Search for pair and single production of vectorlike quarks in final states with at least one Z boson decaying into a pair of electrons or muons in pp collision data collected with the ATLAS detector at $\sqrt{s} = 13$ TeV

M. Aaboud et al.*
(ATLAS Collaboration)

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A search for vectorlike quarks is presented, which targets their decay into a Z boson and a third-generation Standard Model quark. In the case of a vectorlike quark $T (B)$ with charge $+2/3e$ ($-1/3e$), the decay searched for is $T \rightarrow Zt (B \rightarrow Zb)$. Data for this analysis were taken during 2015 and 2016 with the ATLAS detector at the Large Hadron Collider and correspond to an integrated luminosity of 36.1 fb$^{-1}$ of pp collisions at $\sqrt{s} = 13$ TeV. The final state used is characterized by the presence of $b$-tagged jets, as well as a Z boson with high transverse momentum, which is reconstructed from a pair of opposite-sign same-flavor leptons. Pair and single production of vectorlike quarks are both taken into account and are each searched for using optimized dileptonic exclusive and trileptonic inclusive event selections. In these selections, the high scalar sum of jet transverse momenta, the presence of high-transverse-momentum large-radius jets, as well as—in the case of the single-production selections—the presence of forward jets are used. No significant excess over the background-only hypothesis is found and exclusion limits at 95% confidence level allow masses of vectorlike quarks of $m_T > 1030$ GeV ($m_B > 1210$ GeV) and $m_B > 1010$ GeV ($m_B > 1140$ GeV) in the singlet (doublet) model. In the case of 100% branching ratio for $T \rightarrow Zt (B \rightarrow Zb)$, the limits are $m_T > 1340$ GeV ($m_B > 1220$ GeV). Limits at 95% confidence level are also set on the coupling to Standard Model quarks for given vectorlike quark masses.

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I. INTRODUCTION

In the Standard Model (SM), the electromagnetic and weak interactions arise from a SU(2)$_L \times$ U(1)$_Y$ gauge symmetry that is spontaneously broken by the Englert-Brout-Higgs mechanism. Measurements at collider experiments are so far consistent with its predictions. However, the SM is believed to be only a low-energy approximation of a more fundamental theory due to several unanswered questions. For example, it cannot explain the matter-antimatter asymmetry in the Universe and the origin of dark matter. When the SM is extrapolated to high energies, fine-tuning is required due to divergent corrections to the Higgs boson self-energy [1]. Solutions to this so-called “hierarchy problem” are proposed in several beyond-the-Standard Model (BSM) theories, which can be considered a first step toward a more fundamental theory of particle physics.

Since a large contribution to the fine-tuning originates from top-quark loop corrections, the hierarchy problem can be reduced in models predicting top-quark partners that mitigate the SM top quark’s contribution: while a scalar top-quark partner appears in supersymmetry as the bosonic superpartner of the top quark, fermionic top-quark partners appear in theories with a new broken global symmetry, in which the Higgs boson is interpreted as a pseudo Nambu-Goldstone boson [2], e.g., in Little Higgs [3,4] and Composite Higgs [5,6] models. In these models, the new symmetry corresponds to a new strong interaction, whose bound states include vectorlike quarks (VLQ). These are color-triplet spin-1/2 fermions, but in contrast to the chiral SM quarks their left- and right-handed components have the same properties under SU(2)$_L \times$ U(1)$_Y$ transformations.

Only a limited set of possibilities exists for the quantum numbers of the VLQs if gauge invariance is required to be preserved [7,8]. Their electric charge could be $+2/3e$ ($T$ quark), $-1/3e$ ($B$ quark), $+5/3e$ ($X$ quark) or $-4/3e$ ($Y$ quark), where $e$ is the elementary charge, and they could appear in electroweak singlets, $(T)$ or $(B)$, electroweak doublets, $(X T)$, $(T B)$, or $(B Y)$, or electroweak triplets, $(X T B)$ or $(T B Y)$. This paper focuses solely on the search for $T$ and $B$ quarks, which could couple to SM quarks by...
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mixing [9]. Although couplings of VLQs to first- and second-generation SM quarks are not excluded [10,11], this paper searches for VLQs that couple exclusively to third-generation SM quarks. The couplings of T and B quarks can be described in terms of \( \sin \theta_T \) and \( \sin \theta_B \) [12], where \( \theta_T \) and \( \theta_B \) are the mixing angles with the top quark and the b-quark, respectively, or they can be described in terms of generalized couplings \( \kappa_T \) and \( \kappa_B \) of the T or B quark to third-generation SM quarks [13,14].

Search strategies for VLQs have been proposed [12,15–18] that focus either on the search for VLQ pair production via the strong interaction or on single production via the electroweak interaction. The decay of T and B quarks can either happen via the charged current, i.e., \( T \to Wb \) and \( B \to Wt \), or via flavor-changing neutral currents [19], i.e., \( T \to Zt, T \to Ht, B \to Zb, \) and \( B \to Hb \). Decays including non-SM particles are not excluded [20], but are not considered in this paper, so that for T and B quarks the branching ratios (BR) to the three decay modes add up to unity. While the cross section for pair production is given by quantum chromodynamics, the single-production cross section explicitly depends on the coupling of the VLQ to SM quarks.

The ATLAS and CMS Collaborations have searched for pair production of T and B quarks that decay into third-generation quarks in pp collisions at \( \sqrt{s} = 8 \) TeV [21–26] in all three possible decay modes of each of the VLQs. Current searches at \( \sqrt{s} = 13 \) TeV have used single-lepton final states to search for the \( T \to Zt \) decay with the Z boson decaying invisibly [27,28], \( T \to Wb \) [29,30], \( T \to Ht \) [28], and \( B \to Wt \) [29,31], general single-lepton final states with boosted W and Higgs bosons [32], final states with leptons in the same electric charge [33], and all-hadronic final states [34]. The CMS Collaboration has also searched for pair production of T and B quarks in a combination of single-lepton final states, dilepton final states with the same electric charge and trilepton final states [35] at \( \sqrt{s} = 13 \) TeV. These searches have set upper limits at 95% confidence level (C.L.) on the VLQ pair-production cross section, also interpreted as lower limits on the VLQ mass, \( m_{VLQ} \) depending on the VLQ BRs assumed. The most stringent limits in the case of the T and B singlets are 1.20 TeV [35] and 1.17 TeV [31,35], respectively. In the case of 100% BRs of T to Zt and B to Zb, the most stringent limits are 1.30 TeV [35] and 0.96 TeV [35], respectively. The searches at \( \sqrt{s} = 13 \) TeV are significantly more sensitive than the searches at \( \sqrt{s} = 8 \) TeV due to the larger expected pair-production cross sections at the higher center-of-mass energy. This paper includes searches for pair-produced VLQs at \( \sqrt{s} = 13 \) TeV in final states with more than one lepton which are particularly sensitive to the decays \( T \to Zt \) and \( B \to Zb \).

At large \( m_{VLQ} \), the cross section for the single production of VLQs may be larger than the pair-production cross section because of the larger available phase space, even though single production is mediated by the weak interaction. However, the comparison of single- and pair-production cross sections depends on the assumed coupling to the SM quarks. Single production was searched for at \( \sqrt{s} = 8 \) TeV [23,36,37] by the ATLAS and CMS Collaborations. At \( \sqrt{s} = 13 \) TeV, the CMS Collaboration has searched for the decays \( T \to Wb \) [38], \( T \to Ht \) [39,40], \( T \to Zt \) [41,42], \( B \to Hb \) [43], \( B \to Zb \) [42], and \( B \to Wt \) [44]. In these searches, upper limits were set on the single-production cross section, which were also interpreted as upper limits on the coupling to SM quarks as a function of \( m_{VLQ} \). Similarly to the case of pair production, the expected single-production cross sections are much larger at \( \sqrt{s} = 13 \) TeV than at \( \sqrt{s} = 8 \) TeV, so that the searches at the higher center-of-mass energy are more sensitive. Searches for single-T-quark production at \( \sqrt{s} = 13 \) TeV were not performed before by the ATLAS Collaboration. As in the search for VLQ pair production, final states with more than one lepton are used, which are particularly sensitive to the decay \( T \to Zt \).

The analysis was performed with data collected in pp collisions at \( \sqrt{s} = 13 \) TeV, searching for the pair production of T and B quarks and for the single production of T quarks in final states with at least one Z boson. In the case of single production, the T quark is hence expected to decay into Zt. In the case of pair production, the search targets only one VLQ decay into a Z boson and a third-generation quark explicitly, so that it is particularly sensitive to all decays that include at least one Z boson in the final state, i.e., not only \( T\bar{T} \to Zt \bar{Z}t \) and \( B\bar{B} \to Zb \bar{Z}b \), but also \( T\bar{T} \to ZtWb, T\bar{T} \to ZtHt, B\bar{B} \to ZbWt \), and \( B\bar{B} \to ZbHb \).

The overall analysis strategy is based on a search that was performed with \( \sqrt{s} = 8 \) TeV data [23], which exploited the leptonic Z boson decays \( Z \to e^+e^- \) and \( Z \to \mu^+\mu^- \). Several improvements have been made, in particular new channels have been added and an event selection was used that was optimized for the higher \( \sqrt{s} \) and a larger data set. Five analysis channels are defined; three for the search for T and B pair production, and two for the search for single-T-quark production, as shown in Table 1. An event preselection that is common to all channels is used, in which all events are required to include a Z boson candidate, reconstructed from two same-flavor leptons (e, \( \mu \)) with opposite electric charge. The event selection in each channel was then optimized for a particular final state, as shown in Fig. 1. First, the searches were split into pair- and single-production categories and then further into dilepton channels—requiring no lepton in
addition to the leptons that are used to reconstruct the Z boson candidate—and trilepton channels, in which at least three leptons are required. Since the VLQs are assumed to decay into third-generation SM quarks, the presence of b-tagged jets is exploited in order to discriminate the signal from SM background processes. Since the signal process includes high-energy hadronically decaying massive resonances, large-R jets (J) are used in the dilepton channels, further enhancing the sensitivity of the search. In the dilepton single-production channel, top-tagging is used in order to identify large-R jets originating from the hadronic decays of high-energy top quarks. Only small-R jets are b tagged. As the reconstruction of small-R jets and large-R jets is independent of each other, b-tagged small-R jets can overlap with large-R jets. In both single-production channels, the presence of a forward jet from the t-channel production is used to suppress the background. Due to the large expected values of \( m_{VLQ} \), the transverse momentum \( p_T \), is expected to be much larger in signal than in background events. More requirements, in particular on the event kinematics, were optimized in each channel, as discussed in Sec. V. In the following, the three pair-production channels are referred to as the dilepton channel with at most one large-R jet (PP 2J 0-1J), the dilepton channel with at least two large-R jets (PP 2J ≥ 2J), and the trilepton channel (PP ≥ 3J). The two single-production channels are referred to as the dilepton channel (SP 2J), and the trilepton channel (SP ≥ 3J).

**II. THE ATLAS DETECTOR**

The ATLAS detector [45] at the LHC covers nearly the entire solid angle around the collision point. It consists of an inner tracking detector surrounded by a thin superconducting solenoid, electromagnetic and hadronic calorimeters, and a muon spectrometer incorporating three large superconducting toroidal magnets.

The inner-detector system (ID) is immersed in a 2 T axial magnetic field and provides charged-particle tracking in the range \(|\eta| < 2.5\). The high-granularity silicon pixel detector covers the vertex region and typically provides four measurements per track, the first hit being normally in the innermost layer, the insertable B-layer [46]. It is followed by the silicon microstrip tracker which usually provides four two-dimensional measurement points per track. These silicon detectors are complemented by the transition radiation tracker, which enables radially extended track reconstruction up to \(|\eta| = 2.0\). The transition radiation tracker also provides electron identification information based on the fraction of hits (typically 30 in total) above a higher energy-deposit threshold corresponding to transition radiation.

The calorimeter system covers the pseudorapidity range \(|\eta| < 4.9\). Within the region \(|\eta| < 3.2\), electromagnetic calorimetry is provided by barrel and endcap high-granularity lead/liquid-argon (LAr) electromagnetic calorimeters, with an additional thin LAr presampler covering \(|\eta| < 1.8\), to correct for energy loss in material upstream of the calorimeters. Hadronic calorimetry is provided by the steel/scintillator-tile calorimeter, segmented into three barrel structures within \(|\eta| < 1.7\), and two copper/LAr hadronic endcap calorimeters. The solid angle coverage is completed with forward copper/LAr and tungsten/LAr calorimeter modules optimized for electromagnetic and hadronic measurements respectively.

The muon spectrometer (MS) comprises separate trigger and high-precision tracking chambers measuring the deflection of muons in a magnetic field generated by superconducting air-core toroidal magnets. The field integral of the toroidal magnets ranges between 2.0 and 6.0 Tm across most of the detector. A set of precision chambers covers the region \(|\eta| < 2.7\) with three layers of monitored drift tubes, complemented by cathode strip chambers in the forward region, where the background is highest. The muon trigger system covers the range \(|\eta| < 2.4\) with
resistive plate chambers in the barrel, and thin gap chambers in the endcap regions.

A two-level trigger system is used in order to select interesting events [47]. The first-level trigger is implemented in hardware and uses a subset of detector information to reduce the event rate to a design value of at most 100 kHz. This is followed by a software-based trigger which reduces the event rate to about 1 kHz.

### III. DATA AND MONTE CARLO SAMPLES

For this search, $pp$ collision data collected with the ATLAS detector during 2015 and 2016 at $\sqrt{s} = 13$ TeV...
were used, corresponding to an integrated luminosity of 36.1 fb$^{-1}$. Only events taken during stable beam conditions, and for which all relevant components of the detector were operational, are considered. Events are required to have a primary vertex with at least two tracks with a minimum $p_T$ of 400 MeV each. If several such vertices exist, the vertex with the highest $\sum_{\text{tracks}} p_T^2$ is chosen as the hard-scatter vertex [48]. Events are rejected if they satisfy the criteria [49] designed to reject beam-induced background and backgrounds from cosmic-ray showers and calorimeter noise. Several single-lepton triggers with different $p_T$ thresholds were used for electrons and muons depending on the data-taking period. For data collected in 2015, the thresholds are 24, 60, and 120 GeV for electrons and 20 and 50 GeV for muons, where lepton isolation requirements are applied to the lowest-$p_T$ triggers to reduce their rate. For the highest-$p_T$ electron trigger, the identification criteria are relaxed. For data-taking in 2016, the thresholds were raised slightly to 26, 60, and 140 GeV for electrons and 26 and 50 GeV for muons.

The main sources of background in this search are $Z$ + jets and $t\bar{t}$ production in the case of the dilepton channels and diboson ($WZ$, $WW$, $ZZ$) and $t\bar{t}$ + $X$ production in the case of the trilepton channels, where $t\bar{t}$ + $X$ is dominated by $t\bar{t}$ production with associated vector bosons ($t\bar{t}V$, $V = W$ or $Z$) but also includes $t\bar{t}t\bar{t}$ and $t\bar{t}WW$ production. Smaller sources of background are also considered, which include single-top and triboson production ($WWW$, $WWZ$, $WZZ$, $ZZZ$). The background contribution from $t\bar{t}H$ production was found to be negligible and is not considered in this search. For all background and signal processes, Monte Carlo (MC) samples were generated and the detector response was simulated in GEANT4 [50] with a full model of the ATLAS detector [51], unless stated otherwise. The simulations include the contributions from additional $pp$ collisions in the same or an adjacent bunch crossing (pileup). Corrections for trigger and object-identification efficiencies, and for $b$-tagging misidentification efficiencies, as well as for energy and momentum scales and resolutions of the objects were applied to the simulated samples, based on the differences observed between data and MC samples in reference processes. A summary of the background samples used in this paper is shown in Table II.

The $Z$ + jets process was simulated with SHERPA 2.2.1 [52–55] using the NNPDF3.0 [56] next-to-next-to-leading-order (NNLO) set of parton distribution functions (PDFs), and normalized to the NNLO cross section in QCD calculated with FEWZ [57] and the MSTW 2008 [58–60] NNLO PDF set. The $t\bar{t}$ process was simulated with the POWHEG method [61,62] implemented in POWHEG-Box v2 [63,64] using the NNPDF3.0 NNLO PDF set. POWHEG-Box was interfaced with PYTHIA8 [65] with the A14 set of tuned parameters [66] and the NNPDF2.3 leading order (LO) PDF set [67] for parton showering and hadronization. The $h_{\text{damp}}$ parameter in POWHEG-Box was set to 1.5$m_t$ [68], where $m_t = 172.5$ GeV. The sample was normalized to the NNLO cross section including resummation of next-to-next-to-leading logarithmic (NNLL) soft gluon terms with TOP++ [69–75]. The PDF and $\alpha_S$ uncertainties were calculated using the PDF4LHC prescription [76] with the MSTW 2008 NNLO, CT10 NNLO [77,78] and NNPDF2.3 5f FFN PDF sets, added in quadrature to the scale uncertainty. The diboson processes were simulated with SHERPA 2.2.1 for up to one additional parton at next-to-leading order (NLO) and up to three additional partons at LO using COMIX [54] and OPENLOOPS [79], and merged with the SHERPA parton shower [55] according to the ME + PS@NLO prescription [80]. The NNPDF3.0 NNLO PDF set was used and the samples were normalized to the NLO cross sections calculated with SHERPA. The $t\bar{t}V$ processes were simulated with MADGRAPH5_AMC@NLO.

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**TABLE II. List of background Monte Carlo samples used, giving information about the matrix-element generator, the parton shower program to which it is interfaced and its set of tuned parameters ("tune," if applicable), the PDF sets used in the matrix element (ME), and the order in QCD of the cross-section calculation.**

<table>
<thead>
<tr>
<th>Generator</th>
<th>Shower program and tune</th>
<th>PDF set (ME)</th>
<th>Cross section</th>
</tr>
</thead>
<tbody>
<tr>
<td>$Z$ + jets</td>
<td>SHERPA 2.2.1</td>
<td>SHERPA 2.2.1</td>
<td>NNPDF3.0 NNLO</td>
</tr>
<tr>
<td>$t\bar{t}$</td>
<td>POWHEG-BOX v2</td>
<td>PYTHIA8, A14</td>
<td>NNPDF3.0 NNLO</td>
</tr>
<tr>
<td>Diboson</td>
<td>SHERPA 2.2.1</td>
<td>SHERPA 2.2.1</td>
<td>NNPDF3.0 NNLO</td>
</tr>
<tr>
<td>$t\bar{t}$ + V ($W/Z$)</td>
<td>MADGRAPH5_AMC@NLO</td>
<td>PYTHIA8, A14</td>
<td>NNPDF3.0 NLO</td>
</tr>
<tr>
<td>$t\bar{t}$ + $WW$</td>
<td>MADGRAPH5</td>
<td>PYTHIA8, A14</td>
<td>NNPDF2.3 LO</td>
</tr>
<tr>
<td>$t\bar{t}t\bar{t}$</td>
<td>MADGRAPH5</td>
<td>PYTHIA8, A14</td>
<td>NNPDF2.3 LO</td>
</tr>
<tr>
<td>Single top</td>
<td>POWHEG-BOX v1</td>
<td>PYTHIA 8, Perugia 2012</td>
<td>CT10</td>
</tr>
<tr>
<td>Triboson</td>
<td>SHERPA 2.1</td>
<td>SHERPA 2.1</td>
<td>CT10</td>
</tr>
</tbody>
</table>

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3In the figures in this paper the smaller backgrounds are grouped together and are denoted by “Other.”

4The order in perturbation theory refers to QCD throughout this paper.

5MC programs that model nonperturbative effects, such as the parton shower, hadronization, and multiple parton interaction need to be fit ("tuned") to collider data, as the values of these parameters cannot be derived from first principles.

6The $h_{\text{damp}}$ Parameter controls the transverse momentum of the first additional gluon emission beyond the Born configuration. The main effect of choosing $h_{\text{damp}} = 1.5m_t$ is to regulate the high-$p_T$ emission against which the $t\bar{t}$ system recoils.
using SHERPA 2.1 using the CT10 PDF set, and normalized to the NLO cross sections calculated with MADGRAPH5_AMC@NLO. The single-top processes were simulated with POWHEG-BOX v1 using the CT10 PDF set. POWHEG-Box was interfaced to PYTHIA8 with the Perugia 2012 set of tuned parameters and the CTEQ6L1 PDF set. The single-top samples were normalized to NLO cross sections with additional NNLL soft gluon terms. The triboson processes were simulated using SHERPA 2.1 using the CT10 PDF set, and normalized to the NLO cross sections calculated with SHERPA. The $t\bar{t}t\bar{t}$ and $t\bar{t}+WW$ processes were simulated with MADGRAPH5 and pythia8 using the NNPDF2.3 LO PDF set and the A14 set of tuned parameters, and were normalized to the NLO cross section calculated with MADGRAPH5_AMC@NLO. Additional MC samples were generated for the evaluation of systematic uncertainties due to the choice of factorization and renormalization scales, generator, and parton shower program for the $Z + $jets, $t\bar{t}$, $t\bar{t}+V$ and diboson background processes. These samples are described in Sec. VI.

The pair production of VLQs was simulated at LO with PROTOS using the NNPDF2.3LO PDF set. PROTOS was interfaced to PYTHIA8 with the A14 set of tuned parameters. Samples were produced for $m_{VLQ}$ in the range of 500 to 1400 GeV. Steps of 50 GeV were used in the range from 700 to 1200 GeV, and steps of 100 GeV otherwise. The samples were generated for the singlet model for $T$ and $B$ quarks, but samples at $m_{VLQ}$ of 700, 900 and 1200 GeV were also generated in the $T/B$ doublet model in order to test kinematic differences between singlet and doublet models. In the singlet models, the BRs are independent of the mixing angles between VLQ and SM quarks for small values of the mixing angles and hence only a function of $m_{VLQ}$. With this assumption, for large $m_{VLQ}$, the BRs approach the relative proportions of 50:25:25 for the $W:Z:H$ decay modes in the singlet model for the $T$ quark as well as for the $B$ quark. In the ($X T$) doublet and ($B Y$) doublet models, the BRs approach the relative proportions of 50:50 for the $Z:H$ decays of the $T$ quark and $B$ quark, respectively. The same holds for the ($T B$) doublet model if the top quark mixes much more strongly with its VLQ partner than the bottom quark, a natural scenario for the SM Yukawa couplings. However, kinematic differences may exist between the singlet and doublet models. The samples generated for the ($T B$) doublet were used to verify that such kinematic differences have a small impact on the analysis, and therefore the difference between the two cases is only a change in the BRs. Thus, the singlet model samples were also used for the doublet case, reweighting the yields for each decay mode to obtain the expected observables for any given BR. The pair-production cross sections were calculated with TOP++ at NNLO + NNLL using the MSTW 2008 NNLO PDF set.

The single production of $T$ quarks was simulated using MADGRAPH5 with the “VLQ” UFO model, which implements the Lagrangian described in Ref. [13], using the NNPDF2.3 LO PDF set. MADGRAPH was interfaced to PYTHIA8 with the A14 set of tuned parameters. Only the decay $T \rightarrow Zt$ was considered. Samples were generated with a $T$ quark produced via $Wb$ and also via $Zt$ interactions. Since production via the $Zt$ interaction is suppressed due to the required top quark in the initial state, single-VLQ production refers to production via the $Wb$ interaction in the remainder of this paper, unless stated otherwise. Samples were generated for $m_{VLQ}$ in the range from 700 to 2000 GeV, with steps of 100 GeV (200 GeV) in the range 700–1600 GeV (1600–2000 GeV), with a benchmark coupling of $\kappa_T = 0.5$ for the $Wb$ and $Zt$ interactions. Additional samples were generated with alternative values of $\kappa_T = 0.1$ and 1.0 in order to study the effect of a varying $T$-quark width on kinematic distributions.

The single-production cross sections were calculated [14] at NLO and in narrow-width approximation for $c_W = 1$, with the coupling $c_W$ defined in Ref. [14] and corresponding to $\kappa_T$ up to numerical constants. In order to predict the cross section for different values of $c_W$, they are multiplied by $c_W^2$. It was shown in the context of this analysis that the chirality of the coupling has a negligible impact on the sensitivity of the analysis and hence $c_W$ is taken as the sum in quadrature of the left- and right-handed couplings $c_{W,L}$ and $c_{W,R}$, i.e., $c_W = \sqrt{c_{W,L}^2 + c_{W,R}^2}$. The cross section is additionally corrected for width effects calculated with MADGRAPH5, assuming that the ratio of NLO and LO cross sections remains approximately the same for a nonvanishing $T$-quark width. The cross section is then multiplied by the BR for the decay into $Zt$ in the singlet model, which is $\approx 25\%$ in the range of VLQ masses investigated in this analysis. The benchmark coupling of $\kappa_T = 0.5$ corresponds to a coupling of the $T$ quark to the $W$ boson $c_W = 0.45$.

IV. OBJECT RECONSTRUCTION

Reconstructed electrons, muons and jets are used. Jets are reconstructed with the anti-$k_t$ algorithm [92] with a radius parameter of 0.4 (small-$R$ jets) and with a parameter of 1.0 (large-$R$ jets). A b-tagging algorithm is applied to small-$R$ jets, and a top-tagging algorithm is applied to large-$R$ jets. Moreover, missing transverse momentum ($E_{T,\text{miss}}$) is used for the definition of one signal-enriched region and one background-enriched region. For electrons, muons and jets, an overlap-removal procedure based on their proximity in $\eta$-$\phi$ space is used, as described at the end of this section.

Electrons are reconstructed [93] from energy clusters in the electromagnetic calorimeter with ID tracks matched to them. Their energy is calibrated [94,95], and they are required to fulfill the “tight likelihood” identification.
criteria [93]. Electrons are required to have a minimum transverse energy, $E_T$, of at least 28 GeV and to be within the fiducial region $|\eta_{\text{cluster}}| < 2.47$, excluding the barrel-endcap transition region, $1.37 < |\eta_{\text{cluster}}| < 1.52$. Electron tracks must point to the primary vertex, which is ensured by requiring that the track’s impact parameter significance is smaller than 5, and that $|z_0 \cdot \sin \theta|$ is smaller than 0.5 mm, where $z_0$ is the distance along the z axis between the primary vertex and the track’s point of closest approach. In order to suppress background from electrons originating from hadron decays and from hadrons that are misidentified as electrons, an isolation criterion is applied that requires the scalar sum of the $p_T$ of the tracks which point to the primary vertex within a cone around the electron (but excluding its track) to be less than 6% of its $E_T$. A variable cone size of $|\Delta R| = \min(10 \text{ GeV}/E_T, 0.2)$ is used.

Muons are reconstructed [97] from combined tracks in the MS and the ID. Their transverse momentum, $p_T$, is calibrated [97], and they are required to fulfill the “medium” identification criteria [97]. Muons must have a minimum $p_T$ of 28 GeV and they must be within the fiducial region $|\eta| < 2.5$. Muon tracks must point to the primary vertex, which is ensured by requiring that the track’s impact parameter significance is smaller than 3, and that $|z_0 \cdot \sin \theta|$ is smaller than 0.5 mm. In order to suppress background from muons originating from hadron decays, an isolation criterion similar to that for electrons is applied: the scalar sum of the $p_T$ of the tracks around the muon which point to the primary vertex, excluding the muon track, must be less than 6% of its $p_T$, using a variable cone size of $|\Delta R| = \min(10 \text{ GeV}/p_T, 0.3)$.

Small-$R$ jets are reconstructed from topological clusters of calorimeter cells [98,99] with the anti-$k_t$ algorithm using FASTJET [100] with a radius parameter of 0.4. Small-$R$ jets are calibrated to the jet energy scale (JES) at particle level [101] and are required to be within the fiducial volume $|\eta| < 4.5$. Small-$R$ jets with $|\eta| < 2.5$ must have a minimum $p_T$ of 25 GeV and forward jets, $2.5 < |\eta| < 4.5$, must have a minimum $p_T$ of 35 GeV to reduce contributions from pileup. For small-$R$ jets with $|\eta| < 2.4$ and $p_T < 60$ GeV, pileup contributions are suppressed by the use of the jet vertex tagger [102]. Small-$R$ jets within $|\eta| < 2.5$ are $b$-tagged using the MV2c10 algorithm [103], for which several basic $b$-tagging-algorithms [104] are combined in a boosted decision tree. The MV2c10 algorithm is used such that it provides a $b$-tagging efficiency of $\sim 77\%$ for $b$-jets, and a rejection factor of $\sim 6$ for $c$-jets and $\sim 130$ for other light jets, based on simulated $t\bar{t}$ events.

Large-$R$ jets are also reconstructed from topological clusters with the anti-$k_t$ algorithm, but with a radius parameter of 1.0. In contrast to the small-$R$ jet calibration, the topological clusters that are used as inputs to the large-$R$ jet reconstruction take into account corrections for the calorimeter’s response to hadrons and other effects [105]. Contributions to large-$R$ jets from pileup and the underlying event are removed by applying trimming [106] with parameters that were optimized for separating large-$R$ jets that originate from hadronic decays of high-energy massive resonances [107–109] from those that originate from $b$-quarks, light quarks or gluons. Large-$R$ jets are calibrated to the JES at particle level [110]. They are required to have a minimum $p_T$ of 200 GeV and to be within the fiducial region $|\eta| < 2.0$. The mass of large-$R$ jets is calculated from a combination of calorimeter and tracking information [111]. It is calibrated [111] and required to be at least 50 GeV, which suppresses contributions from $b$-jets and light jets in favor of large-$R$ jets that originate from hadronic decays of high-energy W bosons, Z bosons, Higgs bosons, and top quarks. In the SP 2$\ell$ channel (Sec. VD), top-tagging is used to identify hadronic decays of high-energy top quarks. It is based on a combination [109] of the large-$R$ jet mass and the $N$-subjettiness [112,113] ratio $\tau_3/\tau_2$, calculated in the “winner-take-all” mode [114]. This top-tagger provides an efficiency of $\sim 80\%$ for hadronically decaying top quarks with a $p_T$ of at least 200 GeV with a varying background rejection of $\sim 20$ at $p_T = 200$ GeV that decreases to $\sim 4$ at $p_T = 1$ TeV, as estimated with simulated dijet events.

In order to avoid double-counting of tracks or energy deposits and in order to improve the identification of the different reconstructed objects, a sequential overlap-removal procedure is used. In the first step, electrons that share a track with a muon are removed. In the second step, any small-$R$ jet is removed that has a $|\Delta R|$ to an electron that is smaller than 0.2, and in the third step, electrons are removed if they are closer than 0.4 to any remaining small-$R$ jet. Finally, small-$R$ jets that have a $|\Delta R| < 0.04 + 10 \text{ GeV}/p_T(\mu)$ to a muon are removed if they have at most two associated tracks with $p_T(\text{track}) > 0.5$ GeV, otherwise the muon is removed. Small-$R$ jets and large-$R$ jets are not subject to an overlap-removal procedure, because the analysis strategies in all channels are designed such that the energy deposits in large-$R$ jets and small-$R$ jets are not counted twice, as explained in the following lines: in the trilepton channels, large-$R$ jets are not used (Secs. VC and VE); in the dilepton pair-production channels, large-$R$ jets are only used for the classification of events (Secs. VA and VB); in the dilepton single-production channel, small-$R$ jets are only used for the classification of events, but not for the calculation of the discriminating variable (Sec. VD).

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7 Jets originating from the hadronization of gluons and light quarks ($u$-, $d$-, $s$- and $c$-quarks) are called light jets in this document. Jets originating from the hadronization of $b$-quarks are called $b$-jets.

8 The rejection factor is defined as the inverse of the $b$-tagging efficiency for non-$b$-jets.
Missing transverse momentum is only used for the reduction of the contribution from $T\bar{T}$ pair production in one search region for single-$T$-quark production (Sec. V D) and for the definition of one background-enriched region (Sec. V B), and it is calculated from the vectorial sum of the transverse momenta of reconstructed and calibrated leptons and small-$R$ jets [115], with the overlap between these objects removed. The calculation also includes the contributions from tracks in the ID that are matched to the primary vertex but are not associated with any of the reconstructed objects.

V. EVENT SELECTION AND BACKGROUND CONTROL REGIONS

Five different channels are analyzed, each searching for either pair production or single production of VLQs, as introduced in Sec. I and visualized in Fig. 1. In each channel, event-selection criteria were optimized for maximum sensitivity to benchmark processes by studying expected 95% C.L. exclusion limits. In the pair-production channels, the mass reach for $T$ and $B$ quarks in the singlet and doublet models was maximized. While the search focuses on the decay of one VLQ to a $Z$ boson and a third-generation SM quark, a high sensitivity to all three $T$- and $B$-quark decay modes is ensured by choosing these benchmark models, because the second VLQ is not only allowed to decay into a $Z$ boson, but also into a $W$ boson or a Higgs boson in association with a third-generation SM quark. In the single-production channels, the sensitivity to single-$T$-quark production via the exchange of a $W$ boson with $\kappa_T = 0.5$ was optimized.

A preselection common to the channels was used as the basis for these optimizations. This preselection requires the presence of a $Z$ boson candidate that is constructed from two leptons with opposite-sign electric charge. In all events, at least two leptons of the same flavor with $p_T > 28$ GeV and with opposite-sign electric charge are required. Out of all such lepton pairs in an event, a $Z$ boson candidate is defined by the pair with invariant mass closest to the mass of the $Z$ boson. Events in which this invariant mass is larger than 400 GeV are removed because they are very unlikely to occur in any of the considered signal processes. In addition, at least two small-$R$ jets with $p_T > 25$ GeV must be present. In the SP $2\ell'$ channel, this last criterion is replaced by a requirement on the presence of at least one large-$R$ jet with $p_T > 200$ GeV and $m > 50$ GeV.

In Fig. 2, normalized distributions after preselection are shown for the sum of all background processes, which are estimated from MC simulations, as well as for benchmark signal models for pair and single VLQ production. In Fig. 2 (a), the distribution of the number of leptons is shown. By selecting events with exactly two leptons, a high signal efficiency is achieved. In events with at least three leptons, however, the signal-to-background ratio is significantly improved. The searches for pair and single production are hence split into complementary dilepton and trilepton channels. The distribution of the number of $b$-tagged jets is shown in Fig. 2(b). A higher number of $b$-tagged jets is characteristic of the signal processes, and at least one or two $b$-tagged jets are required in the event selection, depending on the channel. The distribution of the number of large-$R$ jets is shown in Fig. 2(c) for events that contain exactly two charged leptons. Signal events show a higher number of large-$R$ jets than background events, which in signal mostly originate from the hadronic decays of boosted top quarks, $W$ bosons, $Z$ bosons or Higgs bosons. The presence of large-$R$ jets is used in the dilepton channels to suppress backgrounds and hence improve the sensitivity to the signal. In order to achieve a high signal efficiency, in the pair-production case, two complementary dilepton channels are defined, one for events with at most one large-$R$ jet and one for events with at least two large-$R$ jets. In the trilepton channels, large-$R$ jet requirements are not used because the presence of at least three leptons suppresses the backgrounds efficiently. In Fig. 2(d), the forward-jet multiplicity is shown. The single-production process often features a forward jet from $t$-channel production. The presence of a forward jet is hence used in the single-production searches to separate the signal from the background.

The event selection criteria in the different channels are defined in Secs. VA–VE. In each channel, these signal regions (SR) are complemented by a set of control regions (CR), which are rich in the main background processes. The CRs are used to check the modeling of the background and to improve the background prediction in the SRs by a combined fit of CRs and SRs (Sec. VII). In the design of the CRs, not only a high purity of the respective background processes was aimed for, but also a large number of background events, as well as kinematic properties of the background events that resemble those of the events in the SRs. Each CR was checked to ensure that it was not sensitive to any signal process.

All SRs and CRs defined in the three pair-production channels (Secs. VA–VC) are orthogonal (i.e., they have no common events), so that the results in these channels can be combined (Sec. VII). The same holds for all SRs and CRs in the single-production channels (Secs. VD–VE), which are also combined (Sec. VII). Orthogonality is not ensured between pair- and single-production regions. However, single-production channels include requirements designed to suppress the pair-production signal in their SRs.

A. Search strategy: PP $2\ell' 0-1J$

Two orthogonal channels are defined for the pair-production search in dilepton final states, one with at least two large-$R$ jets, described in Sec. VB (PP $2\ell' \geq 2J$), and one with at most one large-$R$ jet (PP $2\ell' 0-1J$), described in this section. All such large-$R$ jets are required to have a $p_T$ of at least 200 GeV and a mass of at least 50 GeV after
trimming. Due to the mass requirement, hadronic decays of boosted top quarks, and of $W$, $Z$, and Higgs bosons are efficiently selected and jets that originate from the hadronization of high-$p_T$ light quarks, $b$-quarks or gluons are suppressed. While in the PP $2\ell \geq 2J$ channel background processes are strongly suppressed, the signal efficiency is also reduced so that a complementary channel optimized for events with at most one large-$R$ jet provides additional sensitivity to the signal.

The definitions of the SRs in the PP $2\ell 0-1J$ channel are summarized in Table III. Two SRs are defined, for which the preselection and the presence of exactly two leptons are required. The mass of the $Z$ boson candidate, built from the two leptons, $m_{\ell\ell}$, must be within a 10 GeV window around the $Z$ boson mass, $m_Z$. At least two $b$-tagged jets must be present, which strongly reduces the background contribution from the production of a $Z$ boson in association with light jets. The sensitivity of the channel is improved by

9Small-$R$ jets that are $b$-tagged and large-$R$ jets may overlap in $\eta-\phi$ space, but no requirement is made on the proximity of $b$-tagged small-$R$ jets and large-$R$ jets.
TABLE III. Definition of the control and signal regions for the PP $2\ell^0-1J$ channel.

<table>
<thead>
<tr>
<th>$t\bar{t}$ CR</th>
<th>$Z +$ jets CR</th>
<th>0-large-$R$ jet SR</th>
<th>1-large-$R$ jet SR</th>
</tr>
</thead>
<tbody>
<tr>
<td>Preselection</td>
<td>$=2$ leptons</td>
<td></td>
<td></td>
</tr>
<tr>
<td>$</td>
<td>m_{\ell\ell} - m_Z</td>
<td>&gt; 10$ GeV</td>
<td>$</td>
</tr>
<tr>
<td>and $m_{\ell\ell} &gt; 50$ GeV</td>
<td>$\geq 2$ $b$-tagged jets</td>
<td>$\leq 1$ large-$R$ jet</td>
<td>$=0$ large-$R$ jets</td>
</tr>
<tr>
<td>$p_{T,\ell\ell} &lt; 600$ GeV</td>
<td>$H_T &gt; 200$ GeV</td>
<td>$200$ GeV $&lt; H_T &lt; 800$ GeV</td>
<td>$H_T &gt; 800$ GeV</td>
</tr>
</tbody>
</table>

In order to validate the modeling of the main background processes, CRs are defined for the $Z +$ jets and $t\bar{t}$ processes. A summary of the CR definitions is given in Table III. The $Z +$ jets CR is defined by the same criteria as the SRs, except for the large-$R$ jets and $H_T$ criteria. Events with no large-$R$ jets and events with exactly one large-$R$ jet are considered together and $H_T$ is required to be in the range $200–800$ GeV, ensuring that the CR is almost free of a potential signal. The resulting CR sample is expected to be $88\%$ $Z +$ jets events. The $t\bar{t}$ CR is defined by requiring the same preselection, lepton multiplicity, and $b$-tagged-jet multiplicity criteria as in the SRs. However, the mass of the $Z$ boson candidate, $m_{\ell\ell}$, must be outside of a $10$ GeV window around the $Z$ boson mass, $m_Z$. In addition, $m_{\ell\ell}$ is required to be larger than $50$ GeV, because events with lower $m_{\ell\ell}$ do not stem mainly from $t\bar{t}$ production, but from Drell-Yan production in association with jets. Also in the $t\bar{t}$ CR, events without large-$R$ jets and events with exactly one large-$R$ jet are considered together. In contrast to the definition of the SRs, the $p_T$ of the $Z$ boson candidate is required to be less than $600$ GeV in order to ensure that the CR does not contain signal contributions from potential VLQ pair production with two leptons that do not stem from the decay of a $Z$ boson, such as $T\bar{T} \rightarrow HtWb$. Moreover, the lower bound on $H_T$ is lowered to $200$ GeV in order to increase the number of events in the CR and to test the modeling of the full $H_T$ distribution. The resulting CR sample is expected to be $93\% t\bar{t}$ events. The ratio of expected signal and background events in the $Z +$ jets ($t\bar{t}$) CR is as low as $0.0005 \, (0.003)$ for $B\bar{B}$ and $T\bar{T}$ production in the singlet model for $m_{VLQ} = 900$ GeV.

B. Search strategy: PP $2\ell^0 \geq 2J$

In addition to the PP $2\ell^0-1J$ channel, a second dilepton channel was optimized for events with at least two large-$R$ jets (PP $2\ell^0 \geq 2J$) in order to exploit the presence of highly boosted, hadronically decaying massive resonances in the signal processes.

The definition of the SR in the PP $2\ell^0 \geq 2J$ channel is summarized in Table IV. The same requirements as in the PP $2\ell^0-1J$ channel are imposed: the preselection, the presence of exactly two leptons with $m_{\ell\ell}$ within a $10$ GeV window around $m_Z$, and the presence of at least two $b$-tagged jets. In addition, at least two large-$R$ jets are required in each event. Also in this channel, the large expected values for $p_{T,\ell\ell}$ and $H_T$ are exploited to discriminate the signal from the background processes. The optimized requirements are $p_{T,\ell\ell} > 250$ GeV and $H_T > 1150$ GeV. In order to search for an excess of data over the background prediction, the invariant mass of the $Z$ boson candidate and the highest-$p_T$ $b$-tagged jet, $m_{Zb}$, is used as a discriminating variable. In the search for $B\bar{B}$ production, $m_{Zb}$ would show a resonant structure around $m_{VLQ}$ if VLQs were present, because it often corresponds to the reconstructed mass of the VLQ. Also, in the search for $T\bar{T}$ production, this variable shows very good discrimination between signal and background, with the signal resulting in larger values of $m_{Zb}$ than the background.
The main background processes are $Z + \text{jets}$ production with two jets originating from the hadronization of $b$-quarks, and $\bar{t}\bar{t}$ production in the dileptonic decay mode. As in the PP $2\ell'$ 0-1J channel, $\bar{t}\bar{t}$ production is strongly suppressed by requiring $m_{\ell\ell}$ to be close to the mass of the $Z$ boson, and the contributions from all background processes are significantly reduced by the requirements on $p_{T,\ell\ell}$ and $H_T$. The contributions from $Z + \text{jets}$ production and dileptonic $\bar{t}\bar{t}$ decays are efficiently reduced by the presence of two large-$R$ jets, because no massive hadronically decaying resonance is present in these processes.

For the two main background processes, $Z + \text{jets}$ and $\bar{t}\bar{t}$ production, CRs are defined. A summary of the CR definitions is given in Table IV. Similarly to the $\bar{t}\bar{t}$ CR in the PP $2\ell'$ 0-1J channel, the definition of the $\bar{t}\bar{t}$ CR is based on the requirement that $m_{\ell\ell}$ must be outside a 10 GeV window around $m_Z$ but must still fulfill $m_{\ell\ell} > 50$ GeV. In order to suppress potential signal contributions in the CR, $p_{T,\ell\ell}$ is required to be smaller than 600 GeV. The requirement on $H_T$ is removed, which increases the number of events in the CR. In addition, $E_T^{\text{miss}}$ is required to be smaller than 200 GeV, which reduces potential signal contributions from VLQ pair production with two leptons that do not stem from the decay of a $Z$ boson, but e.g., from the decay of $W$ bosons from the VLQ decay chain. Moreover, the $\Delta R$ between the $Z$ boson candidate and the highest-$p_T$ large-$R$ jet is required to be smaller than 2.0 or larger than 2.8, which further reduces the contributions from a potential signal because in signal events the highest-$p_T$ large-$R$ jet and the $Z$ boson candidate are typically not back to back due to the presence of additional final-state particles. The resulting CR sample is expected to be 82\% $\bar{t}\bar{t}$ events. The CR for the $Z + \text{jets}$ process is defined by the same criteria as in the SR, but the requirement on $H_T$ is inverted in order to remove potential signal contributions, and the requirement on $p_{T,\ell\ell}$ is removed in order to increase the number of events in the CR. The resulting CR sample is expected to be only 64\% $Z + \text{jets}$ events, but also 17\% $\bar{t}\bar{t}$ events. The ratio of expected signal and background events in the $Z + \text{jets}$ ($\bar{t}\bar{t}$) CR is as low as 0.03 (0.06) for $BB$ and 0.04 (0.04) for $T\bar{t}$ production in the singlet model for $m_{\text{VLQ}} = 900$ GeV.

### Table IV. Definition of the control regions and the signal region for the PP $2\ell' \geq 2\,\text{J}$ channel.

<table>
<thead>
<tr>
<th>$\bar{t}\bar{t}$ CR</th>
<th>$Z + \text{jets}$ CR</th>
<th>SR</th>
</tr>
</thead>
<tbody>
<tr>
<td>$</td>
<td>m_{\ell\ell} - m_Z</td>
<td>&gt; 10$ GeV and $m_{\ell\ell} &gt; 50$ GeV</td>
</tr>
<tr>
<td>$\geq 2$ leptons</td>
<td></td>
<td></td>
</tr>
<tr>
<td>$p_{T,\ell\ell} &lt; 600$ GeV</td>
<td></td>
<td></td>
</tr>
<tr>
<td>$E_T^{\text{miss}} &lt; 200$ GeV</td>
<td></td>
<td></td>
</tr>
<tr>
<td>$\Delta R(\ell\ell,\text{highest-}p_T\text{-tagged jet}) &lt; 2.0$ or $&gt; 2.8$</td>
<td></td>
<td></td>
</tr>
<tr>
<td>$</td>
<td>m_{\ell\ell} - m_Z</td>
<td>&lt; 10$ GeV</td>
</tr>
<tr>
<td>$\geq 2$ $b$-tagged jets</td>
<td></td>
<td></td>
</tr>
<tr>
<td>$p_{T,\ell\ell} &gt; 250$ GeV</td>
<td></td>
<td></td>
</tr>
<tr>
<td>$H_T &lt; 1150$ GeV</td>
<td></td>
<td></td>
</tr>
</tbody>
</table>

### C. Search strategy: PP $\geq 3\ell'$

The trilepton pair-production channel (PP $\geq 3\ell'$) is sensitive to signal events in which at least one lepton appears in addition to the leptons from the $Z$ boson decay that originates from $T \rightarrow Zt$ or $B \rightarrow Zb$. Additional leptons can originate from the decay of the other VLQ, such as in $B \rightarrow Wt \rightarrow \ell\nu_b qq'$ or $T \rightarrow Ht \rightarrow b\bar{b}\ell\nu_b$. In $T\bar{T}$ production, an additional lepton can also originate from the $T \rightarrow Zt$ decay itself, if the top quark decays into $\ell\nu_{\ell}b$.

The definition of the SR is summarized in Table V. Events must pass the preselection, and they must have at least three leptons including a $Z$ boson candidate with $m_{\ell\ell}$ within a 10 GeV window around $m_Z$. Only one $b$-tagged jet is required, because background contributions are already strongly reduced by the requirement of at least one additional lepton. Relaxing the $b$-tagging requirement compared to the dilepton channels improves the sensitivity to the signal processes because of the larger signal efficiency. As in the dilepton channels, a large transverse momentum of the $Z$ boson candidate is required, $p_{T,\ell\ell} > 200$ GeV. In order to search for an excess of data over the background prediction, the scalar sum of the small-$R$ jet and lepton transverse momenta, $S_T$, is used. In contrast to the use of $H_T$ in the PP $2\ell'$ 0-1J channel (Sec. VA), the lepton transverse momenta are added to the discriminating variable $S_T$, which exploits the $p_T$ of all leptons in order to discriminate the signal from the background in addition to the use of $p_{T,\ell\ell}$, which is constructed from only two leptons.

The main background processes are diboson, in particular $WZ$ and $ZZ$, production, and $\bar{t}\bar{t} + X$ production.

### Table V. Definition of the control regions and the signal region for the PP $\geq 3\ell'$ channel.

<table>
<thead>
<tr>
<th>Diboson CR</th>
<th>$\bar{t}\bar{t} + X$ CR</th>
<th>SR</th>
</tr>
</thead>
<tbody>
<tr>
<td>Preselection</td>
<td></td>
<td></td>
</tr>
<tr>
<td>$\geq 3$ leptons</td>
<td></td>
<td></td>
</tr>
<tr>
<td>$</td>
<td>m_{\ell\ell} - m_Z</td>
<td>&lt; 10$ GeV</td>
</tr>
<tr>
<td>$= 0$ $b$-tagged jets</td>
<td></td>
<td></td>
</tr>
<tr>
<td>$\geq 1$ $b$-tagged jets</td>
<td></td>
<td></td>
</tr>
<tr>
<td>$p_{T,\ell\ell} \leq 200$ GeV</td>
<td></td>
<td></td>
</tr>
<tr>
<td>$p_{T,\ell\ell} \geq 200$ GeV</td>
<td></td>
<td></td>
</tr>
</tbody>
</table>
(dominated by $t\bar{t} + Z$ production), which can both result in events with three leptons. The diboson background is strongly reduced by the $b$-tagging requirement, so that only diboson events with additional $b$-jets or mistagged light jets pass the event selection. Both main backgrounds are suppressed by the requirement on $p_{T,\ell\ell}$, because in background events Z boson candidates rarely have a large transverse momentum.

For the two main background processes, diboson and $t\bar{t} + X$ production, CRs are defined and summarized in Table V. The diboson CR is defined by the same criteria as the SR, except for the $b$-tagging and $p_{T,\ell\ell}$ requirements. No $b$-tagged jets are allowed in the diboson CR, which reduces contributions from $t\bar{t} + X$ production and from a potential VLQ signal. The $p_{T,\ell\ell}$ requirement is removed in order to further increase the number of diboson events in the CR. The resulting CR is expected to consist of 92% diboson events, mainly from $WZ$ production. The $t\bar{t} + X$ CR is defined by inverting only the $p_{T,\ell\ell}$ requirement, which removes contributions from a potential VLQ signal. The resulting CR sample is expected to consist mainly of $t\bar{t} + X$ and diboson events in similar proportions (39% and 43%, respectively). The ratio of expected signal and background events in the diboson ($t\bar{t} + X$) CR is as low as 0.001 (0.004) for $B\bar{B}$ and 0.001 (0.006) for $t\bar{t}T$ production in the singlet model for $m_{V_{LQ}} = 900$ GeV.

### Table VI. Definition of the control regions and the signal region for the SP 2$\ell\ell$ channel.

<table>
<thead>
<tr>
<th>0 - $b$-tagged-jet CR</th>
<th>$\geq 1 - b$-tagged-jet CR</th>
<th>SR</th>
</tr>
</thead>
<tbody>
<tr>
<td>Preselection with $\geq 1$ large-$R$ jet</td>
<td></td>
<td></td>
</tr>
<tr>
<td>=2 leptons</td>
<td></td>
<td></td>
</tr>
<tr>
<td>$</td>
<td>m_{\ell\ell} - m_{Z}</td>
<td>&lt; 10$ GeV</td>
</tr>
<tr>
<td>$p_{T,\ell\ell} &gt; 200$ GeV</td>
<td></td>
<td></td>
</tr>
<tr>
<td>=0 $b$-tagged jets</td>
<td></td>
<td></td>
</tr>
<tr>
<td>$\geq 1$ loose-not-tight top-tagged large-$R$ jet</td>
<td></td>
<td></td>
</tr>
<tr>
<td>$\geq 1$ $b$-tagged jets</td>
<td></td>
<td></td>
</tr>
<tr>
<td>$\geq 1$ top-tagged large-$R$ jet</td>
<td></td>
<td></td>
</tr>
<tr>
<td>$\geq 1$ forward jet</td>
<td></td>
<td></td>
</tr>
<tr>
<td>$H_T + E_T^{miss} &lt; m_{Zt}$</td>
<td></td>
<td></td>
</tr>
</tbody>
</table>

The definition of the SR is summarized in Table VI. Events are required to pass the preselection with the minimum requirement of two small-$R$ jets replaced by the presence of at least one large-$R$ jet. Events must have exactly two leptons that form a Z boson candidate with an invariant mass within a 10 GeV window around $m_Z$. In this channel, a minimum $p_T$ of the Z boson candidate is also required, $p_{T,\ell\ell} > 200$ GeV. At least one $b$-tagged jet is required in the event. Although a second $b$-quark from gluon splitting (Fig. 1) is present in the signal, only in a fraction of signal events is a second $b$-tagged jet found within the $|\eta|$ acceptance of the ID. The hadronically decaying top quark originating from the T-quark decay often has such a large $p_T$ that the top-quark decay products are contained within one large-$R$ jet. Top-tagging is used to discriminate large-$R$ jets from hadronic top-quark decays in single-$T$-quark production from the main background process, $Z +$ jets production, which can only fulfill this requirement if a quark or gluon jet is falsely top tagged (mistags). At least one forward jet is required in each event, which is a characteristic property of single-$T$-quark production.

In order to search for an excess of data over the background prediction, the invariant mass of the Z boson candidate and the highest-$p_T$ top-tagged large-$R$ jet, $m_{Zt}$, is used, which, if VLQs were present, would show a resonant structure around $m_{V_{LQ}}$. In order to facilitate the interpretation of the search for single-$T$-quark production, the potential signal contribution from $t\bar{t}T$ production is reduced by requiring $H_T + E_T^{miss} < m_{Zt}$. This requirement has an efficiency of $\approx 20\%$ for $t\bar{t}T$ pair production in the singlet model in the mass range 800–1400 GeV, while maintaining an efficiency of 90%–95% for single-$T$-quark production with $x_T = 0.5$ across the whole mass range studied.

The main background process is $Z +$ jets production, which mainly passes the event selection in the SR if it contains jets that originate from the hadronization of $b$-quarks. The Z boson is mostly produced with low values of $p_T$, so that the $p_{T,\ell\ell}$ requirement strongly reduces this background. In addition, the requirement of at least one top-tagged large-$R$ jet efficiently suppresses the contribution from $Z +$ jets production, because it does not contain top quarks and can only fulfill the top-tagging
requirement through mistags. Similarly, the requirement of at least one forward jet reduces the $Z +$ jets background, because forward jets are not characteristic for the main production mode of this process.

For the $Z +$ jets production background, two CRs are defined. One CR, called 0-$b$-tagged-jet CR, requires that no $b$-tagged jets be present, allowing to correct the modeling of $Z +$ jets production in a region that is kinematically close to the SR. In a second CR, called $\geq 1$-$b$-tagged-jet CR, the modeling of $Z +$ jets production in association with $b$-tagged jets is controlled. If good data-MC agreement is observed in both CRs consistently, this provides confidence in the overall modeling of $Z +$ jets production.

A summary of the CR definitions is given in Table VI. Both CRs are based on the SR with changes to the top-tagging, forward-jet and $b$-tagging requirements. For both CRs, the top-tagging requirement is changed, so that there must be at least one large-$R$ jet that fails the top-tagging requirements on $\tau_{32}$ but fulfills the top-tagging requirements on the large-$R$ jet mass. Out of these large-$R$ jets, called “loose-not-tight top tagged,” the large-$R$ jet with the largest $p_T$ is used in the calculation of $m_{Zj}$ in the CRs. The change in the top-tagging requirement enriches the CRs in $Z +$ jets production in comparison with a potential signal contribution. In both CRs, the forward-jet requirement is removed, which increases the number of events in the CRs. Finally, in the 0-$b$-tagged-jet CR, no $b$-tagged jet is allowed, while in the $\geq 1$-$b$-tagged-jet CR the same $b$-tagging requirement as in the SR is used. The resulting samples in the CRs are expected to be 96% and 91% $Z +$ jets events, respectively, and to contain a negligible amount of a potential single-$T$-quark signal. The ratio of expected signal and background events in the 0-$b$-tagged-jet ($\geq 1$-$b$-tagged-jet) CR is as low as 0.001 (0.02) for single-$T$-quark production with $m_{VLQ} = 900$ GeV with $\kappa_T = 0.5$. As the CRs do not contain requirements on the number of forward jets and make use of a modified top-tagging requirement (loose-not-tight), the modeling of the $Z +$ jets background was cross-checked in another region with no $b$-tagged jets, but requiring the presence of at least one forward jet and using the nominal top-tagging algorithm. The modeling of the distributions of kinematic properties was found to be consistent between the CRs and the cross-check region and a small difference observed between the overall numbers of events was assigned as a systematic uncertainty (Sec. VI).

### E. Search strategy: SP $\geq 3\ell$

The search for single-$T$-quark production in the trilepton channel (SP $\geq 3\ell$) is sensitive to the decay $T \rightarrow Zt \rightarrow Z \ell \ell \nu \bar{\nu}b$, featuring an additional lepton from the top-quark decay. It is hence complementary to the SP 2$\ell$ channel (Sec. V D).

The definition of the SR is summarized in Table VII. Events must pass the preselection, and they must have at least three leptons including a $Z$ boson candidate with $m_{\ell\ell}$ within a 10 GeV window around $m_Z$. In this channel, a minimum $p_T$ of the $Z$ boson candidate is also required, $p_{T,\ell\ell} > 150$ GeV. As in the SP 2$\ell$ channel (Sec. V D), at least one $b$-tagged-jet and at least one forward jet are required. In order to suppress background contributions in which leptons have lower $p_T$ on average than in the signal, the transverse momentum of the highest-$p_T$ lepton in each event, max $p_T^l$, must be larger than 200 GeV. As in the SP 2$\ell$ channel, the potential signal contribution from $T\bar{T}$ production is reduced in the search for single-$T$-quark production. In the SP $\geq 3\ell$ channel, this is achieved by requiring that $H_T$ multiplied by the number of small-$R$ jets in the event is smaller than 6 TeV. This requirement has an efficiency of 50%-30% for $T\bar{T}$ pair production in the singlet model in the mass range 800–1400 GeV, while maintaining an efficiency of $\approx 95\%$ for single-$T$-quark production with $\kappa_T = 0.5$ across the whole mass range studied. In order to search for an excess of data over the background prediction, $S_T$ is used, as in the PP $\geq 3\ell$ channel (Sec. V C).

The main background processes are diboson production with additional $b$-quarks and $t\bar{t} + X$ production (dominated by $t\bar{t} + Z$ production). The contributions of these backgrounds are strongly reduced by the requirements on $p_{T,\ell\ell}$ and max $p_T^l$, as well as by requiring at least one forward jet, because forward jets are not characteristic for these processes. For the two main background processes, diboson and $t\bar{t} + X$ production, two CRs are defined and summarized in

<table>
<thead>
<tr>
<th>Diboson CR</th>
<th>$t\bar{t} + X$ CR</th>
<th>SR</th>
</tr>
</thead>
<tbody>
<tr>
<td>Preselection $\geq 3$ leptons $</td>
<td>m_{\ell\ell} - m_Z</td>
<td>&lt; 10$ GeV</td>
</tr>
<tr>
<td>$=0$ $b$-tagged jets</td>
<td>$=0$ forward jets $\geq 1$ $b$-tagged jets $p_{T,\ell\ell} &gt; 150$ GeV</td>
<td></td>
</tr>
<tr>
<td>$\geq 1$ $b$-tagged jets $28$ GeV $&lt; \max p_T^l &lt; 200$ GeV</td>
<td>$\max p_T^l &gt; 200$ GeV</td>
<td></td>
</tr>
<tr>
<td>$H_T \times (\text{number of small-$R$ jets}) &lt; 6$ TeV</td>
<td></td>
<td></td>
</tr>
</tbody>
</table>
The diboson CR is defined following the criteria in the SR, but the requirements on $p_{T,\ell}/$, max $p_T^\ell$ and the presence of at least one forward jet are removed in order to increase the number of events in the CR. In addition, no $b$-tagged jet is allowed in the diboson CR. The resulting CR sample is expected to be 92% diboson events and to contain a negligible number of potential signal events. The $t\bar{t} + X$ CR is based on the SR by inverting the requirement on max $p_T^\ell$ and by requiring that no forward jet is present. These changes remove potential signal contributions. In addition, the requirement on $p_{T,\ell}/$ is removed in order to increase the number of events in the CR. The resulting CR sample is expected to consist mainly of $t\bar{t} + X$ and diboson events in similar proportions (40% and 44%, respectively). The ratio of expected signal and background events in the diboson ($t\bar{t} + X$) CR is as low as 0.002 (0.007) for single-$T$-quark production with $m_{\text{VLQ}} = 900$ GeV with $\kappa_T = 0.5$.

VI. SYSTEMATIC UNCERTAINTIES

Systematic uncertainties are divided into experimental uncertainties, mostly related to the uncertainty in the modeling of the detector response in the simulation, and theoretical uncertainties, related to the theoretical modeling of the background processes in the MC simulation. Experimental uncertainties on the signal efficiencies and the signal shape of the discriminating variables are also taken into account.

Systematic uncertainties are evaluated by varying each source by $\pm 1\sigma$ of its uncertainty. As a result, the predicted background and signal event yields in the different CRs and SRs can vary as well as the predicted shapes of the discriminating variables in these regions. For some sources only one systematic variation is defined. In such cases, the effect on the yields and shapes are symmetrized in order to construct the corresponding variation in the other direction.

The uncertainty in the integrated luminosity of the analyzed data set is 2.1%. It is derived following a methodology similar to that in Ref. [116] from a calibration of the luminosity scale using $x$-$y$ beam-separation scans in August 2015 and May 2016.

Uncertainties in electron and muon trigger, reconstruction, and identification efficiencies are derived from data using $Z \rightarrow e^+e^-$ decays [93] and $Z \rightarrow \mu^+\mu^-$ decays [97]. Uncertainties in the electron (muon) energy (momentum) calibration and resolution are also derived using $Z \rightarrow e^+\ell^-\ell^-$ events [95,97].

Uncertainties in the small-$R$ jet energy scale are evaluated from MC simulations and from data using multijet, $Z +$ jets, and $\gamma +$ jets events [101]. Additional small-$R$ jet uncertainties arise from the jet energy resolution [117], which are also derived from multijet, $Z +$ jets and $\gamma +$ jets events and from the jet vertex tagger.

Uncertainties in the $b$-tagging efficiency of small-$R$ jets are derived from data [104] for $b$-jets, $c$-jets, and other light jets. For the derivation of the $b$-tagging efficiency and its uncertainty for $b$-jets, dileptonic $t\bar{t}$ events are used [118]. Additional uncertainties are derived using MC simulations for the extrapolation of this efficiency beyond the kinematic reach of the calibration.

Uncertainties in the large-$R$ jet energy scale, mass and $N$-subjettiness ratio $\tau_2$ are derived from a comparison of the calorimeter-to-track-jet ratio in data and MC simulations [110,119]. While the uncertainty in the mass is taken to be correlated with the uncertainty in the energy scale, the $\tau_2$ uncertainty is taken to be uncorrelated with these two. The uncertainty in the resolutions of the large-$R$ jet energy, mass and $\tau_2$ is estimated by comparing the prediction from the nominal MC simulations with simulations where the resolution is 20% poorer.

The electron, muon, and small-$R$ jet uncertainties are propagated to the calculation of the $E_T^{\text{miss}}$. Additional uncertainties are assigned to contributions to the $E_T^{\text{miss}}$ calculation that arise from the theoretical modeling of the detector response in the simulation, and the theoretical modeling of the energy scale, mass and $\tau_2$-tagging efficiency of small-$R$ jets. For the derivation of the $E_T^{\text{miss}}$ and its uncertainty, the uncertainties associated with the predictions from the jet energy scale, mass and $\tau_2$-tagging efficiency are propagated to the calculation of the $E_T^{\text{miss}}$. Additional uncertainties are derived using MC simulations in data and MC simulations [110,119]. While the uncertainty in the mass is taken to be correlated with the uncertainty in the energy scale, the $\tau_2$ uncertainty is taken to be uncorrelated with these two. The uncertainty in the resolutions of the large-$R$ jet energy, mass and $\tau_2$ is estimated by comparing the prediction from the nominal MC simulations with simulations where the resolution is 20% poorer.

All MC distributions are reweighted so that the distribution of the average number of interactions per bunch crossing corresponds to the distribution in data. In order to assess the associated systematic uncertainty, the reweighting is varied within its uncertainty.

A 5% uncertainty is assigned to the cross section for $Z +$ jets production [120]. Additional uncertainties in the selection efficiency and in the shape of the final discriminator due to the theoretical modeling of the $Z +$ jets process are evaluated by comparing the nominal SHERPA sample with alternative samples, normalized to the same cross section. An uncertainty due to the choice of generator and parton shower is assigned by comparing the nominal sample with a sample generated with MADGRAPH5, AMC@NLO and the NNPDF3.0 NLO PDF set, and showered with PYTHIA8 and using the A14 set of tuned parameters with the NNPDF2.3 LO PDF set. An uncertainty due to the scale choice is evaluated by varying the renormalization and factorization scales in the nominal sample independently by factors of 2 and 0.5. The assigned uncertainty is based on the largest deviations from the nominal sample observed in each bin of the final discriminator. An uncertainty due to the choice of PDF set is evaluated by comparing the nominal SHERPA sample using the NNPDF3.0 NLO PDF set with samples using the MMHT2014 NNLO [121] and CT14 NNLO PDF sets [122]. The largest observed deviations from the nominal sample in each bin of the final discriminator are used to assign the uncertainty.

The uncertainty in the cross section for $t\bar{t}$ production is assigned as $+5.6\%/-6.1\%$ [123]. Also for $t\bar{t}$ production, additional uncertainties in the selection efficiency and in the shape of the final discriminator are assigned by comparing the nominal sample with alternative MC samples. An uncertainty due to the choice of generator is
evaluated from a comparison of the nominal POWHEG-BOX sample with a sample generated with MADGRAPH5_ AMC@NLO with the NNPDF3.0 NLO PDF set, and showered with PYTHIA8 using the A14 set of tuned parameters and the NNPDF2.3 LO PDF set. An uncertainty due to the choice of shower model is assigned by comparing the nominal sample, showered by PYTHIA8, with an alternative sample showered by HERWIG 7 [124,125] with the H7-UE-MMHT set of tuned parameters and the MMHT PDF set. The uncertainties due to the choice of renormalization and factorization scales are evaluated by independently varying the scales by factors of 2 and 0.5. The largest differences observed in each bin of the final discriminant are assigned as the systematic uncertainty for these two scales. An uncertainty due to the choice of PDF set is evaluated by comparing the nominal sample with samples generated with the MMHT2014 NLO and CT14 NLO PDF sets. The largest observed deviations from the nominal sample in each bin of the final discriminant are used to assign the uncertainty.

An uncertainty of 6% is assigned to the cross section for diboson production [120]. As with the Z + jets and HONE processes, alternative MC samples are used to assess additional uncertainties in the selection efficiency and in the shape of the final discriminant of the diboson processes. In order to assess the uncertainty due to the choice of renormalization and factorization scales, the nominal SHERPA samples are compared with alternative samples with the scales varied independently by factors of 2 and 0.5 and the largest observed differences in each bin of the final discriminant are assigned as the uncertainty. An uncertainty due to the choice of PDF set is assessed by comparing the nominal samples, generated with the NNPDF3.0 NNLO PDF set, with samples generated with the MMHT2014 NNLO and CT14 NNLO PDF sets. The largest deviations in each bin of the final discriminant are used to assign the uncertainty.

For the HONE + V processes, uncertainties of +13%/-12% are assigned for the HONE + W production cross section and of +10/-12% for the HONE + Z production cross section [126]. For the assessment of additional uncertainties in the selection efficiency and in the shape of the final discriminant of the HONE + V processes, the nominal samples are compared with alternative MC samples. An uncertainty due to the choice of generator is assigned by comparing the nominal sample with a sample generated with SHERPA 2.2 and the NNPDF3.0 NLO PDF set. For these samples, a fast simulation of the ATLAS detector [51] was used, which relies on a parametrization of the calorimeter response [127]. The nominal sample was additionally produced with the fast simulation configuration and the relative differences observed in the comparison with the samples with varied scales are assigned as the systematic uncertainty. An uncertainty due to the parton shower is assigned by comparing the nominal sample with samples with a varied amount of initial-state radiation. These alternative samples were produced with fast detector simulation and the procedure to assign a systematic uncertainty is again based on the relative difference observed in comparison with the nominal sample obtained with fast detector simulation in each bin of the final discriminant.

Backgrounds due to misidentified electrons and muons play a minor role in this analysis, because such leptons typically have low transverse momentum and are hence strongly suppressed by the SR requirements, in particular by the lower thresholds for $p_T^{EE}$ in the different channels. However, in the $t\bar{t}$ CRs in the PP $2\ell^\pm$ 0-1J and PP $2\ell^\pm \geq 2J$ channels and in the $Z$ + jets CR in the PP $2\ell^\pm \geq 2J$ channel, low-$p_T^{EE}$ events are included. Similarly, $Z$ + jets and $t\bar{t}$ events could contribute to the CRs and SRs in the PP $\geq 3\ell^\pm$ and SP $\geq 3\ell^\pm$ channels due to misidentified leptons. The maximum observed difference between data and MC simulations in the lepton $p_T$ spectra in the CRs is 25%. This is assigned as an uncertainty to Z + jets and $t\bar{t}$ events in the trilepton channels and to $t\bar{t}$ events with $p_T^{EE} < 200$ GeV in the PP $2\ell^\pm$ 0-1J and PP $2\ell^\pm \geq 2J$ channels.

No b-tagged jet are allowed in the diboson CRs for the PP $\geq 3\ell^\pm$ and SP $\geq 3\ell^\pm$ channels (Secs. V C and V E). While this requirement ensures a high purity in diboson processes, it differs from the requirements in the SRs. An uncertainty of 50% is assigned to the production of diboson events in association with b-quarks, motivated by the precision of measurements of W- and Z-boson production in association with b-quarks [128,129].

In order to ensure a large number of events in the CRs for the dilepton single-production search, the SR forward-jet requirement is removed (Sec. V D). A cross-check was performed in a region that only differs from the SR by a veto on b-tagged jets. While the modeling of the shapes of kinematic variables in this region is satisfactory, the 11% difference in the overall number of events between data and background expectation is assigned as an additional uncertainty in the SR due to the forward-jet requirement.

The uncertainties on the reconstructed objects and the luminosity also affect the predictions for VLQ pair and single production. No further uncertainties on the signal processes were considered. As discussed in Sec. III, the MC samples for VLQ pair production were generated in the singlet model and alternative BR hypotheses for T and B quarks are obtained by reweighting the singlet BRs to the alternative BRs. This procedure is validated by comparing kinematic distributions of the nominal VLQ pair production samples with alternative samples that were generated in the (T B) doublet model. After reweighting both to the same BRs, no large differences were observed between these samples. Hence, the reweighting procedure is considered validated and no systematic uncertainty is assigned.
TABLE VIII. Observed number of events in data and prefit expected number of signal and background events in the control and signal regions for the PP $2\ell'\,0-1J$ channel, i.e., before the fit to data. For the signal, the expected number of events for the $BB$ and $T\bar{T}$ benchmark processes with $m_{VLO} = 900$ GeV is shown for the singlet model. Statistical uncertainties from the limited size of MC samples and systematic uncertainties are added in quadrature. The uncertainty in the ratio of the observed and expected numbers of events is calculated.

<table>
<thead>
<tr>
<th></th>
<th>$\bar{t}\bar{t}$ CR</th>
<th>$Z + \text{jets}$ CR</th>
<th>0-large-(R) jet SR</th>
<th>1-large-(R) jet SR</th>
</tr>
</thead>
<tbody>
<tr>
<td>Singlet $BB$ (900 GeV)</td>
<td>$16.2 \pm 1.0$</td>
<td>$2.29 \pm 0.31$</td>
<td>$1.94 \pm 0.27$</td>
<td>$10.6 \pm 0.8$</td>
</tr>
<tr>
<td>Singlet $T\bar{T}$ (900 GeV)</td>
<td>$14.9 \pm 0.9$</td>
<td>$1.81 \pm 0.21$</td>
<td>$0.43 \pm 0.09$</td>
<td>$5.1 \pm 0.4$</td>
</tr>
<tr>
<td>$Z + \text{jets}$</td>
<td>$1090 \pm 310$</td>
<td>$630 \pm 190$</td>
<td>$21 \pm 9$</td>
<td>$43 \pm 21$</td>
</tr>
<tr>
<td>$\bar{t}\bar{t}$</td>
<td>$30000 \pm 8000$</td>
<td>$8 \pm 4$</td>
<td>$2 \pm 5$</td>
<td>$2 \pm 5$</td>
</tr>
<tr>
<td>Single top</td>
<td>$640 \pm 60$</td>
<td>$5.3 \pm 0.6$</td>
<td>$0.40 \pm 0.23$</td>
<td>$0.71 \pm 0.24$</td>
</tr>
<tr>
<td>$\bar{t}\bar{X}$</td>
<td>$199 \pm 26$</td>
<td>$37 \pm 7$</td>
<td>$0.55 \pm 0.23$</td>
<td>$4.6 \pm 1.4$</td>
</tr>
<tr>
<td>Diboson</td>
<td>$44 \pm 16$</td>
<td>$37 \pm 12$</td>
<td>$0.9 \pm 0.4$</td>
<td>$3.1 \pm 1.9$</td>
</tr>
<tr>
<td>Total background</td>
<td>$32000 \pm 8000$</td>
<td>$710 \pm 190$</td>
<td>$24 \pm 9$</td>
<td>$54 \pm 21$</td>
</tr>
<tr>
<td>Data</td>
<td>$32216$</td>
<td>$699$</td>
<td>$35$</td>
<td>$51$</td>
</tr>
<tr>
<td>Data/background</td>
<td>$1.00 \pm 0.26$</td>
<td>$0.98 \pm 0.26$</td>
<td>$1.4 \pm 0.6$</td>
<td>$1.0 \pm 0.4$</td>
</tr>
</tbody>
</table>

TABLE IX. Observed number of events in data and postfit expected number of background events in the control and signal regions for the PP $2\ell'\,0-1J$ channel, i.e., after the fit to the data $H_T$ distributions under the background-only hypothesis. The uncertainty in the expected number of events is the full uncertainty from the fit, from which the uncertainty in the ratio of the observed and expected numbers of events is calculated.

<table>
<thead>
<tr>
<th></th>
<th>$\bar{t}\bar{t}$ CR</th>
<th>$Z + \text{jets}$ CR</th>
<th>0-large-(R) jet SR</th>
<th>1-large-(R) jet SR</th>
</tr>
</thead>
<tbody>
<tr>
<td>$Z + \text{jets}$</td>
<td>$1100 \pm 100$</td>
<td>$622 \pm 34$</td>
<td>$21.6 \pm 2.6$</td>
<td>$43 \pm 4$</td>
</tr>
<tr>
<td>$\bar{t}\bar{t}$</td>
<td>$30200 \pm 600$</td>
<td>$8.7 \pm 3.0$</td>
<td>$3.1 \pm 2.3$</td>
<td>$2.4 \pm 2.0$</td>
</tr>
<tr>
<td>Single top</td>
<td>$630 \pm 50$</td>
<td>$5.2 \pm 0.6$</td>
<td>$0.40 \pm 0.23$</td>
<td>$0.72 \pm 0.20$</td>
</tr>
<tr>
<td>$\bar{t}\bar{X}$</td>
<td>$197 \pm 22$</td>
<td>$36 \pm 6$</td>
<td>$0.60 \pm 0.26$</td>
<td>$4.5 \pm 1.2$</td>
</tr>
<tr>
<td>Diboson</td>
<td>$44 \pm 6$</td>
<td>$37 \pm 4$</td>
<td>$0.87 \pm 0.24$</td>
<td>$3.1 \pm 0.7$</td>
</tr>
<tr>
<td>Total background</td>
<td>$32100 \pm 700$</td>
<td>$709 \pm 33$</td>
<td>$26.5 \pm 3.2$</td>
<td>$54 \pm 4$</td>
</tr>
<tr>
<td>Data</td>
<td>$32216$</td>
<td>$699$</td>
<td>$35$</td>
<td>$51$</td>
</tr>
<tr>
<td>Data/background</td>
<td>$1.003 \pm 0.020$</td>
<td>$0.99 \pm 0.05$</td>
<td>$1.32 \pm 0.16$</td>
<td>$0.95 \pm 0.08$</td>
</tr>
</tbody>
</table>

VII. RESULTS

In each channel, a binned likelihood fit is performed to the discriminating variable. Control and signal regions are fit simultaneously and systematic uncertainties are included in the fit as a set of nuisance parameters (NP), $\theta$. The likelihood function $L(\mu, \theta)$ consists of Poisson probabilities for each bin in the discriminating variable in each region, and a Gaussian or log-normal distribution for each NP. In the likelihood fit, the signal cross section $\sigma$ is parametrized by multiplying the predicted cross section with a correction factor $\mu$, called the signal-strength factor, which is a free parameter of the fit. In a background-only fit $\mu$, and hence $\sigma$, is set to zero. For the combined control and signal region fit the modeling of the main background processes was adjusted during the fit via changes in the NPs, so that the background prediction in the signal regions is improved. The binning of the discriminating variable in the different channels was chosen in order to retain as much shape information about the distribution as possible given the number of background MC events in each bin.

The effect of each single source of systematic uncertainty is treated as correlated across all regions and processes with the following two exceptions. In order to avoid that CRs with high statistical power are able to constrain NPs in very different regions of phase space, for the uncertainties associated with misidentified leptons, separate NPs are defined for the different CRs and SRs in each channel, and for the uncertainties related to the choice of MC generator and hadronization model, separate NPs are defined for each channel. Different sources of systematic uncertainty are treated as uncorrelated with each other, except for the case of the large-\(R\) jet scale uncertainties affecting the $p_T$ and mass, which are treated as 100\% correlated. In addition to the systematic uncertainties discussed in Sec. VI, an additional NP is added for each bin in the discriminating variable in each region due to the statistical uncertainty of the MC samples.

A. Results: PP $2\ell'\,0-1J$

The observed number of events in the SRs and CRs and the expected number of events for the different background
FIG. 3. Comparison of the distribution of the scalar sum of small-\(R\) jet transverse momenta, \(H_T\), between data and the background prediction in (a) the \(t\bar{t}\) control region, (b) the \(Z + \) jets control region, (c) the 0-large-\(R\) jet-signal region, and (d) the 1-large-\(R\) jet-signal region of the pair-production (PP) \(2\ell^0\) 0-1J channel. The background prediction is shown postfit, i.e., after the fit to the data \(H_T\) distributions under the background-only hypothesis. The last bin contains the overflow. An upward pointing triangle in the ratio plot indicates that the value of the ratio is beyond scale. An example distribution for a \(BB\) signal in the singlet model with \(m_{\text{VLQ}} = 900\) GeV is overlaid. For better visibility, it is multiplied by a factor of 5. The data are compatible with the background-only hypothesis.
FIG. 4. Comparison of the distribution of the transverse momentum of the $Z$ boson candidate, $p_T$, between data and the background prediction in (a) the $t\bar{t}$ control region, (b) the $Z$ + jets control region, (c) the 0-large-$R$ jet-signal region, and (d) the 1-large-$R$ jet-signal region of the pair-production (PP) 2$\ell$ 0-1J channel. The background prediction is shown postfit, i.e., after the fit to the data $H_T$ distributions under the background-only hypothesis. The last bin contains the overflow. An upward pointing triangle in the ratio plot indicates that the value of the ratio is beyond scale. An example distribution for a $B\bar{B}$ signal in the singlet model with $m_{VLQ} = 900$ GeV is overlaid. For better visibility, it is multiplied by a factor of 5. The data are compatible with the background-only hypothesis.
channel. Also shown is the expected number of events for $BB$ and $T\bar{T}$ production in the singlet model for $m_{\text{VLQ}} = 900$ GeV. The signal efficiencies for these benchmarks are 0.060% (0.013%) for $BB$ ($T\bar{T}$) in the 0-large-$R$ jet SR and 0.33% (0.16%) in the 1-large-$R$ jet SR, and include the branching ratios of the VLQ as well as of its decay products, including the decay $Z \rightarrow \ell^+ \ell^-$. A fit of the background prediction to the $H_T$ distributions in data was performed. The postfit yields are shown in Table IX. The uncertainty in the background prediction is significantly reduced in all regions compared to the prefit value (Table VIII). The overall $Z + \text{jets}$ ($\tau\tau$) normalization is adjusted by a factor of $0.99 \pm 0.05$ ($0.996 \pm 0.021$) in the $Z + \text{jets}$ ($\tau\tau$) CR. The ratios of the postfit and prefit background yields are consistent with unity in all regions.

In Fig. 3, the $H_T$ distribution is shown in the CRs and SRs for data and the background prediction after the fit. The VLQ pair-production signal would be expected to result in an excess of data over the background prediction at large values of $H_T$, as shown in Figs. 3(c) and 3(d). The modeling of the main backgrounds was validated by comparing the distributions of kinematic variables and object multiplicities between data and background prediction in each respective CR. As an example, the $p_{T,\ell\ell}$ distribution is shown in Fig. 4 in the two CRs and the two SRs. The background prediction is shown after the fit to the $H_T$ distribution. Good agreement between data and the background prediction is observed in both kinematic variables in the CRs, validating the background prediction.

### B. Results: PP $2\ell \geq 2J$

The observed and expected yields in the SR and the CRs and the expected number of events for the different background contributions are shown in Table X for the PP $2\ell \geq 2J$ channel. Also shown is the expected number of events for $BB$ and $T\bar{T}$ production in the singlet model for $m_{\text{VLQ}} = 900$ GeV. The signal efficiency in the SR for these benchmarks is 0.28% for both $BB$ and $T\bar{T}$ production, and includes the branching ratios of the VLQ as well as of its decay products, including the decay $Z \rightarrow \ell^+ \ell^-$. A fit of the background prediction to the $m_{Z\bar{b}}$ distributions in data was performed. The postfit yields are shown in Table XI. The uncertainty in the background prediction was significantly reduced in all regions compared to the prefit value (Table X). The overall $Z + \text{jets}$ ($\tau\tau$) normalization was adjusted by a factor of $0.91 \pm 0.15$ (1.21 $\pm$ 0.15) in the $Z + \text{jets}$ ($\tau\tau$) CR. The ratios of the postfit and prefit background yields are consistent with unity in all regions.

In Fig. 5, the $m_{Z\bar{b}}$ distribution is shown in the CRs and SR for data and the background prediction after the fit. The VLQ pair-production signal would be expected to result in an excess of data over the background prediction at large values of $m_{Z\bar{b}}$, as shown in Fig. 5(c). The modeling of the main backgrounds was validated by comparing the distributions of kinematic variables and object multiplicities between data and background prediction in the respective CR. As an example, the $H_T$ distribution is shown in Fig. 6 in the two CRs and in the SR. The background prediction is shown after the fit to the $m_{Z\bar{b}}$ distribution. Good agreement between data and the background prediction is apparent in kinematic variables in the CRs, validating the background prediction.

### C. Results: PP $\geq 3\ell$

The observed number of events in the SR and the CRs and the expected number of events for the different background contributions are shown in Table XII for the PP $\geq 3\ell$ channel. Also shown is the expected number of events for $BB$ and $T\bar{T}$ production in the singlet model for $m_{\text{VLQ}} = 900$ GeV. The uncertainty in the expected number of events is the full uncertainty from the fit, from which the uncertainty in the ratio of the observed and expected numbers of events is calculated.

---

**Table X.** Observed number of events in data and prefit expected number of signal and background events in the control regions and the signal region for the PP $2\ell \geq 2J$ channel, i.e., before the fit to data. For the signal, the expected number of events for the $BB$ and $T\bar{T}$ benchmark processes with $m_{\text{VLQ}} = 900$ GeV is shown for the singlet model. Statistical uncertainties from the limited size of MC samples and systematic uncertainties are added in quadrature. The uncertainty in the ratio of the observed and expected numbers of events contains the systematic uncertainties and the statistical uncertainty of the prediction from Poisson fluctuations.

<table>
<thead>
<tr>
<th>$\tau\tau$ CR</th>
<th>$Z + \text{jets}$ CR</th>
<th>SR</th>
</tr>
</thead>
<tbody>
<tr>
<td>$Z + \text{jets}$</td>
<td>$9.0 \pm 2.3$</td>
<td>$60 \pm 10$</td>
</tr>
<tr>
<td>$\tau\tau$</td>
<td>$95 \pm 12$</td>
<td>$20 \pm 6$</td>
</tr>
<tr>
<td>Single top</td>
<td>$1.5 \pm 0.6$</td>
<td>$0.63 \pm 0.28$</td>
</tr>
<tr>
<td>$\tau\tau + X$</td>
<td>$4.5 \pm 0.8$</td>
<td>$14.7 \pm 2.7$</td>
</tr>
<tr>
<td>Diboson</td>
<td>$0.74 \pm 0.20$</td>
<td>$4.2 \pm 0.8$</td>
</tr>
<tr>
<td>Total background</td>
<td>$111 \pm 12$</td>
<td>$100 \pm 10$</td>
</tr>
<tr>
<td>Data</td>
<td>$112$</td>
<td>$100$</td>
</tr>
<tr>
<td>Data/background</td>
<td>$1.01 \pm 0.11$</td>
<td>$1.00 \pm 0.10$</td>
</tr>
</tbody>
</table>

---

**Table XI.** Observed number of events in data and postfit expected number of background events in the control regions and the signal region for the PP $\geq 3\ell$ channel, i.e., after the fit to the data $m_{Z\bar{b}}$ distributions under the background-only hypothesis. The uncertainty in the expected number of events is the full uncertainty from the fit, from which the uncertainty in the ratio of the observed and expected numbers of events is calculated.

<table>
<thead>
<tr>
<th>$\tau\tau$ CR</th>
<th>$Z + \text{jets}$ CR</th>
<th>SR</th>
</tr>
</thead>
<tbody>
<tr>
<td>$Z + \text{jets}$</td>
<td>$9.0 \pm 2.3$</td>
<td>$60 \pm 10$</td>
</tr>
<tr>
<td>$\tau\tau$</td>
<td>$95 \pm 12$</td>
<td>$20 \pm 6$</td>
</tr>
<tr>
<td>Single top</td>
<td>$1.5 \pm 0.6$</td>
<td>$0.63 \pm 0.28$</td>
</tr>
<tr>
<td>$\tau\tau + X$</td>
<td>$4.5 \pm 0.8$</td>
<td>$14.7 \pm 2.7$</td>
</tr>
<tr>
<td>Diboson</td>
<td>$0.74 \pm 0.20$</td>
<td>$4.2 \pm 0.8$</td>
</tr>
<tr>
<td>Total background</td>
<td>$111 \pm 12$</td>
<td>$100 \pm 10$</td>
</tr>
<tr>
<td>Data</td>
<td>$112$</td>
<td>$100$</td>
</tr>
<tr>
<td>Data/background</td>
<td>$1.01 \pm 0.11$</td>
<td>$1.00 \pm 0.10$</td>
</tr>
</tbody>
</table>
FIG. 5. Comparison of the distribution of the invariant mass of the $Z$ boson candidate and the highest-$p_T$ $b$-tagged jet, $m_{Zb}$, between data and the background prediction in (a) the $t\bar{t}$ control region, (b) the $Z +$ jets control region, and (c) the signal region of the pair-production (PP) $2\ell \geq 2J$ channel. The background prediction is shown postfit, i.e., after the fit to the data $m_{Zb}$ distributions under the background-only hypothesis. The last bin contains the overflow. An upward or downward pointing triangle in the ratio plot indicates that the value of the ratio is beyond scale. An example distribution for a $BB$ signal in the singlet model with $m_{VLQ} = 900$ GeV is overlaid. The data are compatible with the background-only hypothesis.
FIG. 6. Comparison of the distribution of the scalar sum of small-$R$ jet transverse momenta, $H_T$, between data and the background prediction in (a) the $t\bar{t}$ control region, (b) the $Z$+jets control region, and (c) the signal region of the pair-production (PP) $2l' \geq 2J$ channel. The background prediction is shown postfit, i.e., after the fit to the data $m_{Zb}$ distributions under the background-only hypothesis. The last bin contains the overflow. An upward or downward pointing triangle in the ratio plot indicates that the value of the ratio is beyond scale. An example distribution for a $BB$ signal in the singlet model with $m_{VLQ} = 900$ GeV is overlaid. The data are compatible with the background-only hypothesis.
TABLE XII. Observed number of events in data and postfit expected number of signal and background events in the control regions and the signal region for the PP ≥ 3ℓ channel, i.e., before the fit to data. For the signal, the expected number of events for the BB and T T benchmark processes with m_{VLQ} = 900 GeV is shown for the singlet model. Statistical uncertainties from the limited size of MC samples and systematic uncertainties are added in quadrature. The uncertainty in the ratio of the observed and expected numbers of events contains the systematic uncertainties and the statistical uncertainty of the prediction from Poisson fluctuations.

| TABLE XIII. Observed number of events in data and postfit expected number of background events in the control regions and the signal region for the PP ≥ 3ℓ channel, i.e., after the fit to the data S_{T} distributions under the background-only hypothesis. The uncertainty in the expected number of events is the full uncertainty from the fit, from which the uncertainty in the ratio of the observed and expected numbers of events is calculated. |

| TABLE XIV. Observed number of events in data and postfit expected number of background events in the control regions and the signal region for the PP ≥ 3ℓ channel, i.e., after the fit to the data S_{T} distributions under the background-only hypothesis. The uncertainty in the expected number of events is the full uncertainty from the fit, from which the uncertainty in the ratio of the observed and expected numbers of events is calculated. |

for BB and T T production in the singlet model for m_{VLQ} = 900 GeV. The signal efficiency in the SR for these benchmarks is 0.31% for BB and 0.44% for T T production, and includes the branching ratios of the VLQ as well as of its decay products, including the decay \text{Z} \rightarrow \ell^{+}\ell^{-}.

A fit of the background prediction to the S_{T} distributions in data was performed and the postfit yields are shown in Table XIV. The uncertainty in the background prediction was significantly reduced in all regions compared to the prefit value (Table XII). The overall diboson (\text{t} \text{t} + X) normalization is adjusted by a factor of 0.94 ± 0.06 (1.06 ± 0.12) in the diboson (\text{t} \text{t} + X) CR. The ratios of the postfit and prefit background yields are consistent with unity in all regions.

In Fig. 7, the S_{T} distribution is shown in the CRs and SR for data and the background prediction after the fit. The VLQ pair-production signal would be expected to result in an excess of data over the background prediction at large values of S_{T}, as shown in Fig. 7(c). The modeling of the main background was validated by comparing the distributions of kinematic variables and object multiplicities between data and background prediction in the respective CR. As an example, the distribution of the p_{T} of the highest-p_{T} lepton, max p_{T} in the event is shown in Fig. 8 in the two CRs and in the SR. The background prediction is shown after the fit to the S_{T} distribution. Good agreement between data and the background prediction is observed in both kinematic variables in the CRs, validating the background prediction.

D. Results: SP 2ℓ

The observed number of events in the SR and the CRs and the expected number of events for the different background contributions are shown in Table XIV for the SP 2ℓ channel. Also shown is the expected number of events for single-T-quark production for m_{VLQ} = 900 GeV and \kappa_T = 0.5. The signal efficiency in the SR is 0.58% for T \rightarrow Zℓ decays produced via a bW_{T} coupling, and includes the branching ratios of the VLQ as well as of its decay products, including the decay Z \rightarrow \ell^{+}\ell^{-}.

A fit of the background prediction to the m_{Zℓ} distributions in data was performed and the postfit yields are shown in Table XV. The uncertainty in the background prediction was significantly reduced in all regions compared to the prefit value (Table XIV). The overall Z + jets normalization was adjusted by factors of 0.99 ± 0.04 and 0.93 ± 0.07 in the 0-b-tagged-jet CR and the ≥ 1-b-tagged-jet CR, respectively. The ratios of the postfit and prefit background yields are consistent with unity in all regions. The ratio for Z + jets production in the SR is 0.84 ± 0.10, which is consistent with unity within 2\sigma at most.

In Fig. 9, the m_{Zℓ} distribution is shown in the CRs and SR for data and the background prediction after the fit. The VLQ single-production signal would be expected to result in an excess of data over the background prediction in the m_{Zℓ} distribution, as shown in Fig. 9(c). The modeling of the main background was validated by comparing the distributions of kinematic variables and object multiplicities between data and background prediction in the two CRs. As an example, the p_{T} distribution of the highest-p_{T} top-tagged large-R jet in the event is shown in Fig. 10 in the two CRs and the SR. The background prediction is shown after the fit to the m_{Zℓ} distribution. Contributions from VLQ single production would be expected at high values of the large-R jet p_{T}. Good agreement between data and the background
FIG. 7. Comparison of the distribution of the scalar sum of small-$R$ jet and lepton transverse momenta, $S_T$, between data and the background prediction in (a) the diboson control region, (b) the $t\bar{t} + X$ control region, and (c) the signal region of the pair-production (PP) $\geq 3l$ channel. The background prediction is shown postfit, i.e., after the fit to the data $S_T$ distributions under the background-only hypothesis. The last bin contains the overflow. An upward pointing triangle in the ratio plot indicates that the value of the ratio is beyond scale. An example distribution for a $B\bar{B}$ signal in the singlet model with $m_{V_{LQ}} = 900$ GeV is overlaid. For better visibility, it is multiplied by a factor of 5. The data are compatible with the background-only hypothesis.
FIG. 8. Comparison of the distribution of the transverse momentum of the highest-$p_T$ lepton (leading lepton), $\max p_T^l$, between data and the background prediction in (a) the diboson control region, (b) the $t\bar{t} + X$ control region, and (c) the signal region of the pair-production ($PP \geq 3l$) channel. The background prediction is shown postfit, i.e., after the fit to the data $S_T$ distributions under the background-only hypothesis. The last bin contains the overflow. An example distribution for a $B\bar{B}$ signal in the singlet model with $m_{VLQ} = 900$ GeV is overlaid. For better visibility, it is multiplied by a factor of 5. The data are compatible with the background-only hypothesis.
The observed number of events in the SR and the CRs, validating the background prediction.

**E. Results: SP \( \geq 3\ell' \)**

The observed number of events in the SR and the CRs and the expected number of events for the different background contributions are shown in Table XVI for the SP \( \geq 3\ell' \) channel. Also shown is the expected number of events for single-\( T \)-quark production for \( m_{VLQ} = 900 \text{ GeV} \) and \( \kappa_T = 0.5 \). Due to a low number of MC events for the single-\( T \)-quark signal in the SP \( \geq 3\ell' \) channel, in this channel the signal efficiency was interpolated as a function of \( m_{VLQ} \) with a third-order polynomial describing the efficiencies estimated from MC simulations within the uncertainties. The resulting signal efficiency in the SR is 0.16% for \( T \to Zt \) decays produced via a \( bWT \) coupling, and includes the branching ratios of the VLQ as well as of its decay products, including the decay \( Z \to \ell^+\ell^- \).

A fit of the background prediction to the \( S_T \) distributions in data was performed. The postfit yields are shown in Table XVII. The uncertainty in the background prediction was significantly reduced in all regions compared to the prefit value (Table XVI). The overall diboson (\( \tilde{t}\tilde{t} + X \)) normalization was adjusted by a factor of 0.95 \( \pm \) 0.04 (1.12 \( \pm \) 0.15) in the diboson (\( \tilde{t}\tilde{t} + X \)) CR. The ratios of the postfit and prefit background yields are consistent with unity in all regions.

In Fig. 11, the \( S_T \) distribution is shown in the CRs and SR for data and the background prediction after the fit. For large values of \( m_{VLQ} \), VLQ single-production signal would be expected to result in an excess of data over the background prediction at large values of \( S_T \). An example for a lower value of \( m_{VLQ} \) is shown in Fig. 11(c). The modeling of the main backgrounds was validated by comparing the distributions of kinematic variables and object multiplicities between data and background prediction in the respective CR. As an example, the \( p_{T,\ell'} \) distribution is
FIG. 9. Comparison of the distribution of the invariant mass of the $Z$ boson candidate and the highest-$p_T$ top-tagged large-$R$ jet, $m_{Zt}$, between data and the background prediction in (a) the 0-b-tagged-jet control region, (b) the $\geq 1$-b-tagged-jet control region, and (c) the signal region of the single-production (SP) $2l$ channel. The background prediction is shown postfit, i.e., after the fit to the data $m_{Zt}$ distributions under the background-only hypothesis. The last bin contains the overflow. An upward pointing triangle in the ratio plot indicates that the value of the ratio is beyond scale. An example distribution for a single-$T$-quark signal with $m_{VLQ} = 900$ GeV and $\kappa_T = 0.5$ is overlaid. For better visibility, it is multiplied by a factor of 3. The data are compatible with the background-only hypothesis.
FIG. 10. Comparison of the distribution of the transverse momentum of the highest-\(p_T\) top-tagged large-\(R\) jet between data and the background prediction in (a) the \(0\)-\(b\)-tagged-jet control region, (b) the \(\geq 1\)-\(b\)-tagged-jet control region, and (c) the signal region of the single-production (SP) \(2\ell\) channel. The background prediction is shown postfit, i.e., after the fit to the data \(m_{Zt}\) distributions under the background-only hypothesis. The last bin contains the overflow. An upward pointing triangle in the ratio plot indicates that the value of the ratio is beyond scale. An example distribution for a single-\(T\)-quark signal with \(m_{V_{LQ}} = 900\) GeV and \(\kappa_T = 0.5\) is overlaid. For better visibility, it is multiplied by a factor of 3. The data are compatible with the background-only hypothesis.
showed in Fig. 12 in the two CRs and in the SR. The background prediction is shown after the fit to the $S_T$ distribution. Contributions from VLQ single production would be expected at high values of $p_{T,t}/E_T$. Good agreement between data and the background prediction is observed in both kinematic variables in the CRs, validating the background prediction.

VIII. INTERPRETATION

No excess of data over the background-only hypothesis is observed and 95% C.L. limits are set on the cross section ($\sigma$) as a function of the model parameters in the case of the pair-production channels, and on the cross section times branching ratio to $Zt$ [$\sigma \times BR(T \rightarrow Zt)$] in the single-production channels. For this purpose, the profile-likelihood ratio $q_\mu = -2 \ln(L(\mu, \hat{\theta})/L(\hat{\mu}, \hat{\theta}))$ was used as the test statistic, with $\hat{\mu}$ and $\hat{\theta}$ the values of the signal strength and the set of NPs that maximize the likelihood under the constraint $0 < \hat{\mu} < \mu$, and $\hat{\theta}$ the set of NPs that maximizes the likelihood for a given value of $\mu$. The test statistic $q_\mu$ was evaluated with RooFIt [130,131] and upper limits were derived from the probability distribution of $q_\mu$, evaluated with the asymptotic approximation [132]. The limits were calculated with the CL$_s$ method [133,134], excluding values of $\sigma$ at 95% C.L. for the pair-production channels and $\sigma \times BR(T \rightarrow Zt)$ for the single-production channels that resulted in a CL$_s$ value <0.05.

The three pair-production channels were combined in order to enhance the sensitivity to $TT$ and $BB$ production. A combined binned likelihood fit was performed including all CRs and SRs of the three channels. The systematic uncertainties related to the luminosity, the leptons, small-$R$ jets, $b$-tagging, large-$R$ jets, $E_T^{miss}$, and the average number of interactions per bunch crossing are correlated among all channels, as are the uncertainties in the cross sections for the background processes. Residual systematic uncertainties related to the MC modeling of the different background processes and misidentified leptons, were treated separately for each channel. This was done in order to avoid NPs constrained in the CRs of one channel inadvertently constraining kinematics in very different regions of other channels. It was verified that correlating these NPs in the combination of the channels has little impact on its sensitivity.

In Fig. 13, the expected and observed upper limits on the pair-production cross section are shown as a function of $m_{VLQ}$ for $T$ and $B$ quarks with different assumptions for the BRs: for singlet BRs; doublet BRs; and the case of 100% BR, to $Zt$ or $Zb$, respectively. Also shown are the expected upper limits on the cross section for the individual pair-production channels. The limits are compared with the predicted pair-production cross section, which results in lower limits on the mass of the $T$ and $B$ quarks in the
FIG. 11. Comparison of the distribution of the scalar sum of small-$R$ jet and lepton transverse momenta, $S_T$, between data and the background prediction in (a) the diboson control region, (b) the $t\bar{t} + X$ control region, and (c) the signal region of the single-production (SP) $\geq 3$ channel. The background prediction is shown postfit, i.e., after the fit to the data $S_T$ distributions under the background-only hypothesis. The last bin contains the overflow. An upward pointing triangle in the ratio plot indicates that the value of the ratio is beyond scale. An example distribution for a single-$T$-quark signal with $m_{V_{\text{VLQ}}} = 900$ GeV and $\kappa_T = 0.5$ is overlaid. The data are compatible with the background-only hypothesis.
FIG. 12. Comparison of the transverse momentum of the $Z$ boson candidate, $p_{T,\ell\ell}$, between data and the background prediction in (a) the diboson control region, (b) the $t\bar{t} + X$ control region, and (c) the signal region of the single-production (SP) $\geq 3\ell$ channel. The background prediction is shown postfit, i.e., after the fit to the data $S_T$ distributions under the background-only hypothesis. The last bin contains the overflow. An upward pointing triangle in the ratio plot indicates that the value of the ratio is beyond scale. An example distribution for a single-$T$-quark signal with $m_{VLQ} = 900$ GeV and $\kappa_T = 0.5$ is overlaid. The data are compatible with the background-only hypothesis.
different benchmark scenarios. These are summarized in Table XVIII for the individual channels, as well as for their combination.

All three pair-production channels contribute differently to the sensitivity of the analysis in the different benchmark scenarios. The PP $\geq 3\ell$ channel is particularly important for the sensitivity to $T\bar{T}$ production, where it has the best sensitivity in all three cases shown in Fig. 13. While the PP $2\ell \geq 2J$ channel also contributes significantly to the sensitivity of the analysis, the PP $2\ell \geq 0-1J$ channel is less sensitive to $T\bar{T}$ production. At very low $T$-quark masses, the PP $2\ell \geq 2J$ channel loses sensitivity compared with the
TABLE XVIII. Observed (expected) 95% C.L. mass limits for the singlet and doublet benchmark models, as well as for the case of 100% BR to $T \rightarrow Zt$ and $B \rightarrow Zb$ for the three pair-production channels and their combination.

<table>
<thead>
<tr>
<th>Model</th>
<th>PP $2\ell$ 0-1J</th>
<th>PP $2\ell \geq 2$J</th>
<th>PP $\geq 3\ell$</th>
<th>Combination</th>
</tr>
</thead>
<tbody>
<tr>
<td>$T\bar{T}$ singlet</td>
<td>740 (720) GeV</td>
<td>950 (930) GeV</td>
<td>950 (1010) GeV</td>
<td>1030 (1060) GeV</td>
</tr>
<tr>
<td>$T\bar{T}$ doublet</td>
<td>850 (820) GeV</td>
<td>1100 (1100) GeV</td>
<td>1090 (1150) GeV</td>
<td>1210 (1210) GeV</td>
</tr>
<tr>
<td>100% $T \rightarrow Zt$</td>
<td>920 (900) GeV</td>
<td>1210 (1210) GeV</td>
<td>1260 (1290) GeV</td>
<td>1340 (1320) GeV</td>
</tr>
<tr>
<td>$B\bar{B}$ singlet</td>
<td>860 (840) GeV</td>
<td>930 (950) GeV</td>
<td>890 (940) GeV</td>
<td>1010 (1030) GeV</td>
</tr>
<tr>
<td>$B\bar{B}$ doublet</td>
<td>1040 (1000) GeV</td>
<td>1060 (1070) GeV</td>
<td>820 (880) GeV</td>
<td>1140 (1120) GeV</td>
</tr>
<tr>
<td>100% $B \rightarrow Zb$</td>
<td>1110 (1080) GeV</td>
<td>1120 (1130) GeV</td>
<td>930 (980) GeV</td>
<td>1220 (1180) GeV</td>
</tr>
</tbody>
</table>

PP $\geq 3\ell$ channel, because the decay products of the $T$ quarks are less boosted and result in fewer large-$R$ jets. For $B\bar{B}$ production, the sensitivity is driven by the PP $2\ell$ 0-1J and PP $2\ell \geq 2$J channels in the case of the doublet and 100% BR benchmarks, with less sensitivity from the PP $\geq 3\ell$ channel. In general, the PP $2\ell$ 0-1J and PP $2\ell \geq 2$J channels have a similar sensitivity to $B\bar{B}$ production, with the PP $2\ell \geq 2$J becoming slightly more sensitive than the PP $2\ell$ 0-1J channel at higher $B$-quark masses. In the case of the singlet BRs for $B\bar{B}$ production, the PP $\geq 3\ell$ channel contributes more to the sensitivity than for the doublet and 100% BR cases. In the singlet case, the BR to $Zb$ is only $\approx 25\%$ with $\approx 25\%$ of the $B$ quarks decaying into $Hb$ and $\approx 50\%$ decaying into $Wt$, while in the doublet and 100% BR cases, the decay into $Wt$ is not allowed. Due to the significant probability of either the $W$ boson or the top quark decaying into a final state with an electron or muon, the PP $\geq 3\ell$ channel is particularly sensitive to the final state $ZbWt$, which explains the high sensitivity of the PP $\geq 3\ell$ channel to $B\bar{B}$ production in the singlet case.

![Graphs](a)(b)(c)(d)

FIG. 14. Expected (a), (c) and observed (b), (d) 95% C.L. lower limits from the combination of the pair-production channels on the mass of vectorlike quarks for all combinations of BRs for (a), (b) $T \rightarrow Zt$, $T \rightarrow Ht$, $T \rightarrow Wb$, and (c), (d) $B \rightarrow Zb$, $B \rightarrow Hb$, $B \rightarrow Wt$, adding up to unity. The white lines are contours for fixed values of $m_{VLQ}$. 

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In Fig. 14, the expected and observed limits on the $T$-quark ($B$-quark) mass from the combination of the pair-production channels are shown as a function of the BRs to $H\ell$ ($Hb$) and $W\ell$ ($Wt$), where the BR into $Z\ell$ ($Zb$) is calculated by requiring that the BRs to these three decay modes add up to unity. It can be seen that the analysis is particularly sensitive to high BRs to $Z\ell$ or $Zb$ (lower left corners), but it also has good sensitivity for many other combinations of the three BRs.

Systematic uncertainties play a smaller role in the sensitivity of the different channels than the statistical uncertainties. In order to quantify the impact of systematic uncertainties, the limits obtained with the nominal analysis, which includes systematic uncertainties, are compared to an analysis where only statistical uncertainties are included. Compared to the nominal analysis, the expected upper limits on the pair-production cross section improve by approximately 30%, 15% and 10% when systematic uncertainties are neglected in the PP $2\ell$ 0-1J channel, in the PP $2\ell$ ≥ 2J channel, and in the PP ≥ 3$\ell$ channel, respectively, for $m_{VLQ} = 750$ GeV. For higher VLQ masses, the effect of systematic uncertainties decreases further and reaches values of 10%–15%, 6%–7%, and 5% in the three channels. In the PP $2\ell$ 0-1J and PP $2\ell$ ≥ 2J channels, the main contributions come from the modeling uncertainties of the $Z +$ jets and $t\bar{t}$ backgrounds and the large-$R$ jet resolution uncertainties. The NPs associated with these uncertainties each change the total background expectation in the SR before the fit by up to 9% (for $t\bar{t}$ modeling in the SR with exactly one large-$R$ jet) to 24% (for large-$R$ jet $p_T$ resolution in the SR with no large-$R$ jet), depending on the uncertainty, the dilepton channel (PP $2\ell$ 0-1J or PP $2\ell$ ≥ 2J), and the SR. In the PP ≥ 3$\ell$ channel, the modeling of the diboson background, in particular the uncertainty in the background from dibosons produced in association with $b$-quarks, is responsible for the main contributions to the systematic uncertainties. The impact of this uncertainty is 13% on the total background expectation in the PP ≥ 3$\ell$ channel SR before the fit.

As in the case of the pair-production channels, the SP $2\ell$ and SP ≥ 3$\ell$ channels were combined using the same correlation scheme for the NPs as for the pair-production channels described above. Possible interference effects with SM background processes were estimated to be small and were not taken into account in the interpretation. Only production via the coupling of the $T$ quark to the $W$ boson was considered. The signal efficiency in the SR of the SP $2\ell$ channel is similar for production via the coupling of the $T$ quark to the $Z$ boson and it is about a factor of 2 higher for the SP ≥ 3$\ell$ channel. The expected signal cross section for production via the $Z$ boson is, however, roughly an order of magnitude smaller than for production via the $W$ boson for the same coupling value [14], so that production via the $Z$ boson was neglected in this analysis.

In Fig. 15, the expected and observed upper limits on the single-$T$-quark production cross section times BR to $Z\ell$ are shown as a function of $m_T$. Also shown are the expected upper limits on the cross section times BR for the individual single-production channels. The observed limit deviates from the expected limit by about 2σ for high values of $m_T$, which is consistent with the upward fluctuations observed in the discriminating variables in both single-production channels [Figs. 9(c) and 11(c)]. The limits are compared with the predicted single-production cross section times BR for the benchmark coupling of $\kappa_T = 0.5$ (at which the MC samples were produced) which corresponds to a coupling of $c_W = \sqrt{c_{W,L}^2 + c_{W,R}^2} = 0.45$ [14]. The SP 2$\ell$ channel, which explicitly exploits the presence of high-$p_T$ top quarks with top-tagging, is more sensitive than the SP ≥ 3$\ell$ channel for all values of $m_{VLQ}$ studied, but the SP ≥ 3$\ell$ channel contributes significantly to the combination of the two channels.

Similarly to the pair-production analysis, systematic uncertainties play a smaller role in the sensitivity of the different single-production channels than the statistical uncertainties. In order to quantify the impact of systematic uncertainties, the limits obtained with the nominal analysis, which includes systematic uncertainties, are compared to an analysis where only statistical uncertainties are included. Compared to the nominal analysis, the expected upper limits on the single-production cross section times BR improve by approximately 30% in the SP $2\ell$ channel and approximately 10% in the SP ≥ 3$\ell$ channel for

![ATLAS
13 TeV, 36.1 fb$^{-1}$
Single-T Production
Combination](image)

**FIG. 15.** Upper limits at 95% C.L. on the cross section times BR to $Z\ell$ of single production (SP) of a $T$-quark. The expected limits are shown for the individual channels and for the combination of the channels, as are the observed limits for the combination. The expected cross section times BR to $Z\ell$ for single-$T$-quark production is also shown for a coupling $\kappa_T = 0.5$, which corresponds to a coupling of $c_W = \sqrt{c_{W,L}^2 + c_{W,R}^2} = 0.45$ from Ref. [14]. The BR assumed here corresponds to the singlet benchmark model, i.e., ≈25%.
$m_{\text{VLQ}} = 900$ GeV when systematic uncertainties are neglected. At higher masses, the impact on the expected upper limits decreases to 5%–10% in both channels. The main contributions in the SP 2$\ell$ channel originate from the uncertainties in the forward-jet modeling, the modeling of the $Z +$ jets background and in the large-$R$ jet mass resolution. The NPs associated with these uncertainties each change the total background expectation in the dilepton SR before the fit by up to 5%–25%. In the SP $\geq 3\ell$ channel, the main contributions to the systematic uncertainty arise from the $t\bar{t} + V$ theoretical cross section, misidentified leptons, and the modeling of the background from dibosons produced in association with $b$-quarks. The impact of these uncertainties is 1%–12% on the total background expectation before the fit in the SP $\geq 3\ell$ channel SR.

The cross section for single-$T$-quark production does not only depend on the VLQ mass, but also on its coupling to SM particles, in particular the coupling to $Wb$, which enters the lowest-order $t$-channel diagram for this process. A change in the coupling, however, also results in a change in the width of the $T$-quark mass distribution. The effect of the changing resonance width with the coupling is taken into account by reweighting the discriminating variable in the nominal samples with $\kappa_T = 0.5$ to different couplings, based on large MC samples that are generated without a detector simulation. The reweighting procedure was validated using samples that were generated with $\kappa_T = 0.1$ and 1.0 at $m_T = 900$ GeV including the detector simulation. Comparing distributions from these validation samples with distributions that were reweighted from the nominal samples with $\kappa_T = 0.5$ to values of 0.1 and 1.0, a small nonclosure uncertainty of 3% was assigned to the single-$T$-quark normalization and this has negligible impact on the sensitivity of the analysis.

Expected and observed limits on the coupling as a function of $m_T$ are shown in Fig. 16(a), assuming the singlet model with $c_W = 2\frac{m_W}{m_T}c_Z$, which results in the singlet BR to $Zt$ of $\approx 25\%$ over the mass range studied in this analysis. For low values of $m_T$, couplings larger than 0.3–0.4 are excluded. For larger masses, the lower limits on the coupling increases because the single-production cross section decreases for a given coupling value with increasing $m_T$. The coupling $c_W$ can also be expressed in terms of a mixing angle with the top quark in the singlet model, $|\sin \theta_L|$, as defined in Ref. [12] by $c_W = \sqrt{\frac{2}{m_T^2}c_Z}$ and $c_Z = \frac{m_Z}{m_T} |\sin \theta_L \cos \theta_L|$. Since the mixing angle enters not only in the production cross section but also in the calculation of the BRs, the expected and observed limits shown in Fig. 16(b) show a lower and an upper branch. For a given mass, only values of $|\sin \theta_L|$ between these two branches are excluded. For values of $m_T$ larger than $\approx 1200$ GeV, no value of the mixing angle can be excluded.

The limits presented in Fig. 16(a) are only valid for BRs as predicted for the singlet model. In order to lift this assumption, the results of the search for single-$T$-quark production are interpreted in terms of couplings to the $W$, $Z$ and Higgs boson, $c_W$, $c_Z$ and $c_H$, with the assumption that the BRs to $Zt$ and $Ht$ are equal in the large-$m_T$ limit, as it is the case in many multiplets [12]. This assumption defines the value of $c_H$ for given values of $c_W$ and $c_Z$. In Fig. 17, expected and observed limits on the $T$-quark mass are shown as a function of $c_W$ and $c_Z$. Again, no distinction between left- and right-handed couplings is made because the analysis is not sensitive to differences in the chirality of the couplings. Therefore, $c_W$ and $c_Z$ are defined as the sum in quadrature of left- and right-handed couplings. It can be seen that for large values of $c_W$ and $c_Z$, $T$-quark masses smaller than 1600 GeV can be excluded, while for very

![Figure 16](112010-34)
A search for vectorlike quarks is presented, which uses 36.1 fb\(^{-1}\) of pp collision data taken with the ATLAS detector at the Large Hadron Collider at \(\sqrt{s} = 13\) TeV. Five channels are used for sensitivity to the production of vectorlike quarks with at least one vectorlike quark decaying into a Z boson and a third-generation Standard Model quark.

Three channels are optimized for sensitivity to the pair production of vectorlike quarks. Two dilepton channels make use of large-R jets to discriminate the signal from the Standard Model background, and a trilepton channel uses the presence of an additional charged lepton to define a signal-enriched region. The modeling of the main background processes was validated in background-dominated regions and no excess over the background-only expectation was found in the search regions. The two channels were combined and 95% C.L. upper limits were set on the coupling of vectorlike quarks to Standard Model quarks as a function of the mass of the vectorlike quark. The corresponding limits on the production cross section times branching fraction into Zt are in the range 0.16–0.18 pb at \(m_T = 700\) GeV and decrease to 0.03–0.05 pb at \(m_T = 2000\) GeV, depending on the value of the coupling in the range \(\kappa_T = 0.1–1.6\).

The results presented in this paper significantly tighten the existing bounds on the pair production of vectorlike T and B quarks that decay with a large branching ratio into a Z boson and a third-generation quark and they present competitive bounds on the single production of vectorlike T quarks that decay into a Z boson and a top quark. The results on the pair-production search were combined with other searches by the ATLAS Collaboration \cite{27–29,31,33,34}, in order to improve the overall sensitivity to vectorlike T and B quarks.

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Charles University, Faculty of Mathematics and Physics, Prague, Czech Republic
Particle Physics Department, Rutherford Appleton Laboratory, Didcot, United Kingdom
IRFU, CEA, Université Paris-Saclay, Gif-sur-Yvette, France
Santa Cruz Institute for Particle Physics, University of California Santa Cruz, Santa Cruz, California, USA
Department of Física, Pontificia Universidad Católica de Chile, Santiago, Chile
Departamento de Física, Universidad Técnica Federico Santa María, Valparaíso, Chile
Department of Physics, University of Washington, Seattle, Washington, USA
Department of Physics and Astronomy, University of Sheffield, Sheffield, United Kingdom
Department of Physics, Shinshu University, Nagano, Japan
Department Physik, Universität Siegen, Siegen, Germany
Department of Physics, Simon Fraser University, Burnaby, British Columbia, Canada
SLAC National Accelerator Laboratory, Stanford, California, USA
Physics Department, Royal Institute of Technology, Stockholm, Sweden
Departments of Physics and Astronomy, Stony Brook University, Stony Brook, New York, USA
Department of Physics and Astronomy, University of Sussex, Brighton, United Kingdom
School of Physics, University of Sydney, Sydney, Australia
Institute of Physics, Academia Sinica, Taipei, Taiwan
E. Andronikashvili Institute of Physics, Iv. Javakhishvili Tbilisi State University, Tbilisi, Georgia
High Energy Physics Institute, Tbilisi State University, Tbilisi, Georgia
Department of Physics, Technion, Israel Institute of Technology, Haifa, Israel
Raymond and Beverly Sackler School of Physics and Astronomy, Tel Aviv University, Tel Aviv, Israel
Department of Physics, Aristotle University of Thessaloniki, Thessaloniki, Greece
International Center for Elementary Particle Physics and Department of Physics, University of Tokyo, Tokyo, Japan
Graduate School of Science and Technology, Tokyo Metropolitan University, Tokyo, Japan
Department of Physics, Tokyo Institute of Technology, Tokyo, Japan
Tomsk State University, Tomsk, Russia
Department of Physics, University of Toronto, Toronto, Ontario, Canada
TRIUMF, Vancouver, British Columbia, Canada
Department of Physics, York University, Toronto, Ontario, Canada
Division of Physics and Tomonaga Center for the History of the Universe, Faculty of Pure and Applied Sciences, University of Tsukuba, Tsukuba, Japan
Department of Physics and Astronomy, Tufts University, Medford, Massachusetts, USA
Department of Physics and Astronomy, University of California Irvine, Irvine, California, USA
Department of Physics and Astronomy, University of Uppsala, Uppsala, Sweden
Department of Physics, University of Illinois, Urbana, Illinois, USA
Instituto de Física Corpuscular (IFIC), Centro Mixto Universidad de Valencia—CSIC, Valencia, Spain
Department of Physics, University of British Columbia, Vancouver, British Columbia, Canada
Department of Physics and Astronomy, University of Victoria, Victoria, British Columbia, Canada
Fakultät für Physik und Astronomie, Julius-Maximilians-Universität Würzburg, Würzburg, Germany
Department of Physics, University of Warwick, Coventry, United Kingdom
Waseda University, Tokyo, Japan
Department of Particle Physics, Weizmann Institute of Science, Rehovot, Israel
Department of Physics, University of Wisconsin, Madison, Wisconsin, USA
Fakultät für Mathematik und Naturwissenschaften, Fachgruppe Physik, Bergische Universität Wuppertal, Wuppertal, Germany
Department of Physics, Yale University, New Haven, Connecticut, USA
Yerevan Physics Institute, Yerevan, Armenia

*Deceased.
†Also at Department of Physics, King’s College London, London, United Kingdom.
‡Also at Istanbul University, Department of Physics, Istanbul, Turkey.
§Also at Instituto de Física Teórica de la Universidad Autónoma de Madrid, Spain.
∥Also at Institute of Physics, Azerbaijan Academy of Sciences, Baku, Azerbaijan.
¶Also at TRIUMF, Vancouver, British Columbia, Canada.
‖Also at Department of Physics and Astronomy, University of Louisville, Louisville, Kentucky, USA.
¶¶Also at Department of Physics, California State University, Fresno, California, USA.
ƒAlso at Department of Physics, University of Fribourg, Fribourg, Switzerland.
ghiAlso at Departament de Física de la Universitat Autònoma de Barcelona, Barcelona, Spain.