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\section*{ABSTRACT}

\textbf{Context.} The \textit{Gaia} spacecraft of the European Space Agency (ESA) has been securing observations of solar system objects (SSOs) since the beginning of its operations. Data Release 2 (DR2) contains the observations of a selected sample of 14,099 SSOs. These asteroids have been already identified and have been numbered by the Minor Planet Center repository. Positions are provided for each \textit{Gaia} observation at CCD level. As additional information, complementary to astrometry, the apparent brightness of SSOs in the unfiltered $G$ band is also provided for selected observations.

\textbf{Aims.} We explain the processing of SSO data, and describe the criteria we used to select the sample published in \textit{Gaia} DR2. We then explore the data set to assess its quality.

\textbf{Methods.} To exploit the main data product for the solar system in \textit{Gaia} DR2, which is the epoch astrometry of asteroids, it is necessary to take into account the unusual properties of the uncertainty, as the position information is nearly one-dimensional. When this aspect is handled appropriately, an orbit fit can be obtained with post-fit residuals that are overall consistent with the a-priori error model that was used to define individual values of the astrometric uncertainty. The role of both random and systematic errors is described. The distribution of residuals allowed us to identify possible contaminants in the data set (such as stars). Phometry in the $G$ band was compared to computed values from reference asteroid shapes and to the flux registered at the corresponding epochs by the red and blue photometers (RP and BP).

\textbf{Results.} The overall astrometric performance is close to the expectations, with an optimal range of brightness $G\sim12$-17. In this range, the typical transit-level accuracy is well below 1 mas. For fainter asteroids, the growing photon noise deteriorates the performance. Asteroids brighter than $G\sim12$ are affected by a lower performance of the processing of their signals. The dramatic improvement brought by \textit{Gaia} DR2 astrometry of SSOs is demonstrated by comparisons to the archive data and by preliminary tests on the detection of subtle non-gravitational effects.

\textbf{Key words.} astrometry – Solar System: asteroids – methods: data analysis – space vehicles: instruments

\section*{1. Introduction}

The ESA \textit{Gaia} mission (Gaia Collaboration et al. 2016) is observing the sky since December 2013 with a continuous and predetermined scanning law. While the large majority of the observations concern the stellar population of the Milky Way, \textit{Gaia} also collects data of extragalactic sources and solar system objects (SSOs). A subset of the latter population of celestial bodies is the topic of this work.

\textit{Gaia} has been designed to map astrophysical sources of very small or negligible angular extension. Extended sources, like the major planets, that do not present a narrow brightness peak are indeed discarded by the onboard detection algorithm. This mission is therefore a wonderful facility for the study of the population of SSOs, including small bodies, such as asteroids, Jupiter trojans, Centaurs, and some Transneptunian Objects (TNO) and planetary satellites, but not the major planets.

The SSO population is currently poorly characterised, because basic physical properties including mass, bulk density, spin properties, shape, and albedo are not known for the vast majority of them.

The astrometric data are continuously updated by ground-based surveys, and they are sufficient for a general dynamical classification. Only in rare specific situations, however, their accuracy allows us to measure subtle effects such as non-gravitational perturbations and/or to estimate the masses. In this respect, \textit{Gaia} represents a major step forward.

\textit{Gaia} is the first global survey to provide a homogeneous data set of positions, magnitudes, and visible spectra of SSOs, with extreme performances on the astrometric accuracy (Mignard et al. 2007; Cellino et al. 2007; Tanga et al. 2008; Hestroffer et al. 2010; Delbo’ et al. 2012; Tanga et al. 2012; Tanga & Mignard 2012; Spoto et al. 2017). \textit{Gaia} astrometry, for $\sim 350\,000$ SSOs by the end of the mission, is expected to produce a real revolution. The additional physical data (low-resolution reflection spectra, accurate photometry) will at the same time provide a much needed physical characterisation of SSOs.
Within this population, the Gaia DR2 contains a sample of 14,099 SSOs (asteroids, Jupiter trojans, and a few TNOs) for a total of 1 977 702 different observations, collected during 22 months since the start of the nominal operations in July 2014. A general description of Gaia DR2 is provided in Gaia collaboration et al. (2018).

The main goal of releasing SSO observations in Gaia DR2 is to demonstrate the capabilities of Gaia in the domain of SSO astrometry and to also allow the community to familiarise itself with Gaia SSO data and perform initial scientific studies. For this reason, the following fundamental properties of the release are recalled first.

- Only a sub-sample of well-known SSOs was selected among those observed by Gaia. Moreover, this choice is not intended to be complete with respect to any criterion based on dynamics of physical categories.
- The most relevant dynamical classes are represented, including near-Earth and main-belt objects, Jupiter trojans, and a few TNOs.
- For each of the selected objects, all the observations obtained over the time frame covered by the Gaia DR2 are included, with the exception of those that did not pass the quality tests described later in this article.
- Photometric data are provided for only a fraction of the observations as a reference, but they should be considered as preliminary values that will be refined in future data releases.

The goals of this paper are to illustrate the main steps of the data processing that allowed us to obtain the SSO positions from Gaia observations and to analyse the results in order to define the overall accuracy of the sample, as well as to illustrate the selection criteria that were applied to identify and eliminate the outliers.

The core of our approach is based on an accurate orbital fitting procedure, which was applied on the Gaia data alone, for each SSO. The data published in the DR2 contain all the quantities needed to reproduce the same computations. The post-fit orbit residuals generated during the preparation of this study are made available as an auxiliary data set on the ESA Archive.

The TDI rate is an instrumental constant, and the spacecraft spin rate is calibrated on the stars. The exposure time is determined by the crossing time of a single CCD, that is, 4.4 s. Shorter exposure times are obtained when needed to avoid saturation, by intermediate electric barriers (the so-called gates) that swallow all collected electrons. Their positioning on the CCD in the AL direction is chosen in such a way that the distance travelled by the source on the CCD itself is reduced, thus reducing the exposure time.

To drastically reduce the data volume processed on-board and transmitted to the ground, only small patches around each source (windows) are read out from each CCDs. The window is assigned after the source has been detected in a first strip of CCD, the sky mapper (SM), and confirmed in AF1. For the vast majority of the detected sources (G>16), the window has a size of 12×12 pixels, but the pixels are binned in the direction perpendicular to the scanning direction, called across-scan (AC). Only 1D information in the AL direction is thus available, with the exception of the brightest sources (G<13), for which a full 2D window is transmitted. Sources of intermediate brightness are given a slightly larger window (18×12 pixels), but AC binning is always present.

As the TDI rate corresponds to the nominal drift velocity of stars on the focal plane, the image of an SSO that has an apparent sky motion is slightly spread in the direction of motion. Its AL position also moves with respect to the window centre during the transit. The signal is thus increasingly truncated by the window edge. For instance, the signal of an SSO with an apparent motion (in the AL direction) of 13.6 mas/s moves by one pixel during a single CCD crossing, with corresponding image smearing.

We can assume that the image is centred in the window at the beginning of the transit, when it is detected first by the SM, and its position is used to define the window coordinates. Then, while drifting on the focal plane and crossing the AF CCDs, due to its motion relative to the stars, the SSO will leave the window center. When the AF5 strip is reached, about half of the flux will be lost.

In practice, the uncertainty in determining the position of the source within the window is a function of its centring and can vary over the transit due to the image drift described above. This contribution to the error budget is computed for each position and published in Gaia DR2.

2.1. Selection of the sample

For Gaia DR2, the solar system pipeline worked on a predetermined list of transits in the field of view (FOV) of Gaia. To build it, a list of accurate predictions was first created by cross-matching the evolving position of each asteroid to the sky path of the Gaia FOVs. This provides a set of predictions of SSO transits that were then matched to the observed transits. At this level, the information on the SSO transits comes from the output of the daily processing (Fabricius et al. 2016) and in particular

1 https://gea.esac.esa.int/archive/
from the initial data treatment (IDT). IDT proceeds by an approximate, daily solution of the astrometry to derive source positions with a typical uncertainty of the order of ~70-100 mas. There was typically one SSO transit in this list for every 100,000 stellar transits.

SSO targets for the Gaia DR2 were selected following the basic idea of assembling a satisfactory sample for the first mass processing of sources, despite the relatively short time span covered by the observations (22 months). The selection of the sample was based on some simple rules:

- The goal was to include a significant number of SSOs, between 10,000 and 15,000.
- The sample had to cover all classes of SSOs: near-Earth asteroids (NEAs), main-belt asteroids (MBAs), Jupiter trojans, and TNOs.
- Each selected object was requested to have at least 12 transits in the 22 months covered by the Gaia DR2 data.

The final input selection contains 14,125 SSOs, with a total of 318,290 transits. Not all these bodies are included in Gaia DR2: 26 objects were filtered out for different reasons (see Sect. 3.2 and 5). The coverage in orbital semi-major axes is represented in Fig. 1.

2.2. Time coverage

The Gaia DR2 contains observations of SSOs from 5 August 2014, to 23 May, 2016\(^2\). During the first two weeks of the period covered by the observations, a special scanning mode was adopted to obtain a dense coverage of the ecliptic poles (Gaia Collaboration et al. 2016, the ecliptic pole scanning law, EPSL). Due to the peculiar geometry of the EPSL, the scan plane crosses the ecliptic in the perpendicular direction with a gradual drift of the node longitude at the speed of the Earth orbiting the Sun.

A smooth transition then occurred towards the nominal scanning law (NSL) between 22 August and 25 September 2014 that was maintained constant afterwards. In this configuration, the spin axis of Gaia precesses on a cone centred in the direction of the Sun, with a semi-aperture of 45° and period of 62.97 days (Fig. 4). As a result, the scan plane orientation changes continuously with respect to the ecliptic with inclinations between 90° and 45°. The nodal direction has a solar elongation between 45° and 135°.

The general distribution of the observations is rather homogeneous in time, with very rare gaps, in general shorter than a few hours; these are due to maintenance operations (orbital maneuvers, telescope refocusing, micrometeoroid hits, and other events; Fig. 2).

A more detailed view of the distribution with a resolution of several minutes (Fig. 3) reveals a general pattern that repeats at each rotation of the satellite (6 hours) and is dominated by a sequence of peaks that correspond to the crossing of the ecliptic region by the two FOVs, at intervals of ~106 minutes (FOV 1 to FOV 2) and ~254 minutes (FOV 2 to FOV 1). The peaks are strongly modulated in amplitude by the evolving geometry of the scan plane with respect to the ecliptic.

The observation dates are given in barycentric coordinate time (TCB) Gaia-centric\(^3\), which is the primary timescale for Gaia, and also in coordinated universal time (UTC) Gaia-centric. Timings correspond to mid exposure, which is the instant of crossing of the fiducial line on the CCD by the photocentre of the SSO image.

The accuracy of timing is granted by a time-synchronisation procedure between the atomic master clock onboard Gaia (providing onboard time, OBT) and OBMT, the onboard mission timeline (Gaia Collaboration et al. 2016). OBMT can then be converted into TCB at Gaia. The absolute timing accuracy requirements for the science of Gaia is \(2 \mu s\). In practice, this requirement is achieved throughout the mission, with a significant margin.

2.3. Geometry of detection

The solar elongation is the most important geometric feature in Gaia observations of SSOs. By considering the intersection of the scan plane with the ecliptic, as shown in Fig. 5, it is clear that SSOs are always observed at solar elongations between 45° and 135°.

This peculiar geometry has important consequences on solar system observations. The SSOs are not only observed at non-negligible phase angles (Fig. 12), in any case never close to the opposition, but also in a variety of configurations (high/low proper motion, smaller or larger distance, etc.), which have some influence on many scientific applications and can affect the detection capabilities of Gaia and the measurement accuracy.

The mean geometrical solar elongation of the scan plane on the ecliptic is at quadrature. In this situation, the scan plane is inclined by 45° with respect to the ecliptic. During the precession cycle, the scan plane reaches the extreme inclination of 90° on the ecliptic. In this geometry, the SSOs with low-inclination orbits move mainly in the AC direction, which have some influence on many scientific applications and can affect the detection capabilities of Gaia.

These variations of the orientation and the distribution of the SSO orbit inclinations translate into a wide range of possible orientations of the velocity vector on the (AL, AC) plane. Even for a single object, a large variety of velocities and scan directions is covered over time.

2.4. Errors and correlations

The SSO apparent displacement at the epoch of each observation is clearly a major factor affecting the performance of Gaia, even within a single transit. Other general effects acting on single

\(^2\) As a rule, Gaia DR2 data start on 25 July 2014, but for SSOs and for technical reasons, no transits have been retained before August, 5.

\(^3\) Difference between the barycentric JD time in TCB and 2455197.5.
CCD observations exist, such as local CCD defects, local point spread function (PSF) deviations, cosmic rays, and background sources. For all these reasons, the exploitation of the single data points must rely on a careful analysis that takes both the geometric conditions of the observations and appropriate error models into account.

A direct consequence of the observation strategy employed by Gaia is the very peculiar error distribution for the single astrometric observation.

Because of the AC binning, most accurate astrometry in the astrometric field for most observations is only available in the AL direction. This is a natural consequence of the design principle of Gaia, which is based on converting an accurate measurement of time (the epoch when a source image crosses a reference line on the focal plane) into a position. In practical terms, the difference between AC and AL accuracy is so large that we can say that the astrometric information is essentially one-dimensional.

As illustrated in Fig. 6, the resulting uncertainty on the position can be represented by an ellipse that is extremely stretched in the AC direction. When this position is converted into another coordinate frame (such as the equatorial reference $\alpha, \delta$), a very strong correlation appears between the related uncertainties $\sigma_{\alpha}, \sigma_{\delta}$. Therefore it is of the utmost importance that the users take these correlations into account in their analysis. The values are provided in the ESA Archive and must be used to exploit the full accuracy of the Gaia astrometry and to avoid serious misuse of the Gaia data.

3. Outline of the data reduction process

The solar system pipeline (Fig. 7) collects all the data needed to process the identified transits (epoch of transit on each CCD, flux, AC window coordinates, and many auxiliary pieces of information).

A first module, labelled "Identification" in the scheme, computes the auxiliary data for each object, and assigns the identifying correct identification label to each object. Focal plane coordinates are then converted into sky coordinates by using the transformations provided by AGIS, the astrometric global iterative solution, and the corresponding calibrations (astrometric reduction module). This is the procedure described below in Sect. 3.1. We note that this approach adopts the same principle as absolute stellar astrometry (Lindegren et al. 2018): a local information equivalent to the usual small-field astrometry (i.e. position relative to nearby stars) is never used.

Many anomalous data are also rejected by the same module. The post-processing appends the calibrated photometry to the data of each observation (determined by an independent pipeline, see Sect. 4) and groups all the observations of a same target. Eventually, a "Validation" task rejects anomalous data.

The origin of the anomalies are multiple: for instance, data can be corrupted for technical reasons, or a mismatch with a nearby star on the sky plane can enter the input list. Identifying truly anomalous data from peculiarities of potential scientific interest is a delicate task. Most of this article is devoted to the results obtained on the general investigation of the overall data properties, and draws attention to the approaches needed to exploit the accuracy of Gaia and prepare a detailed scientific exploitation.

3.1. Astrometric processing

We now describe the main steps of the astrometric processing. A more comprehensive presentation is available in the Gaia DR2 documentation and Lindegren et al. (2016, 2018). The basic processing of the astrometric reduction for SSOs consists of three consecutive coordinate transformations.

The first step in the processing of the astrometry is the computation of the epoch of observations, which is the reconstructed timing of crossing of the central line of the exposure on the CCD. The first coordinate transformation is the conversion from the Window Reference System (WRS) to the Scanning Reference System (SRS). The former consist of pixel coordinates of the SSO inside the transmitted window along with time tagging from the On Board Mission Timeline (OBMT), the internal time scale of Gaia (Lindegren et al. 2016). The origin of the WRS
is the reference pixel of the transmitted window. The SRS coordinates are expressed as two angles in directions parallel and perpendicular to the scanning direction of Gaia, and the origin is a conventional and fixed point near the centre of the focal plane of Gaia.

The second conversion is from SRS to the centre-of-mass reference system (CoMRS), a non-rotating coordinate system with origin in the centre of mass of Gaia.

The CoMRS coordinates are then transformed into the barycentric reference system (BCRS), with the origin in the barycentre of the solar system. The latter conversion provides the instantaneous direction of the unit vector from Gaia to the asteroid at the epoch of the observation after removal of the annual light aberration (i.e., as if Gaia were stationary relatively to the solar system barycenter). These positions, expressed in right ascension ($\alpha$) and declination ($\delta$), are provided in DR2. They are similar to astrometric positions in classical ground-based astrometry.

A caveat applies to SSO positions concerning the relativistic bending of the light in the solar system gravity field. In Gaia DR2, this effect is over-corrected by assuming that the target is at infinite distance (i.e. a star). In the case of SSOs at finite distance, this assumption introduces a small discrepancy (always <2 mas) that must be corrected for to exploit the ultimate accuracy level.

3.2. Filtering and internal validation

An SSO transit initially includes at most nine positions, each corresponding to one AF CCD detection (see Sec. 2). However, in many cases, fewer than nine observations in a transit are available in the end. The actual success of the astrometric reduction depends on the quality of the recorded data: CCD observations of too low quality are quickly rejected; the same holds true if an observation occurs in the close vicinity of a star or within too short a time from a cosmic ray event, the software fails to produce a good position.

These problems represent only a small part of all the possible instances encountered in the astrometric processing, which has required an efficient filtering. Observations have been carefully analysed inside the pipeline to ensure that positions that probably do not come from an SSO are rejected, as well as positions that do not meet high quality standards. We applied the filtering both at the level of individual positions and at the level of complete transits. We list the main causes of rejection below.

- Problematic transit data. The positions were rejected when some transit data were too difficult to treat or if they gave rise to positions with uncertain precision.
The errors in AL and AC are coordinate system (AL, AC), and it is eventually converted into pixels in the pipeline down from the signal processing. Error sources are the error from the centroiding. It is propagated tically independent from one CCD to another. One of the main all positions of the same transit, while random errors are statist-ic independent. Since in addition to the uncorrelated random noise, there are some systematics, like the attitude error, that have a coherence time longer than the few seconds interval be-tween two successive CCDs. This induces complex correlations between the errors in the different CCDs from the same transit that are practically impossible to account for rigorously. Hence, we adopted a simplified approach separating the error into a sys-tematic and a random part. Systematic errors are the same for all positions of the same transit, while random errors are statist-ically independent from one CCD to another. One of the main error sources is the error from the centroiding. It is propagated in the pipeline down from the signal processing in pixels in the coordinate system (AL, AC), and it is eventually converted into right ascension and declination. The errors in AL and AC are usually uncorrelated, but the rotation from the system (AL,AC) to the system \((\alpha \cos \delta, \delta)\) makes them highly correlated.

Along-scan uncertainties are very small (of the order of 1 mas), and they show the extreme precision of Gaia. The error on the centroiding represents the main contribution to the random errors for SSOs fainter than magnitude 16. For SSOs fainter than magnitude 13, all pixels are binned in AC to a single win-dow, and the only information we have is that the object is inside the window. Therefore the position is given as the centre of the window, and the uncertainty is given as the dispersion of a rect-angular distribution over the window. The errors in AC are thus very large (of the order of 600 mas) and highly non-Gaussian. For SSOs brighter than magnitude 13, the uncertainty in AC is smaller. In these cases, a 2D centroid fitting is possible, but the error in AC is generally still more than three times larger than in AL direction, essentially because of the shape of the Gaia pixels. An important consequence is that uncertainties given in the \((\alpha \cos \delta, \delta)\) coordinate system may appear to be large as a result of the large uncertainties in AC, which contributes to the uncertainty in both right ascension and declination after the coordinate transformation.

Other errors also affect the total budget, such as the error from the satellite attitude and the modelling errors that are due to some corrections that are not yet fully calibrated or imple-mented. They contribute to both the random and the systematic error and are of the order of a few milliarcseconds.

4. Asteroid photometry in Gaia DR2

The Gaia Archive provides asteroid magnitudes in Gaia DR2 in the \(G\) band (measured in the AF white band), for 52% of the observations. This fraction is a result of a severe selection that is described below.

Asteroids, due to their orbital motion, move compared to stellar sources on the focal plane of Gaia. Hence, it is possible that they can drift out of the window during the observations of the AFs. This drift can be partial or total, resulting in potential loss of flux during the \(AF_1, \ldots, AF_x\) with \(x > 1\) observations. Asteroid photometry at this stage is processed with the same ap-proach as is used for stellar photometry (Carrasco et al. 2016; Riello et al. 2018) and no specific optimisation is currently in place to account for flux loss in moving sources. This situation is expected to improve significantly in the future Gaia releases.

The photometry of Gaia DR2 is provided at transit level; the brightness values (magnitude, flux, and flux error) repeat identi-cally for each entry of the Gaia archive that is associated with the same transit. The transit flux is derived from the average of the calibrated fluxes recorded in each CCD strip of the AF, weighted by the inverse variance computed using the single CCD flux uncertainties. This choice minimises effects that are related, for instance, to windows that are off-centred with respect to the central flux peak of the signal. However, when the de-centring becomes extreme during the transit of a moving object, or worse, when the signal core leaves the allocated window, significant bi-asess propagate to the value of the transit average and increase its associated error. This happens in particular for asteroids whose apparent motion with respect to stars is non-negligible over the transit duration. A main-belt asteroid with a typical motion of 5 mas/s drifts with respect to the computed window by several pixels during the \(\approx 40\)s of the transit in the Gaia FOV.

As provided by the photometric processing, a total of 234,123 transits of SSOs have an associated, fully calibrated magnitude (81% of the total). Fig. 8 shows the distribution of the relative error per transit \(\sigma_G\) of the whole dataset before filtering.
We found out that the sharp bi-modality in the distribution correlates positively with transits of fast moving objects. For this reason, we decided to discard all transits that fell in the secondary peak of large estimated errors $\sigma_{G} > 10\%$ as they almost certainly correspond to fluxes with a large random error and might be affected by some (unknown) bias.

A second rejection was implemented on the basis of a set of colour indices, estimated by using the red and blue photometer (RP and BP), the two low-resolution slitless spectrophotometers. Again due to asteroid motion, the wavelength calibration of RP/BP can be severely affected, and this in turn can affect the colour index that is used to calibrate the photometry in AF. In future processing cycles, when the accurate information on the position of asteroids, produced by the SSO processing system, will become available to the photometric processing, we expect to have a significant improvement in the calibration of the low-resolution spectra and photometric data for these objects. After checking the distribution of the observations of SSOs on a space defined by three colour indices (BP-RP, RP-G, and G-BP), we decided to discard the photometric data falling outside a reasonable range of colour indices, corresponding to the interval (0.0, 1.0) for both RB-G and G-RP.

The two criteria above, based on the computed uncertainty and on the colour, are not independent. Most transits that were rejected due to poor photometry in the $G$ band also showed colour problems, which proves that the two issues are related.

Both filtering procedures together result in the rejection of a rather large sample of 48% of the initial brightness measurements available. In the end, 52% of the the transits of SSOs in Gaia DR2 have an associated G-band photometry.

The resulting distribution of phase angles and reduced magnitudes ($G_{red}$, at 1 au distance from Gaia and the Sun) for the transits in Gaia DR2 is plotted in Fig. 12. In addition to the core of the distribution represented by MBAs, a small sample of NEAs reaching high phase angles is visible, as well as some transits associated with large TNOs at the smallest phase angles.

Despite the severe rejection of outliers, assessing the reliability of the published photometry at the expected accuracy of Gaia, specifically for solar system bodies, is not straightforward. The intrinsic variability of the asteroids due to their changing viewing and illumination geometry and to their complex shapes makes the comparison of observed fluxes with theoretical ones very challenging. Sunlight scattering effects from the asteroid surfaces also play a role and must be modelled to reproduce the observed brightness.

We attempted to model the observed brightness following two different approaches, on a small sample of asteroids. First, we used a genetic inversion algorithm derived from a full inversion algorithm developed by Cellino et al. (2009) and massively tested by Santana-Ros et al. (2015) to derive for a few selected objects the best–fitting three–axial ellipsoid (axis ratios) from Gaia observations alone. The procedure assumes known values of the spin period and spin-axis direction (“asteroid pole”) available in the literature for objects that have been extensively observed from the ground, and takes into account a linear phase-
magnitude dependence. The procedure is extensively explained in the Gaia DR2 documentation.

Independently, we exploited the detailed shape models available for the two asteroids (21) Lutetia and (2867) Šteins derived by combining ground-based data with those obtained during the ESA Rosetta flybys to reproduce their observed Gaia brightness. Both attempts, of course, concern modelling the flux variations relative to a given observation in the sample, not its absolute value.

The results from the sparse photometry inversion are presented in Fig. 13-15. They are obtained by assuming a Lommel-Seeliger scattering law, a realistic choice when a more detailed mapping of the scattering properties across the surface is not available (Muinonen & Lumme 2015; Muinonen et al. 2015).

Despite the very simplified shape model, the residuals (observations minus computed) O-C are always within ±0.05 magnitudes, and the typical scatter can be estimated around 2-3%. Using the shape models of (21) Lutetia (Carr et al. 2010) and (2867) Šteins (Jorda et al. 2012), we tried to assess the photometric accuracy limit of Gaia on asteroids. In the case of (21) Lutetia, it was found that Gaia data are in very good agreement with expectations based upon the best available shape model of this asteroid, derived from disk-resolved imaging by Rosetta (which only imaged one hemisphere of the object) and a lower-resolution model based on disk-integrated, ground-based photometry. The high-resolution shape model reproduces the Gaia photometry with a small RMS value of 0.025 mag, corresponding to 2.3% RMS in flux. This strongly suggests that Gaia photometry is probably better than 2% RMS, within the limitations imposed by the shape model accuracy and the assumptions on the scattering model. Moreover, Gaia data seem to offer an opportunity to improve the currently accepted shape solution for Lutetia, which is based partly upon ground-based data.

The results obtained for (2867) Šteins, for which a high-resolution shape model is also available, strongly support the conclusion that the photometry is indeed very accurate. For (2867) Šteins two pole solutions exist, essentially differing only by the value of the origin of the rotational phase. By directly using the shape model to reproduce Gaia data, resampled at 5 degree resolution, with a Lommel-Seeliger scattering corresponding to E-type asteroid phase functions, the RMS value of the O-C is 1.64% and 1.51% for the two pole solutions, a very good result. Changing the resolution to 3 degrees does not improve the fit further. The remaining limitations in the case of (2867) Šteins are still related to details of the shape, and to the assumptions made (and/or scattering properties) when it was derived from Rosetta images.

In conclusion, our validation appears to show that Gaia epoch photometry, appropriately filtered to eliminate the outliers, probably has an accuracy below 1-2% up to the magnitude of (2867) Šteins, in the range G 17-19. However, given the current limitations on the calibration and processing, we cannot exclude that the sample published in Gaia DR2 still contains a non-negligible fraction of anomalous data. For this reason, we recommend detailed analysis and careful checks for any applications based on Gaia DR2 photometry of asteroids.

5. Validation of the astrometry

The processing of the solar system data described above has eventually produced a list with 14 124 objects (all numbered SSOs), 290 704 transits, and 2 005 683 CCD observations. The sky distribution is shown in Fig. 16 in a density plot in equatorial coordinates. As expected, most SSOs are found in a limited range of ecliptic latitudes. The distribution in longitude is not uniform because over a relatively short duration of 22 months, the Gaia scanning returned to the same regions of the sky, only in a limited number of areas.

Assessing the quality of the astrometry is challenging, and it needs an ad hoc treatment. Various filters have been applied during the activity of the astrometric reduction processing. The filtering process ensures the rejection of a maximum number of bad detections, while keeping the number of good positions that are rejected as small as possible (for more details, see the Gaia DR2 documentation). To prove that Gaia is already close to the performances expected at the end of the mission, we designed an ad hoc procedure for the external validation of the results. To this end, we fitted an orbit (initialising the fit with the best existing orbit) using only the available 22 months of Gaia observations, and we examined the residuals in right ascension and declination, and also in AL and AC (see Sec. 5.1). The main differences between Gaia and ground-based observations (or any other satellite observations) can be summarised as follows:
Fig. 13. Observed and computed magnitude from the best fit of Gaia observations of an ellipsoidal model for the asteroid (39) Laetitia. In the right panel, we show the corresponding residuals. The origin of the time axis is J2010.0.

Fig. 14. As in Fig. 13 for the asteroid (283) Emma.

– Gaia observations are given in TCB, which is the primary timescale for Gaia.
– Positions (right ascension and declination) are given in the BCRS as the direction of the unit vector from the centre of mass of Gaia to the SSOs.
– The observation accuracies are up to the order of few $\sim 10^{-9}$ radians (sub-mas level) in the AL direction.
– The error model contains the correlations in $\alpha \cos \delta$ and $\delta$ because of the rotation from the (AL, AC) plane to the ($\alpha \cos \delta$, $\delta$) plane (Sec. 3.3).

5.1. Orbit determination process

The orbit determination process usually consists of a set of mathematical methods for computing the orbit of objects such as planets or spacecraft, starting from their observations. For our validation purpose, we considered only the list of numbered asteroids for which the orbits were already well-known from ground-based (optical or radar) /satellite observations. We used the least-squares method and the differential correction algorithm (see Milani & Gronchi 2010) to fit orbits on 22 months of Gaia observations, using as initial guess the known orbits of these objects. To be consistent with the high quality of the data, we employed a high-precision dynamical model, which includes the Newtonian pull of the Sun, eight planets, the Moon, and Pluto based on JPL DE431 Planetary ephemerides$^4$. We also added the contribution of 16 massive main-belt asteroids (see A). We used a relativistic force model including the contribution of the Sun, the planets, and the Moon, namely the Einstein-Infeld-Hoffman approximation (Moyer 2003) or (Will 1993). As a result of the orbit determination process, we obtained for every object a corrected orbit fitted on Gaia data only together with the post-fit residuals.

The core of the least-squares procedure is to minimise the target function (Milani & Gronchi 2010),

$$Q = \frac{1}{m} \chi^T W \chi,$$

where $m$ is the number of observations, $\chi$ are the residuals (observed positions minus computed positions), and $W$ is the weight matrix. The solution is given by the normal equations,

$$C = B^T W B; \quad D = -B^T W \chi; \quad \left( B = \frac{\delta \chi}{\delta x} \right).$$

$^4$ We also performed the orbit determination process using INPOP13c (Fienga et al. 2014) ephemerides and did not find significant differences in the results.
\[ \Delta x = C^{-1} D. \]

It is clear from Eqs. 1 and 2 that the weight matrix plays a fundamental role in the orbit determination. It is usually the inverse of a diagonal matrix \( \Gamma \) that contains on the diagonal the square of the uncertainties in right ascension and declination for each observation, according to the existing debiasing and error models (as in Farnocchia et al. (2015)). Each Gaia observation comes with its uncertainties on both coordinates and the correlation, which are key quantities in the orbit determination process.

\[ \Gamma = \begin{pmatrix} \sigma_{\alpha_1}^2 & \text{cov}(\alpha_1, \delta_1) & 0 & \cdots & 0 \\ \text{cov}(\alpha_1, \delta_1) & \sigma_{\delta_1}^2 & 0 & \cdots & 0 \\ \vdots & \vdots & \ddots & \ddots & \vdots \\ 0 & 0 & \cdots & \sigma_{\alpha_m}^2 \text{cov}(\alpha_m, \delta_m) & 0 \\ 0 & 0 & \cdots & \text{cov}(\alpha_m, \delta_m) & \sigma_{\delta_m}^2 \end{pmatrix}. \]

The uncertainties used to build the \( W \) matrix are given by the random component of the error model, but we also take into account the systematic contribution when this is needed, as explained in the following section.

5.2. Outlier rejection procedure

The rejection of the outliers is a fundamental step in the orbit determination procedure. Since we assumed that the residuals are distributed as normal variables, the rejection was based on the post-fit \( \chi^2 \) value for each observation, computed as in Carpino et al. (2003):

\[ \chi^2_i = \xi_i^T \xi_i, i = 1, \ldots, m, \]

where \( m \) is the total number of observations, \( \xi_i \) is the vector of the residuals for each observation, and \( \chi^2_i \) is the expected covariance of the residuals. Each \( \chi^2_i \) has a distribution of a \( \chi^2 \) variable with two degrees of freedom. We call outlier each observation whose \( \chi^2 \) value is greater than 25. The choice of 25 as a threshold was driven by the fact that we wished to keep as many good observations as possible and wished to discard only the observations (or the transits) that are very far from the expected Gaia performances. During this procedure, we took random and systematic errors into account.

Firstly, we rejected all the observations whose \( \chi^2 \) value was greater than 25. Then, when the systematic part was larger than the random part, we performed a second step in the outlier rejection, described as follows:

- We computed the mean of the residuals for each transit.
- We checked if the value of the mean is lower than the systematic error for the transit.
- If the value was higher than the systematic error, we discarded the entire transit.
If the value was lower than the systematic error, we computed for each observation the difference between the residual and the mean value.

We checked whether the difference was smaller than the random error. When that was the case, we kept the observation, otherwise we discarded it.

This approach is consistent with the uncertainties produced for Gaia DR2. Its underlying hypothesis is that the error correlations over a single transit can be completely represented by just one quantity, which is the value of the systematic component alone. Although this is an approximation, we currently do not have the impression that a more complex correlation model is required.

5.3. Results

We fitted the orbits of the 14,124 asteroids contained in the validation sample using an updated version of the OrbFit software, developed to handle Gaia observations and Gaia error model (Sections 5.1 and 5.2).

We were unable to fit the observations to the existing orbit for only three asteroids because the time span covered by the available transits was too short. They were removed from the final output of Gaia DR2. We also removed 22 bright objects (transits with G < 10) whose residuals were substantially larger than the uncertainties we expected, and we considered these solutions as not reliable.

Figure 17 shows the distribution in semi-major axis and eccentricity of the 14,099 SSOs published in Gaia DR2. We can distinguish the NEA population (q < 1.3) from the MBAs (including Jupiter trojans in this class) and the TNOs (q > 28).

The total number of fitted observations is 2,005,683, which corresponds to 290,704 transits. During the outlier rejection procedure (Sec. 5.2), we discarded 27,981 observations (~1% of the total). Figure 18 shows all the residuals in the (AL, AC) plane in milliarcseconds. Outliers are the red points, while accepted observations are all contained in the blue thick line in the centre of the figure.

After the filtering and the outlier rejection, Gaia DR2 contains 1,977,702 observations, corresponding to 14,099 SSOs and 287,904 transits. Figure 19 represents a density plot of the residuals at CCD level in the (AL, AC) plane, for all the observations published in Gaia DR2. This plot, together with the plots of the residuals (Figures 20 and 21), shows the epoch-making change brought about by Gaia astrometry: 96% of the AL residuals fall in the interval [-5, 5] mas and 52% are at sub-milliarcsecond level. The behaviour of the residuals in AC is markedly different as a result of the geometry of the spacecraft observations. The AC residuals as a rule are much larger than AL, for the reasons detailed in Sec. 3.3. Figures 20 and 21 highlight the performances of Gaia even better. They show the residuals in AL and AC with respect to the G magnitude of the asteroids at the epoch of observation. The right panels of both Fig. 20 and Fig. 21 display the histogram of the residuals in AL and AC, respectively. The clear peak around 0 is well visible in the histogram of the residuals in AC (Fig. 20), and it corresponds to the core of the density plot in Fig. 19.

Even the histogram of the residuals in AC (Fig. 21) shows a peak around 0, which is strictly related to the distribution of the residuals as a function of the G magnitude. For objects brighter than G = 13, the full 2D window is transmitted (see Sec. 2), thus the accuracies in AC and AL are similar (although still slightly larger in the across direction because of the pixel size), while for objects fainter than G = 13, the errors in AC are much larger.

6. Interpretation of asteroid residuals

The residuals in AL, as in Figures 19 and 20, show the quality and extreme precision of Gaia observations. We now examine the residuals in more detail, using first as an example a mainbelt asteroid, and then showing the properties at transit-level.
Fig. 19. Zoom-in of the density plot of the residuals in the (AL, AC) plane expressed in milliarcsecond for all the observations published in Gaia DR2. 96% of the AL residuals fall in the interval [-5, 5], and 52% are at sub-milliarcsecond level. Almost all the residuals in AC (98%) fall in the interval [-800, 800]..

6.1. CCD-level residuals

We chose (367) Amicitia as a test case to analyse the residuals in right ascension and declination and to explain their relationship (and main differences) with the residuals in AL and AC. Residuals in right ascension and declination are important because they are the direct output of the fit and are probably more easily understood than the residuals in AL and AC, which are closely related to the Gaia scanning mode. The residuals in right ascension and declination are by-products of the orbit correction and computed as the differences between the observed and computed positions. Afterwards, given the position angle shown in Fig. 6, we can rotate the residual vector in $\alpha \cos \delta$ and $\delta$ to compute the residuals in AL and AC (3),

$$\frac{\Delta AL}{\Delta AC} = \begin{bmatrix} \sin(PA) & \cos(PA) \\ -\cos(PA) & \sin(PA) \end{bmatrix} \begin{bmatrix} \Delta \alpha \cos \delta \\ \Delta \delta \end{bmatrix}.$$  

For the sake of simplicity, we call $(\Delta \alpha \cos \delta, \Delta \delta)$ the vector of the residuals in $\alpha \cos \delta$ and $\delta$ and $(\Delta AL, \Delta AC)$ the vector of the residuals in AL and AC.

Asteroid (367) Amicitia is a typical object among SSOs observed by Gaia: its average G magnitude is 14, which means that it is not one of the brightest objects for which we have the 2D window. It has 22 Gaia transits, which corresponds to 132 CCD observations. Figure 22 shows all the residuals in right ascension and declination. Each transit is represented by a different symbol.

Figure 23 shows the residuals rotated in the (AL, AC) plane. They are clearly very small in AL and considerably larger in AC (as expected for an asteroid of that magnitude with almost no across-scan data). The majority of the residuals in AL are at sub-milliarcsecond level (Fig. 23, right panel), which means that almost all are inside 1σ (dashed vertical lines).

We have already mentioned the particular features of the residuals in the (AL, AC) plane (Sec. 3.3 and Sec. 5.3). We now focus on the residuals in $(\alpha \cos \delta, \delta)$. They are a linear combination of the residuals in AL and AC as in Eq. 3. Thus they are in general larger in both coordinates (Fig. 22) and highly correlated. Even if the residuals in the (AL, AC) plane are uncorrelated, the large difference in their standard deviations gives rise to a very strong correlation between the residuals expressed as $(\Delta \alpha \cos \delta, \Delta \delta)$. This strong correlation between $\Delta \alpha \cos \delta$ and $\Delta \delta$ is expressed visually by the fact that the residuals for each transit lie roughly on a straight line.

The error ellipses associated with each observation, and thus with each residual, are shown in Fig. 24. They are very elongated as a result of the large errors in AC, and they are not parallel to the axes because of the orientation of the Gaia scanning law, which changes from one transit to the next.

To explain the distance of each point from the centre (0, 0) of the residuals for each transit, we illustrate the detailed properties of a single transit (Fig. 25). To this end, we consider a single transit. We chose one of the transits for which none of the nine CCD observations (AF1-AF9) was rejected during the processing (Fig. 25). In this case, the asteroid motion was not fast enough to move it outside the window during the transit.

The main striking feature is the alignment of the residuals. The direction of maximum spread corresponds to the motion across scan, as oriented during the transit. The AC motion of the SSOs is due both to the slow precession of the spin axis of Gaia as imposed by the NSL and to the proper motion of the asteroid.

Another important feature is the order of the AF CCDs, provided by their numbering, in the sequence of residuals. While on average the drift proceeds in the figure from AF1 at the bottom right towards AF9 at top left, the sequence is sometimes inverted in direction. This is an effect of the quantisation of the window position AC at integer steps of one full sample size.

The compact clustering of the residuals shows that the in the AL direction, the determination of the position during the transit has a very low spread, as expected thanks to the much higher accuracy.

The last point we need to analyse is the trend of the residuals in the negative side of the Cartesian plane. The black vectors in Fig. 26 are the projections of the AC velocity in the plane described by $\alpha \cos \delta$ and $\delta$. The residuals follow the direction of the velocity vectors, which explain the main dispersion of the detections in each CCD across scan.

6.2. Transit-level residuals

The observations collected during a single transit extend over a limited period of time during which the motion of the SSOs can be taken as linear, and over this interval its position changes by less than 1 arcsec. Likewise, the scan direction is approximately constant at first order. The same applies in general to the SSO orientation in space (rotational phase, direction of the pole) and as a consequence of its brightness.

In addition, successive transits are well separated in time, with a minimum interval of 106 minutes (preceding the following FOV) to 6 hours (one rotation) or much more (days, months) before the Gaia pointing returns to the same SSO. Since a single transit can be considered as a coherent unit that is well separated from the others, different transits are clearly statistically independent measurements. This is also supported by the time resolution of the attitude solution, with nodes spaced by 5 s in AL but with a much longer coherence time. On the other hand, one can expect that during a transit the attitude from one CCD to
the next is significantly correlated, while it is not correlated over
longer timescales.

Some systematics that can be related to the asteroid itself
(such as motion, apparent size, and photocentre position relative
to centre of mass) are also expected to be correlated during a
transit, but they are completely different in general when differ-
ent transits are compared.

For these reasons, it makes sense to group single observa-
tions within a transit and analyse the residuals at transit level. We
consider first the average of the residual values during a transit
and their scatter separately.

The average is an analogue of accuracy, as it is expected to
provide the overall discrepancy of the SSO position with respect
to the fitted orbital solution around the transit epoch. The result
of the transit-level average of residuals is shown in Fig. 27. The
large residuals associated with the AC direction are due to the AF
lack of resolution, with the exception of bright (G<13) targets.
The plot in AL is much more impressive, as it catches the full
accuracy of Gaia DR2 data for SSOs, with an average well below
1 mas for all sources G<19.5. The best performance appears to
be around G~17.

The scatter of the residuals during a transit (Fig. 28) can be
considered as an indication of the transit-level astrometric pre-
cision. We compute this precision as a standard deviation. Of
course, given the small number of data points (at most nine per
transit), this is a rather poor statistical estimator of the true stan-
dard deviation of the population. We show here the results ob-
tained with transits that had four or more observations, but even
without this cut, the general picture holds true.

The AL scatter component has a remarkable minimum at
G<16, around 400 μas. A transition at G<13 is a clear signa-
Fig. 22. Residuals in $\alpha \cos \delta$ and $\delta$ for the MBA (367) Amicitia. Different symbols correspond to the 22 different transits of the object.

Fig. 23. Residuals in AL and AC for the MBA (367) Amicitia. The residuals are obtained as a rotation from the plane of the residuals ($\alpha \cos \delta$, $\delta$) to the plane of the residuals in (AL, AC). The right panel is a zoom-in of the residuals and shows that almost all the residuals are at sub-milliarcsecond level and inside 1$\sigma$ (dashed lines).

Fig. 24. Residuals in $\alpha \cos \delta$ and $\delta$ for the MBA (367) Amicitia. Different symbols correspond to different transits of the object. The lines represent the error ellipse for each observation, including the correlations, as given by the error model.

Fig. 25. Residuals in $\alpha \cos \delta$ and $\delta$ of one transit of the MBA (367) Amicitia. Each astrometric field (AF) is highlighted.

As the core of the distribution is very dense in the plots, we collected in a set of histograms (Fig. 29) the distribution of the scatter for four ranges of $G$ to better illustrate the difference in performance.

A common feature of both systematic and random residuals is the lack of improvement for SSOs brighter than $G$~16. The systematic component clearly shows a degradation. This can be due to several overlapping effects:

- The apparent size of the asteroid increases with brightness. Although in general it remains below the pixel size, it can introduce a bias in the centroid position, as no special treatment is applied in Gaia DR2 to extended SSOs.
- The difference between the centre of mass and the photocentre can introduce a further systematic effect.
- The various thresholds of gating of the CCD to avoid saturation and the associated photon loss at $G$<13 also tend to suppress a gain in accuracy.

The scatter reaches $\sim$5 mas at $G$=20.
Fig. 26. Residuals in the \((\alpha \cos \delta, \delta)\) plane and projection of the AC velocity (black lines) on the same plane for the MBA (367) Amicitia.

Fig. 27. Systematic component of transit-level residuals estimated as the absolute value of the average of post-fit residuals associated with a single position during each transit as a function of \(G\) magnitude. Transit-level residuals in AC and AL are shown in the top and bottom panel, respectively. The black line represents the average value. The transition in the AC direction at \(G \sim 13\) is due to the change of window dimension. The colour scale represents the local density of data points.

Fig. 28. Random component of transit-level residuals estimated as the standard deviation of the post-fit residuals associated with a single position, during each transit (top panel: AC; bottom panel: AL) as a function of \(G\) magnitude. Only transits with more than four positions are considered. The black line represents the average value. The colour scale represents the local density of data points.

Fig. 29. Scattering of the transit-level residuals in Fig. 28 for four magnitude ranges.

To these factors, one must also add the signal smearing that is due to the apparent motion of SSOs relative to the stars. While it does not depend on brightness, it can add a noise floor to the whole distribution of residuals.

Fig. 30 summarises the two residual components and compares them to the average apparent size of the observed asteroids. This is computed by assuming a spherical shape and by taking into account the distance of the SSO from \(Gaia\) at the mean epoch of the FOV transit. The physical radius used is provided by the Wide-field Infrared Survey Explorer (WISE) telescope (Mainzer et al. 2016). In \(Gaia\) DR2, 11,984 SSOs have a WISE
size determination. As size here is just for statistical comparison, errors and biases on the WISE sizes are of no consequence.

The trend of the size shows that its median value is higher than any residual for objects brighter than $G \sim 19$ and reaches the AL pixel size of (60 mas) at $G \sim 13$. As the centroiding algorithm used in Gaia DR2 is only optimised for the stars (point sources), some degradations from the image extension can show up, which is a likely cause of the increase in the systematic residuals. More detailed investigations are required and will provide indications to further improve the astrometric quality in the next releases.

**Fig. 30.** Average and one-sigma range for the residuals in Fig. 28 (red) and 27 (blue). The black line is the average apparent size of the SSOs.

The effect of motion can be roughly assimilated to an increased size, as a signal elongation occurs in the direction of displacement. If the hypothesis above on the role of size is valid, a signature should also be found as a dependency of residuals from motion. However, the situation is also more complex, as a displacement of the image with respect to the window centre is expected, with an asymmetric loss of signal from the PSF tails. For fast SSOs, the displacement can move the signal outside the CCD window, and in this situation, the number of valid observations per transit decreases. Fig. 31 shows the distribution of the number of single CCD measurements per transit and illustrates the reduction of the number of valid observations due to displacement of the signal out of the allocated windows.

We found no clear evidence of a difference between centre-of-mass and photocentre. Although the phase angle of Gaia observations is rather high, the typical photocentre shift can reach at most a few percent of the SSO diameter, but its direction can have any orientation with respect to the AL position angle. When we select asteroids with similar astrometric accuracy (i.e. similar $G$ within a one-magnitude interval, for instance), no clear trend of the average residuals with respect to phase angle is found. The effect can be considered of second order with respect to the other uncertainty sources illustrated above.

**7. Analysis of the orbits**

**7.1. Comparisons with existing orbital data sets.**

The orbit fitting discloses interesting properties of Gaia asteroid observations. Figure 32 shows the results of the current situation (22 months of Gaia) obtained as output of the orbit determination process and what we may expect at the end of the nominal mission (5 years), or of a possible extension (10 years), based on our simulations using the same error model.

**Fig. 31.** Distribution of the number of single CCD positions.

**Fig. 32.** Quality of the orbit determination measured by the post-fit uncertainty of the semi-major axis for the whole sample of objects contained in Gaia DR2 after the nominal 5 years (red points) and 10 years (blue points) of mission. Black points represent the current situation (initial orbits taken from AstDyS). The orange points are the post-fit uncertainties using only 22 months of Gaia observations available for the Gaia DR2.

The data represent the uncertainty in the semi-major axis ($a$) (a good and easy to determine indicator of the orbit quality) as a function of the semi-major axis $a$ (in au). Red and blue points are the results of the simulation after the nominal 5- or 10-year mission. Black points are the current uncertainty from the AstDyS website. The orange points represent the accuracy of the orbits resulting from the processing of the 22-month Gaia DR2 data.

The simulations show an improvement of almost a factor 10 in the orbit determination after 5 years of mission, except for Jupiter trojans, which indeed have a period of 11 years. Thus after 10 years of mission, the improvement is clearly visible not
only for main-belt asteroids (a factor 20), but also for the trojans. On the other hand, the Gaia DR2 short time-span of 22 months (compared to tens/hundreds years for AstDys, and 5 or 10 years for Gaia itself) represents a limitation on the expected quality of the orbits. However, some asteroids observed by Gaia already reach a quality equivalent to ground-based data (and in 350 cases, it is even better).

Figure 33 shows the uncertainty on the semi-major axis obtained as a result of the orbit determination process using only Gaia observations, with respect to the current uncertainty from the orbits available on the AstDys website as function of the perihelion distance (q). The different clouds of points represent different classes of objects in the solar system population: NEAs (dark blue), MBAs (different shades of light blue), Hildas, and trojans (orange and red). The black line is the bisector of the first quadrant: the orbits of the objects below the line have a better estimate using only Gaia observations. Among these objects are also five NEAs, namely (3554) Amun, (4957) BruceMurray, (10563) Izhdabar, (12538) 1998 OH, and (161989) Cacus.

7.2. Perspectives: detection of non-gravitational perturbations.

The unprecedented quality of Gaia SSO observations, demonstrated above, opens new perspectives for study. These include the computation of subtle non-gravitational effects.

The most important of these is the so-called Yarkovsky effect, a small recoil force that is due to the emission of photons in the thermal infrared from the surface of SSOs. The consequence of this emission is a drift in the semi-major axis of asteroids, which changes their orbits in the long term (Vokrouhlický et al. 2000).

The Yarkovsky effect depends on numerous physical quantities, such as the density and the thermal inertia of the asteroids. Usually, they are unknown and estimated on the base of reasonable guesses. When very accurate astrometry is available, the Yarkovsky drift can be measured directly, but this remains a challenge today. While the Yarkovsky effect has previously been measured for about 90 NEAs (Farnocchia et al. 2013; Del Vigna et al. 2018), it has never been measured for MBAs because their distances are larger and their temperatures and surface properties are different. Moreover, NEA are smaller objects (the Yaskovsky intensity decreases with size), which are close enough to enable precise astrometry by radar ranging techniques.

Gaia is the key to change the current situation. At present, Gaia DR2 SSO observations are affected by a limitation through their short time span, 22 months, which in most cases does not even cover the whole orbit of an object. Therefore they cannot be used alone to detect small perturbations such as the Yarkovsky effect, but need to be combined with available ground-based observations.

The joint use of Gaia and ground-based astrometry is possible, but because the accuracies are very different (a few milliarcseconds for Gaia astrometry versus a few hundred milliarcseconds for most ground-based observations), adequate techniques are required to reduce the signature of zonal errors on SSO astrometry due to pre-Gaia stellar catalogues. An improved error model is required as well. These complex tasks are beyond the purpose of this article.

In some exceptional situations, however, ground-based data are so good that the joint use of Gaia DR2 astrometry becomes possible even without additional optimisations. We therefore selected an NEA for which the Yarkovsky effect has previously been measured in Del Vigna et al. (2018), namely (2062) Aten, and directly combined 69 Gaia astrometric observations to the 959 pre-existing ground-based optical measurements and 7 measurements by radar, from 1955 to 2017.

Table 1. Asteroid name and number, value of the $A_2$ with its uncertainty, S/N (obtained as $A_2/\sigma_{A_2}$), value of $da/dt$ with its uncertainties, and the corresponding references for this result.

<table>
<thead>
<tr>
<th>Asteroid Name and Number</th>
<th>$A_2 \times 10^{15} \text{au/d}^2$</th>
<th>S/N</th>
<th>$da/dt \times 10^{-13} \text{au/Myr}$</th>
<th>Reference</th>
</tr>
</thead>
<tbody>
<tr>
<td>(2062) Aten</td>
<td>$-1.03 \pm 0.07$</td>
<td>14.03</td>
<td>$-3.90 \pm 0.34$</td>
<td>This article</td>
</tr>
<tr>
<td>(2062) Aten</td>
<td>$-1.18 \pm 0.53$</td>
<td>8.64</td>
<td>$-3.59 \pm 0.83$</td>
<td>Del Vigna et al. (2018)</td>
</tr>
</tbody>
</table>

The Yarkovsky effect can be modelled as a transverse acceleration depending on one parameter, the so-called $A_2$, which can be determined in an orbital fit together with the six orbital elements (Vokrouhlický et al. 2000) and then converted into $da/dt$ (the variation of the semi-major axis due to the non-gravitational force). Using this approach, we then compared our results with the previously published result. Table 1 shows that the use of Gaia DR2 observations not only changes the value significantly, but also improves the signal-to-noise ratio (S/N) of the detection and its uncertainty.

We wish to stress that even though it is meaningful, this is only a preliminary result that can certainly be improved further by reducing biases (zonal errors) and introducing a better error model for the non-Gaia observations. The systematic exploitation of Gaia astrometry in this domain appears to be very promising.

8. Conclusions

Gaia DR2 contains SSO astrometry with an accuracy better than 2-5 mas for the faintest asteroids (around G~20.5) and reaches sub-milliarcisecond level for objects with G<17.5, as estimated from post-fit residuals. This accuracy is essentially 1D in the direction of the Gaia scan, but an appropriate orbital fitting procedure shows that the strong footprint of the orientation vanished when several transits, and therefore different scan direc-
tions were combined. This situation is similar to the one encountered for the astrometric solution of stars whose parameters are optimally constrained when data obtained during several scans in different directions are combined to obtain precise 2D locations. For SSOs, the location is subject to great changes at each epoch, but despite the one-dimensionality of the Gaia astrometric data, a unique orbital solution can be efficiently adjusted to the trajectory on the sky, and it provides residuals close to the expectations.

We find that the apparent size of the asteroids can indeed play a role in the deterioration of the astrometric accuracy for the brightest targets. The apparent size for bright SSOs (G < 16) increases well beyond the accuracy of the measurements, and it even appears to mask the effect of velocity to some extent. Although more careful investigations are required, second-order effect such as the displacement of the photo-centre with respect to the centre of mass as a function of the phase angle does not seem to be detectable in the bulk distribution of residuals. This does not necessarily imply that their signature is entirely absent, as the orbital fit could partially absorb and compensate it.

The SSO data in Gaia DR2 clearly have some limitations that will be corrected in the future releases. These include corrections to the astrometry as a function of the object motion, size and shape, and better instrumental calibration. The bright end is also expected to be much improved. Despite these limitations, the Gaia absolute astrometry of SSOs is clearly the best ever obtained at optical wavelengths. Only well-observed stellar occultations can compete, but with the important limitation that they provide only the relative positions of an SSO and the occulted star.

Acknowledgements

This work presents results from the European Space Agency (ESA) space mission Gaia. Gaia data are being processed by the Gaia Data Processing and Analysis Consortium (DPAC). Funding for the DPAC is provided by national institutions, in particular the institutions participating in the Gaia MultiLateral Agreement (MLA). The Gaia mission website is https://www.cosmos.esa.int/gaia. The Gaia archive website is https://archives.esac.esa.int/gaia.

The Gaia mission and data processing have financially been supported by, in alphabetical order by country:

- the Algerian Centre de Recherche en Astronomie, Astrophysique et Géophysique of Bouzareah Observatory;
- the Austrian Fonds zur Förderung der wissenschaftlichen Forschung (FWF) Hertha Firnberg Programme through grants T359, P20046, and P23737;
- the BELgian federal Science Policy Office (BELSPO) through various PROgramme de Développement d’Expériences scientifiques (PRODEX) grants and the Polish Academy of Sciences - Fonds Wetenschappelijk Onderzoek through grant VS.091.16N;
- the Brazil-France exchange programmes Fundação de Amparo à Pesquisa do Estado de São Paulo (FAPESP) and Coordenação de Aperfeiçoamento de Pessoal de Nível Superior (CAPES) - Comité Français d’Evaluation de la Coopération Universitaire et Scientifique avec le Brésil (COFECUB);
- the Chilean Dirección de Gestión de la Investigación (DGI) at the University of Antofagasta and the Comité Mixto ESO-Chile;
- the National Science Foundation of China (NSFC) through grants 11573054 and 11703065;
- the Czech-Republic Ministry of Education, Youth, and Sports through grant LG 15010, the Czech Space Office through ESA PECS contract 98058, and Charles University Prague through grant PRIMUS/SCI/17;
- the Danish Ministry of Science;
- the Estonian Ministry of Education and Research through grant IUT40-1;
- the European Commission’s Sixth Framework Programme through the European Leadership in Space Astrometry (ELSA) Marie Curie Research Training Network (MRTN-CT-2006-033481), through Marie Curie project PIOF-GA-2009-255267 (Space AsteroSeismology & RR Lyrae stars, SAS-RRL), and through a Marie Curie Transfer-of-Knowledge (ToK) fellowship (MTKD-CT-2004-014188); the European Commission’s Seventh Framework Programme through grant FP7-606740 (FP7-SPACE-2013-1) for the Gaia European Network for Improved data User Services (GENIUS) and through grant 264895 for the Gaia Research for European Astronomy Training (GREAT-ITN) network;
- the European Research Council (ERC) through grants 320360 and 647208 and through the European Union’s Horizon 2020 research and innovation programme through grants 670519 (Mixing and Angular Momentum transport of massive stars – MAMSIE) and 687378 (Small Bodies: Near and Far);
- the European Science Foundation (ESF), in the framework of the Gaia Research for European Astronomy Training Research Network Programme (GREAT-ESF);
- the European Space Agency (ESA) in the framework of the Gaia project, through the Plan for European Co-operating States (PECS) programme through grants for Slovenia, through contracts C98090 and 400106398/12/NL/KML for Hungary, and through contract 4000115263/15/NL/IB for Germany;
- the European Union (EU) through a European Regional Development Fund (ERDF) for Galicia, Spain;
- the Academy of Finland and the Magnus Ehrnrooth Foundation;
- the French Centre National de la Recherche Scientifique (CNRS) through action ‘Défi MASTODONS’, the Centre National d’Études Spatiales (CNES), the L’Agence Nationale de la Recherche (ANR) ‘Investissements d’avenir’ Initiatives d’Excellence (IDEX) programme Paris Sciences et Lettres (PSL+) through grant ANR-10-IDEX-0001-02, the ANR ‘Défi de tous les savoirs’ (DS10) programme through grant ANR-15-CE31-0007 for project ‘Modelling the Milky Way in the Gaia era’ (MOD4Gaia), the Région Aquitaine, the Université de Bordeaux, and the Utinam Institute of the Université de Franche-Comté, supported by the Région de Franche-Comté and the Institut des Sciences de l’Univers (INSU);
the German Aerospace Agency (Deutsches Zentrum für Luft- und Raumfahrt e.V., DLR) through grants 50QQG0501, 50QQG0601, 50QQG0602, 50QQG0701, 50QQG0901, 50QQG1001, 50QQG1101, 50QQG1401, 50QQG1402, 50QQG1403, and 50QQG1404 and the Centre for Information Services and High Performance Computing (ZIH) at the Technische Universität (TU) Dresden for generous allocations of computer time;

the Hungarian Academy of Sciences through the Lendület Programme LP2014-17 and the János Bolyai Research Scholarship (L. Molnár and E. Plachy) and the Hungarian National Research, Development, and Innovation Office through grants NKFIH K-115709, PD-116175, and PD-121203;

the Science Foundation Ireland (SFI) through a Royal Society - SFI University Research Fellowship (M. Fraser);

the Israel Science Foundation (ISF) through grant 848–16;

the Agenzia Spaziale Italiana (ASI) through contracts I/037/08/0, I/058/10/0, 2014-025-R-0, and 2014-025-R.1.2015 to the Italian Istituto Nazionale di Astrofisica (INAF), contract 2014-049-R.0/1 to INAF dedicated to the Space Data Science Centre (SSDC, formerly known as the ASI Sciece Data Centre, ASDC), and contracts I/008/10/0, 2013/03/1.0, 2013-03-1.0.1-2015, and 2016-17-1.0 to the Aerospace Logistics Technology Engineering Company (ALTEC S.p.A.), and INAF;

the Netherlands Organisation for Scientific Research (NWO) through grant NWO-M-614.061.414 and through a VICI grant (A. Helmi) and the Netherlands Research School for Astronomy (NOVA);

the Polish National Science Centre through HARMONIA grant 2015/18/M/ST9/00544 and ETIUDA grants 2016/20/S/ST9/00162 and 2016/20/T/ST9/00170;

the Portugeuse Fundação para a Ciência e e Tecnologia (FCT) through grant SFRH/BPD/74697/2010; the Strategic Programmes UID/FIS/00099/2013 for CENTRA and UID/EEA/00066/2013 for UNINOVA;

the Slovenian Research Agency through grant P1-0188;

the Spanish Ministry of Economy (MINECO/FEDER, UE) through grants ESP2014-55996-C2-1-R, ESP2014-55996-C2-2-R, ESP2016-80079-C2-1-R, and ESP2016-80079-C2-2-R, the Spanish Ministerio de Economía, Industria y Competitividad through grant AyA2014-55216, the Spanish Ministerio de Educación, Cultura y Deporte (MECD) through grant FPU16/03827, the Institute of Cosmos Sciences University of Barcelona (ICCCUB, Unidad de Excelencia ‘María de Maeztu’) through grant MDM-2014-0369, the Xunta de Galicia and the Centros Singulares de Investigación de Galicia for the period 2016-2019 through the Centro de Investigación en Tecnologías de la Información y las Comunicaciones (CITIC), the Red Española de Supercomputación (RES) computer resources at MareNostrum, and the Barcelona Supercomputing Centre - Centro Nacional de Supercomputación (BSC-CNS) through activities AECT-2016-1-0006, AECT-2016-2-0013, AECT-2016-3-0011, and AECT-2017-1-0020;

the Swedish National Space Board (SNSB/Rymdstyrelsen);

the Swiss State Secretariat for Education, Research, and Innovation through the ESA PRODEX programme, the Mesures d’Accompagnement, the Swiss Activités Nationales Complémentaires, and the Swiss National Science Foundation;

the United Kingdom Rutherford Appleton Laboratory, the United Kingdom Science and Technology Facilities Council (STFC) through grant ST/L006553/1, the United Kingdom Space Agency (UKSA) through grant ST/N000641/1 and ST/N00117/1, as well as a Particle Physics and Astronomy Research Council Grant PP/C503703/1.

Our work was eased considerably by the use of the data handling and visualisation software TOPCAT, and STILTS (Taylor 2005).

This publication makes use of data products from NEOWISE, Wide-field Infrared Survey Explorer (WISE), a joint project of the University of California, Los Angeles, and the Jet Propulsion Laboratory/California Institute of Technology, funded by the National Aeronautics and Space Administration.


1. We are grateful to the following people for their substantial contributions to Gaia:"
Marty, Benjamin Massart, Emmanuel Mercier, Frédéric Meynadier, Shan Mignot, Bruno Miranda, Marco Molinaro, Marc Moniez, Alain Montmory, Stephan Morgensthal, Ulisse Murani, Jérôme Narbonne, Anne-Thérèse Nguyen, Thomas Nordlander, Markus Nollmeier, Derek O’Callaghan, Pierre Ocvirk, Ennio Poretti Merate, F. Spoto et al.: Gaia Data Release 2. Solar system
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Appendix A: Orbit determination process: perturbing asteroids

In the orbit determination process, in addition to the Sun, the eight planets, and the Moon, we also considered the perturbations due to the 16 massive asteroids and Pluto (Table A.1).

Table A.1. Perturbing bodies included in the dynamical model in the orbit determination process. The table contains the asteroid number and name and the corresponding mass and reference

<table>
<thead>
<tr>
<th>Asteroid name</th>
<th>Grav. mass (km^3/s^2)</th>
<th>References</th>
</tr>
</thead>
<tbody>
<tr>
<td>(1) Ceres</td>
<td>63.20</td>
<td>Standish &amp; Campbell (1984)</td>
</tr>
<tr>
<td>(2) Palla</td>
<td>14.30</td>
<td>Standish &amp; Campbell (1984)</td>
</tr>
<tr>
<td>(3) Juno</td>
<td>1.98</td>
<td>Konopliv et al. (2011)</td>
</tr>
<tr>
<td>(4) Vesta</td>
<td>17.80</td>
<td>Standish &amp; Campbell (1984)</td>
</tr>
<tr>
<td>(6) Hebe</td>
<td>0.93</td>
<td>Carry (2012)</td>
</tr>
<tr>
<td>(7) Iris</td>
<td>0.86</td>
<td>Carry (2012)</td>
</tr>
<tr>
<td>(10) Hygiea</td>
<td>5.78</td>
<td>Baer et al. (2011)</td>
</tr>
<tr>
<td>(15) Eunomia</td>
<td>2.10</td>
<td>Carry (2012)</td>
</tr>
<tr>
<td>(16) Psyche</td>
<td>1.81</td>
<td>Carry (2012)</td>
</tr>
<tr>
<td>(29) Amphitrite</td>
<td>0.86</td>
<td>Carry (2012)</td>
</tr>
<tr>
<td>(52) Europa</td>
<td>1.59</td>
<td>Carry (2012)</td>
</tr>
<tr>
<td>(65) Cybele</td>
<td>0.91</td>
<td>Carry (2012)</td>
</tr>
<tr>
<td>(87) Sylvia</td>
<td>0.99</td>
<td>Carry (2012)</td>
</tr>
<tr>
<td>(88) Thisbe</td>
<td>1.02</td>
<td>Carry (2012)</td>
</tr>
<tr>
<td>(511) Davida</td>
<td>2.26</td>
<td>Carry (2012)</td>
</tr>
<tr>
<td>(704) Interamnia</td>
<td>2.19</td>
<td>Carry (2012)</td>
</tr>
<tr>
<td>(134340) Pluto</td>
<td>977.00</td>
<td>Folkner et al. (2014)</td>
</tr>
</tbody>
</table>

Appendix B: Example of queries to the ESA Archive for SSO tables.

All the SSO data are made available through the ESA Archive https://gea.esac.esa.int/archive/. We here provide some examples of queries to Gaia DR2 tables concerning asteroids.

This query calls the whole list of SSOs published in Gaia DR2, with the number and name/provisional designation as in the Minor Planet Center website (https://www.minorplanetcenter.net/db_search):

```
SELECT number_mp, denomination
FROM gaiadr2.sso_source
```

The following query selects epoch, right ascension \( \alpha \), and declination \( \delta \) for a given SSO, ordered by their observation time. In this case, we have chosen the asteroid (8) Flora, but any asteroid can be selected from the list of objects published in Gaia DR2.

```
SELECT epoch, ra, dec
FROM gaiadr2.sso_observation
WHERE number_mp = 8 ORDER BY epoch
```

This query counts the number of NEAs in Gaia DR2:

```
SELECT COUNT(number_mp)
FROM user_dr2int6.aux_sso_orbits
WHERE a*(1-eccentricity)<1.3
```

List of Objects

‘(21) Lutetia’ on page 9
‘(2867) Šteins’ on page 9
‘(21) Lutetia’ on page 9
‘(39) Laetitia’ on page 10
‘(283) Emma’ on page 10
‘(704) Interamnia’ on page 11
‘(367) Amicitia’ on page 13
‘(367) Amicitia’ on page 15
‘(367) Amicitia’ on page 16
‘(3554) Amun’ on page 18
‘(4957) BruceMurray’ on page 18
‘(10563) Izhdubar’ on page 18
‘(12538) 1998 OH’ on page 18
‘(161989) Cacus’ on page 18
‘(2062) Aten’ on page 18

This query calls the observations (epoch, \( \alpha, \delta \)) and the residuals in AL and AC for a given object (in this case, we have chosen the NEA (2062) Aten):

```
SELECT obs.epoch, obs.ra, obs.dec,
res.residual_al, res.residual_ac
FROM user_dr2int6.sso_observation AS obs
JOIN user_dr2int6.aux_sso_orbit_residuals AS res
USING(observation_id)
WHERE obs.number_mp = 2062
```

This query selects all the asteroids with the corresponding values of \( G \) magnitude, observations and residuals in AL and AC when the \( G \) magnitude is between 13 and 17.

```
SELECT obs.number_mp, obs.epoch,
ob.ra, obs.dec, obs.g_mag,
res.residual_al, res.residual_ac
FROM user_dr2int6.sso_observation AS obs
JOIN user_dr2int6.aux_sso_orbit_residuals AS res
USING(observation_id)
WHERE obs.g_mag BETWEEN 13 AND 17
ORDER BY obs.number_mp
```

This query selects all the observations for a given asteroid (in this case, (8) Flora) with a non-null magnitude value.

```
SELECT obs.epoch, obs.ra, obs.dec, obs.g_mag
FROM user_dr2int6.sso_observation AS obs
WHERE obs.g_mag>0 AND obs.number_mp = 8
ORDER BY obs.epoch
```

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