Radio broadband visualization of global three-dimensional magnetohydrodynamical simulations of spiral galaxies – I. Faraday rotation at 8 GHz

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ABSTRACT

Observational study of galactic magnetic fields is hampered by the fact that the observables only probe various projections of the magnetic fields. Comparison with numerical simulations is helpful to understand the real structures, and observational visualization of numerical data is an important task. In this paper, we investigate 8 GHz radio synchrotron emission from spiral galaxies, using the data of global three-dimensional magnetohydrodynamic simulations. We assume a frequency independent depolarization in our observational visualization. We find that the appearance of the global magnetic field depends on the viewing angle: a face-on view seemingly has hybrid magnetic field types combining axisymmetric modes with higher order modes; at a viewing angle of ~70°, the galaxy seems to contain a ring-like magnetic field structure; while in edge-on view, only field structure parallel to the disc can be seen. The magnetic vector seen at 8 GHz traces the global magnetic field inside the disc. These results indicate that the topology of global magnetic field obtained from the relation between azimuthal angle and Faraday depth strongly depends on the viewing angle of the galaxy. As one of the examples, we compare our results at a viewing angle of 25° with the results of IC342. The relation between azimuthal angle and Faraday depth of the numerical result shows a tendency similar to IC342, such as the peak values of the Faraday depth.

Key words: MHD – polarization – galaxies: magnetic fields.

1 INTRODUCTION

The origin and evolution of magnetic fields in spiral galaxies is a longstanding question. Radio observations of synchrotron radiation and Faraday rotation have provided various pieces of information of magnetic fields perpendicular to and parallel to the line of sight (LOS), respectively. The global magnetic field of spiral galaxies has been classified into axisymmetric spiral (ASS) seen in M31 or bi-symmetric spiral (BSS) in M81, based on the topology. Since the discovery of hybrid (ASS and BSS) structure in M51, many galaxies are classified into hybrid-types which consist of ASS and higher modes (Fletcher et al. 2011; Beck 2016). Such global magnetic fields are also known to co-exist with turbulent magnetic fields with comparable magnetic energy densities, which correspond to field strengths of micro gauss. (e.g. Beck 2007).

Such galactic magnetic fields are produced for billions of years by the maintenance mechanisms, which are related to the field topology. Parker (1970) and Parker (1971) proposed a galactic dynamo known as the alpha–omega dynamo and a mean-field galactic dynamo. That mechanism is able to produce toroidal magnetic fields from poloidal fields by the $\alpha$-effect and poloidal fields from toroidal fields by the $\Omega$-effect. It can amplify weak seed field into micro gauss field over 10⁸ yr converting kinetic energy of the differentially rotating disc and energy from associated turbulent gas motions into magnetic energy. Extended dynamo theories were proposed in the 1980s. These models explain both ASS and BSS features of magnetic fields (Chiba & Tosa 1989; Fujimoto & Sawa 1987).

More recently, the importance of the magneto-rotational instability (MRI) was recognized (Balbus & Hawley 1991). Its effect on gaseous motions is taken into account in several global simulations of a galactic gas disc (Nishikori, Machida & Matsumoto 2006; Hanasz, Wójtasiński & Kowalik 2009; Machida et al. 2009, 2013).
For instance, Machida et al. (2013) performed a three-dimensional (3D) magnetohydrodynamic (MHD) simulation of the galactic gas disc. They demonstrated the evolution of the galactic disc induced by the dynamo effect according to the MRI and Parker instabilities. Gressel, Elstner & Ziegler (2013) carried out hybrid dynamo simulations in which they considered the effects of both the MRI and the $\alpha -$ $\Omega$ dynamo excited by supernova explosions. Recently, the formation and evolution of a Milky Way-like disc galaxy is researched in full cosmological context with magnetic fields (Pakmor, Marinacci & Springel 2014).

In order to examine the topology of magnetic fields and understand their origin and evolution, theoretical predictions of observables are important. For example, using data of 3D MHD turbulence simulations, high-precision modeling, and observational visualization of diffuse ionized gas toward high Galactic latitudes was conducted (Akahori et al. 2013). Wide-field and high-spatial-resolution radio observations with future radio interferometers such as the Square Kilometre Array (SKA) would dramatically improve imaging quality in galaxy surveys, and would allow us to study complex structures that reflect the MRI-Parker instability. Moreover, future radio observations will achieve wideband polarimetry, which will deliver a new research dimension and will become a breakthrough of the study of galactic magnetic fields (e.g. Heald et al. 2015). For example, the use of Faraday tomography for astronomical objects has started (see e.g. Akahori et al. 2014; Ideguchi et al. 2014).

Radio broadband visualization is, however, challenging because the effect of depolarization is significant particularly at low frequencies (Burn 1966; Arshakian & Beck 2011). In this study, we attempt to perform broadband observational visualization of a spiral galaxy, using the data of a global 3D MHD simulation of a galactic gas disc (Machida et al. 2013). It aims to clarify the relation between projected observables and actual 3D structure of magnetic fields in our simulation. We introduce the numerical data in Section 2 and the method of calculation in Sections 3. The numerical results are shown in Section 4, followed by discussion and summary in Sections 5 and 6, respectively.

## 2 MHD Simulation of a Spiral Galaxy

We analyze the results of global MHD simulations of a galactic gaseous disc. The simulation was performed in the cylindrical coordinate system ($r$, $\phi$, $z$). The simulation box size is defined in the radial direction as $r < 56$ kpc, in the azimuthal direction as $0 < \phi < 2\pi$, and in the vertical direction as $-10$ kpc < $z$ < 10 kpc, and is gridded evenly with cells of $(250, 256, 640)$ in the ($r$, $\phi$, $z$) directions, respectively. In the main domain where we address in this paper, $0$ kpc < $r$ < 6 kpc and $-2$ kpc < $z$ < 2 kpc, the spatial resolution of the simulation is $\Delta r = 50$ pc and $\Delta z = 10$ pc. With $\Delta \phi = 2\pi /256$, the resolution of the azimuthal direction, $\Delta \phi$, depends on $r$ and is 25 pc at $r = 1$ kpc.

The initial condition of the simulation was an equilibrium torus threaded by weak azimuthal magnetic fields embedded in a non-rotating hot corona under the Miyamoto and Nagai potential (Miyamoto & Nagai 1975). The self-gravity of the gaseous disc, radiative cooling, and spiral-arm potential of the stellar disc were all ignored in their paper. The initial torus with the temperature $10^5$ K and the density 1 cm$^{-3}$ at $r = 10$ kpc changes its shape to the disc by redistribution of the angular momentum, because the magnetic turbulence caused by MRI transports the angular momentum outward. The resultant disc has the equatorial density of 0.1 cm$^{-3}$ at $r = 2$ $\sim$ 3 kpc. Angular momentum of the gas in the disc is transported by the MRI, and the gas temperature increases to $10^5$ K due to the adiabatic compression and the Joule heating by magnetic reconnection in the disc and the boundary layer between the disc and the halo. Magnetic field in the disc is amplified in such a high temperature plasma. The plasma $\beta$ (the ratio of the gas pressure to the magnetic pressure) in the disc ranges from 5 to 100 and the averaged value becomes about 20. Note that the temperature varies with time but its fluctuation is small, because we did not consider gas cooling mechanism by radiation.

Although the disc magnetic field is tangled and becomes turbulent, structures of the global magnetic field in the disc and the halo have the compositions of the higher-order mode and ASS-like topologies, respectively. Such a duality seems to be consistent with the result of Faraday tomography for M51 (Fletcher et al. 2011). Both the mean and turbulent components show similar peak strengths of about 10 $\mu$G. But the volume filling factor of such high strength regions is less than 0.1 in the disc and the volume-averaged strength in the disc is about a few $\mu$G. The average magnetic energy of the turbulent component is about three times larger than that of the mean (regular) component inside the gas disc, and they become comparable to each other in the halo region.

Our model exhibits a few magnetic spiral arms on the contour of the magnetic energy. But the magnetic spiral arms in the numerical results do not corresponds to the grand-design spiral such as M51, because we do not consider the cooling effect of the gas. The spiral galaxies showing grand-design spirals (e.g. M51 and so on) and higher star forming activities are beyond the scope of this paper. See Appendix A and Machida et al. (2013) for more details of the simulation data. Meanwhile, IC342 is one of the targets of our model (see recent review by Beck 2016). We attempt to compare IC342 with our simulation in Section 5.

## 3 Observational Visualization

We consider observations of an external galaxy and calculate radio synchrotron observables such as the Stokes parameters and Faraday rotation measure. Since numerical simulation data has the physical values such as magnetic field vector and density at each grid point, we directly calculate the Faraday depth (FD), which is an integral of the LOS component of magnetic field weighted with the density. If the Faraday rotation occurs at the foreground of the synchrotron emitting source, the FD is equal to the Faraday rotation measure.

Fig. 1 shows the schematic drawing of the visualization region. The computational volume of the visualization is a cube ($x$, $y$, $z$) with sides of 20 kpc, which is centered on the galactic center. Two-dimensional maps are constructed with ($N_x$, $N_y$) = (200, 200) image pixels centered at the projected galactic center which corresponds to the bottom square in $x$–$y$ plane on Fig. 1. Hence the image resolution becomes 100 pc. This resolution corresponds to $\sim$2 arcsec, if we assume a galaxy is placed in the Virgo cluster at a distance of $\sim$20 Mpc.

For each image pixel, we integrate observables along the $z$-axis. We incline the $z$-axis of the cylindrical coordinate of the data along the $y$–$z$ plane and the inclination angle, $\theta$, is defined as the angle from the $z$-axis to the $z$-axis; $\theta = 0^\circ$ and $\theta = 90^\circ$ correspond to face-on and edge-on view, respectively.

### 3.1 Procedure of visualization

The integration for the image pixel at ($i$, $j$) is performed as follows. The local FD within a certain computational cell is given by $0.81 n_e B_0 \Delta l$, where $\Delta l = 100$ pc is the line element. The electron density, $n_e$, and the LOS component of the magnetic field, $B_0$, are...
Here, we consider the electron energy spectral index, $p$, and the coefficients, $g_1(p)$ and $g_2(p)$ (Appendix B), and the term $e^{-\tau_{i,j,k}}$ gives free–free absorption of synchrotron emission. 

Faraday rotation of the PA in equations (5) and (6) is given by

\[
\chi_{i,j,k} = \frac{1}{2} \cos^{-1} \left( \frac{B_{\perp}}{B_{\parallel}} \right) + F D_{ave,i,j,k} \lambda^2, 
\]

where the first term gives the intrinsic PA. We integrate $\Delta I$, $\Delta Q$, and $\Delta U$ along the LOS to obtain the specific Stokes parameters ($I$, $Q$, and $U$). Because we do not consider the distance from the observer to the galaxy, absolute values of Stokes parameters are rather arbitrary and only relative brightness is meaningful in this paper. It means that the length of the LOS is about 20 kpc which corresponds to the diameter of the galaxy.

We also present the PA,

\[
\chi = \frac{1}{2} \tan^{-1} \left( \frac{U}{Q} \right),
\]

and the PD,

\[
\Psi = \frac{P}{I} = \sqrt{Q^2 + U^2} \frac{I}{I},
\]

where we do not consider circular polarization, which is weak in the context of this study.

According to Werner et al. (2015), electrons with energies greater than 100 GeV are confined to their source regions and trace the cosmic-ray source distribution closely. Because cosmic-ray electrons responsible for radio emission in 8 GHz in a magnetic field of 10 $\mu$G have energies of 7 GeV, the cosmic-ray electron is diffused from the magnetic spiral arm. The diffusion lengths of GeV electrons are about 1 kpc during their lifetime of a few $10^7$ yr. Since this time scale is much more than the resolution in our model, the assumption of local equipartition is not valid. However, the diffusion of cosmic-ray is beyond the scope of this paper. If the total energy of cosmic-ray is comparable to the thermal energy and energy equipartition with magnetic fields is assumed, this contradicts $\beta = 10$ as derived in the MHD model (Appendix A). The energy spectral index $p = 3$ is adopted as a typical value (Sun et al. 2008).

4 RESULTS

We present the result of the simulation at a few tens of rotation periods at $r = 10$ kpc as a representative case. It corresponds to about 48 billion years after the start of the simulation, at which both regular and turbulent magnetic fields are well-established by the MRI-Parker instability. Below, we show the results of face-on view, edge-on view, and intermediate inclination view in this order.

4.1 Face-on view

Fig. 2(a) shows the FD ($FD_{ave}$) map for the case of inclination angle 5$^\circ$. It is clearly seen that the FD distribution is patchy and complex due to turbulent magnetic fields. Fig. 2(b) displays FDs in above-average bright regions of the simulated synchrotron total intensity (TI) at 8 GHz in order to highlight FDs at brighter regions. TI and polarized intensity (PI) at the observing frequency of 8 GHz are shown in Figs 2(c) and (d), respectively. Arrows show the magnetic vector, $2\chi + 90^\circ$, with $\chi$ obtained from the Stokes Q.

\[
\Delta I = g_1(p) F \Delta l,
\]

\[
\Delta Q = g_2(p) F \cos (2\chi_{i,j,k}) \Delta l,
\]

\[
\Delta U = g_2(p) F \sin (2\chi_{i,j,k}) \Delta l,
\]

where

\[
F = C(r) B_{\perp}^{(1-p)/2} (2\pi v)^{(1-p)/2} e^{-\tau_{i,j,k}}.
\]
Figure 2. (a) FD contour map of the simulated spiral galaxy for an inclination angle $\theta = 5^\circ$. Both horizontal and vertical axes have units of kpc, and the FD has units of rad m$^{-2}$. (b) Same as (a) but only the pixels with TI(8 GHz) larger than the average of TI(8 GHz) within the image are shown. (c) Simulated synchrotron TI at the observed frequency of 8 GHz. (d) Simulated PI at the observed frequency of 8 GHz, all in units of Jy/sr. Arrows indicate the magnetic vector ($2\chi + 90^\circ$) whose strength is normalized by the maximum strength in the map. The sample vector indicates the strength of magnetic field which is 20 per cent of the maximum one.

and U (equation 9), whose strength is normalized by the strength of the maximum one in the map. The sample vector on Fig. 2(d) denote 20 per cent of the strongest magnetic strength. At some places, the direction of the magnetic field turns $\sim 180^\circ$ across an arm/interarm. This is because the magnetic spiral arms have neutral current sheets.

TI clearly shows spiral structure. Such patterns are also seen in PI, where PI and TI are similar to each other. Actually, Faraday rotation is weak at 8 GHz, and the magnetic vector, which is parallel to the spiral pattern of PI, traces the direction of magnetic fields. This indicates that TI and PI reflect the spiral magnetic-field structure inside the gas disc rather than magnetic fields in the halo.

4.2 Edge-on view

Fig. 3(a) shows the FD map for $\theta = 85^\circ$. The FD is mainly derived from the gas at the mid-plane of the LOS, because the azimuthal magnetic field is dominant and only the LOS component of magnetic fields can contribute to the FD. Similarly, FD around the rotation axis ($x \sim 0$), at which denser gas exists, is rather small. Because the azimuthal magnetic field is dominant in the gaseous disc, the azimuthal magnetic field becomes parallel to the LOS around the $z$-axis.

There are reversals of the sign of FD along the radial direction. The reversals mean multiple inversions of the direction of the global azimuthal magnetic field. Actually, azimuthal magnetic fields, which emerged from the disc owing to the Parker instability, show periodic reversals. Such positive and negative FDs can be seen as stripes in the vicinity of the rotation axis. The length scale of emerging flux tubes from the disc to the halo are about a few kpc, although the length depends on their radius. The striped FD patterns could be unique evidence that the magnetic flux flows out into the galactic halo successfully. Note that the pattern seems simply random around the rotation axis, if we focus on brighter regions (Fig. 3b). This means that it is difficult to identify the global patterns, if we only have low-sensitivity polarization data.

Figs 3(c) and (d) show the maps of TI and PI at 8 GHz, respectively. Overall, TI becomes larger towards the galactic mid-plane, because the global magnetic field is strongest in the disc. Structures seen in PI are similar to those seen in TI, and the magnetic vector nicely traces the global azimuthal magnetic field.
4.3 Intermediate inclination angles

Fig. 4 shows the results for the inclination angles $\theta = 25^\circ$, $45^\circ$, and $70^\circ$ from left to right, respectively. As already mentioned in Fig. 3, the FD is relatively small along the rotation axis of the galaxy ($x \sim 0$), since the dominant, azimuthal magnetic field is not parallel to the LOS and hence does not contribute to the FD. In contrast, PI, which intrinsically depends on the magnetic fields perpendicular to the LOS, is maximum around $x \sim 0$ and weaker away from $x \sim 0$.

We find that the topology of the magnetic vector field in PI is different between small and large viewing angles, although we have used the same numerical data of a spiral galaxy. The magnetic vector field apparently can be explained with a mixed mode of ASS and higher modes with smaller scales for $\theta = 25^\circ$. As we increase $\theta$, a ring-like structure partly mixes in the pattern inside $2 \text{kpc}$.

Fig. 5 shows an azimuthal variation of FD, which was calculated by integrating value of the FD in ranges of $3 \text{kpc} < r < 4 \text{kpc}$ and $4 \text{kpc} < r < 7 \text{kpc}$, each of which are indicated with black and gray curves, respectively. To compare with the observation of IC342, the gray curves are integrated in the wide region. The dependence of the inclination angles is shown from top to bottom. The number of the reversals is comparable to the scale length of the Parker instability, which is about a few kpc in the azimuthal direction. This length corresponds to the vertical scale height. The number of the reversals in the range of $3 \text{kpc} < r < 4 \text{kpc}$ are larger than that in the range of $4 \text{kpc} < r < 7 \text{kpc}$. Because the width of the magnetic tube formed by the Parker instability is about $1 \text{kpc}$, the resultants are cancelled by the integration. Remaining components of the reversal is driven by the Parker instability near the center region and mean components by the dynamo activities. In the almost face-on view ($\theta = 5^\circ$), these structures indicate that reversals of the vertical components along the LOS are observed. When the inclination angle becomes large, there are less reversals in the FD. Essentially, the higher mode with smaller scale is expected in our numerical simulation data because there are a few magnetic spiral arms. On the other hand, since the integrated region of the gray curves are larger than the scale length of the turbulence. The fluctuations in the curves are disappeared and $\phi$-FD relations show a sinusoidal distribution ($5b, c, d$), which are typical structure of ASS. The FD curves of the outer region (gray one) still show the reversals of FD, which is considered to combination of the ASS and the higher mode with smaller scale.

5 DISCUSSION

5.1 LOS distribution of magnetic fields

To link the projected observables to actual 3D structures, we plot the physical quantities along the LOS. Fig. 6 shows the cross sections...
Figure 4. Maps of the simulated observables. Top and bottom panels show the FD and PI at 8 GHz. Also shown are the magnetic vector angles ($2\chi + 90^\circ$) as arrows. Panels from left to right show the results for the inclination angles $\theta = 25^\circ$, $45^\circ$, $70^\circ$, respectively. Both horizontal and vertical axes have units of kpc.

Figure 5. The azimuthal distribution of the FD. The black curves show the FD in the region of $3 \text{kpc} < r < 4 \text{kpc}$, and gray curves show that in the region $4 \text{kpc} < r < 7 \text{kpc}$. Top and bottom panels show the results of $\theta = 5^\circ$ and $85^\circ$, respectively.

Figure 6. Distribution of physical quantities along the LOS (in kpc) for the inclination angle $\theta = 5^\circ$. Panels show (a) the gas number density in cm$^{-3}$, (b) the local FD (in rad m$^{-2}$) within each computational cell with a depth of 100 pc, (c) $B_\perp^2$ in ($\mu$G)$^2$, and (d) $B_\parallel$ in $\mu$G. Black and gray curves show the values toward the interarm ($-3 \text{kpc}, 0 \text{kpc}$) and the arm ($2 \text{kpc}, -0.5 \text{kpc}$), respectively. The galactic mid-plane is located at $\sim 10 \text{kpc}$. 
to the low density in the halo. However, because the halo density is low, the FD induced by such magnetic wind resulting from the flotation of the Parker instability.

The resultant cumulative FD toward the disc is 151 rad m$^{-2}$, although the local FDs show about $-60$ rad m$^{-2}$.

5.2 Is X-field missing due to reduced outflows?

Our visualizations for the edge-on view do not indicate the X-shape structure of the magnetic vector, which is seen in, for example, NGC 253 (Heesen et al. 2009). Even though we choose a higher frequency such as 8 GHz, at which both Faraday rotation and depolarization are negligible and the magnetic vector thus traces the intrinsic direction of magnetic fields, the magnetic vectors indicate not vertical but azimuthal magnetic fields (e.g. Fig. 3b).

In our global MHD simulation of a spiral galaxy, it is possible that the growth of vertical magnetic fields is reduced on some level and thus the X-field does not exceed the azimuthal magnetic field. This is because the outflow velocity was $\sim 30$ km s$^{-1}$, which is $\sim 10$ per cent of that observed in starburst galaxies. A possible reason for such a low outflow velocity is that we ignored cosmic-ray pressure and/or we assumed high gas pressure initially. The effects of cosmic rays on magnetic instability were studied by several authors (e.g. Kuwabara, Nakamura & Ko. 2004; Khajenabi 2012; Suzuki, Takahashi & Kudoh 2014; Kuwabara & Ko 2015). According to these studies, the cosmic-ray pressure can support the growth of a magnetic instability such as the MRI or Parker instability, although the results depend on the diffusion of cosmic-rays and magnetic field structure. When starburst becomes dominant, the stellar wind could also produce powerful winds and cosmic-ray pressure could assist the acceleration of galactic winds.

5.3 Comparison with IC342

The FD reversal within the spiral arms are found in the galaxy IC342 which shows a low star formation rate and unclear spiral arms (Beck 2015). To compare to the observations, we made a plot of the FD in the spiral arms (see Fig. 2b). The periodical reversals of FD are observed in the spiral arms. Because the scale length correlates with the disc scale height, the reversal length of the FD signs are proportional to the radius. It means that these reversals are caused by the Parker instability. These results support to the observational results for IC342 and theoretical predictions of the Parker instability. Fig. 5(b) shows the relation between azimuthal angle and FD inside 4 kpc $< r < 7$ kpc for $\theta = 25^\circ$, whose inclination angle seems to be IC342. The tendency of azimuthal angle – FD relation shows similar with IC342.

Since we ignored the cool components of galactic gas disc, the gas density and magnetic field strength will be underestimated. When we will consider the multitemperature distribution of galactic disc, these discrepancies will be resolved.

5.4 Enhancement of global magnetic fields

In our simulation, the volume-averaged energy of turbulent magnetic fields is three times larger than that of the mean magnetic field which is dominated by the azimuthal component in the disc. The peak strength of the mean azimuthal component, which corresponds to the magnetic spiral arm, is 70 per cent of that of the turbulent component. These magnetic spiral arms are much fainter than the grand-design spiral of the galaxies. This is because the temperature inside the disc becomes about $10^4$ K, the turbulent cell becomes large. According to the Machida, Nakamura & Matsumoto (2006) which reported about the state transition of X-ray binaries, when the cooling effect worked in the accretion disc, the accretion disc shrunk in vertical direction with magnetic flux and mean magnetic fields enhanced inside the accretion disc. For the accretion disc case, the accretion disc became magnetically supported when the shrinking was stopped and the disc scale height of magnetically supported disc became 20 per cent of the gas pressure (high temperature) disc. The turbulent components of magnetic fields are dissipated inside the thin disc and the ordered field remained inside the disc.
speculate that magnetic field evolution through the gas heating and cooling qualitatively work in a similar manner between the galactic disc and the accretion disc. First, a part of neutral gas is ionized by supernovae, OB-star ultraviolet radiation and magnetic reconnection, etc. These ionization mechanisms are strongly coupled with magnetic fields. Secondly, turbulence is generated and magnetic field is enhanced by the MRI and Parker instability in the radial direction. Thirdly, the ionized gas returns to neutral if the density is high enough to work the molecular cooling. The magnetic flux shrinks in vertical direction and the mean magnetic field enhances inside the disc. However, the scale height of warm H\textsc{i} components of galactic gas disc is comparable to the high temperature plasma, since there are extra energy inputs caused by the super novae and magnetic activities. Therefore, in the case of the galactic gaseous disc, we expect that the turbulent field is not much dissipated and the ordered magnetic energy will be comparable to the turbulent magnetic energy. In addition, the spiral potential of the galactic star disc has an important effect to produce the ordered magnetic fields.

6 SUMMARY

We summarize the points discussed in the present work:

(i) PI becomes stronger towards the rotation axis of the galaxy, while FD shows the opposite tendency. This is because the azimuthal component of magnetic field is predominant inside the disc and thus the LOS component contributing to FD and the perpendicular component inducing PI depend on the distance from the rotation axis. These tendencies do not depend on the inclination angle of the galaxy.

(ii) TI and PI(8 GHz) are both stronger along denser magnetic spiral arms, where depolarization is insignificant at such high frequencies. The PA traces the orientation of the azimuthal magnetic field inside the disc.

(iii) An ASS-like structure appears in the magnetic-vector map for the case of \( \theta = 85^\circ \), and one sine curve is seen in the azimuthal angle–FD relation. Meanwhile, since a few magnetic spiral arms are present in the numerical simulation data, a sine curve with three to four periods is expected in the azimuthal angle–FD relation in the case of \( \theta = 5^\circ \). The topology, however, cannot be clearly classified as BSS with an inclination angle less than 70\(^\circ\). The \( \phi – FD \) relations show a sinusoidal distribution which is typical structure of ASS.

An X-shape vertical structure is not observed in our results. It may be ascribed to the fact that our numerical results have weak outflows produced by Parker instability. If we include the effect of cosmic rays, the growth rate of the Parker instability becomes large and the outflow speed becomes high enough to explain the observations. Our assumption that the cosmic ray density is proportional to the perpendicular component inducing PI depend on the distance from the rotation axis. Therefore, in the case of the galactic gaseous disc, we expect that the turbulent field is not much dissipated and the ordered magnetic energy will be comparable to the turbulent magnetic energy. In addition, the spiral potential of the galactic star disc has an important effect to produce the ordered magnetic fields.

Finally, we did not employ Faraday tomography, which is clearly complementary to our work and may be more powerful so as to deproject the LOS structure. It is, however, not trivial so far how we can translate the Faraday spectrum into real 3D structure of the galaxy (Ideguchi et al. 2014). We need further studies of both observational visualization and Faraday tomography for numerical data.

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**APPENDIX A: NUMERICAL SIMULATION OF GALACTIC GAS DISC**

Machida et al. (2013) performed a 3D MHD simulation of the galactic gas disc. Below, we briefly summarize the evolution of magnetic field in the simulation.

The normalization of the velocity is $v_0 = (GM_\odot r_0)^{0.5}$ where we assume the unit length is $r_0 = 1 \text{ kpc}$ and $M_\odot = 10^{10} \text{M}_\odot$. The unit temperature is calculated by the unit velocity. This means that the unit velocity corresponds to the sound velocity. The thermal energy of the initial torus is balanced the gravitational energy which is made by the central black hole. They assumed the ratio of thermal energy to the gravitational energy is 0.05. Because the initial magnetic field in both radial and vertical directions inverts quasi-periodically, the time scale of the flotation cycle is about 10 times the rotation period at 1 kpc.

When the disc reaches quasi-steady state, gaseous disc becomes turbulent and a strong magnetic flux forms locally, and the magnetic field strength parallel to the seed fields grows faster than the one that adopted in this paper, respectively. This value can be used to judge whether the most unstable wavelength of the MRI was resolved or not. From the comparison, we concluded that 128-grid model did not significantly differ from the results with 256-grid model in the nonlinear stage. The azimuthal spatial resolution adopted in our work is thus sufficient to reproduce the MRI.

**APPENDIX B: SYNCHROTRON RADIATION AND FARADAY ROTATION**

When relativistic charged particles such as cosmic-ray electrons move in a magnetized plasma, their tracks follow a helical curve along a magnetic field line, emitting polarized synchrotron radiation. Considering an isotropic cosmic-ray electron distribution with the cosmic-ray electron density $C(r)$, the energy spectral index $p$, and the number density $N(r)\ dy = C\gamma^{-7}dy$ between the electron Lorentz factor $\gamma$ and $\gamma + dy$, specific Stokes parameters of synchrotron radiation from the electron population can be written as

$$ I = \int G_1(p)\sigma_{\text{el}}(\gamma)B_\perp(r)\gamma^{(1+p)/2}C(r)\ dr, $$

$$ P = Q + iU = \int G_2(p)\sigma_{\text{el}}(\gamma)B_\perp(r)\gamma^{2\chi(r)}\ dr $$

(Sun et al. 2008; Waelkens et al. 2009), where $B_\perp$ is the magnetic field perpendicular to the LOS, $\chi$ is the initial polarization angle at $r$, and $\omega$ is the angular frequency. Other physical coefficients are $G_1(p) = 2g_1(p)$, $G_2(p) = 2g_2(p)$.

$$ j(p) = \frac{1}{4\pi} \sqrt{3q^3} \frac{2mc}{3q} \frac{(1-p)^{1/2}}{\Gamma(p+1/2)}. $$

$$ g_1(p) = \frac{1}{1+p} 2^{(1+p)/2} \frac{p-1}{12} \Gamma \left( \frac{p}{4} + \frac{19}{12} \right). $$

$$ g_2(p) = \frac{1}{1+p} 2^{(1+p)/2} \frac{p-1}{12} \Gamma \left( \frac{p}{4} + \frac{7}{12} \right). $$

where, $c$, $m$, $q$, and $\Gamma$ are the speed of light, electron mass, electric charge, and $\Gamma$ function, respectively.

FD can be derived from the free-electron density ($n_e$) of the magnetized plasma and the magnetic field parallel to the LOS ($B_\parallel$) as

$$ FD = \frac{q^3}{2\pi m^2 c^4} \int_0^\infty n_e B_\parallel dx \sim 0.81 \int_0^\infty n_e B_\parallel dx \ [\text{rad} \ m^{-2}]. $$