The FRATS project: real-time searches for fast radio bursts and other fast transients with LOFAR at 135 MHz

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Received 21 December 2017 / Accepted 16 October 2018

ABSTRACT

Context. In the previous decade, two new classes of fast radio transients were detected: the Galactic, rotating radio transients (RRATs) and the extragalactic fast radio bursts (FRBs). If the detectable emission of these objects extends to lower radio frequencies, the LOw Frequency ARray (LOFAR) is ideally suited to seek and localize these transients at frequencies of 10–250 MHz. This is due to LOFAR’s sensitivity, diverse beamform capabilities, and transient buffers for the individual elements that allow post-event imaging of events, potentially at arcsecond resolution.

Aims. Our aim is to identify and localize pulses at frequencies below 250 MHz and, in the case of nondetections, derive upper limits on the sky and volume rates of FRBs.

Methods. A real-time search program for fast radio transients is installed on the LOFAR systems which runs commensally with other observations, and uses the wide incoherent LOFAR beam (11.25 deg² at 150 MHz). Buffered data from hundreds of dipoles are used to reconstruct the direction and polarization information of the event, and to distinguish between celestial, terrestrial, and instrumental origins.

Results. Observations were taken covering either the frequency range 119–151 MHz or in four frequency bands, each of 2 MHz in width, centered at 124, 149, 156, and 185 MHz. A first pilot survey covered a range of dispersion measures (DM) below 120 pc cm⁻³, focusing on Galactic sources, and resulted in an upper limit on the transient rate at LOFAR frequencies of less than 1500 events per sky per day above a fluency of 1.6 kJy ms for an 8-ms pulse. A second pilot survey covered a range of DMs below 500 pc cm⁻³, focusing on extragalactic sources to about 1 Gpc, and resulted in an upper limit of 1400 events per sky per day above a fluency of 6.0 kJy ms for an 8-ms pulse. Using a model for the distance-DM relationship, this equates to an upper limit of 134 events per Gpc³ per day.

Key words. surveys – pulsars: general – instrumentation: interferometers – techniques: high angular resolution

1. Introduction

The study of fast radio transients, or subsecond dispersed pulses, is a field that has been rediscovered over the past decade. This has led to the identification of rotating radio transients (RRATs, McLaughlin et al. 2006), pulsars that are more easily detectable through their individual pulses than by their average emission profile (Burke-Spolaor et al. 2013), and fast radio bursts (FRBs; Lorimer et al. 2007; Thornton et al. 2013), that are highly dispersed pulses from an extragalactic origin.
For both of these source classes, localization is an important part of unraveling the nature of their emission. For RRATs in fields with many high-energy sources, a precise localization is important for determining the X-ray or gamma-ray source to which they belong (Burke-Spolaor et al. 2013). Fast radio bursts could provide a probe to study the intergalactic medium, for example to identify missing baryons (Deng & Zhang 2014; McQuinn 2014). For this, a host galaxy and corresponding redshift need to be determined. Localizing FRBs to within a host-galaxy can help us understand what sources could be responsible for the emission itself (Bassa et al. 2017). Additional information may come from observing FRBs and RRATs at lower frequencies. The high dispersion measure (DM, the integrated column density of free electrons along the line of sight, see Sect. 2.2 for more detail) of FRBs is caused by the contribution from the interstellar medium of our galaxy, the intergalactic medium, and the interstellar medium of the host galaxy. Each of the three regions could in principle be the main contribution of the high dispersion: for instance the intergalactic medium, an ionized medium around the source, or a cloud of ionized material in between the source and the observer. A cloud of ionized material has not been detected in the Milky Way for the first known FRB (Lorimer et al. 2007), but this explicit check is not performed/published for all FRBs (e.g., Thornton et al. 2013; Champion et al. 2016). An ionized medium around the source has been suggested for two FRBs: to explain either the scattering and Faraday rotation of FRB110523 (Masui et al. 2015) or the steep spectrum of FRB121102 (Kulkarni et al. 2015). In both cases, the bursts are still thought to be extragalactic, as was afterwards proven for FRB121102 (Tendulkar et al. 2017). If most of the DM contribution is because of the intergalactic medium, the FRBs are placed at redshifts of 0.2–1 and must be intrinsically very bright (e.g., $10^{38}$ erg for FRB121102 at $z = 0.19273(8)$; Tendulkar et al. 2017).

The initial single pulse nature observed for FRBs suggested a cataclysmic scenario; for example, evaporating black holes (Rees 1997), coalescing neutron stars (Hansen & Lyutikov 2001), core-collapse supernova (Egorov & Postnov 2009), and the collapse of a supra-massive rotating neutron star (or “Blitzar”, Falcke & Rezzolla 2014).

An exception to this scenario is the repeating FRB121102 (Spitler et al. 2014), where other models are required to explain the repetitions. These models include collisions between neutron stars and asteroids (Geng & Huang 2015; Dai et al. 2016), soft gamma-ray repeaters (Popov & Postnov 2007), magnetars (Popov & Postnov 2013; Kulkarni et al. 2014), and signals enhanced by pulsar-orbiting bodies (Mottez & Zarka 2014; a repeating model is in preparation). As repetitions have not been found for other FRBs, it is possible that cataclysmic and repeating FRBs form two different classes of objects.

The recurrence of FRB121102 made its localization possible at a high angular resolution (Chatterjee et al. 2017; Marcote et al. 2017). Optical observations identified the host to be a dwarf galaxy at a redshift of $z = 0.19273(8)$, demonstrating its extragalactic origin (Tendulkar et al. 2017).

The first FRBs were detected at 1.4 GHz by the Parkes Radio Telescope (Lorimer et al. 2007; Thornton et al. 2013; Champion et al. 2016), and later also by Arecibo (Spitler et al. 2014) and ASKAP (Bannister et al. 2017). Since then, searches have also been performed at lower frequencies with several detections at around 800 MHz: one FRB by the GBT (Masui et al. 2015), three by the Molonglo telescope (Caleb et al. 2016a), and at least one by CHIME (Boyle & CHIME/FRB Collaboration 2018). Searches at even lower frequencies using the GBT (Chawla et al. 2017, 350 MHz), Arecibo (Deneva et al. 2016, 327 MHz), LOFAR (Coenen et al. 2014; Karastergiou et al. 2015, 145 MHz) and the MWA ( Tingay et al. 2015; Rowlinson et al. 2016, 154 + 182 MHz) only set upper limits on the FRB rates.

Despite the high rates reported ($6.3 \times 10^3$ FRBs sky$^{-1}$ day$^{-1}$; Champion et al. 2016), only about 40 FRB sources have been discovered so far (Petroff et al. 2016, FRBCAT1). This is mainly due to the limited field of view of the telescopes used. New techniques, such as phased array feeds (e.g., the Bannister et al. (2017) study that used ASKAP data) and aperture arrays, may increase the detection rate significantly.

FRBs have been observed in a range of pulse durations and DMs. Of the first 29 verified FRBs in FRBCAT, the shortest FRB has a width of 0.35 ms. There are 4 FRBs with a width smaller than 1 ms, 15 with a width of 1–4 ms, 6 with a width of 4–8 ms, and 4 with a width of more than 8 ms. These widths are the measured duration and can be intrinsically narrower, but due to propagation and instrumental effects, can be smeared out over a longer period giving the observed duration. Instrumental effects are known to cause DM smearing due to the channelization of the data used by low-frequency surveys. The measured DMs for these 29 FRBs range from $176.4 \text{ pc cm}^{-3}$ to $2596.1 \text{ pc cm}^{-3}$, with 6 FRBs having a DM below 500 pc cm$^{-3}$ and a further 3 in the 500–600 pc cm$^{-3}$ range.

The localization of FRBs is important to help describe their origins but this information is often lacking. In the case of the repeating FRB, its localization was accomplished using sensitive single-dish telescopes and interferometers on a local or even global scale (Marcote et al. 2017). For non-repeating FRBs, localization is more difficult and has not yet been demonstrated. One possible way to achieve this is to have simultaneous interferometric and beamformed observations at similar frequencies. Non-simultaneous observations are also possible by triggering an interferometer working at a lower frequency than the detecting telescope. To this end, the LOw Frequency ARray (LOFAR; operating at 10–250 MHz; van Haarlem et al. 2013) is a telescope of interest as it is capable of both beamforming and interferometry, and has a wide field of view (11 square degrees per beam at 150 MHz), meaning that it can be used for both strategies. Here we present a real-time search strategy using LOFAR aimed at detecting and localizing FRBs.

The outline of this paper is as follows. Section 2 describes LOFAR and the FRATS project. Sect. 3 describes how limits are derived from the observations while Sect. 4 presents the results of the measurements, including upper limits on FRBs. This limit is compared with other measurements and predictions in Sect. 5. A conclusion is presented in Sect. 6.

2. The FRATS project

The aim of the Fast Radio Transient Search (FRATS) project is to search for individual outbursts of transient radio emission such as FRBs and RRATs and to localize them. An aperture array such as LOFAR can do this by combining time-domain methods to detect transients using a subset of the array and imaging techniques for localization with the entire array. FRATS consists of custom-written real-time triggering algorithms using streaming beamformed data, and the use of off-line imaging techniques

1 http://frbcat.org; we note that not all parameters, e.g., regarding scattering, are displayed by default, but they can be selected by clicking “visible columns”.

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on the buffered data from individual tiles of the LOFAR stations to obtain a localization. The initial focus is on dispersed pulses of 2–128 ms in length and a fluence of the order of 1 kJy ms.

A brief introduction to LOFAR, the real-time trigger, and the off-line imaging techniques is given below, followed by an introduction to the setup of pilot surveys. The details of the analysis pipelines are described in ter Veen (2015, hereafter TV15). This paper presents the results of the first three pilot surveys. Two surveys are used to set limits on the rate of FRBs at low frequencies and to give predictions for further observations. The third survey demonstrates the feasibility of commensal observing for the FRATS project.

2.1. LOFAR

LOFAR is a very flexible radio telescope as most of the signal processing is digital. LOFAR consists of stations separated by distances from less than 100 m to over 1000 km. Each station consists of fields with 48–96 antennas that can be pointed in multiple directions at once. The signals from the different stations can be combined in different ways.

The specific features of LOFAR used for this project are the ability to create incoherent array beams with a large field of view, the ability to form these beams in parallel during other observing modes, and the ability to store the raw signal from each of the thousands of antennas in ring buffers known as transient buffer boards (TBBs). The ability to do commensal observing allows for a large duty cycle. The TBB data contain the last 5.2 (previously 1.3) seconds of the observation as raw voltages, which can be read out to study transient events in great detail. So far they have mainly been used for cosmic ray research (e.g., Schellart et al. 2013; Buitink et al. 2016), but this research uses them for sky localization of fast radio transients and detailed analysis of signals (TV15, Sect. 4). For the case of FRBs, localization is very important to identify host galaxies, and thus redshifts and energies (Tendulkar et al. 2017).

2.2. The real-time triggering algorithm

The FRATS real-time triggering algorithm consists of four steps: radio-frequency interference (RFI) mitigation, dedispersion into four or five sub-bands, pulse searching in these sub-bands, and a coincidence trigger across the sub-bands. It was designed to trigger with very low latency and to have a low false-detection rate. The trigger time is close to 3 s: that is, 1 s to obtain the data at the correlator, 1 s to beamform the data, and 1 s to analyze them in the FRATS pipeline. Occasionally, the process takes longer, for example due to data containing a lot of RFI. To make sure the process runs close to real-time, the data are analyzed in chunks of typically five-minute blocks. This ensures that, if this chunk is delayed, the next chunk may still run in real-time. In this way the raw data are still within the five-second TBB buffer.

All steps of the triggering algorithm are described in detail in TV 15 (Sects. 3.3 and 5.2). Here only a short description is given of the four steps:

1. The RFI mitigation removes narrow-band interference by assuming the data are Gaussian in each channel and flagging the channels that deviate from that. It also flags wide-band local transient events that show no dispersion, but are visible simultaneously in at least two out of four sub-bands.

2. The dedispersion algorithm corrects for the dispersive delay induced by free electrons on the arrival time of radio waves. The number of free electrons is referred to as the DM. The DM is given by DM = ∫ n_e(t)dt with n_e the number density of free electrons along the path between the source and the observer. The delay ∆t between signals arriving at frequency ν_1 and ν_2, both in gigahertz, is calculated as

\[ \Delta t \approx 4.15 \text{ ms} \left( \frac{1}{\nu_1^2} - \frac{1}{\nu_2^2} \right) \tag{1} \]

The DM is different for each pulsar and transient burst, and therefore a search over this parameter is performed. Incoherent dedispersion is applied in five separate sub-bands of 6.25 MHz. The dispersive correction is applied at the integer sample level, for example, 2 ms. The five sub-bands are used for three reasons: to provide a coincidence trigger (step 4) that significantly reduces the false trigger rate, for dedispersion efficiency as a wider band needs more DM trials, and to match the sensitivity of the TBB data analysis, which is limited by the bandwidth in the five-second buffer for the high-DM pulses.

3. Each of these sub-bands is searched for a signal above a threshold, over different integration times, using a boxcar profile. The threshold is the average +Nσ, where σ is the standard deviation in each sub-band (typically N = 7). Outliers are not taken into account when calculating the average and standard deviation.

4. Lastly, a coincidence algorithm checks that three out of five sub-bands trigger within a time window of 200 ms, allowing for a delay between the sub-bands caused by the offset between trial DM and physical DM. In theory, a smaller window for this is possible. The coincidence trigger cuts the false trigger rate from over a thousand triggers per hour to a rate of one per hour. This is essential for a real-time trigger system that uses a TBB data read-out, as the read out takes from 30 min to 3 h and produces a data volume of up to 8 TB per event.

Because of the coincidence algorithm, the triggering is most sensitive to broadband pulses. This is the case in general, as narrowband pulses integrated over a larger frequency range will reduce the sensitivity. FRBs that show a particular narrowband structure can be missed if only one or two sub-bands are triggered. This effect is reduced by requiring that three instead of all five sub-bands are triggered, such that an on-off-on-off-on pulse will also trigger. Most FRBs show a broadband spectrum, but FRB 121102 is known to emit over a limited frequency range, which is different per pulse. At 3 GHz, this range is 290–690 MHz (Law et al. 2017), thus much larger than the 6 MHz bandwidth used in this survey. It is, however, not known what the behavior would be at low frequencies. If it scales as ∆ν ∼ ν^{−4.4} like scintillation (Cordes et al. 1985), the bandwidth at 150 MHz would be ~1 kHz, much smaller than the 6 MHz bandwidth, and thus not a problem for the coincidence algorithm.

2.3. Off-line analysis and localization

Upon triggering, the TBBs are frozen. The astronomer, alerted by e-mail, inspects the beamformed data by eye to verify that the trigger is from a real astrophysical source. If the data are interesting, the TBB is read out to disk for off-line analysis. For the full 5 s of data the read-out currently takes 3 h. By using a parallel read-out, this may be reduced to 30 min in the future. The raw TBB data can be used to create pointings
in any direction, though above 100 MHz it is mostly sensitive within the tile beam and side lobes. A high-resolution image is created, using long-baseline stations to find its precise location. In principle, it is possible to obtain up to arcsecond resolution if good (ionospheric) calibration can be achieved when adding the international LOFAR stations. Given the long read-out time, only the first pulse of an RRAT or repeating FRB can be localized using the TBB data. However, reading out the TBB data does not stop the observation and subsequent pulses would still be detectable in the beamformed data, as long as the source is still being observed. The long duration of LOFAR observations (1 h for Pilot A and B, and 8 h for a typical interferometric observation) gives a high probability of observing repeating pulses in a commensal survey.

2.4. Analysis setup
The first FRATS pilot surveys ran commensally during observations of the LOFAR tied array all-sky survey (LOTAAS). The three incoherent array beams already produced by the survey at 119–151 MHz were used. Data were recorded for 3 h per pointing. The data were analyzed in 5 sub-bands of 512 channels of 12.207 kHz, then downsampled from 81.92 µs to 491.52 µs and further downsampled for the analysis to 2 or 4 ms. Data were analyzed in blocks of 3–10 min, with the majority of blocks being 5 min in duration. There were two different setups, Pilot A and B, whose settings are displayed in Table 1. Pilot B used a DM range of 0–500 pc cm$^{-3}$, while the upper DM of Pilot A was variable, depending on the available compute power, with 3, 11, 12, and 10 observations using a DM range of 0 to 70, 90, 110, or 120 pc cm$^{-3}$, respectively. These ranges were chosen according to the maximum amount of data that could be stored in the TBBs (1.3 s at that time) that still allowed for enough bandwidth to localize sources. An upgrade of the TBBs to 5 s allowed the larger DM range to be searched. The DM step for pilot A was 0.3 pc cm$^{-3}$ and the data were first downsampled to a 1.99608 ms time resolution. Pilot B used a DM step of 1.0 pc cm$^{-3}$ with the data downsampled to 3.99216 ms. The dedispersed time series were searched for pulses, using sliding windows between 2 and 16 ms for the first setup and between 4 and 128 ms for the second setup with power-of-two steps. Pilot A observed between 2013-01-16 and 2013-03-07 and Pilot B between 2013-08-09 and 2014-04-09.

In addition, Pilot C was completed with a different setup. Pilot C is presented to demonstrate the commensal observing capability during interferometric observations and is not used to derive limits on the rate of FRBs. An incoherent array beam was formed parallel to observations of the Radio Sky Monitor (Fender et al. 2008) project using all available stations. This is a 24-h zenith observation that searches for transients in the imaging domain on second to minute timescales, and on even longer timescales between epochs. Observations were taken on 2014-01-15 and 2014-01-16. It uses 11-min observation of six fields at declinations +50.94°, +52.90°, and +54.86°, each separated by a two-minute calibrator observation. Each field is observed twice. The observations are performed in four frequency bands of 2 MHz width centered at 123.9, 148.9, 156, and 184.9 MHz, respectively. The FRATS trigger ran on two parts of 5 min for each observation. The DM range covered was 0–500 pc cm$^{-3}$, in steps of 1 pc cm$^{-3}$, and the trigger threshold was 7σ. This is, to our knowledge, the first survey that used beamforming and imaging techniques to search for transients of millisecond and minute duration, simultaneously.

### Table 1. Observation and trigger properties.

<table>
<thead>
<tr>
<th>Property</th>
<th>Pilot A</th>
<th>Pilot B</th>
</tr>
</thead>
<tbody>
<tr>
<td>Incoherent array beams</td>
<td>3</td>
<td></td>
</tr>
<tr>
<td>Frequency range (MHz)</td>
<td>119–151</td>
<td></td>
</tr>
<tr>
<td>Pointing duration (h)</td>
<td>1</td>
<td></td>
</tr>
<tr>
<td>Pointings</td>
<td>35</td>
<td>83</td>
</tr>
<tr>
<td>Effective observing time (beam h)</td>
<td>68.51</td>
<td>98.76</td>
</tr>
<tr>
<td>Frequency resolution (kHz)</td>
<td>12</td>
<td></td>
</tr>
<tr>
<td>Time resolution (data) (ms)</td>
<td>0.5</td>
<td></td>
</tr>
<tr>
<td>Time resolution (search) (ms)</td>
<td>2</td>
<td>4</td>
</tr>
<tr>
<td>Search width (ms)</td>
<td>2,4,8,16</td>
<td>4,8,16,32,64,128</td>
</tr>
<tr>
<td>Station configuration</td>
<td>Superterp$^{a}$</td>
<td>4.77$^{a}$</td>
</tr>
<tr>
<td>FWHM 1 beam 119 MHz (zenith)</td>
<td>3.78°</td>
<td></td>
</tr>
<tr>
<td>FoV 1 beam 119 MHz</td>
<td>17.9 deg$^{a}$</td>
<td></td>
</tr>
<tr>
<td>DM range (pc cm$^{-3}$)</td>
<td>0</td>
<td>10</td>
</tr>
<tr>
<td>Minimum trigger DM (pc cm$^{-3}$)</td>
<td>5 or 10</td>
<td></td>
</tr>
<tr>
<td>DM step (pc cm$^{-3}$)</td>
<td>0.3</td>
<td>1.0</td>
</tr>
<tr>
<td>Maximum DM (pc cm$^{-3}$)</td>
<td>70–120</td>
<td>500</td>
</tr>
<tr>
<td>Sub-band bandwidth (MHz)</td>
<td>6.25</td>
<td></td>
</tr>
<tr>
<td>Number of sub-bands</td>
<td>5</td>
<td></td>
</tr>
<tr>
<td>Sub-bands required to trigger</td>
<td>3</td>
<td></td>
</tr>
<tr>
<td>Coincidence window (ms)</td>
<td>2 × 100</td>
<td></td>
</tr>
<tr>
<td>Single sub-band threshold (sigma)</td>
<td>7</td>
<td></td>
</tr>
</tbody>
</table>

**Notes.** Pilot B values are only shown when different from Pilot A. $^{a}$ Dense core of 12 HBA substations.

### 3. Event rate derivation
In order to find a rate for the occurrence of transients, the sky rate $\mathcal{R}_{sky}$ at a certain fluence $\mathcal{F}$ is obtained by summing over each observation $o$ the minimum beam size $B$ across the band multiplied by the effective duration $D$ of a pointing, for all observations with a detectable fluence $\mathcal{F}(o)$ lower or equal to the threshold $\mathcal{F}$. The rate is the number of detections $N$ divided by this sum. Thus the expected rate in the case of $N$ detections is

$$\mathcal{R}_{sky}(\mathcal{F}) = N / \sum_{\mathcal{F} > \mathcal{F}(o)} B(o) * D(o).$$

Similarly, the volume rate $\mathcal{R}_{vol}$ is obtained by summing over the extragalactic volume $V$ that is searched in each observation

$$\mathcal{R}_{vol}(\mathcal{F}) = N / \sum_{\mathcal{F} > \mathcal{F}(o)} V(o) * D(o),$$

where $V$ is determined by the beam size and by the DM range searched, as this limits the redshifts searched (Sect. 3.4). The coverage is therefore a function of the beam size, volume (DM), duration, and sensitivity of each pointing. In this section the effective beam size, volume, duration, and sensitivity are discussed.

In case of non-detections ($N = 0$), one can use Eqs. (2) and (3) with $N = 1$ to obtain an estimate for the upper limit for the sky and volume rates. Using Poissonian statistics, the obtained rate for $N = 1$ then gives a chance of $1/e \approx 36\%$ to obtain $N = 0$. We also adopt this common choice (Coenen et al. 2014; Karastergiou et al. 2015) in this paper.

http://www.astron.nl/lotaas/
3.1. Effective observing time and beam size

The effective observing time is reduced due to the presence of RFI that is too strong to be removed by our cleaning process, and because of incomplete dedispersion at the start and end of a chunk of data. The latter is DM dependent. For Pilots A and B this reduces the observing time by 15% and 42%, respectively, at the highest DM searched. The remaining observing time is referred to as the effective observing time and is used for setting limits.

The beam size of a LOFAR station depends on elevation (EL) as 1/sin(EL), in addition to the well-known dependency on frequency. The field of view (FoV) in Table 1 corresponds to the minimum FoV at an elevation of 90° (zenith).

3.2. Sensitivity

To set a limit on the transient rate, the detection threshold needs to be determined. The noise level for an incoherent array beam of \( N_t \) sub-stations at zenith is determined by \( S_{\text{sys}} = \text{SEFD}/\sqrt{\Delta f \Delta t} \), where SEFD is the system equivalent flux density, \( \Delta f \) is the integration time, and \( \Delta t \) is the bandwidth. For \( \Delta t = 2 \text{ ms} \) and \( \Delta f = 6.25 \text{ MHz} \), the \( S_{\text{sys}} = 6.5 \text{ Jy} \) from 120 MHz to 150 MHz, (following van Haarlem et al. 2013). The value at 120 MHz is used as the highest and therefore most conservative value when calculating \( S_{\text{sys}} \). The effective bandwidth is decreased by 10% on average by flagged channels because of the two-step channelization (1 out of 16 channels, 6%, contains no information because of the polyphase filter DC channel) and RFI (4%). The noise level will also depend on the elevation EL. To correct for this, we use an antenna model with a simple correction factor of \( \text{sin}(EL) \) (Hamaker 2011) within 5%. In addition, the noise level is divided by 0.73 to compensate for unequal gain across the beam (following e.g., Edwards et al. 2001).

The noise level also depends on the sky temperature \( T_{\text{sky}} \) which depends on the observing direction. The sky temperature towards the Galactic plane is higher, so an additional correction is applied to the SEFD, as \( \text{SEFD} = \text{SEFD}_0(\text{sky} + \text{int})/(\text{sky} + \text{int}) \). \( T_{\text{sky}} = T_{\text{Haslam}} + \lambda_0 \), where \( \lambda_0 \) is the wavelength at 120 MHz (2.5 m), \( T_{\text{sky}} \) is the temperature from the 408 MHz map by Haslam et al. (1982), corrected to a wavelength of 1 m using a spectral index of 2.55 (Lawson et al. 1987). \( T_{\text{sky}} = 60 + \lambda^2 \) K is the average temperature used to calculate SEFD, and \( T_{\text{int}} = 400 \text{ K} \) is the instrumental noise as measured by Wijnholds & van Cappellen (2011). An additional loss in sensitivity comes from the deviation of the real DM of the pulse from the trial DM used. For this situation, the overlap between the summed samples for the real DM and the trial DM can be calculated (TV15, Sect. 3.3.2). For Pilot A, the maximum loss is 25% for the 2-ms pulses and 10% for 8-ms pulses. For Pilot B, the maximum loss is 60% for 4-ms pulses and 30% for 8-ms pulses.

The DM smearing within one channel at these low frequencies is considerable. At a DM of 110 pc cm\(^{-3}\) (Pilot A) the smearing is 3.2–6.5 ms for 12 kHz channels at 151 and 119 MHz, respectively. For Pilot B, at a DM of 500 pc cm\(^{-3}\) the intra-channel smearing is 14.7–29.7 ms over the same range. When searching with a shorter sliding window, only part of the pulse is summed. For an 8-ms pulse at a DM of 500 pc cm\(^{-3}\), the detection threshold therefore increases with a factor 3.7 or a loss of 73%. However, this effect cancels out the loss in sensitivity caused by the deviation from the real DM, explained above, for shorter pulse lengths. The low DMs therefore have a threshold for Pilot B that is 2.6 times lower than that of the highest DM values. For Pilot A, this has no consequences for pulses of 8 ms and longer, even at the highest DMs, but shorter pulses will be smeared out.

3.3. Scattering

Bhat et al. (2004) performed an empirical study on the effects of scattering on pulsar signals in the Milky Way. They found that pulse broadening scales with frequency and DM. The frequency scaling evolves as \( \tau_{\text{d}} \sim \nu^{-0.1} \) with \( \tau_{\text{d}} \sim 3.9 \pm 0.2 \), giving 4000 times more scattering at 119 MHz compared to 1 GHz. At 1 GHz, the scattering is on average 1 μs at a DM of 50 pc cm\(^{-3}\), and 10 ms at a DM of 500 pc cm\(^{-3}\). There is a large spread in these values, so the scatter time can be a factor of ten higher or lower. Applied to 119 MHz, this yields scattering times of 4 ms and 40 s for a DM of 50 pc cm\(^{-3}\) and 500 pc cm\(^{-3}\), respectively. If this also holds for extragalactic pulses, the current search will not see any FRBs at the timescales probed. However, Lorimer et al. (2013) pointed out that, for extragalactic bursts, scattering is highest if a scattering screen is midway between the source and the observer. For FRBs, it is more likely that scattering originates from the host galaxy (less strong, because of redshifted emission frequency) or our Galaxy, likely dependent on the observing direction. Therefore, the scattering may be expected closer to the value for a DM of 50 pc cm\(^{-3}\) in our Galaxy and at least some FRBs may be observed on millisecond timescales.

FRBCAT contains scattering times for half the FRBs ranging from 0.71 to 23 ms, corrected to 1 GHz. These are low values compared to the Bhat et al. (2004) findings. However, if these are correctly measured and scale with frequency in the same way as pulsars, these pulses would be of the order of seconds at LOFAR frequencies, requiring longer integration time and thereby reducing the sensitivity of the measurements. Nonetheless, there may still be other FRBs with less scattering. More results by CHIME will be interesting for comparison in this regard. Their first detection (Boyle & CHIME/FRB Collaboration 2018) shows no scattering on a pulse of 2 ms at a frequency as low as 580 MHz, and mentions other FRBs to be observable down to 400 MHz. For now, we assume there may still be FRBs at 8 ms at 119 MHz and set limits accordingly; however, we also discuss the implications of scatter broadening to 128 ms where appropriate (Sects. 4.3.2, 5.1, and 5.6).

In general, we assume that scattering from intergalactic space can be neglected. It will not have an effect on the probed volumes for a given DM range. As long as we apply our limits only to the properties of observed pulses, we can disregard...
scattering in their derivation, and do so henceforth in this paper. However, due to the strong frequency dependence of scattering, scattering will have an effect when rates obtained at different frequencies are compared. If scattering is an erratic effect depending mainly on the line of sight, a fraction of the pulses may not be detected for a given experimental setup. This will essentially translate into a factor of less than one to be applied to the detection rate. We mention this whenever it affects our conclusions.

3.4. Volume rate limit for extragalactic sources

The DM in a certain direction depends on redshift \( z \) as:

\[
DM(l, b, z) = DM_{\text{MW}}(l, b) + DM_{\text{IGM}}(z) + \frac{DM_{\text{host}}}{1 + z}
\]

\[
\approx DM_{\text{MW}}(l, b) + 1100z + \frac{100}{1 + z}.
\]

In these equations, \( DM_{\text{MW}} \) is the predicted DM of the Milky Way at the Galactic coordinates \((l, b)\) of the observations using the NE2001 model (Cordes & Lazio 2002), \( DM_{\text{IGM}}(z) \approx 1100z \) is the contribution from the intergalactic medium using Eq. (2) from Ioka (2003) in an approximation for \( z < 0.25 \), and using the updated latest values for the constants of cosmology from Planck Collaboration XVI (2014). In this paper an estimated host DM of 100 pc cm\(^{-3}\) is used. Its contribution is corrected for the redshift of the transmitting frequency.

There are large uncertainties for both \( DM_{\text{MW}} \) and for \( DM_{\text{host}} \). The value of \( DM_{\text{MW}} \) cannot be measured in all directions and distances, and is therefore an interpolation and extrapolation of the points where it can be measured. The value of \( DM_{\text{host}} \) depends on galaxy type, inclination angle and can be increased by ionized clouds along the path. The only \( DM_{\text{host}} \) measured is for the repeating FRB121102 at DM \( \leq 324 \) pc cm\(^{-3}\) (Tendulkar et al. 2017), which appears high compared to average DMs of 37 pc cm\(^{-3}\) for elliptical galaxies and 45 pc cm\(^{-3}\) for spiral galaxies (Xu & Han 2015), although averaging over inclination increases the latter to 142 pc cm\(^{-3}\). This high DM can be caused by ionized material close to the source, because of a star forming region there (Bassa et al. 2017). A very high \( DM_{\text{host}} \) will decrease the \( DM_{\text{IGM}} \) contribution significantly, and will therefore decrease the galactic volume searched. As whether or not this really is the typical DM for FRBs is unknown, because FRBs with a DM as low as 174 pc cm\(^{-3}\) have also been measured, we assume in our analysis a \( DM_{\text{host}} \) of 100 pc cm\(^{-3}\), after Lorimer et al. (2007), but also in line with some orientations of elliptical and spiral galaxies and an additional contribution from the local environment.

Equation (4) was used to give the maximum redshift corresponding to the maximum DM that was searched. The result is plotted in Fig. 1 for Pilot B. The CosmoLoPy package\(^3\), following Hogg (1999), is used to find the co-moving distance, luminosity distance, and observed volume for that redshift. The co-moving distance is typically \( \sim 1 \) Gpc, as shown in Fig. 1. With this method, the DM-limited volume for each observation is calculated as used in Eq. (3).

4. Results

Here we show results from the pilot surveys A, B, and C. From the first two we present the first exploratory results of the dispersed pulse search (Sects. 4.3.1 and 4.3.2). Pilot C shows the potential of commensal observing during imaging observations (Sect. 4.2). We first show the detection of a solar radio burst as a proof of concept of the potential for localization with the TBBs.

4.1. Localization of a solar radio burst

Localization of FRBs is one of the most important goals for current developments in FRB searches. As a proof of concept of the potential for localization with the TBBs, we describe here the detection of a solar radio burst.

During observations of Pilot A, the real-time trigger detected peculiar emission at a DM of 43 pc cm\(^{-3}\). Figure 2 shows the original detection plot generated by the trigger software. The triggering emission is between the two blue lines that denote the dispersion relation. We note that we plot the time of the first trigger, instead of the time with the highest peak. The trigger occurred due to the highly non-Gaussian behavior of the dispersed sub-bands created by the emission from the solar radio burst, in combination with the normalization functions. Even though it is clear that this signal is not an FRB or pulsar, it is also not clear that it is regular RFI. Therefore, we recorded TBB data for further analysis.

\[^3\]roban.github.io/CosmoLoPy/
pulsars were detected in Pilot A (PSRs B0834+06, B1133+16
and B1541+09) and seven in Pilot B (PSRs B2016+29,
B2111+46, B0320+39, B1919+21, B2217+47, B2021+51 and
B0301+19). The pulsar with the highest DM detected was PSR
B2111+46 with a DM of 141.26 pc cm$^{-3}$, showing the potential
discovered FRBs.

Pilot B showed two interesting rediscoveries: PSRs
B2021+51 and B0301+19. Based on flux densities from higher
frequencies, they have an extrapolated peak flux density of
only 11 and 2 Jy, respectively, while the trigger threshold is
100 Jy for an 8-ms pulse. This indicates a broad distribution
in pulse flux densities, a known behavior for these pulsars. In fact,
these pulsars were originally detected in single pulse surveys at
408 MHz, where B0301+19 was generally weak, but occasionally
emitted two or three bright pulses (Bonsignori-Faccondi et al.
1973), and B2021+51 showed a large distribution in pulse amplitudes
(Davies & Large 1970). This behavior is still present at
135 MHz.

During the commensal Pilot C survey, five pulsars were
rediscovered: PSR B0329+54, PSR B1120+50, PSR B1508+55,
PSR B1953+50, and PSR B2021+51. They are shown in
Fig. 4, where the right ascension, declination and DM of the
triggers are compared with those of known pulsars in the field
up to a DM of 100 pc cm$^{-3}$. Most notable is PSR B1112+50,
that has a weak average flux density, but is known to emit giant
pulses (Ershov & Kuzmin 2003; Karuppusamy et al. 2011). The
successful rediscovery of five pulsars shows that LOFAR can
run these two observing modes in parallel and detect dispersed
pulses.

4.3. Fast radio burst limits

All dispersed pulses found can be attributed to known pulsars.
From this, an upper limit on the occurrence of FRBs and other
fast radio transients at 135 MHz is derived in this section.

4.3.1. Sky rate limit from Pilot A

The rate limit in events per sky per day as a function of fluence is
determined as described in Sect. 3. The result for Pilot A, based
on an effective observing time of 68.5 beam h, is presented in
Fig. 5. This figure shows the observed sky for fluence thresh-
holds between 1 and 2 kJy ms, as calculated by Eq. (2). This is
not the complete range that could be observed, but gives the
best overview. Of the pointings, 40% have a fluence between
0.7 and 1 kJy ms, while 10% have a fluence above 1.6 kJy ms,
and up to 6 kJy ms for pointings in the Galactic plane. Taking
90% of the pointings into account, we set a limit for the
event rate of 1500 events per sky per day above a threshold of
1.6 kJy ms for an 8-ms pulse. The pulse duration is important in
this limit. For pulses shorter than 8 ms, the average brightness
needs to be larger, because of the intra-channel DM smearing
and the decrease in efficiency caused by the finite DM step (see
TV15, Sect. 5.2.1). For longer pulses, the minimum detectable
fluence increases with $\sqrt{\Delta t}$, where $\Delta t$ is the pulse duration ($S_{\text{sys}}$
does down with $1/\sqrt{\Delta t}$, but for fluence it is multiplied by the
duration $\Delta t$). No volume rate is derived for Pilot A, because
the volume probed is minimal due to the limited DM range
searched.

4.3.2. Sky rate and volume rate limits from Pilot B

In Pilot B, triggers below a DM of 10 pc cm$^{-3}$ were omitted
because of the high probability that they are caused by local RFI.
After the data-quality cut, including the DM-dependent data loss
because of incomplete dedispersion at the start and end of a
chunk, 91.2 beam h remained at a DM of 500 pc cm$^{-3}$. A sky
rate limit and a volume rate limit on isolated dispersed pulses
have been calculated as a function of fluence. These are shown in
Fig. 6 for an 8 ms, 32 ms, and 128 ms pulse duration. Because
of the DM smearing affecting the 8-ms results, the 32-ms results
are 40% more sensitive, while the 128-ms results are only 13%
less sensitive than the 8-ms results. The limit is 1400 events
per sky per day, or equivalently 134 events per Gpc$^3$ per day
above a fluence of 6.0 kJy ms for an 8-ms pulse up to a DM of
500 pc cm$^{-3}$. Limits at a lower fluence threshold, for a smaller
DM range, and for longer pulse durations are presented in
Table 2.
5. Discussion

In this section we compare the event rates from our nondetections to values in the literature. We first discuss the sky rate limits (Sect. 5.1) and the implications for RRATs (Sect. 5.2). Subsequently, we compare the rate per volume from Pilot B with expectations from Sect. 5.3 onwards, and discuss the options of a star formation history dependence (Sect. 5.4) and a nonuniform distribution (Sect. 5.5). Finally, we give an outlook on the detectability of FRBs with LOFAR (Sect. 5.6).

5.1. Sky rate

In Fig. 7, we compare the sky rate and upper limits from various surveys that were performed below 1 GHz, where fewer detections are available with respect to 1.4 GHz. The surveys considered are summarized in Table 3. The MWA surveys were named

We note that the current fast pace of this field makes it likely that the list may be incomplete by the time of publication.
by us. The results in this and subsequent sections are corrected for a pulse duration of 8 ms, as most detected FRBs so far have a length shorter than this. Because of scattering, the pulse length may also be longer for lower frequencies leading to different detection thresholds. If the pulse length is of the order of 128 ms at 135 MHz, the sensitivity for FRATS is 13% less, and the previous surveys below 200 MHz will lose about a factor of four in sensitivity, while the previous surveys above 320 MHz are not affected as the scattering would be below 8 ms. Our results for Pilot B are presented by the black line and shaded region in the upper right corner. Limits and results from other surveys are represented by the different shapes in the plot. The limit on the FRB rate determined by our results is comparable with the rate limit determined by the GBNCC survey, the GBTIM survey (Caleb et al. 2017). The latter reports a detectable rate limit of 1.6 ± 0.8 events per Gpc$^3$ per day at 135 MHz, the sensitivity for FRATS is 13% less, and the previous surveys below 200 MHz will lose about a factor of four in sensitivity, while the previous surveys above 320 MHz are not affected as the scattering would be below 8 ms. Our results for Pilot B are presented by the black line and shaded region in the upper right corner. Limits and results from other surveys are represented by the different shapes in the plot. The limit on the FRB rate determined by our results is comparable with the rate limit determined by the GBNCC survey, the GBTIM survey (Caleb et al. 2017), and the MWA-154 survey, albeit at a different frequency threshold. In sensitivity, our results are comparable with AO327 and the MWA-154 survey. The only two published detections have been made by the GBTIM and UTMOST survey (Caleb et al. 2017). The latter reports a detectable rate limit of 0.78 (±0.2) $\times 10^4$ events per sky per day at a fluence above 11 Jy ms and a fluence complete rate limit of 5.0 ($\pm$3) $\times 10^3$ events per sky per day above a fluence of 69 Jy ms.

The rate at different frequency thresholds and observing frequencies depends on how the number of FRBs changes as a function of frequency, and how the frequency changes as a function of observing frequency. This is expressed by the relationships $R(\gtrsim f_{\text{lim}}) \propto f^{-\alpha} \text{ and } S \propto v^\beta$, where $R$ is the rate, $f$ is the frequency, $S$ the spectral energy distribution and $v$ the observing frequency. Caleb et al. (2017) find that if $\alpha = -3/2$, as in Euclidean space, the spectral index $\gamma = -1.1(1.2)$, and if, on the other hand, $\gamma = 0$, they find $\alpha = -1.0(1.1)$. This is more in line with the evolution of volume with redshift; see Sect. 5.3. These relations are represented by the lines in Fig. 7, where the case of $\gamma = -1.1$ has been corrected to the survey frequency at 140 MHz. Given these rates, it is not surprising that our pilot surveys and the other surveys have not discovered FRBs so far.

The results from two other LOFAR surveys are also shown: the off-line survey LPPS (Coenen et al. 2014) and the real-time survey ARTEMIS (Karastergiou et al. 2015), both observing only one band of 7 and 6 MHz, respectively, around 145 MHz. They have reached a lower rate limit than this work because they use more beams and more observing hours than in our pilot surveys. They are also more sensitive due to the increased number of stations (LPPS) or better dedispersion accuracy (LPPS and ARTEMIS). ARTEMIS uses one international station that is 15% more sensitive than the LOFAR superterp combined incoherently. In addition, we applied a correction factor of 2.5 between the theoretical and actual sensitivity (Sect. 3.2), as was done for the LPPS survey. To the LPPS flux density threshold we apply an additional factor two to account for intra-channel DM smearing of LPPS at a DM of 500 pc cm$^{-3}$ for an 8-ms pulse. While LPPS analyzed the data up to a DM of 2000 pc cm$^{-3}$, ARTEMIS limited itself to 320 pc cm$^{-3}$, observing a smaller instantaneous volume than FRATS with a cut-off at 500 pc cm$^{-3}$. Using all stations, instead of the 12 sub-stations used in the pilot survey, FRATS will be more sensitive than LPPS and ARTEMIS (see also Sect. 5.6). Also, unlike FRATS, they are not designed to use TDB data to localize pulses, which is the main goal of the FRATS project.

### 5.2. Rotating radio transients

RRATs are pulsars of which only single pulses are detected (Burke-Spolaor et al. 2013). The time between these pulses can last from minutes to hours. The long integration times of commensal observations gives FRATS a high potential of discovering RRATs with a long “off” time. Burke-Spolaor et al. (2011) detected RRAT with an off time of three times the observing time, which would extend this time even further. Pilot A is more sensitive to RRATs, as they are local, meaning that the DM limit of 110 pc cm$^{-3}$ is not a problem, but the DM search is more sensitive because of the smaller DM step. We determine that in Pilot A, covering 1610 square degrees (3.7% sky), no bright RRATs were observed in a typical effective observation duration of 42 min (after data-quality cuts), above a threshold of 1.6 Jy ms for an 8-ms pulse. Based on the RRATs population published (early) in the literature this is not surprising. Only 1 of approximately 60 RRATs (McLaughlin et al. 2006; Deneva et al. 2009; Burke-Spolaor & Bailes 2010; Burke-Spolaor et al. 2011; Keane et al. 2011) would be bright enough to be detected by our observations, assuming RRATs have a pulsar-like average spectral index of $-1.8$ (Maron et al. 2000; Miller et al. 2011). Almost all RRATs require a sensitivity at least four times higher than that of our observations presented here to be detected. This is without taking scattering into account, which would further weaken the emission at low frequencies. With long commensal observations, in conjunction with additional stations to reach the sensitivity required, it would be possible to detect RRATs with off times of several hours.

### 5.3. Volume rate, comparison, and expectations

Because of intra-channel DM smearing, the low frequencies are restricted in their DM range and thus in the redshift range in which sources will be detected. Therefore, to compare survey results and make predictions, it is useful to compare the volume rate $R_{\text{vol}}$ (events per Gpc$^3$ per day) rather than the sky rate $R_{\text{sky}}$ (events per sky per day).

Hassall et al. (2013) determined $R_{\text{vol}}$ by simulations. Based on this study, we use an adjusted $R_{\text{vol}}$ of 12 events per Gpc$^3$ per day (under the assumption that there is no scattering), by choosing the rate for the results by Thornton et al. (2013) as most reliable, and correcting it for the new $R_{\text{sky}}$ of Champion et al. (2016).

The rate of 12 events per Gpc$^3$ per day is still more than one order of magnitude less than the upper limit derived in this pilot survey, which is $R_{\text{vol}} < 134$ events per Gpc$^3$ per day. If these predictions are correct, it is clear that at least ten times more observing time is needed in order to be able to detect a similar event rate, even if all FRBs could be detected by our setup. A more recent result (Law et al. 2017) predicts a ten times higher volumetric rate, based on
on the assumption that the repeater FRB121102 is a prototype for
$\gamma<0$.

Another aspect required to detect FRBs is the brightness of the FRBs compared to the sensitivity of the instrument. To estimate this, we show in the upper panel of Fig. 8 the fluence of the first 20 known FRBs as a function of redshift. The fluence threshold of Pilot B is plotted as the horizontal dashed line for a flat spectrum at $\gamma = 0$. From this plot, it is clear that all FRBs detected so far have a fluence, at their observed frequencies, below the threshold of Pilot B. There are two ways in which FRATS would still be sensitive enough to these FRBs. Firstly, an FRB that is closer appears brighter. Secondly, they could be intrinsically brighter at lower frequencies (spectral index $\gamma<0$).

For the first option, we have extrapolated the fluence to lower redshifts for three cases: the brightest FRB (green line), the dimmest FRB (blue line), and the median value (red line). From this, we see that even the brightest FRB detected so far would only be visible for $\gamma=0$ up to a redshift of 0.07, corresponding to a DM of $\sim 210$ pc cm$^{-3}$. For the second option we have also drawn lines for the threshold at $\gamma=-1, -2$, and -3. The figure shows that to detect half of the known FRBs, correcting for a redshift up to the survey limit of 500 pc cm$^{-3}$ ($z \approx 0.36$), a spectral index of $-3$ is required. In the bottom plot of Fig. 8, we show the rate as a function of redshift, by multiplying the volume by the rate mentioned above of 12 events per Gpc$^3$ per day, for the three cases: all FRBs (blue line), half of the FRBs (red line), and the brightest FRB (1 out of 20, green line). From this, we see that Pilot B (blue triangle) is likely much closer to a detection threshold than pilot A (green triangle), with approximately 16 observing beam days required, assuming a beam size of 16 square degrees and that the FRBs have a spectral index of less than $-3$. For this setup with three beams, it will take 5.3 days of observing per event. We summarize this and predictions from the following sections in Table 3.

Another way to visualize observing expectations is to plot the event rate as a function of fluence, as in Fig. 7. This is shown in Fig. 9, where we plot this relation based on the volume rate of 12 events per Gpc$^3$ per day, by calculating the luminosity distance and volume for each redshift. We have plotted vertical lines for the values corresponding to the redshift up to a DM of 110 pc cm$^{-3}$ and 500 pc cm$^{-3}$. We show again, as in Fig. 7, the rates versus fluence of the different surveys, as well as our rates, but now for different spectral indices. The expected rate up to a DM of 500 pc cm$^{-3}$ is 154 events per sky per day, above a fluence of 6 kJy ms. Given the current limits, using the same setup, a factor of nine more observing time is required, as well as a spectral index of less than $-3$ to see a single FRB. If the spectral index is less steep, or if only a small fraction of FRBs detected at $\sim 1$ GHz are observable at lower frequencies within the pulse width limits of our survey due to line-of-sight-dependent scattering, a longer observing time is required. In that case, other observing strategies may be more beneficial, as we discuss in Sect. 5.6.

### Table 3. Survey parameters for Figs. 7 and 9.

<table>
<thead>
<tr>
<th>Survey</th>
<th>Central Freq (MHz)</th>
<th>DM range (pc cm$^{-3}$)</th>
<th>Reference</th>
</tr>
</thead>
<tbody>
<tr>
<td>GBTIM</td>
<td>800</td>
<td>20–2000</td>
<td>1</td>
</tr>
<tr>
<td>GBNCC</td>
<td>350</td>
<td>0–500</td>
<td>2</td>
</tr>
<tr>
<td>UTMOST</td>
<td>843</td>
<td>100–2000</td>
<td>3</td>
</tr>
<tr>
<td>MWA-182</td>
<td>182</td>
<td>&lt; 0–700</td>
<td>4</td>
</tr>
<tr>
<td>MWA-154</td>
<td>154</td>
<td>&lt; 170–675</td>
<td>5</td>
</tr>
<tr>
<td>CHIME pf</td>
<td>600</td>
<td>20–2000</td>
<td>6</td>
</tr>
<tr>
<td>AO327</td>
<td>327</td>
<td>0–1095</td>
<td>7</td>
</tr>
<tr>
<td>LPPS</td>
<td>142</td>
<td>0–2000</td>
<td>8</td>
</tr>
<tr>
<td>ARTEMIS</td>
<td>145</td>
<td>0–320</td>
<td>9</td>
</tr>
<tr>
<td>FRATS</td>
<td>135</td>
<td>10–500</td>
<td>10</td>
</tr>
</tbody>
</table>

### References.
FRATS is searching at. The expected rate including the SFR decreases the probability of finding FRBs at the DMs that towards $z$ are taken as

Fig. 8. Upper panel: fluence as a function of redshift for the first 20 published FRBs. Their measured values are marked by the stars. Fluence is calculated as flux density multiplied by width and the redshift is calculated as $z = (\text{DM}_{\text{FRB}} - \text{DM}_{\text{gal,NE2001}}) / 1000$. Values for the DMs are taken from the FRB catalog (Petroff et al. 2016). Extrapolated values are shown by the lines from top to bottom for the brightest FRB, the median FRB, and the weakest FRB in green, red, and blue, respectively. To show if they would be bright enough to be detected by LOFAR, the LOFAR fluence limit is plotted by the dotted horizontal lines for four different spectral indices ($\nu'$). Lower panel: estimated event rate as a function of redshift. From top to bottom: for all FRBs, half of the FRBs and the ‘brightest’ FRB (FRB160317), in blue, red, and green respectively. The redshift is limited by the DM, as indicated by the vertical dashed lines for a DM of 110 (Pilot A), and 500 (Pilot B) pc cm$^{-3}$. The upper limits for Pilot A and B are shown in the figure as green and blue triangles, respectively.

5.4. Star formation history

Hassall et al. (2013) assumes a uniform distribution of FRBs. This is the most basic assumption one can make. However, it is also possible that these events are correlated with the star formation rate (SFR), as simulated in Caleb et al. (2016b). If we use the SFR as a function of redshift, we can derive a different expected rate at the distances probed here. The rate up to a redshift $z$ is then $\mathcal{R}_{\text{sky}}(z) \sim \int_{0}^{z} \text{SFR}(z') \frac{\text{d}V_{\text{intensity}}(z')}{\text{d}z'} \text{d}z'$. This needs to be normalized to yield the same result of $7 \times 10^4$ events per sky per day up to the appropriate distance.

As an example, the Modified Salpeter A initial mass function from Table 2 of Hopkins & Beacom (2006) is used to calculate the SFR. As the SFR is highest at $z > 1$ and decreases towards $z = 0$, the higher DMs (around 1000 pc cm$^{-3}$) have an extra weight and fewer events are expected at lower DMs. This decreases the probability of finding FRBs at the DMs that FRATS is searching at. The expected rate including the SFR correction is plotted as the lower line in Fig. 9. At a DM of 500 pc cm$^{-3}$, the rate is decreased by a factor 3.6 compared to a uniform distribution, requiring 58 observing beam days per event for the nonscattering case and for $\gamma < -3$.

5.5. Local population

Masui et al. (2015) and Kulkarni et al. (2015) discussed a large contribution to the DM from surrounding material for the case of two FRBs. In this case, the DM is not a direct measure for the distance of the bursts and the expected rates should be adjusted for that. In the extreme case, the difference in DM for the different FRBs is all from the surrounding material, and therefore all FRBs are local. In this case, the expected rate up to a DM of 500 pc cm$^{-3}$ scales with the fraction of bursts that have a DM below 500 pc cm$^{-3}$. Out of 29 FRBs, 6 have a DM below 500 pc cm$^{-3}$, so we could expect about a fifth of the bursts to be visible up to a DM of 500 pc cm$^{-3}$, provided they are bright enough.

In this case, there is no correction on the flux density for FRBs with a lower DM (or $z$), as was used in Sect. 5.3. Such a relationship is also not directly evident from Fig. 8. Keane & Petroff (2015) reported a rate of 2500 events per sky per day at a fluence of $\mathcal{F} > 2\text{Jy ms}$. This is also the median fluence of the known bursts. Therefore, below a DM of 500 pc cm$^{-3}$ the rate is 500 events per sky per day.

From Table 2 we note that at 3.3 kJy ms the limit set is 2240 events per sky per day, a factor 4.4 away from the expected rate. At this energy threshold, a spectral index of $-3.2$ is required, as well as 18 observing beam days per event.

5.6. Outlook

In this section we give an outlook on what can be achieved with LOFAR, discussing a few different strategies. LOFAR can be used in different setups. We discuss the incoherent Stokes mode, the coherent Stokes mode, the Fly’s Eye mode (see van Haarlem et al. 2013), and an external trigger mode. The predictions are summarized in Table 4. The general strategy here is to determine which flux density can be reached with a certain setup and derive from this an upper limit on the rate in events per sky per day given by a luminosity function $\mathcal{R}(\nu, \mathcal{F}) \propto \nu^\alpha \mathcal{F}^\gamma$. The relation between fluence and rate is taken from Fig. 7 for $(\alpha = -1, \gamma = 0)$ and $(\alpha = -3/2, \gamma = -1.1)$. Using the total instantaneous sky coverage for a given setup, we can translate this into the number of days required for a single detection, or determine how many events will be detected in, for example, a two-year campaign.

We note that in these calculations we assume that scattering does not play a large role; see Sect. 3.3 for a discussion. If pulses are smeared out, for example, 128 ms, the detection threshold increases and the corresponding rate goes with $\propto \mathcal{F}^\alpha$. For $\alpha = -1$, the rate for 128 ms is a factor four lower and for $\alpha = -3/2$ it is a factor eight lower than the numbers for the duration of 8 ms calculated here.

5.6.1. Commensal incoherent Stokes

One option is to do commensal observing during the normal LOFAR cycles using incoherent Stokes beams. The detectable rate depends on the fluence and thus on the sensitivities that can be reached. The sensitivity can be improved with respect to the pilot surveys in various ways. The improvement factor on fluence is shown between parentheses. The improvements are as follows: using narrower frequency channels (3 kHz) to counter the effects of intra-channel DM smearing and increasing the dedispersion efficiency to 90% by using small enough DM steps ($\times 3.3$), better calibration to reach the theoretical sensitivity ($\times 2.5$), increasing the number of (sub-)jitter bins from 12 to 62 ($\times 2.2$), and increasing the bandwidth to three sub-bands of 16 MHz ($\times 1.6$). After implementing all these improvements, one can expect a total gain of a factor 30, giving a typical fluence threshold of 100 Jy ms based on a 3 kJy ms typical fluence from Pilot B. For this threshold, the expected rate is eight events per sky per day for both $\alpha = -1$ and $\alpha = -3/2$. Using all LOFAR stations, and two beams per station, each with a beam size of 40 deg$^2$ at an average elevation of 60 deg, on average 129 days of

\[\text{5. The incoherent stokes mode was previously referred to as incoherent array beam, but we now refer to the LOFAR naming of the sub-modes.}\]
integration time are required to detect one event at this rate; equal to almost 3200 h. LOFAR currently offers 1600 h of observing per semester. Assuming that half of the observations have a setup compatible with ours, there are 3200 observing hours in 2 years, or an overall duty cycle of 20%. Thus, we expect to detect approximately one event every 2 years of commensal observing, if there is no significant loss of detectable pulses at low frequencies due to scattering and all events above threshold have a DM in the range searched.

5.6.2. Commensal coherent Stokes

A second option is to do commensal observing with coherent Stokes beams, improving the sensitivity. The downside is that the beam size decreases, such that many more beams, and thus much more processing power, are required for the analysis. On the positive side, this already provides an initial location which optimizes the search for a precise location with the TBB data. Using coherent beams, the sensitivity gain for 48 core sub-stations is a factor of 13.8. This brings down the typical fluence limit to 18 Jy ms. The sky coverage decreases to 4 deg², which after two years of commensal observing gives a total of 0.0125 (1/80) sky days observed. The predicted event rate for this fluence limit is 44 or 104 events per sky per day, for the luminosity functions ($\alpha = -1, \gamma = 0$) and ($\alpha = -3/2, \gamma = -1.1$), respectively. Therefore, there is a chance of 50% to detect an FRB with this strategy over a period of 2 years if $\alpha = -1$ and one event is expected if $\alpha = -3/2$.

5.6.3. Fly’s Eye observations

A third option is to optimize the sky coverage by tiling out the sky in a Fly’s Eye mode, using only one station per beam and a lot of beams per station with less bandwidth, with each station

Table 4. Rate predictions for different LOFAR observing modes and population modes.

<table>
<thead>
<tr>
<th>FRB Population Model</th>
<th>Stations</th>
<th>Mode</th>
<th>beams</th>
<th>Predicted Rate (sky⁻¹ day⁻¹)</th>
<th>DM (pc cm⁻³)</th>
<th>Spectral index</th>
<th>Req. obs. time (days event⁻¹)</th>
<th>Min. Fluence (Jy ms)</th>
<th>Section</th>
<th>Fig.</th>
</tr>
</thead>
<tbody>
<tr>
<td>Volume rate SFH</td>
<td>12</td>
<td>IS</td>
<td>3</td>
<td>12 a</td>
<td>0–500</td>
<td>−3</td>
<td>5.3</td>
<td>6000</td>
<td>5.3</td>
<td>8, 9</td>
</tr>
<tr>
<td>Volume rate</td>
<td>12</td>
<td>IS</td>
<td>3</td>
<td>3.3 a</td>
<td>0–500</td>
<td>−3</td>
<td>19.3</td>
<td>6000</td>
<td>5.4</td>
<td>9</td>
</tr>
<tr>
<td>Local population</td>
<td>12</td>
<td>IS</td>
<td>3</td>
<td>500 a</td>
<td>0–500</td>
<td>−3.2</td>
<td>6</td>
<td>3300</td>
<td>5.5</td>
<td>9</td>
</tr>
<tr>
<td>Caleb et al. (2017); $\alpha = -1$</td>
<td>62</td>
<td>IS</td>
<td>2</td>
<td>8</td>
<td>−</td>
<td>0</td>
<td>150</td>
<td>100</td>
<td>5.6.1</td>
<td>7</td>
</tr>
<tr>
<td>Caleb et al. (2017); $\alpha = -3/2$</td>
<td>62</td>
<td>IS</td>
<td>2</td>
<td>8</td>
<td>−</td>
<td>−1.1</td>
<td>150</td>
<td>100</td>
<td>5.6.1</td>
<td>7</td>
</tr>
<tr>
<td>Caleb et al. (2017); $\alpha = -1$</td>
<td>12</td>
<td>CS</td>
<td>&gt;100</td>
<td>44</td>
<td>−</td>
<td>0</td>
<td>292</td>
<td>18</td>
<td>5.6.2</td>
<td>7</td>
</tr>
<tr>
<td>Caleb et al. (2017); $\alpha = -3/2$</td>
<td>12</td>
<td>CS</td>
<td>&gt;100</td>
<td>104</td>
<td>−</td>
<td>−1.1</td>
<td>112</td>
<td>18</td>
<td>5.6.2</td>
<td>7</td>
</tr>
<tr>
<td>Caleb et al. (2017); $\alpha = -1$</td>
<td>62</td>
<td>FE</td>
<td>6</td>
<td>0.7</td>
<td>−</td>
<td>0</td>
<td>24</td>
<td>788</td>
<td>5.6.3</td>
<td>7</td>
</tr>
<tr>
<td>Caleb et al. (2017); $\alpha = -3/2$</td>
<td>62</td>
<td>FE</td>
<td>6</td>
<td>0.4</td>
<td>−</td>
<td>−1.1</td>
<td>10</td>
<td>1600</td>
<td>5.6.3</td>
<td>7</td>
</tr>
<tr>
<td>Caleb et al. (2017); $\alpha = -1$</td>
<td>48</td>
<td>TBB</td>
<td>−</td>
<td>200 0–2000+</td>
<td>0</td>
<td>−</td>
<td>0</td>
<td>−</td>
<td>2.5</td>
<td>5.6.4</td>
</tr>
<tr>
<td>Caleb et al. (2017); $\alpha = -1$</td>
<td>62</td>
<td>TBB</td>
<td>−</td>
<td>200 0–2000+</td>
<td>0</td>
<td>−</td>
<td>1.5</td>
<td>5.6.4</td>
<td></td>
<td></td>
</tr>
</tbody>
</table>

Notes. The columns denote the population model, as mentioned in the text, the number of LOFAR sub-stations used, the number of beams per observation, the predicted rate per sky per day for the minimum fluence, the DM range searched, the spectral index of the FRB, the required observing time per event, the given rate and the sky coverage for this setup, the minimum fluence for the given setup, and the section and the figure this model and setup refers to. The modes stand for Incoherent Stokes (IS), Coherent Stokes (CS), Fly’s Eye (FE) and a Transient buffer board only mode (TBB), as explained in the corresponding sections. 

![Fig. 9. Event rate vs. fluence for different surveys, corrected for a pulse length of 8 ms. Limits from the results of Pilot B are presented by lines in the upper-right corner for spectral indices of 0, −1, −2, and −3. The symbols represent rate (pentagram and cubes) and upper limits for other instruments observing below 1 GHz, where green symbols observe around 800 MHz, red symbols around 350 MHz, and blue symbols below 200 MHz. Survey or telescope name, mid-frequency, DM range, and references are given in Table 3. The blue line shows event rate as a function of fluence based on a fixed rate per Gpc⁻³, relating luminosity distance and volume as function of redshift, as explained in Sect. 3: the green dashed line shows the same but taking into account star formation history. The fluence limits for distances corresponding to DM values are indicated by the vertical lines for 110 (yellow, right) and 500 pc cm⁻³ (magenta).](image-url)
pointing in a different direction. In this case dedicated observing time is needed, so instead of finding an event rate per 2 years of commensal observing, we instead determine the amount of dedicated observing time required. We derive the numbers from the calculation in Sect. 5.6.1. Using one station instead of 62, the detection threshold is increased by a factor \( \sqrt{62} \) to a fluence of 788 Jy ms, while the instantaneous sky coverage increases by a factor of 62 to 2480 deg\(^2\) or 0.06 sky. If we further decrease the bandwidth per sub-band to 4 MHz instead of 16, the detection threshold increases by a factor of \( \sqrt{4} \) to 1.6 Jy ms, while the sky coverage increases by a factor of 4 to 9920 square degrees, or half the visible sky instantaneously. The rate at 788 Jy ms, for \( \alpha = -1 \) is \(-0.7\) events per sky per day, and at 1.6 Jy ms this is 0.4 events per sky per day. Because of the large sky coverage, this requires only 24 days and 10 days of observing for these two respective options. If such bright FRBs exist, this is a favorable observing strategy for LOFAR but requires dedicated computer power and observations, and cannot be commensally observed. It will also be difficult to find positions using the TBB data because the tile beams of all stations are pointed in different directions.

5.6.4. External trigger

To detect and localize FRBs with the TBB data there is another possibility, namely to trigger on FRBs at higher frequencies (e.g., 1.4-GHz). The single antenna buffers can then be read out at the time the FRB arrives at the lower frequencies minutes after the trigger. However, this requires the pulse to be detectable and an accurate DM estimate determined within the time delay given, otherwise the pulse might be missed in the TBB buffers. This was tested using the Effelsberg 100-m Radio Telescope to trigger on a known pulsar (Houben 2016) and on the FRB repeater: FRB121102 (Houben et al. 2018) by means of a specialised VOEvent standard (Petroff et al. 2017).

The buffered data can then be used to localize the pulse, a factor 100 more accurate than the Effelsberg detection. The benefit then is the certainty that there is an FRB in the data, such that all stations can be added coherently to increase the sensitivity compared to the real-time surveys. Additionally, coherent dedispersion can be applied, so intra-channel DM smearing is not an issue. For an 80 MHz bandwidth around 150 MHz\(^6\), the fluence limit at a 5 sigma level at zenith is 2.5 Jy ms for core stations or 1.5 Jy ms if all Dutch stations can be combined fully coherently. At that threshold, more than half of the known FRBs up to a DM of 500 pc cm\(^{-3}\) would be bright enough to be detected. This may be the most promising route to observe FRBs with LOFAR, since it would be possible to detect flat spectrum FRBs at 150 MHz.

6. Conclusions

The FRATS project searches in real-time for millisecond-scale radio transients with the LOFAR radio telescope. Some known transients of this kind are FRBs and RRATs. The focus is to obtain an optimal sky coverage by using commensal observations and a large field of view. An innovative addition is the use of ring buffers that hold the last seconds of data from each individual antenna which ultimately allows for post-event beamforming and imaging. This increases the positional accuracy, potentially to the full arc second resolution. This is important for pinpointing the location of FRBs.

The potential of LOFAR is demonstrated by two different results. The first demonstration is the successful commensal observing from the Pilot C survey, where beamformed data were produced to search for millisecond-scale radio transients, during regular interferometric observations. Five pulsars were discovered in a 24-h scan. The second is the identification of a transient as a type II solar radio burst by localizing it in a side lobe. This could only be done by using the buffered data to create an all sky image.

Besides these demonstrations we showed the results from the pilot surveys A and B, which searched up to a DM of \( \sim 110 \) pc cm\(^{-3}\) and 500 pc cm\(^{-3}\), respectively. While known pulsars were rediscovered, no unknown single-pulse sources have been detected. We have derived limits on the local FRB rates from these surveys.

The first pilot survey (A) had an effective observing time of 68.51 beam h, observed from 119 to 151 MHz, the lowest frequency range on which FRBs have been searched. Taking into account the pointing direction and noise level for each observation, this sets a limit on the occurrence of FRBs of less than 1500 events per sky per day above a threshold of 1.6 kJy ms below a DM of \( \sim 110 \) pc cm\(^{-3}\). Pilot study B had an effective observing time of 91.2 beam h in the same band. This sets limits at 1400 events per sky per day or 134 events per Gpc\(^3\) per day at a fluence threshold of 6.0 kJy ms for an 8-ms pulse.

The expected rate is one per beam per 16 days, for a uniform extragalactic distribution, provided the source flux density follows a steep spectrum of \( \nu^{-3} \). In the case where the source population as a function of redshift follows the star formation rate, the rate drops to one per beam every 58 days. If the spectrum is less steep and/or a significant fraction of FRBs are broadened by scattering beyond our detection limits, a longer integration time is required. To be able to obtain the required observing time, we have tested commensal observing with imaging observations in an additional pilot survey (C) of 24 h, using four 2-MHz bands between 120 and 185 MHz. The detection of five known pulsars during this last survey validates the possibility of such commensal observations.

The future prospects are given, using as input the relations found by the UTMOST survey (Caleb et al. 2017), for a spectral index of 0 or -1. A two-year commensal survey, assuming a realistic 20% duty cycle, would detect one event if pulse-broadening due to scattering plays no significant role. The lack of scatter broadening is not a trivial assumption at such low frequencies and high DMs, but for extragalactic bursts, it may still hold true.

Acknowledgements. We thank Cees Bassa, Evan Keane, Daniele Michilli and Maura Pilia for useful discussions and Anya Bilous for her help with observing. We acknowledge funding for this work from an Advanced Grant of the European Research Council under the European Union’s Seventh Framework Program (FP7/2007-2013)/ERC Grant Agreement n. 227610. RBP acknowledges funding from the European Research Council (ERC) under the European Union’s Horizon 2020 research and innovation programme (ERC Starting Grant agreement 715051 “Spiders”). SC acknowledges financial support from the UniveEarthS...
Labex program of Sorbonne Paris Cité (ANR-10-LABX-0023 and ANR-11-IDEX-0005-02). JvL acknowledges funding from the European Research Council under the European Union’s Seventh Framework Programme (FP/2007-2013)/ERC Grant Agreement n. 671799. This paper is based (in part) on data obtained with the International LOFAR Telescope (ILT) under project codes LC0_034, LC1_033 and LC1_052. LOFAR (van Haarlem et al. 2013) is the Low Frequency ARray designed and constructed by ASTRONN. It has observing, data processing, and data storage facilities in several countries, that are owned by various parties (each with their own funding sources), and that are collectively operated by the ILT foundation under a joint scientific policy. The ILT resources have benefited from the following recent major funding sources: CNRS-INSU, Observatoire de Paris and Université d’Orléans, France; BMBF, MIWF-NRW, MPG, Germany; Science Foundation Ireland (SFI), Department of Business, Enterprise and Innovation (DBEI), Ireland; NWO, The Netherlands; The Science and Technology Facilities Council, UK; Ministry of Science and Higher Education, Poland.

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