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A Strong Jet Signature in the Late-Time Lightcurve of GW170817

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ABSTRACT

We present new 0.6–10 GHz observations of the binary neutron star merger GW170817 covering the period up to 300 days post-merger, taken with the upgraded Karl G. Jansky Very Large Array, the Australia Telescope Compact Array, the Giant Metrewave Radio Telescope and the MeerKAT telescope. We use these data to precisely characterize the decay phase of the late-time radio light curve. We find that the temporal decay is consistent with a power-law slope of $t^{-2.2}$, and that the transition between the power-law rise and decay is relatively sharp. Such a slope cannot be produced by a quasi-isotropic (cocoon-dominated) outflow, but is instead the classic signature of a relativistic jet. This provides strong observational evidence that GW170817 produced a successful jet, and directly demonstrates the link between binary neutron star mergers and short-hard GRBs. Using simple analytical arguments, we derive constraints on the geometry and the jet opening angle of GW170817. These results are consistent with those from our companion Very Long Baseline Interferometry (VLBI) paper, reporting superluminal motion in GW170817.

Keywords: gravitational waves — stars: neutron — radio continuum: stars

1. INTRODUCTION

The detection of gravitational waves (GW) from the binary neutron star merger event GW170817 (Abbott et al. 2017a), was accompanied by two distinct electromagnetic (EM) counterparts (Abbott et al. 2017b). The first EM counterpart was a short-lived, thermal-like

component. It initially had bright optical/UV emission that faded on a timescale of a few days (Coulter et al. 2017; Evans et al. 2017; Arcavi et al. 2017; Lipunov et al. 2017; Soares-Santos et al. 2017; Valenti et al. 2017), to be replaced by redder emission which dominated the bolometric luminosity until it too faded on a timescale of a few weeks (Tanvir et al. 2017; Cowperthwaite et al. 2017; Drout et al. 2017; Kasliwal et al. 2017). Optical/near-IR spectroscopy detected the spectral fingerprints of r-process elements (Pian et al. 2017; Smartt et al. 2017), and a broad consensus has formed

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that this thermal component was a “kilonova” powered by the dynamic ejecta from the merger event (e.g. Kasen et al. 2017).

Additionally, the EM counterpart was also detected as a prompt, low-luminosity burst of gamma-rays with duration ~ 2 s but delayed from the GW merger event by 1.7 s (Goldstein et al. 2017). This was followed by the discovery of non-thermal “afterglow” emission at X-ray (Haggard et al. 2017; Margutti et al. 2017; Troja et al. 2017) and radio wavelengths (Hallinan, Corsi et al. 2017), substantially delayed by 9 and 16 days, respectively. Both the prompt and the afterglow emission are thought to be generated in a relativistic shock, but a consensus on the nature of this second EM component has been slower to emerge. Two viable models were eliminated based on the early data. From the delayed onset of the afterglow it was conclusively shown that GW170817 was not a classical short-hard gamma-ray burst (SHB) with an on-axis jet (e.g. Kasliwal et al. 2017). Furthermore, an off-axis jet with a uniform or “top-hat” geometry was ruled out by the slow rise ($t^{+0.8}$) of the radio emission up to 100 days post-merger (Mooley et al. 2018a), later confirmed at both optical and X-ray wavelengths (Margutti et al. 2018; Troja et al. 2018a; Lyman et al. 2018; Ruan et al. 2018).

There still remain two competing models for the prompt and afterglow emission of GW170817, both of which are well motivated physically. Both scenarios launch an ultra-relativistic jet (bulk Lorentz factor $\Gamma \sim 100$), pointing away from the Earth, that interacts with the neutron-rich material dynamically ejected during the merger to give rise to a mildly relativistic ($\Gamma \sim 4$) outflow (a.k.a “cocoon”) moving in the direction of the Earth. The mildly relativistic material is likely responsible for the gamma-ray signal (e.g. Kasliwal et al. 2017; Gottlieb et al. 2018; Matsumoto et al. 2018) and is primarily responsible for the slow rise ($t^{+0.8}$) of the afterglow at early times (e.g. Mooley et al. 2018a). However, in one scenario the jet successfully escapes the dynamical ejecta, while in the other it fails to do so. In the literature the former case has been referred to as the successful jet-cocoon model or the structured jet model (where the successful jet is considered to be a narrow core with a “sheath” of lower Lorentz factor material), in which the jet dominates the late-time afterglow, whereas the latter case is that of a choked-jet, in which the afterglow is cocoon-dominated at all times. In the successful jet scenario, an observer located along the axis of the jet likely sees a regular SHB, while in the choked jet scenario they do not.

In the discussion that follows on the late-time light curves, we will refer to these as jet-dominated and

cocoon-dominated outflows. Both outflow models require significant azimuthal and radial structure to explain the rise of the afterglow light curve (Nakar & Piran 2018; Xie et al. 2018), but the open question that we hope to address here is whether the relativistic jet survived.

Several experimental tests have been suggested to distinguish between these two alternative scenarios (Gill & Granot 2018; Nakar et al. 2018; Lazzati et al. 2018). Elsewhere we report on GW170817 polarization measurements and our high angular resolution imaging (Corsi et al. 2018; Mooley, Deller, Gottlieb et al. 2018b). In this paper we focus on the continuum intensity of the afterglow light curve at late times. Several authors have noted that the rising portion of the light curve has limited discriminating power since the lower Lorentz factor ejecta dominate the emission in both models (Nakar et al. 2018; Margutti et al. 2018; D’Avanzo et al. 2018; Gill & Granot 2018). However, as first noted by Dobie et al. (2018), and subsequently confirmed by Alexander et al. (2018), the afterglow light curve peaked around day 150 post-merger and has begun to decline. Our motivation for this work has been to characterize this decay phase (as attempted by previous studies that reported the peak and decline) and to see whether the geometry and dynamical state of the outflow can be inferred as it has been done in the past with the late-time light curves of long-duration gamma-ray burst (GRB) afterglows (Mészáros et al. 1998; Sari et al. 1999; Livio & Waxman 2000).

In this paper we present further radio observations of GW170817 using the NSF’s Karl G. Jansky Very Large Array (VLA), the Australia Telescope Compact Array (ATCA), the upgraded Giant Metrewave Radio Telescope (uGMRT) and new observations from the MeerKAT telescope, covering the period 180–300 days post-merger. With this longer time-baseline we are able to accurately constrain the late-time power-law decay index and compare the results against expectations for a cocoon-dominated versus a jet-dominated outflow. In §2 we describe the observations and data reduction techniques employed, §3 gives the spectral and light curve analysis with the interpretation based on widely used theory of GRB afterglows given in §4, and we end with the summary and conclusions in §5.

2. OBSERVATIONS AND DATA REDUCTION

Our observations of GW170817 carried out over the decline of the light curve are described below, and the observing log together with the flux densities of GW170817 are reported in Table 1. While our new VLA and ATCA observations span frequencies between 2–12

GHz, the addition of MeerKAT and uGMRT data gives us important spectral coverage below 2 GHz, which not only probes the low-frequency behavior of GW170817, but also gives very precise measurements of the radio spectral indices.

2.1. VLA

We observed GW170817 on 2018 Mar 21, Mar 25–26, May 11–12, and Jun 07 with the VLA (PI: Corsi). The Wideband Interferometric Digital Architecture (WIDAR) correlator was used at S band (2–4 GHz) and X band (8–12 GHz) to maximize sensitivity. We used PKS J1248–1959 as the phase calibrator and 3C286 as the flux density and bandpass calibrator. The data were calibrated and flagged for radio frequency interference (RFI) using the NRAO CASA (McMullin et al. 2007) pipeline. We then split and imaged the target data using the CASA tasks `split` and `clean`.

2.2. ATCA

We observed GW170817 with the ATCA (PI: Dobie, Troja) at three epochs between 2018 Mar to 2018 Jun. We determined the flux scale and bandpass response for all epochs using the ATCA primary calibrator PKS B1934–638. Observations of PKS B1245–197 were used to calibrate the complex gains. All observations used two bands of 2048 MHz centered at 5.5 and 9.0 GHz.

Table 1. Radio observations of GW170817 during the light curve decline

UT date	ΔT^\dagger (d)	Telescope	ν (GHz)	F_ν (μJy)	σ_ν (μJy)
2018 Feb 16	183	uGMRT	0.65	211	34
2018 Mar 02	197	MeerKAT	1.3	160	20
2018 Mar 21	216	VLA	10	36.3	3.6
2018 Mar 25–26	220	VLA	3	64.7	2.7
2018 Mar 27	222	ATCA [‡]	7.25	39.7	7.2
2018 Apr 26–May 05	257	MeerKAT	1.3	65.8	7.2
2018 May 11–12	267	VLA	3	40.3	2.7
2018 May 11	267	ATCA [‡]	7.25	25.0	4.1
2018 May 13–25	275	uGMRT	0.65	<153	...
2018 Jun 07	294	VLA	3	31.2	3.6
2018 Jun 11	298	ATCA [‡]	7.25	23.4	4.2

[†] Mean epoch, days post-merger.

[‡] The ATCA flux densities of GW170817 have a correction factor of 1.25 applied (i.e. the values have been decreased by 25%; see §3.1 for details).

We reduced the visibility data using standard MIRIAD (Sault et al. 1995) routines. The calibrated visibility data from both bands were combined, averaged to 32 MHz channels, and imported into DIFMAP (Shepherd 1997). Bright field sources were modeled separately for each band using the visibility data and a combination of point-source and Gaussian components with power-law spectra. After subtracting the modeled field sources from the visibility data, GW170817 dominates the residual image. Restored naturally-weighted images for each band were generated by convolving the restoring beam and modeled components, adding the residual map and averaging to form a wide-band image. Image-based Gaussian fitting with unconstrained flux density and source position was performed in the region near GW170817.

2.3. uGMRT

We observed GW170817 with the uGMRT in Band 3 (effective bandwidth 550–750 MHz) (PI: Mooley). The observations were carried out with 400 MHz correlator bandwidth centered at 750 MHz using the non-polar continuum interferometric mode of the GMRT Wideband Backend (GWB; Reddy et al. 2017). The epochs from 2018 May and 2018 Jun were divided into several short (~ 1 –3 hr) observations carried out over several days. 3C286 was used as the absolute flux scale and bandpass calibrators, while phase calibration was done with 3C283. These data were calibrated and RFI flagged using a custom-developed pipeline in CASA. The data were then imaged interactively with the CASA task CLEAN, while incorporating a few iterations of phase-only self-calibration and one amplitude+phase self-calibration step.

2.4. MeerKAT

We observed GW170817 with the new MeerKAT telescope (Camilo et al. 2018; Jonas & MeerKAT Team 2016) on 2018 Mar 02, Apr 26 and May 05. The first of these observations used 16 antennas and the ROACH2 correlator; the latter used 61 antennas and the SKARAB correlator. All observations were made at L-band, covering 900–1670 MHz. After flagging for RFI, the effective bandwidth used was 486 MHz. PKS 1934–638 was used as the flux and bandpass calibrator and for initial phase reference. Data processing was done with the MeerKATHI pipeline (Makhatini et al. in prep). To correct for the uncertainties in the frequency-dependent primary beam correction and pointing errors, we used direction-dependent gain calibration for bright sources spread across the ~ 1 deg field of view.

3. RESULTS

3.1. Spectral analysis

In [Dobie et al. \(2018\)](#) we studied the radio spectral evolution of GW170817, finding that over the first 120 days the radio spectral index was constant with a value of $\beta = -0.57 \pm 0.04$. This value of β is fully consistent with the value derived by [Alexander et al. \(2018\)](#), $\beta = -0.74 \pm 0.2$, at 217 days. Here and elsewhere in the paper we characterize the flux density evolution of the light curve using $F_\nu(t, \nu) \propto t^\alpha \nu^\beta$ where α and β are the temporal and spectral power-law indices, respectively.

We have used the new data to look for changes in the radio spectral index. Specifically we have searched for a steepening of the spectral index of order $\Delta\beta = 0.5$ as expected if the synchrotron cooling break had moved through the radio band on timescales of 200–300 days ([Sari et al. 1998](#)). We compare our radio measurements from May 2018 reported in [Table 1](#) with the X-ray measurement from 2018 May 3–5 ([Alexander et al. 2018](#); [Nynka et al. 2018](#); [Troja et al. 2018b](#)) to derive a spectral index of $\beta_{\text{XR}} = -0.56 \pm 0.01$. Our most precise (simultaneous) two-point measurement of the radio-only spectral index is with the VLA data between 3–10 GHz in Mar 2018 (day~220), $\beta = -0.52 \pm 0.09$. Both these measurements are consistent with the precise radio-to-X-ray spectral index $\beta = -0.584 \pm 0.006$ at 160 days post-merger derived by [Margutti et al. \(2018\)](#). We see no evidence for a spectral steepening, and can rule out the presence of a cooling break for which we expect $\beta \sim -1.1$ ([Alexander et al. 2018](#)).

In these spectral comparisons between telescopes, we see some evidence for a scaling offset in the late-time ATCA data. While the in-band 5.5–9 GHz spectral indices derived for the ATCA data are consistent with -0.584 broadband value above, the flux densities are higher by about 25% when the data are compared with contemporaneous measurements made with the VLA, MeerKAT and uGMRT. The origin of excess in the ATCA data is currently being investigated¹. In [Table 1](#) we have reported the corrected ATCA flux densities. The radio-only spectral index measurements from four epochs observed during the decline of the light curve are shown in [Figure 1](#). The spectral index between the 0.65 GHz uGMRT and 7.25 GHz ATCA data (corrected from the value reported in [Dobie et al. 2018](#)) obtained around 2018 Feb 16 (183 d post-merger) is -0.54 ± 0.08 .

¹ This appears to be a systematic offset. The origin of the offset is not in the flux scale, since the radio spectrum of the phase reference source is consistent between all the epochs from the different telescopes. The ATCA array has a more compact configuration, so it may be due to host galaxy contamination.

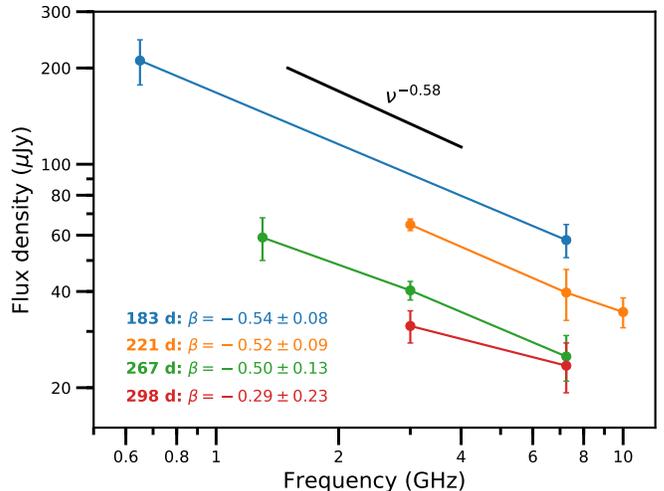


Figure 1. Radio spectral indices between 0.6–10 GHz spanning four epochs observed during the decline part of the light curve. The different epochs are color coded. The approximate number of days post-merger and the corresponding spectral indices are given in the legend. A joint fit to all the radio data implies $\beta = -0.53 \pm 0.04$ (see §3.2), in good agreement with the radio to X-ray spectral index measurements (shown by the black $\nu^{-0.58}$ line). With this measurement, we can rule out any spectral steepening expected, for example, due to the presence of a cooling break in or between the radio/X-ray bands.

Below, we describe a joint fit to multi-frequency light curve data, including the spectral and temporal indices.

3.2. Light curve analysis

We began by performing a joint fit to radio data published till day 300 post-merger. This includes the data in [Table 1](#) together with [Hallinan, Corsi et al. \(2017\)](#); [Alexander et al. \(2017\)](#); [Mooley et al. \(2018a\)](#); [Margutti et al. \(2018\)](#); [Resmi et al. \(2018\)](#); [Dobie et al. \(2018\)](#). We used a smoothly-broken power law model, incorporating the frequency dependence, of the form $2^{1/s} \nu^\beta F_{\nu,p} (t^{-s\alpha_1} + t^{-s\alpha_2})^{-1/s}$ ([Beuermann et al. 1999](#); [Alexander et al. 2018](#)). Here, ν is the observing frequency normalized to 3 GHz, $F_{\nu,p}$ is the flux density at 3 GHz at the time of light curve peak, t is the time in units of the time to light curve peak (t_p), s is the smoothness parameter, and α_1, α_2 are the power-law rise and decay slopes. This Markov chain Monte Carlo (MCMC) fitting was done² using the Python package [emcee](#) ([Foreman-Mackey et al. 2013](#)). We obtain best-fit values of $F_{\nu,p} = 118_{-7}^{+14} \mu\text{Jy}$, $t_p = 167_{-7}^{+14}$ days, $\alpha_1 = 0.80_{-0.05}^{+0.06}$, $\alpha_2 = -2.16_{-0.61}^{+0.23}$, $\log_{10}(s) = 0.59_{-0.37}^{+0.77}$.

² We chose 100 walkers, 1000 steps and flat priors on all of the parameters.

and $\beta = -0.61_{-0.07}^{+0.03}$ (68% confidence interval, i.e. 1σ ; see Table 2). We also introduced a scale factor into the MCMC fit to explore a possible 25% offset in the ATCA flux densities suggested by the spectral fits in §3.1. We find that a scaling factor of $\sim 20\%$ is slightly preferred over unity³.

Next we fit only the data in Table 1 together with previous data at 0.65 GHz, 1.5 GHz, 3 GHz and 7.25 GHz referenced robustly with our method of flux determination (Hallinan, Corsi et al. 2017; Mooley et al. 2018a; Dobie et al. 2018, flux density values given in Table 3). Our best-fit values are given in Table 2, and are consistent with the fit using all of the data above. In particular we find $\alpha_2 = -2.4_{-0.4}^{+0.3}$. Figure 2 shows the multi-frequency radio data scaled to 3 GHz, and the joint fit to these data (solid line). Figure 3 shows the corner plot with the results of the MCMC fit.

By taking the limit in which the $t^{-s\alpha_1}$ term dominates⁴ over the $t^{-s\alpha_2}$ term in the smoothly-broken power law expression given above, we derive that the transition from the power law rise to the power law decay takes place between 158_{-18}^{+13} and 183_{-15}^{+42} days post-merger, i.e. over a timescale of 24_{-24}^{+58} days. This implies that the transition from α_1 to α_2 is fairly sharp, possibly taking place over a small fraction of the time taken to reach the light curve peak. We return to this point in §4.

The reduction in the uncertainties for α_2 in the second fit hints that there may still be systematic uncertainties involved in the calibration across data taken from different telescopes and obtained at different frequencies. Thus we chose to independently fit the 3 GHz VLA-only data as was first done in (Mooley, Deller, Gottlieb et al. 2018b). In this case, the light curve is too sparsely sampled to be able to fit for the smoothness parameter, and hence we use a simple broken power law model (this corresponds to $s \rightarrow \infty$) instead. Table 2 gives the parameter values from the fitting, and we find that $\alpha_2 = -2.2 \pm 0.2$. The decline is somewhat shallower than, but in good agreement with, the smoothly-broken power law model parameters. The remaining parameters such as the slope of the rise, the peak flux density and the time of peak all agree well with each other and

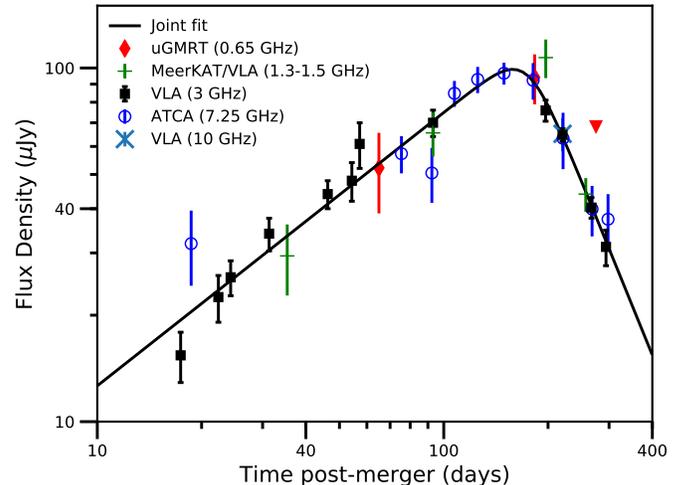


Figure 2. The radio light curve of GW170817 spanning multiple frequencies, and scaled to 3 GHz using the spectral index ($\nu^{-0.53}$) derived from our MCMC analysis. The data from the VLA (filled black squares for 3 GHz and green crosses for 1.5 GHz), the ATCA (blue circles), the MeerKAT (green crosses) and the uGMRT (red diamonds for detections and triangle for upper limit) are as reported in Table 1. We also include the data at 0.65 GHz, 1.5 GHz, 3 GHz, and 7.25 GHz reported previously (Hallinan, Corsi et al. 2017; Mooley et al. 2018a; Dobie et al. 2018). Our best-fit smoothed broken power-law model to all these data (see §3.2) is shown as a solid curve. The power-law decline index obtained is $-2.4_{-0.4}^{+0.3}$. For comparison, a broken power-law fit to the 3 GHz VLA-only data gives -2.2 ± 0.2 . Both fits are thus consistent with t^{-p} decline in the light curve, where p is the electron power-law distribution index.

with previous fits in the literature. The main point here is that our key results are robust to different choices of the data that we used in the fit.

Summarizing, we measure a sharp transition of the afterglow light curve of GW170817 about 170 days post-merger with a steep power-law slope of $\alpha_2 = -2.2$. The result confirms our earlier determination of α_2 first reported in Mooley, Deller, Gottlieb et al. (2018b). With less data and a shorter time-baseline Dobie et al. (2018) derive a more shallow decay index $\alpha_2 = -1.6 \pm 0.2$, which is similar to the value that Alexander et al. (2018) find, $\alpha_2 = -1.6_{-0.3}^{+0.2}$. Our more precise values of α_2 lie within the 68% confidence interval of Troja et al. (2018b) but we measure a larger value for the smoothness parameter.

4. DISCUSSION

Before interpreting the light curve of GW170817 directly, it is illustrative to review the two asymptotes of late-time light curve behavior from afterglow models. Afterglow spectra and the light curves of GRBs have long been used to infer the geometry and dynamical state of the ejecta (e.g. Galama et al. 1998; Har-

³ Median flux multiplication factor is 0.83 and the 68% confidence interval is 0.75–1.07. Note that the scaling factor is required for all ATCA data (reported here and previously). As an experiment, we have also performed a fit without including an ATCA flux scaling factor in the MCMC analysis, and the χ^2 is significantly worse in this case as expected (87.4 versus 67.4). Nevertheless, we get $\alpha_2 = 1.86_{-0.23}^{+0.17}$ without the scaling factor.

⁴ We derive the time at which one term dominates over the other by a factor of ~ 20 . The quoted time values are the median of the distributions and their 16 and 84 percentiles are quoted as the uncertainties.

Table 2. Parameters obtained from fitting a smoothly broken power law model to the radio light curve

No.	$F_{\nu,p}$ (μJy)	t_p (d)	α_1	α_2	$\log_{10}(s)$	β
1	118^{+14}_{-7}	167^{+14}_{-7}	$0.80^{+0.06}_{-0.05}$	$-2.16^{+0.23}_{-0.61}$	$0.59^{+0.77}_{-0.37}$	$-0.61^{+0.03}_{-0.07}$
2	98^{+8}_{-9}	174^{+9}_{-6}	0.78 ± 0.05	$-2.41^{+0.26}_{-0.42}$	$0.70^{+0.49}_{-0.34}$	-0.53 ± 0.04
3*	120 ± 9	164 ± 7	0.83 ± 0.07	-2.23 ± 0.24

Row 1 gives the joint fit for the radio data reported here together with that reported previously, row 2 gives the fit for the radio data reported here and together with previous data referenced robustly with our method of flux determination, and *row 3 gives the fit (broken power law) for the 3 GHz VLA-only data. Column descriptions: $F_{\nu,p}$ (μJy) is the flux density at 3 GHz at the time of light curve peak, t_p is the time of peak (days post-merger), α_1, α_2 are the power-law rise and decay slopes, s is the smoothness parameter, and β is the spectral index. See §3.2 for details.

risson et al. 1999). For a spherical relativistic fireball the flux density will decline as $F_\nu \propto t^\alpha \nu^\beta$, in which $\alpha = -3(p-1)/4$ and $\beta = -(p-1)/2$ when the observing frequency ν_o is below the synchrotron cooling break ν_c , and $\alpha = -(3p-2)/4$ and $\beta = -p/2$ when the cooling break lies below the observing frequency (Sari et al. 1998). Here p is the usual power-law index for the energy of the accelerated electrons ($p > 2$). For a jet viewed on-axis at late times the power-law decay index is $\alpha = -p$, independent of whether the cooling break is above (i.e. $\beta = -(p-1)/2$) or below (i.e. $\beta = -p/2$) the observing frequency (Sari et al. 1999).

For GW170817 we show here (§3.1), as also demonstrated elsewhere (Dobie et al. 2018; Alexander et al. 2018), that in the radio regime β is consistent with the value found from fitting across the radio and X-ray regimes, $\beta = -0.584$, and that ν_c lies well above the radio (and likely also the X-ray) band. Thus $\beta = -(p-1)/2$ and $p = 2.17$, for which we expect the late-time power-law decay index α to lie between -0.88 (i.e. quasi-spherical, cocoon-dominated) and -2.17 (jet-dominated). Eventually we also expect the outflow to become non-relativistic and this can give rise to an achromatic change in the GRB afterglow light curves. Dynamical transitions to the non-relativistic phase have been claimed for both spherical and jet-like outflows (Frail et al. 2000; Frail et al. 2005; van der Horst et al. 2008). The timescale on which this occurs is approximately when the rest mass energy of the material swept up by the shock is comparable to the kinetic energy of the outflow (Frail et al. 2000). The side-ways expansion of the jet becomes important and eventually the outflow becomes quasi-spherical (Frail et al. 2000). At this time $\alpha_{\text{nr}} = -(15p-21)/10$ for $\nu_o < \nu_c$ and $\alpha_{\text{nr}} = -(3p-4)/2$ for $\nu_o > \nu_c$ (Livio & Waxman 2000). Thus for the nominal parameters of GW170817, a spherical outflow undergoing a non-relativistic transition would be expected to

show an achromatic *steepening* while for a jet the light curve would *flatten*, both with a value of $\alpha_{\text{nr}} = -1.15$.

The afterglow light curves of jet-like outflows are altered by observing them at different viewing angles away from their symmetry axis. In this case the structure of the ejecta becomes important. Early work investigated the role of viewing angle for simple uniform or top-hat jets (Livio & Waxman 2000) and jets with azimuthal structure (e.g. Rossi et al. 2002; Kumar & Granot 2003). More recent modeling has considered structure jets whose ejecta have both azimuthal and radial structure (Kathirgamaraju et al. 2018; Gottlieb et al. 2018; Xie et al. 2018; Lazzati et al. 2018). The effects of jet structure and viewing angle are most pronounced at or near the peak of the light curve. These models generally predict a slow temporal evolution of α , with the break between the rise and the decay taking place over a significant fraction of the peak time (Granot & Kumar 2003; Panaitescu & Kumar 2003; Gill & Granot 2018; Lamb et al. 2018). However, at late times all of these off-axis light curves models approach the behavior of an on-axis jet where the slope of the temporal index, as noted earlier, is $\alpha = -p$.

While the predicted late-time light curves of afterglows exhibit a diverse range of behaviors, the observed decay of GW170817 is remarkably simple. A single power-law with $\alpha_2 = -2.4^{+0.3}_{-0.4}$ (2.2 ± 0.2 for the 3 GHz VLA-only data) fits all the data post-peak. This power-law index is a clear signature of a relativistic jet. This is a strong jet-dominated outflow, i.e. there is no support for intermediate slopes as might be expected if a quasi-spherical cocoon was contributing to the emission. Likewise, we see no evidence for a spectral change due to synchrotron cooling (§3.1) nor do we see a dynamical transition to non-relativistic motion that would manifest itself by an achromatic break in the light curve. Another important feature of the light curve in Figure 2 is the sharpness of the transition from a power-law rise to de-

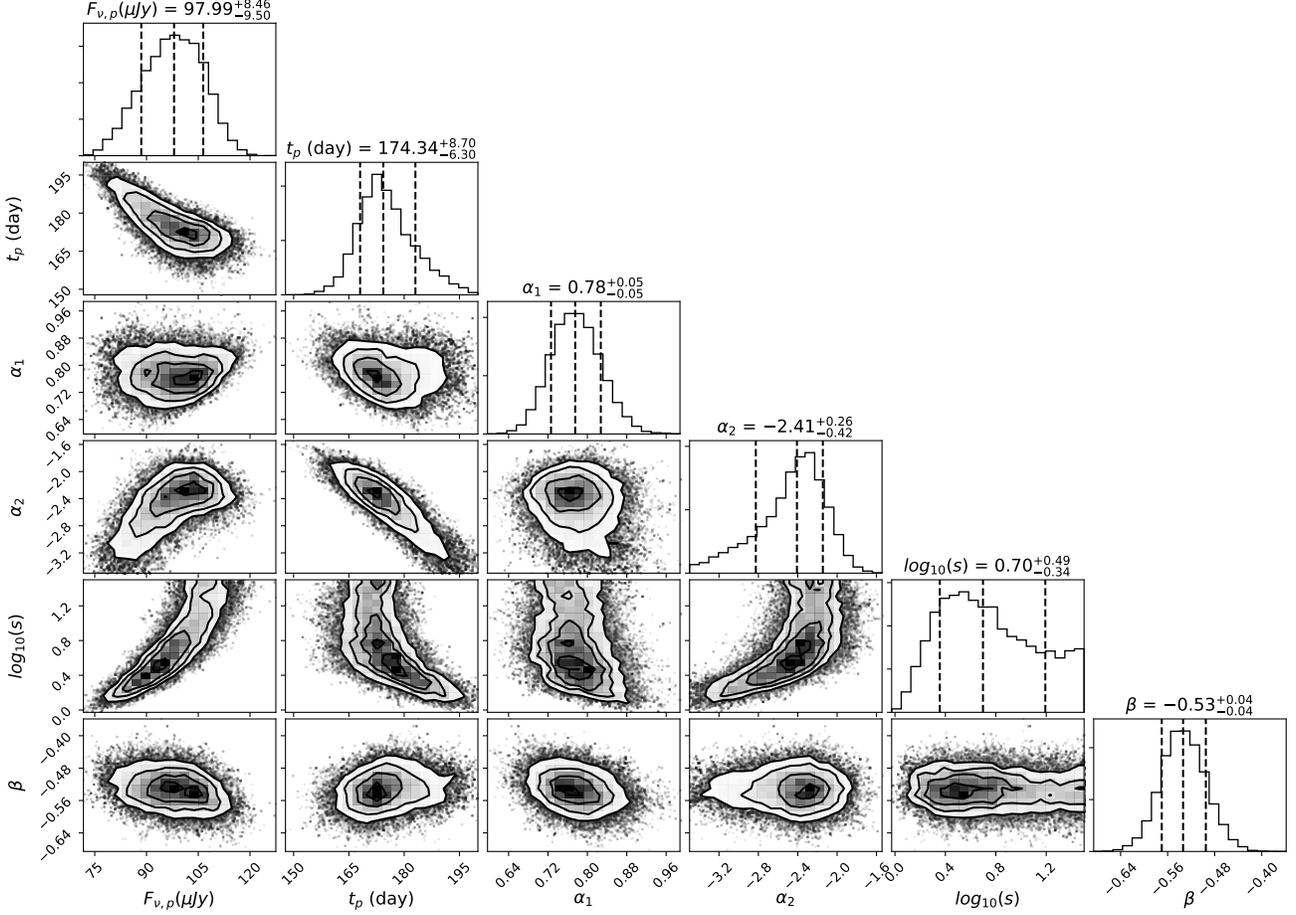


Figure 3. A corner plot showing the results of our MCMC fitting of the radio light curve (Figure 2) using the VLA, ATCA, MeerKAT and uGMRT data. $F_{\nu,p}$ is the flux density at 3 GHz at the time of light curve peak, t_p is the time to light curve peak, α_1, α_2 are the power-law rise and decay slopes, s is the smoothness parameter, and β is the spectral index. See §3.2 for details. In each contour plot and histogram, the 16, 50, 84 percentiles are marked.

decay. The change from $t^{0.8}$ to t^{-p} takes place over 24^{+58}_{-24} days, a result that appears to be at odds with the predicted temporal evolution of α for current off-axis, structured jet models (Granot & Kumar 2003; Panaitescu & Kumar 2003; Gill & Granot 2018). More detailed modeling of GW170817 is needed to see whether structured jet-like outflows can reproduce this sharp transition.

The sharpness of the peak and the slope of the power-law decline depend on the viewing/observing angle, θ_v , and jet core half-opening angle⁵, θ_j , and more specifically on the ratio between them. In order to constrain this ratio we consider only the contribution from the core of the jet, which dominates the emission near the peak and during the decay. Thus, while the rising part of the light curves that we calculate does not fit the observations, the peak and the decay should. Using this

⁵ Since the energy distribution at the core is expected to be roughly uniform we approximate its contribution as being generated by a top-hat jet with half-opening angle, θ_j .

approximation, we can now derive constraints on θ_j/θ_v that provides the observed transition from the peak of the light curve and the steep decline.

We make a rough analytic approximation. The peak occurs approximately when we start seeing the near edge of the jet core, and the t^{-p} power-law decline begins roughly when the jet centroid comes into view. The sharpness of the light curve peak and the immediate transition to t^{-p} decline implies that we are in the regime⁶ $\theta_v - \theta_j \gg \theta_j$. We denote by t_1 as the time that we see the edge of the jet, namely $\Gamma(t_1) \simeq 1/(\theta_v - \theta_j)$, and t_2 as the time that we see the jet axis, $\Gamma(t_2) \simeq 1/\theta_v$. Now, ignoring sideways spreading of the jet we can approximate $\Gamma \propto t^{-3/8}$ (e.g. Sari et al. 1998) to obtain $\Delta t/t = (t_2 - t_1)/t_2 \simeq [\theta_v^{8/3} - (\theta_v - \theta_j)^{8/3}]/\theta_v^{8/3} \simeq (8/3)\theta_j/\theta_v$. Here we use the approximation that θ_j/θ_v

⁶ If $(\theta_v - \theta_j) \lesssim \theta_j$ there will be a long-lived phase during which the light curve decays as t^{-1} .

is much smaller than unity. Observationally, t_1 occurs sometime during the transition from the $t^{0.8}$ rise to the peak of the light curve and t_2 occurs when the decay phase approaches t^{-p} . Using the results from our MCMC analysis, we find that $\Delta t/t \lesssim 1/3$ (68% confidence or better, depending on where t_1 and t_2 lie), indicating that $\theta_v \gtrsim 8\theta_j$. To verify this simple estimate we produced light curves from a top-hat jet using semi-analytic code⁷. We find that light curves that fit the transition seen from the peak to the decline of the light curve have $\theta_v \simeq 6\theta_j$. Together with the upper limit on the observing angle from the LIGO-Virgo Collaboration ($\theta_v \lesssim 28^\circ$; Abbott et al. 2017a), our constraint implies $\theta_j \lesssim 5^\circ$. If instead we use the estimate of $\Gamma \simeq 4.1 \pm 0.5$ close to the peak of the light curve from the VLBI measurement (Mooley, Deller, Gottlieb et al. 2018b), then we get $\theta_j \lesssim 3^\circ$ and $\theta_v \simeq 15^\circ$.

5. SUMMARY & CONCLUSIONS

In this companion paper to our polarization and high angular resolution imaging studies, we have presented deep VLA, ATCA, MeerKAT and uGMRT observations (§2) of GW170817 post-peak of the light curve, i.e. between 180–300 days post-merger. Our spectral analysis does not yield any evidence for the cooling break to have entered the radio band, or of any achromatic steepening in the light curve indicating the transition of the outflow into the non-relativistic regime (§3.1). We find that the light curve decay is consistent with $t^{-2.2}$ (§3.2), which is a classic signature of a jet where the slope of the decay is equal to the power-law energy index p of the synchrotron-emitting electrons. We also find that the transition from the power-law rise to decay ($t^{0.8}$ to $t^{-2.2}$) is fairly sharp.

The data on the light curve decline reported previously (Dobie et al. 2018; Alexander et al. 2018) has not been sufficiently constraining to unambiguously distinguish between cocoon-dominated and jet-dominated emission. The new data that we have reported here securely implies a decline in the light curve consistent with t^{-p} (where p is the electron energy distribution power law index), which is a strong evidence for the late-time afterglow being jet-dominated. Our observations support recent claims from hydrodynamic model-

ing that GW170817 produced a successful jet (Duffell et al. 2018). Using these new data we can also derive robust constraints on the smoothness parameter (s) and therefore the sharpness of the light curve peak, something which has not been possible with previously-reported data. Together with the sharpness of the peak, the steep decline indicates that the jet is extremely narrow and that most of the outflow energy of GW170817 resides in the jet. Through simple analytical arguments we are able to place a constraint on the geometry, $\theta_v \gtrsim 8\theta_j$ ($\theta_v \gtrsim 6\theta_j$ with semi-analytical modeling; θ_v is the viewing angle and θ_j is the jet half-opening angle), and implies $\theta_j \lesssim 5^\circ$ if we further use the viewing angle constraint provided by the LIGO-Virgo Collaboration. Using $\Gamma \simeq 4$ close to the peak of the light curve (estimated from the observed superluminal motion in GW170817) gives $\theta_j \lesssim 3^\circ$ and $\theta_v \simeq 15^\circ$.

These conclusions are consistent with results from VLBI and hydrodynamical simulations (Mooley, Deller, Gottlieb et al. 2018b), from parametric modeling of the jet (Hotokezaka et al. 2018; Ghirlanda et al. 2018; Troja et al. 2018b), and from polarization (Corsi et al. 2018). The jet opening angle for GW170817 appears to be somewhat smaller than the median found for short GRBs, $\langle \theta_j \rangle \simeq 16^\circ \pm 10^\circ$ (θ_j estimates for bursts displaying jet breaks lie between $\sim 2^\circ - 8^\circ$; e.g. Fong et al. 2015), but is consistent with the estimates for short GRBs like 090510 and 150101B (Kumar & Barniol Duran 2010; Nicuesa Guelbenzu et al. 2012; Troja et al. 2018c, see also Troja et al. (2018b)) and the tail end of the long GRB distribution (e.g. Goldstein et al. 2016). With the confirmation of the successful jet in GW170817, our polarization upper limit from Corsi et al. (2018) implies high isotropy of the magnetic field.

At early-times ($\simeq 100$ days), the steady rise in the light curve indicated that there was continuous energy injection within the outflow emitting in our line of sight (e.g. Nakar & Piran 2018), and implied the presence of a mildly relativistic wide-angle outflow with significant angular and/or radial structure (consistent with a cocoon-dominated outflow). At later times, the successful narrow jet came into view and dominated the late-time afterglow. The confirmation of a jet strengthens the link between neutron star mergers and regular SHBs.

Like some previous long-duration GRBs (e.g. Berger et al. 2003), GW170817 has given us insights into the structure of the wide-angle outflows surrounding the jet core, and the simple top-hat jet for SHBs will likely have to be revised (Nakar & Piran 2017; Lazzati et al. 2017a,b). The confirmation of the wide angle outflow, that dominated the outflow at early times, bodes well

⁷ The semi-analytic code (Soderberg et al. 2006) takes proper account of all the relativistic effects such as Lorentz boost and light arrival time from each point in the jet and it includes lateral spreading of the jet. Following corollary comparison of the code results to BOXFit (van Eerten et al. 2012) we use lateral spreading of 30% of the local thermal speed. We verify that varying the spread velocity, including taking no spreading at all does not change the result significantly.

Table 3. Previous radio observations of GW170817

UT date	ΔT^\dagger (d)	Telescope	ν (GHz)	F_ν (μJy)	σ_ν (μJy)
2017 Sep 02–04	17.4	VLA	3	15.4	2.5
2017 Sep 08	22.36	VLA	3	22.5	3.4
2017 Sep 10	24.26	VLA	3	25.6	2.9
2017 Sep 17	31.33	VLA	3	34.0	3.6
2017 Oct 02	46.25	VLA	3	44	4
2017 Oct 10	54.29	VLA	3	48	6
2017 Oct 13	57.19	VLA	3	61	9
2017 Nov 18	93.13	VLA	3	70	6
2017 Sep 05	18.66	ATCA	7.25	20.0	4.8
2017 Nov 01	75.49	ATCA	7.25	35.9	4.3
2017 Nov 17	92.4	ATCA	7.25	31.7	5.6
2017 Dec 02	107.36	ATCA	7.25	53.2	4.5
2017 Dec 20	125.3	ATCA	7.25	58.2	5.0
2018 Jan 13	149.26	ATCA	7.25	60.6	4.3
2018 Feb 01	181.64	ATCA	7.25	57.9	6.9
2017 Oct 21	65.14	GMRT	0.61	117	42

Notes: 1. Compilation from: [Hallinan, Corsi et al. \(2017\)](#); [Mooley et al. \(2018a\)](#); [Dobie et al. \(2018\)](#). 2. The ATCA flux densities of GW170817 have a correction factor of 1.25 applied (see §3.1 for details).

\dagger Mean epoch, days post-merger.

for the future detection of the EM counterparts of GW sources observed at larger viewing angles.

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Facility: VLA, ATCA, uGMRT, MeerKAT

Software: Matplotlib([Hunter2007](#)), NumPy([Oliphant 2006](#)), MIRIAD ([Sault et al. 1995](#)), DIFMAP ([Shepherd 1997](#)), CASA ([McMullin et al. 2007](#)), `emcee` ([Foreman-Mackey et al. 2013](#)), `corner` ([Foreman-Mackey 2016](#))

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