**Terahertz-Driven Nonlinear Spin Response of Antiferromagnetic Nickel Oxide**

S. Baier,¹ J. H. Mentink,² M. Hohenleutner,³ L. Braun,³ T.-M. Do,¹ C. Lange,¹
A. Sell,⁴ M. Fiebig,⁵ G. Woltersdorf,⁶ T. Kampfrath,³ and R. Huber¹,∗

¹Department of Physics, University of Regensburg, 93053 Regensburg, Germany
²Radboud University, Institute of Molecules and Materials, Heyendaalseweg 135, 6525 AJ Nijmegen, Netherlands
³Department of Physical Chemistry, Fritz Haber Institute of the Max Planck Society, Faradayweg 4-6, 14195 Berlin, Germany
⁴Department of Physics, University of Konstanz and TOPTICA Photonics AG, Lohchamer Schlag 19, 82166 Gräfelfing, Germany
⁵Department of Materials, ETH Zurich, Vladimir-Prelog-Weg 4, 8093 Zurich, Switzerland
⁶Institute of Physics, Martin Luther University Halle-Wittenberg, 06120 Halle, Germany

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Terahertz magnetic fields with amplitudes of up to 0.4 Tesla drive magnon resonances in nickel oxide while the induced dynamics is recorded by femtosecond magneto-optical probing. We observe distinct spin-mediated optical nonlinearities, including oscillations at the second harmonic of the 1 THz magnon mode. The latter originate from coherent dynamics of the longitudinal component of the antiferromagnetic order parameter, which are probed by magneto-optical effects of second order in the spin deflection. These observations allow us to dynamically disentangle electronic from lattice-related contributions to magnetic linear birefringence and dichroism—information so far only accessible by ultrafast THz spin control. The nonlinearities discussed here foreshadow physics that will become essential in future subcycle spin switching.

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Selectively controlling the electron spin on ultrashort time scales has become a key challenge of condensed-matter physics. Achieving this goal is expected to reveal fascinating fundamental many-body physics and to enable disruptive technology for information processing at optical clock rates [1–27]. A variety of promising magneto-optical control schemes has been developed in recent years, including the inverse Faraday effect and Raman-type nonlinear optical processes [2,4,5,7–14] as well as optical modification of the exchange interaction [15–17]. Although these techniques have revolutionized our understanding of ultrafast spin dynamics, the lion share of the photon energy of the visible or near-infrared pump light is idle with respect to the light–spin interaction, and the dissipation of the large excess energy represents a major challenge.

In contrast, electromagnetic pulses in the terahertz spectral range (1 THz = 10¹² Hz) have accessed the spin degree of freedom most directly: The THz magnetic field exerts a Zeeman torque on the magnetic dipole associated with each spin, at a frequency that may be tuned in resonance with the collective magnon mode [1,3,18–21]. This interaction couples selectively to the spin, without involving charge or lattice degrees of freedom. In materials featuring multiferroic order, spin manipulation has also been mediated by the electric field component of THz pulses [22]. Conversely, magnetic THz control is a universal concept, not restricted to multiferroics. It has, indeed, first been demonstrated in an antiferromagnet, representing the largest class of magnetically ordered matter [3]. Since magnetic dipole coupling is typically weak, however, THz-driven spin excitation has been confined to the linear magneto-optical response regime. Future applications in magnetic storage or quantum computation require a distinctly nonlinear response.

Here, we employ intense THz pulses with peak magnetic amplitudes of up to 0.4 T to promote all-magnetic THz-driven spin dynamics in nickel oxide (NiO) into a new regime characterized by a distinctly nonlinear magneto-optical response. Beside a broadband quasi-instantaneous nonlinearity, an unexpected coherent signature occurs at twice the frequency of the 1 THz antiferromagnetic magnon oscillation. We show that this dynamics is a fingerprint of magneto-optical effects of second order, directly induced by the coherent spin motion. These processes are too fast for magnetostriction to follow and, thus, differ from their static counterparts. Hence they allow us to isolate electron- from lattice-mediated contributions to magnetic linear birefringence (MLB) and dichroism (MLD)—new physics exclusively accessible by strong ultrashort THz fields.

Below the Néel temperature of NiO of 523 K, the spins (quantum number S = 1) of the Ni²⁺ ions order ferromagnetically in equivalent {111} planes, whereas adjacent planes are antiferromagnetically exchange-coupled. The four equivalent {111} stacking directions define T domains, wherein the spins point into equivalent {112} directions, defining three possible S domains for each T domain [3]. The spin system supports well-defined long-wavelength collective magnon modes at frequencies of ω = 0.23 THz and 1.0 THz at room temperature, corresponding to spin deflection within and out of the {111} plane, respectively [1,3,8,10,12,13]. Annealing NiO in an oxygen atmosphere leads to the formation of macroscopic T domains (typical diameter, 10 to 100 μm) containing sub-μm-sized S domains. Strong MLB due to magnetostriction along...
of both diodes) is recorded as a function of the delay time between the THz pump pulse and the optical probe. The magneto-optical effects, the transient spin response imprints dynamic polarization modulations on the near infrared probe pulse. A combination of a half-wave plate (λ/2), a Wollaston prism (WP), and two photodiodes (PD) decodes the magneto-optical signal by tilted-pulse-front optical rectification of near-infrared pulses from a Ti:sapphire laser amplifier (pulse energy, 4 mJ; repetition rate, 3 kHz) [1]. Using two wire-grid polarizers, the peak magnetic amplitude \( B_{\text{peak}} \) may be tuned from 0.05 to 0.4 T, without modifying the waveform of the transients. When focused into a \( \langle 111 \rangle \)-cut NiO window with a thickness of 45 μm [Fig. 1(c)], the THz magnetic field exerts a Zeeman torque on the spins and induces coherent magnon oscillations [3]. The associated transient magneto-optical effects (Faraday effect, MLB, and MLD) are directly captured in the time domain with a temporal resolution of 1 ps. This feature is characteristic of a Faraday signal due to the out-of-plane antiferromagnetic magnon mode of NiO at \( \nu = 1.0 \) THz. The excellent stability of our laser system allows us to record the weak signature from a single magnon oscillation within a time interval of 1 ps. The amplitude of the long-lived monochromatic oscillation scales linearly with \( B_{\text{peak}} \) [Fig. 2(a)]. This direct proportionality proves the Zeeman origin of magnon excitation via the magnetic component of the THz field since linear magneto-electric effects are parity-forbidden in centrosymmetric NiO [3]. From the size of \( \Delta I/2I \) we extract a maximum spin deflection angle of 2° for \( B_{\text{peak}} = 0.4 \) T [3].

In addition to this resonant magnon signature, increasing the peak THz fields induces a nonlinearity of the magneto-optical response, manifesting itself as two maxima of \( \Delta I/2I \) at \( \tau = 0 \) and 0.4 ps, whose amplitudes scale quadratically with the THz field [Fig. 2(b)]. This nonlinear signature occurs solely while the THz field is present, and its shape traces the square of the THz waveform [Fig. 2(c)]. We assign this quasi-instantaneous \( \chi^{(3)} \) nonlinearity to a THz-induced Kerr effect observed in other materials before [28].

Whereas this nonresonant nonlinearity is not directly connected with the coherent spin motion, the strong THz field may also induce a specific nonlinear response due to the spin system, leading to a long-lived magnon response. In order to reveal this aspect, we perform a Fourier transform of \( \Delta I/2I \) recorded for \( B_{\text{peak}} = 0.4 \) T, for delay \( B_{\text{peak}} = 0.1 \) T (lowest curve) quasimonochromatic magnon oscillations with a period of 1.0 ps build up during the THz pulse and decay subsequently with a time constant of \( \tau = 30.5 \) ps. This feature is characteristic of a Faraday signal due to the out-of-plane antiferromagnetic magnon mode of NiO at \( \nu = 1.0 \) THz. The excellent stability of our laser system allows us to record the weak signature from a single magnon oscillation period with a signal-to-noise ratio of \( \approx 10^3 \) in an acquisition time of a few seconds. The amplitude of the long-lived monochromatic oscillation scales linearly with \( B_{\text{peak}} \) [Fig. 2(a)]. This direct proportionality proves the Zeeman origin of magnon excitation via the magnetic component of the THz field since linear magneto-electric effects are parity-forbidden in centrosymmetric NiO [3]. From the size of \( \Delta I/2I \) we extract a maximum spin deflection angle of 2° for \( B_{\text{peak}} = 0.4 \) T [3].

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\Delta I/2I = \frac{\Delta I}{2I} = \frac{I_{\text{peak}} - I_{\text{base}}}{2I_{\text{base}}}.
\]

A half-wave plate and a Wollaston prism translate the THz-induced polarization changes to an imbalance \( \Delta I \) of the photocurrents of two identical photodiodes. The magneto-optical signal \( \Delta I/2I \) (\( I \) denotes the sum of the photocurrents of both diodes) is recorded as a function of the delay time \( \tau \) between the THz pump pulse and the optical probe.

Figure 1(a) displays the temporal traces of the THz-induced magneto-optical signal observed in a single macroscopic \( T \) domain, for various field amplitudes. For delay

\[
\tau = 0 \text{ ps}.
\]

Figure 1(c) shows the magnetic component of the THz field since linear magneto-electric effects are parity-forbidden in centrosymmetric NiO [3]. From the size of \( \Delta I/2I \) we extract a maximum spin deflection angle of 2° for \( B_{\text{peak}} = 0.4 \) T [3].

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Figure 1(d) displays the temporal traces of the THz-induced magneto-optical signal observed in a single macroscopic \( T \) domain, for various field amplitudes. For delay

\[
\Delta I/2I = \frac{\Delta I}{2I} = \frac{I_{\text{peak}} - I_{\text{base}}}{2I_{\text{base}}}.
\]
times \( t > 4 \, \text{ps} \), i.e., after the instantaneous interaction with the THz field. The spectrum [Fig. 3(a)] is dominated by a Lorentzian peak centered at \( \nu = 1.0 \, \text{THz} \), as expected for the Faraday signal due to the out-of-plane magnon mode. The spectral width (FWHM) of 37 GHz is limited by the finite temporal window scanned in the experiment. Intriguingly, an additional maximum is found at \( \nu = 2.0 \, \text{THz} \), which corresponds to a polarization modulation at the second harmonic (SH) of the magnon frequency. Its amplitude amounts to 1.4% of the peak at 1 THz and is consistently observed in all experimental runs with \( B_{\text{peak}} = 0.4 \, \text{T} \). The spectral weight of the SH signature (see [29], part I for details of the analysis) scales quadratically with the THz peak field [inset to Fig. 3(a)]. This finding marks the first THz induced response at a harmonic frequency of a magnetic resonance, to the best of our knowledge. The shape of the SH spectral signature depends sensitively on the probe polarization [Fig. 3(b)]: When the polarization of the THz pump and the position of the crystal is kept fixed while we rotate the polarization of the probe pulse, the SH feature morphs from a peak into a dip and back into a peak with 180° period.

While the nonlinear response of spins in ferrimagnetic materials in the GHz spectral range has been extensively studied [37], the observed SH response in a pure antiferromagnet comes as a surprise. In order to explain this fact, we first analyze the spin motion itself and demonstrate that the corresponding Faraday signal cannot account for the SH signature. For small spin deflection angles, the transient magnetization associated with the coherent magnon oscillates harmonically and nonlinearities of the Faraday signal are obviously excluded. For larger magnon amplitudes, one has to account for the fact that a single electron spin is a prototypical saturable quantum system with an inherently nonlinear response. Yet still in this case, we can show that nonlinearities of the transient magnetization at the SH are expected to cancel exactly in a perfect antiferromagnet. To this end, we model the THz-induced spin dynamics in NiO microscopically, following the theory of Refs. [3] and [38], which describes the collective long-wavelength magnon mode as a uniform precession of all spins located on the two antiferromagnetic sublattices. The model includes exchange coupling, anisotropy, and direct Zeeman coupling of the spins with the measured THz waveform. We analyze the semiclassical three-dimensional trajectories of the two spin vectors \( \mathbf{S}_1 \) and \( \mathbf{S}_2 \) representing the antiferromagnetic sublattices on the Bloch sphere and identify the frequency components supported by the system.

Following THz excitation, \( \mathbf{S}_1 \) and \( \mathbf{S}_2 \) precess about their equilibrium direction (\( z \) axis) on the Bloch sphere [Fig. 4(a)]. Viewing along the \( z \) axis, the spins rotate in opposite directions and undergo different deflections within the \( \{111\} \) plane (containing the \( y \) and \( z \) axes) and out-of-plane (\( x \) axis). The Cartesian \( x \) components of \( \mathbf{S}_1 \) and \( \mathbf{S}_2 \) are 180° out of phase with respect to each other [Fig. 4(b)] whereas the \( y \) components are in phase, due to the action of the anisotropy field. Interestingly, the elliptical trajectories on the Bloch sphere change the \( z \) component of both spins.

![Fig. 3](image1.png)

**Fig. 3.** (a) Normalized spectrum of the magneto-optical signal for \( B_{\text{peak}} = 0.4 \, \text{T} \) [see Fig. 1(d), top curve] extracted for delay times \( t > 4 \, \text{ps} \). The sharp Lorentzian peak at 1 THz results from the long-lived oscillation of the 1-THz magnon mode. Surprisingly, an additional peak is found at the second harmonic frequency \( \nu = 2.0 \, \text{THz} \). Black arrows: spectral positions of sum- and difference-frequency components of the 1 and 0.23-THz magnon mode. Inset: Spectral weight \( A_\nu \) of the peak at \( \nu = 2.0 \, \text{THz} \) as a function of the THz driving field \( B_{\text{peak}} \) (blue spheres, experimental data; dotted line, quadratic fit). (b) Magnon spectra induced by THz peak fields of 0.4 T for various angles \( \phi \) of the probe polarization with respect to the crystal lattice (red curves, experimental data; blue curves, simulation).

![Fig. 4](image2.png)

**Fig. 4.** (a) Bloch sphere representation of typical trajectories of the spins \( \mathbf{S}_1 \) and \( \mathbf{S}_2 \) in the two antiferromagnetic spin sublattices. While the transient magnetization \( \mathbf{M} = S_1 + S_2 \) cancels along \( x \) and \( z \), the anisotropy field causes a nonzero net magnetization along \( y \). The antiferromagnetic vector \( \mathbf{L} = S_1 - S_2 \) oscillates in the \( x-z \) plane. (b) Cartesian components of \( \mathbf{S}_1 \) and \( \mathbf{S}_2 \) and the Cartesian component \( L_z \) of the antiferromagnetic vector \( \mathbf{L} \) for a schematic motion as shown in panel (a).
at the SH frequency. This frequency component, however, does not contribute to the total magnetization $\mathbf{M} \propto \mathbf{S}_1 + \mathbf{S}_2$ because the $z$ coordinates of both spins cancel [Fig. 4(a), green arrow]. The Faraday signal, which is proportional to $\mathbf{M}$, is expected to reflect only the 1-THz oscillation along $y$. This is also fully supported by the established analytical theory of nonlinear dynamics in antiferromagnets (see [29], part 2). In a perfect antiferromagnetic crystal, this observation holds even for large spin deflections, i.e., for strong THz peak fields. Because the cancellation of SH signatures in $\mathbf{M}$ occurs within a single unit cell, it applies equally to all $S$ and $T$ domains. Accordingly, the amplitude spectrum of the transient magnetization $\mathbf{M}$ computed for $B_{\text{peak}} = 0.4$ T (see [29], Fig. S1) is dominated by the fundamental peak at $\nu = 1.0$ THz whereas a SH response is absent. Local maxima at $\nu = 1.23$ and 0.77 THz can be assigned to difference- and sum-frequency mixing of the in-plane and out-of-plane magnon oscillation. Our experimental spectra actually exhibit faint shoulders at these spectral positions [Fig. 3(a), black arrows], but the finite width of the fundamental magnon peak prevents a clear isolation of these maxima.

The SH component of either $\mathbf{S}_1$ or $\mathbf{S}_2$ can only cause a Faraday response if the two sublattices are not perfectly compensated, e.g., due to domain boundaries, crystal defects, or strain. Such effects, however, would be independent of the probe polarization and are thus inconsistent with the symmetry of the response observed in Fig. 3(b) (see [29], part 3). Similarly, our polarization analysis excludes a transient breaking of the antiferromagnetic symmetry by the THz pump pulse as a potential origin of the SH oscillation, since such symmetry breaking would be the same for all probe polarizations (see [29], part 2, for a theoretical analysis).

Finally, we note that for very large spin deflection amplitudes the magnon frequency itself may become amplitude dependent. In a damped oscillation, one would then expect a time dependence of the instantaneous magnon frequency, which may cause intriguing nonlinearities [39]. Such effects, however, are not seen in our experiment. The above considerations lead us to the conclusion that spin dynamics probed by Faraday rotation (scaling linearly with $\mathbf{M}$) cannot be the origin of the SH signal in our experiment.

Consequently, we turn towards possible sources of the SH frequency caused by the probe process itself. First, the oscillating magnetization probed by the Faraday effect may cause a series of harmonic sidebands as observed in phonon-modulated silicon [40]. However, this effect only leads to odd multiples of the magnon frequency (see [29], part 2, especially Eq. (9), for an exact calculation). Second, the interplay between a periodic 1-THz modulation of the complex refractive index and the static birefringence of NiO may cause propagation effects. This is accounted for by a full quantitative model (see [29], part 4), which shows that propagation effects in the crystal are 2 orders of magnitude too small in amplitude to explain the experimental findings of the SH signature ([29], Fig. S1).

Instead, we now show that the strong spin deflection allows us to access transient magneto-optical effects of second order in the antiferromagnetic vector $\mathbf{L} = \mathbf{S}_1 - \mathbf{S}_2$ that are contained in the diagonal elements of the dielectric permittivity tensor [41,42]. Their real and imaginary parts induce a difference in the refractive indices (MLB) and absorption coefficients (MLD), respectively, along and perpendicular to $\mathbf{L}$. In particular, the terms $L_z^1$ and $L_z^2 = L_0^z - L_2^z \approx L_0 dL$ directly probe the coherent [43] nonlinear magnon response functions, where $L_0$ is the equilibrium value of $|\mathbf{L}|$ (see [29], part 5) and $dL$ is the dynamic component of $L_z$. The transient birefringence and dichroism are thus expected to oscillate at the SH frequency (Fig. 4) and to scale quadratically with the THz fields, as seen in the experiment [Fig. 3(a)], while the spin deflection angle [Fig. 2(a)] remains in the linear regime. Analogously to static magnetic linear birefringence and dichroism, transient MLB and MLD are expected to be anisotropic with respect to the probe polarization [42].

To confirm our interpretation, we extended the propagation model used above by introducing a complex Jones matrix including both MLB and MLD (difference of ordinary and extraordinary refractive indices or absorption coefficients for the transient dynamics). As seen in Fig. 3(b) (blue line), our model describes the local maximum of the magneto-optical signal at $\nu = 2$ THz and reproduces the change of the local maximum into a local minimum as the probe polarization is rotated by 90°. This peculiarity is caused by a phase-sensitive superposition of the polarization effect of the transient MLB and MLD at the SH and the broad Lorentzian Faraday signature centered at 1 THz. As the probe polarization is rotated, the relative phase between both effects changes, alternating between constructive and destructive interference.

Note that the subcycle time resolution of the MLB and MLD [44] warrants access to a mechanism that is fundamentally different from static birefringence or dichroism. The latter is dominated by magnetostriction [3,8,10,12,13]. In contrast, the associated elastic lattice deformation cannot follow the ultrafast THz spin precession studied here. Therefore, the transient second-order magneto-optical effects are directly related to the dependence of the electronic structure on the spin deflections and much weaker than their static counterparts. Our experimental data are well reproduced with a maximum phase difference between the ordinary and extraordinary waves on the order of $\mu$rad, whereas static MLB induces phase differences on the order of 1 rad. The dynamic absorption coefficient due to MLD lies on the order of $10^{-4}$ cm$^{-1}$ to account for the experimental results, whereas its static counterpart amounts to $\sim$400 cm$^{-1}$ [45]. In future studies, the contributions to the nonlinear SH signal due to MLB and MLD may even be precisely adjusted by tuning the probe wavelength.
Since the novel nonlinearity is not obscured by lattice dynamics it opens up an elegant way to complement Faraday measurements. While Faraday rotation probes the transverse spin deflection, the transient MLB and MLD simultaneously explore the motion of the longitudinal spin component on a subcycle time scale. Such signatures may serve as valuable indicators for future nonperturbative spin dynamics.

In conclusion, we demonstrated an all-magnetic THz-driven nonlinear optical spin response. Besides an instantaneous $\chi^{(3)}$ nonlinearity and indications of mixing of two antiferromagnetic modes, a distinct SH signal of the fundamental magnon oscillation, scaling quadratically with the THz amplitude, is found in NiO. We demonstrate that this signature is at odds with linear Faraday rotation induced by large-amplitude magnon oscillations. The novel nonlinearity is well explained by ultrafast magneto-optical effects scaling quadratically with the longitudinal spin component. Our results extend the established Faraday measurements of transverse spin deflection to coherent longitudinal spin dynamics. While static MLB has been shown to be mediated by magnetostriction (i.e., a lattice distortion proportional to $L^2$), this coupling mechanism cannot explain the dynamic signature seen at 2 THz. Since there are no long-wavelength acoustic phonons at 2 THz, the crystal lattice cannot adiabatically follow the THz spin precession. Hence our approach allows us to dynamically separate electronic from magnetostrictive contributions to coherent magnon-induced birefringence. We anticipate that these signatures will blaze the trail towards all-magnetic THz spin switching.

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*rupert.huber@physik.uni-regensburg.de

[43] We note that MLB was used in [41] to probe incoherent magnetization dynamics due to laser heating of the magnon system.
[44] The NiO crystal is absorptive and birefringent [45]. Because of the Kramers-Kronig relations, MLB in the presence of absorption must lead to MLD.