology of the calibrators and the target source.

4. IMAGING

We employ the eht-imaging library2, a regularized maximum likelihood imaging software package, to image our sources (Chael et al. 2016, 2018b). Due to the elevated noise level for the VLBA in our observations and the scattering properties of Sagittarius A*, standard imaging software packages like AIPS (Greisen 2003) or Difmap (Shepherd et al. 1995) do not offer the flexibility and necessary tools to obtain an unscattered image of the source. The eht-imaging library is a Python-based software package that is easily scriptable, flexible and modular. It is able to make images with various data products (closure phase and amplitude, bispectra, visibilities), and it contains a suite of image “regulariz-

2 https://github.com/achael/eht-imaging
ers' such as maximum entropy and sparsity regularization. The library also possesses a routine for "stochastic optics", a regularized implementation of scattering mitigation presented in Johnson (2016), making it a natural choice for our analysis. In this section we present our imaging methods for both calibrators (Section 4.1) and for Sgr A* (Section 4.2).

4.1. Calibrators NRAO 530 and J1924−2914

Both NRAO 530 and J1924−2914 appear point-like to ALMA when acting as a connected-element interferometer (\(\sim 70 \text{ k}\lambda, \sim 3 \text{ arcseconds resolution}\)), with NRAO 530 having a flux density of \(2.8 \pm 0.3 \text{ Jy}\) and J1924−2914 having a flux density of \(5.0 \pm 0.5 \text{ Jy}\) (as measured by interferometric-ALMA). Even on the angular scales probed by VLBI, both sources are very compact and stable, making them ideal for imaging. The operational difficulties and poor weather conditions at the VLBA were largely offset by the high sensitivity of ALMA. The extent of all detections is shown in the left panel of Figure 2 for NRAO 530 and Figure 3 for J1924−2914. A third calibrator was also observed, 1749+096, but only

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**Figure 2.** Left: the \((u,v)\)-coverage of NRAO 530 (symbols are as defined in Figure 1). Right: closure-only image of NRAO 530 using the eht-imaging library (Chael et al. 2018b), the contour levels start from 1.2% of the peak and increase in factors of two. The observations have a uniform-weighted beam = \((111 \times 83) \mu\text{as}, \text{PA} = 32^\circ\).

**Figure 3.** Left: the \((u,v)\)-coverage of J1924−2914 (symbols are as defined in Figure 1). Right: closure-only image of J1924−2914 using the eht-imaging library (Chael et al. 2018b), the contour levels start from 1.2% of the peak and increase in factors of two. The observations have a uniform-weighted beam = \((122 \times 88) \mu\text{as}, \text{PA} = 36^\circ\). The European stations did not observe this source.
for a few minutes with the full array, and is thus omitted from further analysis.

The large number of detections on both NRAO 530 and J1924–2914 led to a correspondingly large number of closure phases and closure amplitudes. We thus imaged both sources using only closure quantities, following the method from Chael et al. (2018b), constraining the total flux of the image to match measurements from interferometric-ALMA. We present images of the two calibrators in Figure 2 and Figure 3 (right panels). The morphology of NRAO 530 is consistent with previous observations of the source (Bower et al. 1997; Bower & Backer 1998; Feng et al. 2006; Chen et al. 2010; Lu et al. 2011b). The elongation of the J1924–2914 jet in the north-west direction at 86 GHz is consistent with mm-jet studies from previous observations at 43 GHz by Shen et al. (2002) and 230 GHz by Lu et al. (2012). These two sources are common calibrators for Sgr A*.

Table 1. Station median multiplicative gains to the visibility amplitudes.

<table>
<thead>
<tr>
<th>Station</th>
<th>Sgr A*</th>
<th>NRAO 530</th>
<th>J1924–2914</th>
</tr>
</thead>
<tbody>
<tr>
<td>BR</td>
<td>2.2±1.5</td>
<td>1.7±0.5</td>
<td>2.6±1.4</td>
</tr>
<tr>
<td>FD</td>
<td>2.2±1.2</td>
<td>1.9±1.2</td>
<td>1.8±0.7</td>
</tr>
<tr>
<td>GB</td>
<td>1.2±1.7</td>
<td>1.1±1.0</td>
<td>1.2±0.7</td>
</tr>
<tr>
<td>KP</td>
<td>2.4±0.6</td>
<td>2.2±1.2</td>
<td>2.1±0.4</td>
</tr>
<tr>
<td>LA</td>
<td>2.2±2.8</td>
<td>1.9±1.7</td>
<td>2.9±2.0</td>
</tr>
<tr>
<td>NL</td>
<td>4.6±13.3</td>
<td>4.7±9.7</td>
<td>5.0±22.6</td>
</tr>
<tr>
<td>OV</td>
<td>1.9±3.1</td>
<td>1.9±0.9</td>
<td>1.7±1.6</td>
</tr>
<tr>
<td>PT</td>
<td>11.4±2.2</td>
<td>19.3±17.8</td>
<td>12.9±36.7</td>
</tr>
</tbody>
</table>

NOTE—Median (and 95th percentile) multiplicative gains to the visibility amplitudes for common stations from the two calibration methods: 1) self-calibration of Sgr A* amplitudes below 0.75Gλ to the Gaussian source estimated from O16; B18, and 2) self-calibration of NRAO 530 and J1924–2914 observations to the images produced with closure phases and closure amplitudes. The European stations and ALMA are not shown as they are not self-calibrated for all three sources. We flagged NL and PT due to their high median gain and erratic gain solutions.

4.2. Sagittarius A*

4.2.1. Self-calibration

We obtained far fewer detections on Sgr A* than on the calibrators, and our detections also had lower signal-to-noise ratio (SNR). Consequently, we did not have enough information to synthesize images of Sgr A* using only closure quantities. Moreover, due to the suboptimal performance of the VLBA (bad weather, signal loss likely from pointing issues), additional amplitude calibration was necessary to mitigate severe signal losses at various stations.

We utilized two methods for amplitude calibration:

1. we self-calibrated to closure-only images of NRAO 530 and J1924–2914 to obtain smoothed station gain trends,

2. we self-calibrated all Sgr A* visibility amplitudes within 0.75Gλ (predominantly intra-VLBA measurements) using an anisotropic Gaussian visibility function determined by previous 3.5 mm experiments (O16; B18), with the total flux set by the interferometric-ALMA measurement.

For the second method, we used a visibility function corresponding to a Gaussian source size of 215 by 140 μas with a position angle of 80° (east of north) and a total flux density of 2.0±0.2 Jy. The choice of the Gaussian size is motivated by similar results obtained for O16 and B18 taken one month apart, showing stable source dimensions. Both these experiments had the high sensitivity of the LMT, adding north-south coverage to recover the minor axis size with greater accuracy than older experiments. In our interferometric-ALMA measurements, Sgr A* has flux density variations at the 10% level on a timescale of about 4 hours, not significantly affecting our static imaging. Note that gains were derived by self-calibration using only short baselines, but because they are station-based, they were then applied to correct visibility amplitudes on longer baselines as well.

The two methods gave comparable gain solutions, hence validating the Gaussian assumption for short-baseline measurements (Table 1 shows median multiplicative station gains to the visibility amplitudes). We flagged the VLBA stations NL and PT, which showed extreme signal loss in both methods. The GBT performed well for all three sources, so we chose to keep the original a-priori calibration. Because GBT is only linked to NL in the inner 0.75 Gλ baseline cut for Sgr A*, the derived gains for GBT introduce large variations to the ALMA-GBT amplitudes that come from difficulty locking NL gains due to its bad weather. Ignoring the self-calibration solutions gave more stable amplitudes on the ALMA-GBT baseline.

Figure 4 shows the scan-averaged visibilities for Sgr A* after self-calibration of the inner 0.75 Gλ baselines to the Gaussian source size (method 2). All detections above 1 Gλ are new measurements to ALMA. The ALMA-GBT baseline has significantly higher flux density than expected from the minor axis of the previously fitted Gaussian source size from O16 and B18. VLBA detections to ALMA show clear deviations from Gaussian behavior.
Figure 4. Noise-debiased correlated flux density of Sgr A* as a function of projected baseline length for data after self-calibrating to the Gaussian source from O16 and B18 using only baselines shorter than 0.75 Gλ. Because the a-priori calibration for the GBT was excellent (see Table 1), we did not apply the derived GBT gains. Dashed dark blue curves show expected visibilities along the major and minor axes for an anisotropic Gaussian source with FWHM of 215 μas by 140 μas (the source size from O16 and B18). All detections beyond ∼1Gλ are baselines to ALMA, and all show marked deviations from the Gaussian curves.

Figure 5. Left: the scattered image of Sgr A*, reconstructed with the second moment regularizer and stochastic optics ($\theta_{\text{maj}} = 228 \pm 46$ μas, $\theta_{\text{min}} = 143 \pm 20$ μas from LSQ). Right: the reconstructed image from stochastic optics (Johnson 2016) of the intrinsic source ($\theta_{\text{maj}} = 120 \pm 34$ μas, $\theta_{\text{min}} = 100 \pm 18$ μas from LSQ). In each panel, the ellipses at the bottom indicate half the size of the scatter-broadening kernel ($\theta_{\text{maj}} = 159.9$ μas, $\theta_{\text{min}} = 79.5$ μas, PA = 81.9°) and of the observing beam.

4.2.2. Imaging with regularized maximum likelihood

The performance of the VLBA impaired our ability to model-fit to the dataset and obtain an accurate source size estimate using only short baselines (i.e., baselines that do not heavily resolve the source). In addition, large measurement uncertainties for the visibility amplitudes on intra-VLBA baselines made image convergence difficult and unstable. We thus implemented a new imaging regularization: we constrained the second central moment of the image to match more robust measurements of the scattered source size from Gaussian model fitting to previous observations (O16; B18). If we think of the centroid (first moment) of the image as the mean position of the emission, its variance (or sec-
Figure 6. Model and reconstructed images from four example 3D GRMHD models, plotted here in linear scale. The contour levels represent 25, 50 and 75% of the peak flux. The first column shows the original model images as given from simulations: “th+κ disk” is a thermal disk model with 1% accelerated particles in a power-law (κ) distribution; “th jet” is a thermal jet model; “th+κ jet” is a thermal jet model with 10% accelerated particles in a κ distribution (Mościbrodzka et al. 2009, 2014, 2016; Davelaar et al. 2018). The inclinations of the models are given in the parentheses. The second column shows the model images scattered with the J18 scattering model: these are the images sampled to make the simulated observations. The third column shows the observed (scattered) image reconstructed with the second moment regularizer and stochastic optics, and the fourth column shows the reconstructed image from stochastic optics of the corresponding intrinsic source. In the third and fourth columns, the ellipses at the bottom indicate half the size of the scatter-broadening kernel and of the observing beam.
and large-scale refractive modes that introduce stochastic image substructure (ripples distorting the image). 

The code simultaneously solves for the unscattered image and the large-scale phase screen causing refractive scattering, while assuming a given model for the diffractive blurring kernel and the refractive power spectrum $Q(q)$ (governing the time-averaged scattering properties). In our case, we used the scattering kernel (with a size of $(159.9 \times 79.5) \mu\text{as}$, PA of $81.9^\circ$) and power spectrum (with $\alpha = 1.38$ and $r_{in} = 800 \text{km}$) from the J18 scattering model. See Johnson (2016) for a more detailed description of the method. Two iterations of stochastic imaging and self-calibration are done for convergence. We present in Figure 5 our resulting intrinsic and scattered images of Sgr A*.

4.2.3. Uncertainties of image-derived parameters

To determine the uncertainties in the imaging method and size measurements for Sgr A*, we performed imaging tests on simulated observations where the intrinsic model image was known. We tested our imaging method on four snapshots from 3D GRMHD simulations of Sgr A* at $86 \text{GHz}$ (Mościbrodzka et al. 2009, 2014, 2016; Davelaar et al. 2018), using the same sampling, coverage and noise as our observations. The model images were scattered with the J18 scattering model and sampled with our GMVA+ALMA coverage, before being imaged via the same imaging routine applied to the Sgr A* data described above.

While the imaging procedure is identical, these reconstructions do have some advantages relative to our reconstruction of the actual observations. For example, we used the ensemble-average properties of the J18 scattering model as inputs to the scattering mitigation: i.e., we assume perfect knowledge of the diffractive scattering kernel and the time-averaged power spectrum. We also measure the second moment of the scattered simulated images and use it as an exact input to the second moment regularization. Because the scattering is subdominant to intrinsic structure and because the second moment is estimated to excellent accuracy in previous experiments, we do not expect either of these effects to significantly advantage the reconstructions of simulated data.

In Figure 6 we present the original 3D GRMHD model images, the model images scattered with the J18 scattering model (as observed in the simulated observations), and the reconstructed observed (scattered) and intrinsic images from the imaging method. In Table 2 we compare the true intrinsic source sizes from the models to the intrinsic source sizes derived from the imaging routine. We determined the source size parameters using two methods: first by measuring the second central moment of the image ($Q(q)$ and deriving Gaussian parameters; and second by doing a 2D Gaussian fit with a least-squares minimization (LSQ) onto the image.
The Size, Shape, and Scattering of Sagittarius A*  

Table 2. Comparison of the true size and the derived size from imaging from synthetic datasets for four simulated images.

<table>
<thead>
<tr>
<th>Model</th>
<th>Method</th>
<th>$\theta_{\text{maj}}$ (µas)</th>
<th>$\theta_{\text{min}}$ (µas)</th>
<th>Axial ratio</th>
<th>PA (deg)</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td></td>
<td>True</td>
<td>121.0</td>
<td>97.3</td>
<td>1.24</td>
</tr>
<tr>
<td></td>
<td></td>
<td>Image</td>
<td>184.0</td>
<td>131.8</td>
<td>1.4</td>
</tr>
<tr>
<td>Th+κ disk (60°)</td>
<td>Difference</td>
<td>63.0 (0.4$\theta_{\text{beam}}$)</td>
<td>34.5 (0.1$\theta_{\text{beam}}$)</td>
<td>0.16 (0.1$\theta_{\text{beam}}$)</td>
<td>17.8 (0.6$\theta_{\text{beam}}$)</td>
</tr>
<tr>
<td></td>
<td>True</td>
<td>79.7</td>
<td>77.0</td>
<td>1.04</td>
<td>109.9</td>
</tr>
<tr>
<td></td>
<td>Image</td>
<td>101.9</td>
<td>59.6</td>
<td>1.7</td>
<td>0.8</td>
</tr>
<tr>
<td></td>
<td>Difference</td>
<td>22.2 (0.1$\theta_{\text{beam}}$)</td>
<td>17.4 (0.1$\theta_{\text{beam}}$)</td>
<td>0.66 (0.1$\theta_{\text{beam}}$)</td>
<td>69.3 ($\geq 0.4\theta_{\text{beam}}$)</td>
</tr>
<tr>
<td>Th jet (5°)</td>
<td>2nd mom.</td>
<td>True</td>
<td>112.5</td>
<td>99.0</td>
<td>1.14</td>
</tr>
<tr>
<td></td>
<td></td>
<td>Image</td>
<td>148.7</td>
<td>124.8</td>
<td>1.19</td>
</tr>
<tr>
<td></td>
<td>Difference</td>
<td>36.2 (0.3$\theta_{\text{beam}}$)</td>
<td>25.8 (0.1$\theta_{\text{beam}}$)</td>
<td>0.05 (0.02$\theta_{\text{beam}}$)</td>
<td>60.4 ($\geq \theta_{\text{beam}}$)</td>
</tr>
<tr>
<td></td>
<td>True</td>
<td>88.0</td>
<td>81.2</td>
<td>1.08</td>
<td>179.7</td>
</tr>
<tr>
<td></td>
<td>Image</td>
<td>65.5</td>
<td>51.9</td>
<td>1.26</td>
<td>158.4</td>
</tr>
<tr>
<td></td>
<td>Difference</td>
<td>22.5 (0.2$\theta_{\text{beam}}$)</td>
<td>29.3 (0.1$\theta_{\text{beam}}$)</td>
<td>0.18 (0.03$\theta_{\text{beam}}$)</td>
<td>21.3 (0.2$\theta_{\text{beam}}$)</td>
</tr>
<tr>
<td>Th jet (90°)</td>
<td>2nd mom.</td>
<td>True</td>
<td>174.0</td>
<td>65.8</td>
<td>2.64</td>
</tr>
<tr>
<td></td>
<td></td>
<td>Image</td>
<td>178.1</td>
<td>135.3</td>
<td>1.32</td>
</tr>
<tr>
<td></td>
<td>Difference</td>
<td>4.1 (0.02$\theta_{\text{beam}}$)</td>
<td>69.5 (0.5$\theta_{\text{beam}}$)</td>
<td>1.32 (0.6$\theta_{\text{beam}}$)</td>
<td>3.4 (0.3$\theta_{\text{beam}}$)</td>
</tr>
<tr>
<td></td>
<td>True</td>
<td>160.8</td>
<td>63.2</td>
<td>2.54</td>
<td>178.8</td>
</tr>
<tr>
<td></td>
<td>Image</td>
<td>130.3</td>
<td>42.4</td>
<td>3.07</td>
<td>177.1</td>
</tr>
<tr>
<td></td>
<td>Difference</td>
<td>30.5 (0.2$\theta_{\text{beam}}$)</td>
<td>20.8 (0.1$\theta_{\text{beam}}$)</td>
<td>0.53 (0.04$\theta_{\text{beam}}$)</td>
<td>1.7 (0.2$\theta_{\text{beam}}$)</td>
</tr>
<tr>
<td>Th+κ jet (90°)</td>
<td>2nd mom.</td>
<td>True</td>
<td>182.4</td>
<td>65.7</td>
<td>2.78</td>
</tr>
<tr>
<td></td>
<td></td>
<td>Image</td>
<td>177.5</td>
<td>127.6</td>
<td>1.4</td>
</tr>
<tr>
<td></td>
<td>Difference</td>
<td>4.9 (0.02$\theta_{\text{beam}}$)</td>
<td>61.9 (0.4$\theta_{\text{beam}}$)</td>
<td>1.38 (0.6$\theta_{\text{beam}}$)</td>
<td>2.1 (0.2$\theta_{\text{beam}}$)</td>
</tr>
<tr>
<td></td>
<td>True</td>
<td>166.6</td>
<td>62.9</td>
<td>2.65</td>
<td>178.7</td>
</tr>
<tr>
<td></td>
<td>Image</td>
<td>141.5</td>
<td>49.9</td>
<td>2.83</td>
<td>179.2</td>
</tr>
<tr>
<td></td>
<td>Difference</td>
<td>25.1 (0.1$\theta_{\text{beam}}$)</td>
<td>13.0 ($\pm 0.1\theta_{\text{beam}}$)</td>
<td>0.18 (0.02$\theta_{\text{beam}}$)</td>
<td>0.5 (0.1$\theta_{\text{beam}}$)</td>
</tr>
</tbody>
</table>

Note—In each case, we compute the sizes using two methods: directly from the image second central moment (“2nd mom.”), and from a 2D Gaussian fit to the image with least-squares minimization (“LSQ”). We give the absolute difference between the true and estimated values and also express the difference as a fraction of the projected beam FWHM $\theta_{\text{beam}}$ along the measured axis, or as the fraction of the propagated error from the beam-widths on both axes for the axial ratio. The uncertainty on the position angle (PA) is expressed as the fraction of one-dimensional beam blurring of the image for which the standard deviation in PA with blurring along different directions matches the difference between the true and measured PA (see text for additional details).

Next, we evaluate the difference between true and reconstructed image parameters. We sought to define an approach that quantifies these differences in a way that is related to the reconstructed image properties and the observing beam. When expressed in this way, we can use parameter errors on these reconstructed simulated images to predict uncertainties on parameters derived from our reconstructed image with data.

To this end, Table 2 expresses the difference between the true and measured source major and minor axes as a fraction of the projected beam FWHM $\theta_{\text{beam}}$ along the corresponding axis. For the axial ratio, we express the difference between the true and measured ratios as a fraction of the cumulative error from both axes (the projected beam-widths along the measured major and minor axes added quadratically).

However, while it is straightforward and well-motivated to express uncertainties on axis lengths and their ratio in terms of the observing beam, uncertainty on the position angle (PA) is more subtle. We opted to create an ensemble of beam-convolved reconstructed images and to use the scatter in the PA of the ensemble as an estimate of the PA uncertainty. The ensemble of images is constructed by convolving the single reconstructed image with an ensemble of narrow beams, sampling all position angles. Each of these beams has a major axis...
size given by the projected observing beam size along the same position angle and a minor axis size of zero. We thereby stretch the image along each direction, up to the extent of the observing beam, and examine the overall dependence of the reconstructed image on this stretching. With this approach, images that are nearly isotropic will have large PA uncertainty, while highly elongated images (relative to the beam size) will have small PA uncertainty.

In general, we find that the LSQ method fares better than the second moment method for determining the source parameters, likely due to weak extended flux in the images skewing the second moment parameters to larger values. As expected, both methods perform poorly when determining the position angle of a fairly symmetrical source, for which it remains largely unconstrained. However, for more elongated source geometry, both methods are able to accurately recover the intrinsic position angle. We adopt the LSQ method to quantify the size of Sgr A* via image-domain fitting. Although the Gaussian approximation does not describe fully our source morphology, it is suitable for comparisons to visibility-domain model fits from previous observations of Sgr A* presented in Section 5.

5. RESULTS

5.1. Intrinsic source constraints from imaging

Figure 5 shows the unscattered and scattered images of Sgr A*, as imaged following the method described in Section 4. The (uniform-weighted) beam size of the Sgr A* observations is (235 × 87) μas, with a position angle (east of north) of 53.6°. While the shorter baselines of the array (intra-VLBA, VLBA-GBT, intra-European) see primarily a Gaussian source elongated in the east-west direction, longer baselines are expected to pick up on non-Gaussian source structure or refractive noise from interstellar scattering. In this particular observation, our longest baselines are mainly north-south to ALMA (see Figure 1), where scattering has less of an effect on the source. As seen in Figure 5, left panel, the reconstructed scattered image looks very smooth, and Gaussian-like, showing no obvious refractive noise in the image. We also see a similar outcome in our imaging tests, presented in Section 4.2.3. Although the scattered images (second column in Figure 6) have visible ripples of scattering substructure, the reconstructed scattered images (third column) appear very smooth. This is likely because our GMVA+ALMA observations sample low levels of refractive noise mainly along the north-south direction, whereas our east-west sensitivity and resolution do not provide adequate detections of scattering substructure to be able to reconstruct the fine structure in the scattered images. Thus the low level of refractive noise detected on our ALMA baselines does not produce visible distortions in the reconstructed scattered image.

We present the measured source sizes using our two methods (2nd mom. and LSQ) in Table 3, along with historical measurements and estimates. The uncertainties are conservative estimates taken from the largest relative uncertainties on the parameters of simulated images for each method (see Table 2).
source geometry for size estimates and comparisons, but this may not be the correct source model. As seen in the example images (Figure 6), the true and reconstructed intrinsic images are not Gaussian, therefore this choice of parametrization is only to simplify comparisons with previous measurements and simulations. We find that our source size measurements are consistent with previous observations and indicate the source dimensions and small asymmetry are persistent across multiple years.

Lastly, we note that uncertainties in the intrinsic size caused by remaining uncertainties in the scattering kernel are quite small ($\lesssim 10\mu$as), even allowing for the full range of uncertainty on $\alpha$ and $r_\text{in}$ (J18). The reason they are small is because the scattering parameters for angular broadening are estimated to an accuracy of a few percent, and because the intrinsic structure is not subdominant to scatter broadening.

5.2. Intrinsic source constraints from closure phases

Closure phases provide an alternative and complementary assessment of source asymmetry directly from observations. They are weakly affected by refractive scattering and are unaffected by station-based calibration issues. Thus, they offer robust information on the intrinsic properties of Sgr A*.

We computed closure phases for all sources from scan-averaged visibilities. The GMVA+ALMA array contains 13 stations, yielding many triangles with a wide range of sizes. As seen in Figures 2 and 3, there are multiple long-baseline detections to ALMA on calibrators that do not appear for Sgr A* (Figure 1). We thus selected three example triangles of different sizes and orientations that are present for the two main calibrator sources (NRAO 530 and J1924−2914) and with multiple detections for Sgr A*.

We present in Figure 7 the closure phases on three representative triangles: a small intra-VLBA (LA-KP-FD) triangle; an east-west medium-sized triangle to GBT (GB-KP-FD); and a long north-south triangle to ALMA (AA-GB-FD). Although all three triangles provide robust detections for all three sources, with non-zero closure phases for the calibrators, Sgr A* closure phases remain very close to zero: the weighted mean closure phase on AA-GB-FD is $-1.1\pm 2.4^\circ$; the weighted mean closure phase on GB-KP-FD is $-1.7 \pm 1.1^\circ$; and the weighted mean closure phase on LA-KP-FD is $-1.8 \pm 1.1^\circ$. The largest closure phases on all three triangles deviate from zero by less than 3$\sigma$.

O16 and B16 detected small non-zero closure phases ($\lesssim 10^\circ$) on triangles including the highly sensitive LMT and/or GBT. These non-zero closure phases were observed on triangles not present in our GMVA+ALMA observations, and they probed different scales and directions from our new predominantly north-south triangles with ALMA. Deviations of a few degrees, as observed by O16 and B16, fall within our confidence bounds due to low signal-to-noise on VLBA baselines, and thus would not be detectable with our current observations. Moreover, the geometrical models to describe the asymmetry in B16 produce closure phases on our triangles that would be indistinguishable from zero with our current measurements. Thus, our results are consistent with previous observations of Sgr A*.

6. DISCUSSION

6.1. Constraints on the Refractive Scattering of Sgr A*

Our longest baselines heavily resolve the scattered image of Sgr A* while also providing exceptional sensitivity (especially baselines to ALMA). Therefore they are sensitive to a non-Gaussian scattering kernel (from a finite inner scale) and to “refractive noise,” which corresponds to image substructure introduced by interstellar scattering. In this section, we use our long-baseline measurements to constrain scattering models for Sgr A*.

Figure 8 shows our detected correlated flux density as a function of baseline length. The ALMA-GBT baseline, probing scales along the minor axis of the source, measures significantly higher correlated flux density than predicted from the Gaussian curves from model fitting to shorter baseline data, shown as the dark blue dashed curves in Figure 8 (O16; B18). This enhancement could either indicate non-Gaussian intrinsic structure (e.g., a compact core with a diffuse halo) or a non-Gaussian scattering kernel (requiring an inner scale $r_\text{in} \ll 1.5 \times 10^8 \lambda \approx 5000$ km). For example, the ALMA-GBT measurements are comparable to the values pre-
dicted for an anisotropic Gaussian intrinsic source combined with the J18 scattering model, which has $r_{in} = 800 \, \text{km}$, shown as the light blue dotted curves in Figure 8.

We also detect correlated flux density on baselines that are expected to entirely resolve the scattered source. Here, the enhanced flux density indicates the presence of image substructure that can either be intrinsic or scattering-induced. For scattering substructure, the signal is expected to be significantly stronger for baselines that are aligned with the major axis of the scattering (see Figure 8). The two candidate scattering models presented in Section 2.2 (with different spectral index $\alpha$ and inner scale $r_{in}$ governing the refractive noise power spectrum) predict different levels of refractive noise along both the major and minor axes of the scattering: the GS06 model predicts, on average, nearly one order of magnitude more correlated flux density on long baselines than the J18 model. However, our most sensitive detections (ALMA-VLBA/GBT) are along the minor axis of the scattering.

The mean visibility amplitude (after debiasing to account for thermal noise) on baselines longer than 1.8 G$\lambda$ is 6 mJy. Because this amplitude may contain contributions from both scattering substructure and intrinsic substructure, it only determines an upper limit on the level of refractive noise from scattering substructure. Moreover, even if there were no intrinsic substructure contribution on these baselines, the 6 mJy signal would still not directly determine the level of refractive noise because refractive noise is stochastic: the inner 95% of visibility amplitudes sampled on a single baseline over different scattering realizations will fall in the range $[0.16, 1.9] \times \sigma$, where $\sigma$ is the RMS “renormalized” refractive noise (i.e., refractive noise after removing the contributions of flux modulation and image wander, which our observations would absorb into the overall calibration; see J18).

We can tighten the constraints on refractive noise by combining samples from many baselines, although these will be correlated (see Johnson & Narayan 2016). Following the Monte Carlo approach of J18, we find that
combining baselines longer than 1.8 GA gives a 95% confidence range for the mean amplitude of refractive noise on a baseline with \((u, v) = (1.167, -1.638) \times 10^3 \lambda\) of 3-18 mJy if the 6 mJy of correlated flux density is entirely from refractive noise. For comparison, the J18 model predicts a mean refractive noise amplitude of approximately 7 mJy on this baseline, while the GS06 model predicts a mean refractive noise of 60 mJy on this baseline. Thus, the GS06 model is incompatible with our measurements. The GS06 model also significantly over-predicts the signal on our baselines oriented closer to the major axis, for which our measurements only provide upper limits (labeled black triangles in Figure 8).

If the minor axis detections are from scattering substructure, then they would represent the first detections of substructure along this axis. The presence of substructure along the minor axis requires that magnetic field variations transverse to the line of sight are not restricted to a narrow angular range (the field wander is more likely to sample all angles, but with a preference for angles that are aligned with the minor axis of the scattering). Minor axis substructure would eliminate, for example, the “boxcar” model for refractive fluctuations in Psaltis et al. (2018), which describes magnetic field wander as a uniform distribution over a limited range of angles.

6.2. Constraints on accretion flow and jet models

The intrinsic image of Sgr A* at 3 mm shown in Figure 5 allows us to discriminate between the two main classes of models that now must fit the tight source size and morphology constraints derived from both model-fitting (from previous experiments) and our image-domain measurements. We can explore a small subset of GRMHD simulations to assess possible constraints from our observables. Due to our unconstrained estimate of the PA, we opted to compare the major axis size and the asymmetry (axial ratio), which are independent of the PA of the source on the sky.

Figure 9 compares the sizes and morphology of 7/3/1.3 mm images from a sample of 3D-GRMHD simulations of either disk or jet dominated emission, at varying viewing angle with respect to the black hole spin axis, with observational constraints from current (Table 3) and previous observations of Sgr A* (see Table 4 in J18). Model images are generated by combining the dynamical model with ray-tracing and radiative transfer using only synchrotron opacities. To estimate the size of the radiating region in model images we calculate the eigenvalues of the matrix formed by taking the second central moment of the image on the sky (i.e., the length of the “principal axes”, Hu 1962).

Producing a ray-traced image from single-fluid GRMHD simulations requires providing the electron distribution function (hereafter eDF), which is unconstrained in traditional single-fluid GRMHD simulations. Thermal disk models (“Th disk” in Figure 9) assume a thermal, Maxwell-Jüttner eDF and a proton-to-electron temperature ratio\(^3\) \(T_p/T_e = 3\) everywhere (motivated by results of Moscibrodzka et al. 2009). Models denoted as “Th jet” have \(T_p/T_e = 20\) in the accretion disk and \(T_p/T_e = 1\) along the magnetized jet, which allows the jet to outshine the disk at mm-wavelengths (this jet model has been introduced by Moscibrodzka et al. (2014, 2016)). There is a family of models in-between these two extreme cases. In the models denoted as “Th+κ disk” the eDF is hybrid: 1 percent of all electrons are non-thermal, described by a κ eDF. Adding non-thermal electrons to the emission model results in more extended disk images as the non-thermal electrons produce a diffuse “halo” around the synchrotron photosphere. The “halo” contributes to the disk size estimates (Mao et al. 2017). Finally, the “Th+κ jet” model is a 3D version of the κ–jet model introduced by Davelaar et al. (2018) with 10 percent of jet electrons in a κ eDF. In both hybrid models the κ parameter is set to 4 (see Davelaar et al. 2018, for details).

We find that only disks with a hybrid eDF at moderate viewing angles and both jet-models with viewing angles \(\lesssim 20^\circ\) are consistent with 1.3 and 3 mm sizes and asymmetry constraints. This limit is consistent with the recent low-inclination constraints derived from orbital motions in near-infrared Sgr A* flares by Gravity Collaboration et al. (2018b) observed with the GRAVITY instrument. In the tested models, the dependency of the source sizes as a function of observing wavelength is shallower than the \(\theta \sim \lambda\) dependency estimated from multi-wavelength observations of Sgr A* (Figure 13 in J18). Hence none of the models that satisfy 1.3/3 mm source sizes can account for the 7 mm source size.

Although GRMHD simulations of black hole accretion are inherently time-variable, causing the size and asymmetry to fluctuate in time, these changes are smaller than 10 percent. We conclude that current models under-predict the observed 7 mm emission size, even when accounting for size and asymmetry fluctuations in time. In simulations, the 7 mm photons are emitted from larger radii where the accretion flow structure is less certain due to lower grid resolution, the initial conditions (finite size torus with pressure maximum at \(r = 24 \, GM/c^2\)) and boundary conditions of the simulation that only allow for plasma outflows. These issues as well as the electron acceleration should be addressed by future radiative GRMHD simulations of Sgr A*.

\(^3\) Standard GRMHD simulations provide only the fluid pressure, which is dominated by the protons. In a perfect fluid, the pressure in a grid zone gives a proton temperature. For strongly sub-Eddington accretion flows with \(L_{\mathrm{bol}}/L_{\mathrm{Edd}} \approx 10^{-8}\), protons and electrons are not necessarily well coupled by Coulomb collisions. In these GRMHD simulations the electron temperatures are not self-consistently computed but they are essential in calculating synchrotron emission. The electron temperature is parameterized by a coupling ratio, \(T_p/T_e\), between the proton and electron temperature.
Figure 9. Intrinsic size and asymmetry (axial ratio) estimates from observations of Sgr A* at 1, 3 and 7 mm vs. theoretical predictions based on 3D GRMHD simulations of black hole accretion flows. Line color encodes the wavelength of observation and the bands are size and asymmetry bounds from model-fitting (J18). The upper and lower size and asymmetry image-domain bounds from this work are shown as solid magenta lines. Data constraints at 1 mm extend to a lower asymmetry bound of 1.0. Various line types correspond to models with varying prescriptions for electron acceleration and disk/jet dominated flows generated at each wavelength: “th” for a purely thermal disk or jet dominated emission model, “th+κ” for a thermal model with accelerated particles (1% for disk and 10% for jet) in a power-law (κ) distribution (Mosibrodzka et al. 2009, 2014, 2016; Davelaar et al. 2018). Left: Intrinsic source sizes as a function of the viewing angle. Right: Intrinsic asymmetry (axial ratio) as a function of the viewing angle.

Figure 10. Intrinsic size and asymmetry (axial ratio) estimates from observations of Sgr A* at 1, 3 and 7 mm vs. theoretical predictions based on 3D GRMHD simulations of black hole accretion flows. Line color encodes the wavelength of observation and the bands are size and asymmetry bounds from model-fitting (J18). The upper and lower size and asymmetry image-domain bounds from this work are shown as solid magenta lines. Data constraints at 1 mm extend to a lower asymmetry bound of 1.0. Various line types correspond to models with varying prescription for electron heating and black hole spin generated at each wavelength: “H” for the Howes turbulent cascade prescription, “R” for the Rowan magnetic reconnection prescription, “Lo” for a non-spinning black hole, and “Hi” for a black hole with a dimensionless spin of 0.9375 (Howes 2010; Rowan et al. 2017; Chael et al. 2018a). Left: Intrinsic source sizes as a function of the viewing angle. Right: Intrinsic asymmetry (axial ratio) as a function of viewing angle.
We also explored another set of 3D simulations from Chael et al. (2018a), performed with the two-temperature, radiative GRMHD code \textsc{Koral} (Sadowski et al. 2013, 2014, 2017, see Figure 10). Unlike the simulations presented in Figure 9, where the electron temperature (and potential non-thermal component) is assigned to the simulation in post-processing, \textsc{Koral} evolves the electron temperature throughout the simulation self-consistently with contributions from radiative cooling, Coulomb coupling, and dissipative heating. While the physics of radiation and Coulomb coupling is well understood, the dissipative heating of electrons and ions is governed by unconstrained plasma microphysics that occurs at scales far smaller than the grid scale of the simulation.

Chael et al. (2018a) investigated two different physical prescriptions for the electron dissipative heating. The first prescription is the Landau-damped turbulent cascade model of Howes (2010). Since this prescription primarily heats electrons in regions where the plasma is highly magnetized, it produces prominent emission from the jet and outflow of the GRMHD simulations at 3.5 mm (see also Ressler et al. 2017). The other prescription for electron heating investigated in Chael et al. (2018a) is based on particle-in-cell simulations of particle heating from magnetic reconnection presented in Rowan et al. (2017). This prescription heats electrons and ions equally and only in highly magnetized regions, resulting in cooler jet regions with less emission than the disk. In total, Chael et al. (2018a) presented four simulations spanning the two heating prescriptions considered (“Howes” or “H” for the turbulent cascade prescription of Howes 2010 and “Rowan” or “R” for the reconnection prescription of Rowan et al. 2017) and two values of the dimensionless black hole spin (\(a = 0\) for “Lo”, and \(a = 0.9375\) for “Hi”).

Figure 10 shows that all four models presented in Chael et al. (2018a) fit the 1.3 mm constraints and mostly fit the 3 mm image-domain constraints. However, only the H-Hi and R-Lo models fit the model-fitting 3 mm range at moderate viewing angles, and all models fail to match 7 mm constraints. However, these simulations were only run over a relatively short time, and inflow equilibrium in the disk was only established up to \(\sim 20 \, R_{Sch}\), while the 7 mm emission extends to \(\sim 35 \, R_{Sch}\). To accurately compare the predictions from these two heating models with predictions at 7 mm and longer wavelengths, the simulations will have to be run longer using initial conditions adapted to producing an accretion disk in equilibrium past 20 \(R_{Sch}\).

Figure 11 demonstrates the plausible range of intrinsic source sizes vs. asymmetries at 3 mm for all of the models we have explored. Here it is evident which models fall into the permitted region. Given that our modeling does not involve any detailed parameter fitting, the agreement between models and observables is encouraging. Disk and jet models with different heating prescriptions are also likely to have distinct polarimetric characteristics that can be compared to observables (e.g., Gold et al. 2017; Mościbrodzka et al. 2017).

Furthermore, we can directly compare closure phases from the different models with those presented in Section 5. Closure phases observed are an additional robust criterion to discriminate between models: they are independent of imaging assumptions, the beam of the observations, and scattering effects. In Figure 12 we compare the scan-averaged closure phases from Sgr A* for the three representative triangles to four example models: the thermal+\(\kappa\) disk model at an inclination of 60° and the thermal jet model at an inclination of 5°, which fit the major axis and asymmetry bounds given by the 3.5 mm observations; and the thermal+\(\kappa\) jet model and thermal-only jet model, both at an inclination of 90°, which do not fit the 3.5 mm bounds. We simulated observations of the four different models with the same stations and coverage as our GMVA+ALMA dataset and compare the closure phases for the original model images (Figure 12; top panel), for the model scattered with the J18 refractive scattering (center panel), and for the “ensemble average” models scattered only with the scattering kernel (no refractive noise; bottom panel). We find that for the small and medium triangles it is very difficult to distinguish between models as they all have closure phases near zero, similar to our measurements (Fraga-Encinas et al. 2016). However, for the large triangle (ALMA-GBT-FD), two models show
strong non-zero closure phases: the thermal+κ and the thermal-only jet models at 90° inclination. Interestingly, these are also the example models that do not fit the intrinsic asymmetry and size bounds from 3.5 mm. We also find that interstellar scattering as modeled by J18 does not strongly affect intrinsic closure phase: for both the ensemble average and fully scattered cases, the two jet models at 90° inclination clearly deviate from what is measured on the largest triangle. The Howes and Rowan models are omitted from the comparisons in Figure 12 for clarity, as they are all very symmetrical and compact: their closure phase behavior is similar to the thermal+κ disk and the thermal jet models nearly or fully pointed along the line of sight.

While our comparisons to simulations are limited to a handful of GRMHD models, they demonstrate the strong constraints provided by multi-wavelength measurements of size, shape and point-symmetry of Sgr A*.

7. SUMMARY

We have presented observations of Sgr A* using ALMA in concert with the GMVA at 86 GHz. These are the first observations to use ALMA as part of a VLBI array, improving the angular resolution for observations of Sgr A* at this frequency by more than a factor of two. The improved resolution and sensitivity have allowed us to reconstruct an intrinsic image of Sgr A* for the first time at this frequency, which is also the first image of Sgr A* for which the scattering is subdominant to intrinsic structure. We find that the intrinsic image of Sgr A* has an asymmetry (axial ratio) of 1.2^{+0.3}_{-0.2} and a major axis of 120 ± 34 μas, although we cannot constrain the position angle because of the highly symmetric intrinsic source.

We have demonstrated that the geometrical properties of the intrinsic image and observed closure phases tightly constrain accretion flow models onto Sgr A*. Our measurements require models to have symmetrical morphology, 86 GHz radio emission spanning 12 ± 3.4 Schwarzschild radii, and closure phases close to zero on the triangles sampled in our observation. For the eight theoretical simulations we have considered at 3.5 mm, our data are compatible with disk models at all inclinations and jet models fully or nearly pointed along the line of sight. None of the simulations we consider is able to simultaneously match size and asymmetry limits from 1, 3, and 7 mm observations due to the relatively small domain simulated by state of the art 3D GRMHD models.

While GRMHD models are promising to describe emission near the horizon, semi-analytical models for the accretion flow and jet can be more readily extended to larger domains (e.g., Broderick et al. 2016; Gold et al. 2017; Pu & Broderick 2018). In addition, it is more straightforward to explore parameter dependencies for semi-analytic models. The model of Broderick et al. (2016) is compatible with our 3.5 mm size and asymme-

Figure 12. Scan-averaged closure phases for Sgr A* on three triangles (LA-KP-FD, GBT-KP-FD, ALMA-GBT-FD) with predictions for a thermal+κ-distribution disk model (th+κ disk, $i = 60^\circ$), thermal+κ-distribution jet model (th+κ jet, $i = 90^\circ$) and thermal jet model (th jet, $i = 5^\circ$ and $i = 90^\circ$), where $i$ is the inclination. Each model is shown without scattering (top), with ensemble-average scattering (center), and with a single realization of scattering (bottom). Note that ensemble-average scattering does not affect closure phase, and even a single realization of the scattering has little effect on the closure phases for these triangles.
try estimates. Exploring whether these models can be compatible with the full set of multi-wavelength size and asymmetry constraints for Sgr A* is a promising avenue for continued study.

In addition to the overall image morphology, we have discovered non-Gaussian structure along the minor axis of Sgr A*, hinting at either a non-Gaussian intrinsic source or a non-Gaussian scattering kernel. Comparisons of the observed visibility amplitudes against two scattering models showed that the scattering model presented by Goldehr & Sridhar (2006) over-predicts the correlated flux density on long baselines to ALMA (1.8-2.4 G\text{A}). This model also overpredicts the flux density on east-west baselines longer than 1 G\text{A}. Thus, this model for the scattering of Sgr A* is conclusively ruled out by our observations. The exclusion of the GS06 model shows that refractive scattering is likely to weakly affect 1.3 mm images with the EHT.

The scattering model presented by Johnson et al. (2018), on the other hand, predicts comparable levels of refractive noise to the excess flux density we have observed on baselines above 1.8 G\text{A}. However, using our single observation with ALMA, we cannot conclusively determine whether those detections are entirely due to refractive noise or if they are a combination of intrinsic source structure and scattering substructure. Continued observations of Sgr A* will elucidate these questions, including deeper VLBI observations at 22 and 43 GHz to better estimate the inner scale from the shape of the scatter-broadening kernel (e.g., Zhao et al. 2018), and additional GMVA+ALMA observations that will sample different realizations of the scattering screen.

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