Search for massive supersymmetric particles decaying to many jets using the ATLAS detector in $pp$ collisions at $\sqrt{s} = 8$ TeV

The ATLAS Collaboration

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PACS numbers: 12.60.Jv,12.60.-i,12.38.Qk,13.85.-t,13.80.Da,11.30.Pb,13.87.-a,14.65.Fy

I. INTRODUCTION

Supersymmetry (SUSY) [1–9] is a theoretical extension of the Standard Model (SM) which fundamentally relates fermions and bosons. It is an alluring theoretical possibility given its potential to solve the naturalness problem [10–15] and to provide a dark-matter candidate [16, 17]. Partially as a result of the latter possibility, most searches for SUSY focus on scenarios such as a minimal supersymmetric standard model (MSSM) in which $R$-parity is conserved (RPC) [18–21]. In these models, SUSY particles must be produced in pairs and must decay to a stable lightest supersymmetric particle (LSP). With strong constraints now placed on standard RPC SUSY scenarios by the experiments at the Large Hadron Collider (LHC), it is important to expand the scope of the SUSY search program and explore models where $R$-parity may be violated and the LSP may decay to SM particles, particularly as these variations can alleviate some degree the fine-tuning many SUSY models currently exhibit [22].

In $R$-parity-violating (RPV) scenarios, many of the constraints placed on the MSSM in terms of the allowed parameter space of gluino ($\tilde{g}$) and squark ($\tilde{q}$) masses are relaxed. The reduced sensitivity of standard SUSY searches to RPV scenarios is due primarily to the high missing transverse momentum ($E_T^{miss}$) requirements used in the event selection common to many of those searches. This choice is motivated by the assumed presence of two weakly interacting and therefore undetected LSPs. Consequently, the primary challenge in searches for RPV SUSY final states is to identify suitable substitutes for the canonical large $E_T^{miss}$ signature of RPC SUSY used to distinguish signals from background processes. Common signatures used for RPV searches include resonant lepton pair production [23–25], exotic decays of long-lived particles, and displaced vertices [26–29].

![Figure 1](image-url)  

Figure 1. Diagrams for the benchmark processes considered for this analysis. The solid black lines represent Standard Model particles, the solid red lines represent SUSY partners, the gray shaded circles represent effective vertices allowed by the baryon-number-violating $\lambda''$ couplings with off-shell propagators (e.g. heavy squarks coupling to a $\tilde{\chi}_1^0$ neutralino and a quark), and the blue shaded circles represent effective RPV vertices allowed by the baryon-number-violating $\lambda''$ couplings with off-shell propagators (e.g. heavy squarks coupling to two quarks).

New analyses that do not rely on $E_T^{miss}$ are required in order to search for fully hadronic final states involving RPV gluino decays directly to quarks or via $\tilde{\chi}_1^0$ neutralinos as shown in the diagrams in Fig. 1. Cases in which pair-produced massive new particles decay directly to a total of six quarks, as well as cascade decays with at least ten quarks, are considered. Three-body decays of the type shown in Fig. 1 are given by effective RPV vertices allowed by the baryon-number-violating $\lambda''$ couplings as described in Sec. II with off-shell squark propagators. This analysis is an extension of the search conducted at $\sqrt{s} = 7$ TeV for the pair production of massive gluinos, each decaying directly into three quarks [30].

The diagrams shown in Fig. 1 represent the benchmark processes used in the optimization and design of
the search presented in this paper. The extension to considering cascade decays of massive particles creates the potential for significantly higher hadronic final-state multiplicities and motivates a shift in technique with respect to previous searches. Therefore, the analysis is extended to look for events characterized by much higher reconstructed jet multiplicities as well as with event topologies representative of these complex final states. Two complementary search strategies are thus adopted: a jet-counting analysis that searches for an excess of $\geq$6-jet or $\geq$7-jet events, and a data-driven template-based analysis that uses a topological observable called the total-jet-mass of large-radius (large-$R$) jets. The former exploits the predictable scaling of the number of $n$-jet events ($n = 6,7$) as a function of the transverse momentum ($p_T$) requirement placed on the $n^{th}$ leading jet in $p_T$ for background processes. This analysis is sensitive to the models presented here because this scaling relation differs significantly between the signal and the background. The latter analysis uses templates of the event-level observables is presented in Sec. VII. The combined results while the total-jet-mass analysis using more advanced observables is presented in Sec. VII. The combined results of this search and the final sensitivity to the benchmark processes are then described in Sec. VIII. The results using the total-jet-mass analysis are presented first, in Sec. VIII.A, as they only apply to the ten-quark final states. The jet-counting analysis additionally yields interpretations across the flavor structure allowed by the $\lambda''$ couplings. This comprehensive set of results is presented in Sec. VIII.B. Comparisons between the two analyses are then made in Sec. VIII.C.

II. R-PARITY-VIOLATING SUPERSYMMETRY AND BARYON-NUMBER VIOLATION

The benchmark model used to interpret the results of the search for high multiplicity hadronic final states is the baryon-number-violating RPV SUSY scenario. The RPV component of the generic supersymmetry superpotential can be written as [31, 32]:

$$W_{R_p} = \frac{1}{2} \lambda_{ijk} L_i \bar{L}_j E_k + \lambda'_{ijk} L_i Q_j \bar{D}_k + \frac{1}{2} \lambda''_{ijk} \bar{U}_i \bar{D}_j \bar{D}_k + \kappa_i L_i H_2,$$

(1)

where $i, j, k = 1, 2, 3$ are generation indices. The generation indices are sometimes omitted in the discussions that follow if the statement being made is not specific to any generation. The first three terms in Eq. (1) are often referred to as the trilinear couplings, whereas the last term is bilinear. The $L_i, Q_i$ represent the lepton and quark $SU(2)_L$ doublet superfields, whereas $H_2$ is the Higgs superfield. The $E_j, \bar{D}_j,$ and $\bar{U}_j$ are the charged lepton, down-type quark, and up-type quark $SU(2)_L$ singlet superfields, respectively. The Yukawas couplings for each term are given by $\lambda, \lambda', \lambda''$, and $\kappa$ is a dimensionful mass parameter. In general, the particle content of the RPV MSSM is identical to that of the RPC MSSM but with the additional interactions given by $W_{R_p}$.

Generically, the addition of $W_{R_p}$ into the overall SUSY superpotential allows for the possibility of rapid proton decay. The simultaneous presence of lepton-number-violating (e.g. $\lambda' \neq 0$) and baryon-number-violating operators ($\lambda'' \neq 0$) leads to proton decay rates larger than allowed by the experimental limit on the proton lifetime unless, for example, [33]

$$\lambda_{11k}' \cdot \lambda_{11k}'' \lesssim 10^{-23} \left( \frac{m_{\tilde{q}}}{100 \text{ GeV}} \right)^2,$$

(2)

where $m_{\tilde{q}}$ is the typical squark mass. As a result, even when considering this more generic form of the SUSY superpotential by including $W_{R_p}$, it is still necessary to impose an ad hoc, albeit experimentally motivated, symmetry to protect the proton from decay. It is generally necessary that at least one of $\lambda, \lambda', \lambda''$ be exactly equal to zero. Consequently, it is common to consider each term in Eq. (1) independently. In the case of nonzero $\lambda$ and $\lambda'$, the typical signature involves leptons in the final state. However, for $\lambda''_{ijk} \neq 0$, the final state is characterized by jets, either from direct gluino decay or from the cascade decay of the gluino to the lightest neutralino ($\chi^0_1$), as also considered here. Because of the structure of Eq. (1), scenarios in which only $\lambda''_{ijk} \neq 0$ are often referred to as UDD scenarios.

Current indirect experimental constraints [34] on the sizes of each of the UDD couplings $\lambda''_{ijk}$ from sources other than proton decay are valid primarily for low squark masses, as suggested by Eq. (2). Those limits are driven by double nucleon decay [35] (for $\lambda''_{112}$), neutron oscillations [36] (for $\lambda''_{113}$), and $Z$ boson branching ratios [37].

Hadron collider searches are hindered in the search for an all-hadronic decay of new particles by the fact that the SM background from multi-jet production is very high. Nonetheless, searches have been carried out by several collider experiments. The CDF Collaboration [38] excluded gluino masses up to 240 GeV for light-flavor models. The CMS Collaboration [39] excludes such gluinos up to a mass of 650 GeV and additionally sets limits on some heavy-flavor UDD models. The ATLAS Collaboration [30] has also previously set limits in a search for anomalous six-quark production, excluding gluino masses up to 666 GeV for light-flavor models. The search presented here uniquely probes the flavor structure of the UDD couplings and employs new techniques both in anal-
analysis and theoretical interpretation.

III. THE ATLAS DETECTOR

The ATLAS detector [40] provides nearly full solid angle coverage around the collision point with an inner tracking system covering the pseudorapidity\(^1\) range \(|\eta| < 2.5\), electromagnetic (EM) and hadronic calorimeters covering \(|\eta| < 4.9\), and a muon spectrometer covering \(|\eta| < 2.7\).

The ATLAS tracking system is composed of a silicon pixel tracker closest to the beamline, a microstrip silicon tracker, and a straw-tube transition radiation tracker. These systems are layered radially around each other in the central region. A thin solenoid surrounding the tracker provides an axial 2 T field enabling measurement of charged-particle momenta.

The calorimeter, which spans the pseudorapidity range up to \(|\eta| = 4.9\), is comprised of multiple subdetectors with different designs. The high granularity liquid argon (LAr) electromagnetic calorimeter system includes separate barrel \((|\eta| < 1.475)\), endcap \((1.375 < |\eta| < 3.2)\), and forward subsystems \((3.1 < |\eta| < 4.9)\). The tile hadronic calorimeter \((|\eta| < 1.7)\) is composed of scintillator tiles and iron absorbers. As described below, jets used in the analyses presented here are typically required to have \(|\eta| < 2.8\) such that they are fully contained within the barrel and endcap calorimeter systems.

A three-level trigger system is used to select events to record for offline analysis. The level-1 trigger is implemented in hardware and uses a subset of detector information to reduce the event rate to a design value of at most 75 kHz during 2012. This is followed by two software-based triggers, level-2 and the event filter (collectively called the high-level trigger). The primary triggers used in this analysis collected the full integrated luminosity of the 8 TeV dataset with good efficiency for the event selections described in this paper.

IV. DATA AND MONTE CARLO SAMPLES

The data used in this analysis correspond to 20.3 ± 0.6 fb\(^{-1}\) [41, 42] of integrated luminosity taken during periods in which the data satisfied baseline quality criteria. Further details of the event selections applied, including the ATLAS data quality criteria and trigger strategy, are given in Sec. V. The primary systems of interest in these studies are the electromagnetic and hadronic calorimeters and the inner tracking detector. The data were collected with triggers based on either single-jet or multi-jet signatures. The single-jet trigger selection has a transverse momentum threshold of 360 GeV using a large-R anti-\(k_t\) jet definition [43] with a nominal radius of \(R = 1.0\) within the high-level jet trigger. The multi-jet trigger selection requires at least six anti-\(k_t\) \(R = 0.4\) jets with a nominal \(p_T\) threshold of 45 GeV in the high-level trigger. Data collected using several additional multi-jet requirements (from three to five jets) are also used for background estimation studies.

Multiple simultaneous proton–proton (pp) interactions, or pile-up, occur in each bunch crossing at the LHC. The additional collisions occurring in the same and neighboring bunch crossings with respect to the event of interest are referred to as in-time and out-of-time pile-up, respectively, and are uncorrelated with the hard-scattering process.

The benchmark RPV SUSY signal processes of both the six-quark and ten-quark models (see Sec. I) were simulated using HERWIG++ 6.520 [44] for several gluino and neutralino mass hypotheses using the parton distribution function (PDF) set CTEQ6L1 [45, 46]. For both models, all squark masses are set to 5 TeV and thus gluinos decay directly to three quarks or to two quarks and a neutralino through standard RPC couplings. In the ten-quark cascade decay model, the neutralinos each decay to three quarks via an off-shell squark and the RPV UDD decay vertex with coupling \(\lambda''\). In this model, the neutralino is the lightest supersymmetric particle.

Samples are produced covering a wide range of both \(m_{\tilde{g}}\) and \(m_{\chi^0_i}\). In the six-quark direct gluino decay model, the gluino mass is varied from 500 to 1200 GeV. In the case of the cascade decays, for each gluino mass (400 GeV to 1.4 TeV), separate samples are generated with multiple neutralino masses ranging from 50 GeV to 1.3 TeV.

In each case, \(m_{\chi^0_i} < m_{\tilde{g}}\). In order to ensure the result has minimal sensitivity to the effects of initial state radiation (ISR), which could be poorly modeled in the signal samples, the region with \((m_{\tilde{g}} - m_{\chi^0_i}) < 100\) GeV is not considered. Due to the potentially large theoretical uncertainty on the non-SM colorflow given by UDD couplings, results are presented for a single model of radiation and no systematic uncertainty is assigned for this effect, further justifying the unevauluated region described above. All possible \(\lambda''_{ijk}\) flavor combinations given by the structure of Eq. (1) are allowed to proceed with equal probability. As discussed in Sec. VIII, the analysis maintains approximately equal sensitivity to all flavor modes.

All samples are produced assuming that the gluino and

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\(^1\)ATLAS uses a right-handed coordinate system with its origin at the nominal interaction point (IP) in the center of the detector and the z-axis along the beam pipe. The x-axis points from the IP to the center of the LHC ring, and the y-axis points upward. Cylindrical coordinates \((r, \phi)\) are used in the transverse plane, \(\phi\) being the azimuthal angle around the beam pipe. The pseudorapidity is defined in terms of the polar angle \(\theta\) as \(\eta = -\ln \tan(\theta/2)\).

\(^2\)HERWIG++, which is used for signal simulation, is not expected to model additional energetic jets from ISR well because the leading-order evaluation of the matrix element is only performed for the \(2 \rightarrow 2\) particle scattering process.
neutralino widths are narrow and that their decays are prompt. Cross-section calculations are performed at next-to-leading order in the strong coupling constant, adding the resummation of soft gluon emission at next-to-leading-logarithmic accuracy (NLO+NLL) [47–51].

Dijet and multi-jet events, as well as top quark pair production processes, were simulated in order to study the SM contributions and background estimation techniques. In the case of the vastly dominant background from SM jet production, several MC simulations were compared with data for the suitability of their descriptions of jet and multi-jet kinematic observables and topologies. For signal region selections that use b-tagging (the identification of jets containing B-hadrons), other backgrounds such as $t\bar{t}$, single top, and $W/Z+$ jets become significant as well. These other backgrounds are estimated directly from the simulation.

In order to develop the data-driven background estimation techniques for multi-jet events from QCD processes, comparisons are made among various generators and tunes. In the case of the jet-counting analysis, the ATLAS tune AUET2B LO** [52] of PYTHIA 6.426 [53] is used in estimating the rate of $n$-jet events (where $n = 6,7$) as a function of the jet $p_T$ requirement on the $n^{th}$ jet. For the total-jet-mass analysis, SHERPA 1.4.0 [54] is used to develop and test the method. For the SHERPA multi-jet samples, up to three partons are included in the matrix-element calculation and no electroweak processes are included. Heavy (c and b) quarks are treated as massive. The next largest background after multi-jets is fully hadronic $t\bar{t}$ production, which is also simulated with SHERPA 1.4.0 and is used to estimate any background contamination in the control and signal regions defined in the analysis.

The jet-counting and total-jet-mass analyses use different multi-jet generators because of the different approaches to the background estimation employed by each analysis. The low-to-high jet-multiplicity extrapolation of the jet-counting analysis, described in Sec. VIIA, favors a generator that treats the production of an additional jet in a consistent manner, such as PYTHIA, rather than a generator that treats the multijet matrix element separately from the additional radiation given by a separate parton shower model. In contrast, the total-jet-mass analysis uses the multi-jet simulation only to test the background estimation method and optimize the analysis as described in Sec. VIIA and Sec. VIIIB, and uses SHERPA as it provides a better description of jet substructure variables, such as the jet mass used in this analysis.

The ATLAS simulation framework [55] is used to process both the signal and background events, including a full GEANT4 [56] description of the detector system. The simulation includes the effect of both in-time and out-of-time pile-up and is weighted to reproduce the observed distribution of the average number of collisions per bunch crossing in the data.

V. PHYSICS OBJECTS AND EVENT PRESELECTION

A. Data quality criteria

The data are required to have met criteria designed to reject events with significant contamination from detector noise, noncollision beam backgrounds, cosmic rays, and other spurious effects. The selection related to these quality criteria is based upon individual assessments for each subdetector, usually separated into barrel, forward and endcap regions, as well as for the trigger and for each type of reconstructed physics object (i.e. jets).

To reject noncollision beam backgrounds and cosmic rays, events are required to contain a primary vertex consistent with the LHC beamspot, reconstructed from at least two tracks with transverse momenta $p_T > 400$ MeV. Jet-specific requirements are also applied. All jets reconstructed with the anti-$k_t$ algorithm using a radius parameter of $R = 0.4$ and a measured $p_T^j > 20$ GeV are required to satisfy the “looser” requirements discussed in detail in Ref. [57]. This selection requires that jets deposit at least 5% of their measured total energy in the electromagnetic (EM) calorimeter as well as no more than 99% of their energy in a single calorimeter layer.

The above quality criteria selections for jets are extended to prevent contamination from detector noise through several detector-region-specific requirements. Jets with spurious energy deposits in the forward hadronic endcap calorimeter are rejected and jets in the central region ($|\eta| < 2.0$) that are at least 95% contained within the EM calorimeter are required not to exhibit any electronic pulse shape anomalies [58]. Any event with a jet that fails the above requirements is removed from the analysis.

B. Object definitions

Jets are reconstructed using the anti-$k_t$ algorithm with radius parameters of both $R = 0.4$ and $R = 1.0$. The former are referred to as standard jets and the latter as large-$R$ jets. The inputs to the jet reconstruction are three-dimensional topological clusters [59]. This method first clusters together topologically connected calorimeter cells and classifies these clusters as either electromagnetic or hadronic. The classification uses a local cluster weighting (LCW) calibration scheme based on cell-energy density and longitudinal depth within the calorimeter [60]. Based on this classification, energy corrections derived from single-pion MC simulations are applied. Dedicated corrections are derived for the effects of noncompensation, signal losses due to noise-suppression threshold effects, and energy lost in noninstrumented regions. An additional jet energy calibration is derived from MC simulation as a correction relating the calorimeter response to the true jet energy. In order to determine these corrections, the identical jet definition used in the reconstruc-
tion is applied to particles with lifetimes greater than 10 ps output by MC generators, excluding muons and neutrinos. Finally, the standard jets are further calibrated with additional correction factors derived in situ from a combination of $\gamma$+jet, Z+jet, and dijet balance methods [60].

No explicit veto is applied to events with leptons or $E_T^{miss}$. This renders the analysis as inclusive as possible and leaves open the possibility for additional interpretations of the results. There is no explicit requirement removing identified leptons from the jets considered in an event. Calorimeter deposits from leptons may be considered as jets in this analysis given that the data quality requirements.

The signals considered, typically of failing to satisfy the signal event selection criteria. For identified and distinguished from jets, have a high probability of being at least 60 GeV in order to reside in the fully efficient regions of the analysis. All jets used in this analysis are required to have $|\eta| < 2.8$. The effect of pile-up on jets is negligible for the kinematic range considered, and no selection to reduce pile-up sensitivity is included.

In order to constrain specific UDD couplings to heavy flavor quarks, $b$-tagging requirements are also applied to some signal regions. In these cases, one or two standard jets are required to satisfy $b$-tagging criteria based on track transverse impact parameters and secondary vertex identification [61]. In simulated $t\bar{t}$ events, this algorithm yields a 70% (20%) tagging efficiency for real $b$-(c)-jets and an efficiency of 0.7% for selecting light quark and gluon jets. The $b$-tagging efficiency and misidentification are corrected by scale factors derived in data [61]. These jets are additionally required to lie within the range $|\eta| < 2.5$.

The topological selection based on the total mass of large-$R$ jets (Sec. VII) employs the trimming algorithm [62]. This algorithm takes advantage of the fact that contamination from the underlying event and pile-up in the reconstructed jet is often much softer than the outgoing partons from the hard-scatter. The ratio of the $p_T$ of small subsets (jets composed of the constituents of the original jet) to that of the jet is used as a selection criterion. The procedure uses a $k_t$ algorithm [63, 64] to create subsets with a radius $R_{sub} = 0.3$. Any subsets with $p_{Tsub}^2 > f^2_{cut}$ are removed, where $p_{Tsub}$ is the transverse momentum of the $i$th subset, and $f_{cut} = 0.05$ is determined to be an optimal setting [65]. The remaining constituents form the trimmed jet, and the mass of the jet is the invariant mass of the remaining subsets (which in turn is the invariant mass of the massless topological clusters that compose the subjet). Using these trimming parameters, the full mass spectrum is insensitive to pile-up.

The total-jet-mass analysis uses a sample from the high-$p_T$ single-jet triggers. A requirement that the leading large-$R$ jet have $p_T^{jet} > 500$ GeV is applied to ensure that these triggers are fully efficient.

VI. JET-COUNTING ANALYSIS

A. Method and techniques

The jet-counting analysis searches for an excess of events with $\geq 6$ or $\geq 7$ high $p_T$ jets jets (with at least 80 GeV), with $\geq 0$, $\geq 1$, or $\geq 2$ $b$-jet requirements added to enhance the sensitivity to couplings that favor decays to heavy-flavor quarks. The number of jets, the $p_T$ requirement that is used to select jets, and the number of $b$-tagged jets are optimized separately for each signal model taking into account experimental and theoretical uncertainties.

The background yield in each signal region is estimated by starting with a signal-depleted control region in data and extrapolating its yield into the signal region using a factor that is determined from a multi-jet simulation, with corrections applied to account for additional minor background processes. This can be expressed as:

$$N_{n-jet} = (N_{m-jet} - N_{MC}^{m-jet}, Other BGs) \times \frac{N_{MC}^{m-jet}}{N_{MC}^{m-jet}} + N_{MC}^{m-jet}, Other BGs$$

where the number of predicted background events with $n$ jets ($N_{n-jet}$) is determined starting from the number of events in the data with $m$ jets ($N_{m-jet}^{data}$). The extrapolation factor, $\frac{N_{MC}^{m-jet}}{N_{MC}^{m-jet}}$, is determined from multi-jet simulation and validated in the data. This procedure is performed in exclusive bins of jet multiplicity. Since the simulation is not guaranteed to predict this scaling perfectly, cross-checks in the data and a data-driven determination of systematic uncertainties are performed as described in Sec. VIC. It is assumed here that the simulation used for this extrapolation given by PYTHIA 6.426 predicts the relative rate of events with one additional order in the strong coupling constant in a consistent way across jet-multiplicity regions. This assumption comes from the behavior of the parton shower model used by PYTHIA to obtain configurations with more than two partons and is shown to be consistent with data in the measurement of multi-jet cross-sections [66]. Other models were studied and are discussed in Sec. VIC.

Small corrections from other backgrounds ($t\bar{t}$, single top, and $W/Z$+jet events) are applied based on estimates from the simulation. Without $b$-tagging, the contribution of events from these other backgrounds is less than 1%.
Including two $b$-tagged jets increases this relative contribution to as much as 10%.

B. Signal and control region definitions

Control regions are defined with $m \leq 5$, for which the background contribution is much larger than the expected signal contributions from the benchmark signal processes. Extrapolation factors with $n, m \leq 5$ are used to validate the background model and to assign systematic uncertainties. For $n > 5$, the expected signal contributions can become significant and an optimization is performed to choose the best signal region definitions for a given model. Signal regions are chosen with simultaneous optimizations of the jet-multiplicity requirement ($\geq 6$ or $\geq 7$ jets), the associated transverse momentum requirement (80–220 GeV in 20 GeV steps), and the minimum number of $b$-tagged jets ($\geq 0, \geq 1, \text{or } \geq 2$) for a total of 48 possible signal regions. Alternative control regions are constructed from some $n > 5$ regions when the signal significance is expected to be low as described in Sec. VI.C. Such regions are then excluded from the list of allowed signal regions. For a given signal model, the signal region deemed most effective by this optimization procedure is used for the final interpretations. The signal regions chosen by the optimization procedure tend to pick regions with signal acceptances as low as 0.5% and as high as roughly 20%.

Although other choices are also studied to determine background yield systematic uncertainties from the data, the background contributions are estimated in the final signal regions using extrapolations across two jet-multiplicity bins ($n = m + 2$). This choice leads to negligible signal contamination in the control regions used for this nominal prediction.

C. Validation and systematic uncertainties

Since the 3-, 4-, and 5-jet-multiplicity bins have minimal expected signal contamination they are used to validate the background model based on the MC simulation. The initial validation of the background prediction is performed by extrapolating the background from either the $m = 3$ or $m = 4$ jets control region into the $n = 5$ jets control region and comparing with the data. This comparison is presented in Fig. 2, which shows the number of events passing a given jet $p_T$ requirement with a 5-jet requirement. This procedure is shown to be accurate in the extrapolations to the 5-jet bin in data, both with and without the requirement of $b$-tagging. The conclusion of this validation study is that Eq. (3) can be used with no correction factors, but a systematic uncertainty on the method is assigned to account for the discrepancies between data and the prediction in the control regions. This systematic uncertainty is assigned to cover per $p_T$ bin, the largest discrepancy that is observed between data and the prediction when extrapolating from either the 3-jet or 4-jet bins into the 5-jet control region, as well as from extrapolations to higher jet multiplicities as discussed below.

Alternative MC models of extra-jet production such as those given by SHERPA, HERWIG++, and additional parameter tunes in PYTHIA were studied and either did not satisfy the criterion that the model be consistent through control and signal regions or disagreed significantly with the data in the validations presented here. The internal spread of predictions given by each of these background models in various extrapolations is considered when assigning systematic uncertainties. In all cases, this spread is consistent with the systematic uncertainties obtained using PYTHIA in the manner described above.

In addition to the extrapolation factor described by Eq. (3), it is possible to also study the extrapolation along the jet $p_T$ degree of freedom. In this case, the $n$-jet event yield for a given high jet-$p_T$ selection is predicted using extrapolation factors from lower jet-$p_T$ selections determined from MC simulation. This method is tested exclusively in a low $n$-jet region for the high jet-$p_T$ requirement and the spread is compared to the baseline systematic uncertainty, which is increased in case of disagreement larger than this baseline.

Additional control regions can be constructed from exclusive 6-jet regions with low jet-$p_T$ requirements. Any region with an expected signal contribution less than 10% for the $m_4 = 600$ GeV six-quark model is used as additional control region in the evaluation of the background systematic uncertainties. These regions are used to ensure that the jet-multiplicity extrapolation continues to accurately predict the event rate at higher jet multiplicities, as shown in Fig. 3(a), without looking directly at possible signal regions. This procedure allows the exclusive 6-jet, low jet-$p_T$ region to be probed and shows that the jet-multiplicity extrapolations continue to provide accurate predictions at higher jet multiplicities.

To extend this validation, a requirement that the average jet pseudorapidity $\langle|\eta|\rangle > 1.0$ is applied to create a high-pseudorapidity control region to reduce the signal contribution to a level of less than approximately 10% while retaining a reasonable number of events. Results of these extrapolations are shown for the exclusive 7-jet bin in Fig. 3(b). The largest deviations from the expected values are found to be a few percent larger than for the 5-jet extrapolations.

The uncertainty due to any mismodeling of contributions from backgrounds such as $t\bar{t}$, single top, and $W/Z+j$-jet processes is expected to be small and is covered by the procedure above since these contributions are included in the extrapolation. Therefore, any mismodeling of these sources results in increased systematic uncertainty on the entire background model in this procedure.

Distributions for data in the inclusive $\geq 6$-jet and $\geq 7$-jet signal regions are shown in Fig. 4 compared with background predictions determined using extrapolations.
Figure 2. The number of observed events in the 5-jet bin is compared to the background expectation that is determined by using PYTHIA to extrapolate the number of events in data from the low jet-multiplicity control regions. The contents of the bins represent the number of events with 5-jets passing a given jet $p_T$ requirement. These bins are inclusive in jet $p_T$. Results with various $b$-tagging requirements are shown.

From three different jet-multiplicity bins. In each case, the distributions representing the extrapolations across two jet-multiplicity bins (i.e. $4 \to 6$ and $5 \to 7$) are used as the final background prediction whereas the other extrapolations are simply considered as additional validation. Contributions from higher jet-multiplicity regions are summed to construct an inclusive sample. The systematic uncertainty is constructed from the maximum deviation given by the various validations and for most signal regions is dominated by the baseline uncertainty obtained from the $n \leq 5$ jet regions. Results using the three $b$-tagging selections ($\geq 0$, $\geq 1$, $\geq 2$ $b$-tagged jets) are shown in Fig. 4. The background systematic uncertainties determined from the control regions in the data are shown as the green shaded region in the ratio plots of Fig. 4. This procedure results in a background systematic uncertainty in the $p_T^{\text{jet}} \geq 120$ GeV, $\geq 7$-jet region of 14%, 15%, and 40% for $\geq 0$, $\geq 1$, $\geq 2$ $b$-tagged jets,
The total-jet-mass analysis uses a topological observable $M_J^\Sigma$ as the primary distinguishing characteristic between signal and background. The observable $M_J^\Sigma$ [67–69] is defined as the scalar sum of the masses of the four leading large-$R$ jets reconstructed with a radius parameter $R = 1.0$, $p_T > 100$ GeV and $|\eta| < 2.5$,

$$M_J^\Sigma = \sum_{p_T > 100 \text{ GeV}, |\eta| < 2.5} m^{\text{jet}}.$$  \hfill (4)

This observable was used for the first time in the $\sqrt{s} = 8$ TeV search by the ATLAS Collaboration for events with many jets and missing transverse momentum [70] and provides significant sensitivity for very high-mass gluinos. Four-jet (or more) events are used as four large-$R$ jets cover a significant portion of the central region of the calorimeter, and are very likely to capture most signal quarks within their area. This analysis focuses primarily on the ten-quark models mentioned in Sec. I.

**VII. TOTAL-JET-MASS ANALYSIS**

A. Method and techniques

The bins in these distributions that were not assigned as control regions represent possible signal regions, which may be chosen as a signal region for a particular model under the optimization procedure described in Sec. VIII B. The level of disagreement between the expectation and data is shown in Fig. 5 for the $\geq 0$ $b$-tagged jets control and signal regions. In the $b$-tagged signal regions similar agreement is observed between data and the predicted background, within the assigned uncertainties. In practice, it is seen that for most signals, the $\geq 7$-jet bin is preferred by the optimization procedure as a signal region. The data in each distribution show good agreement with background predictions within uncertainties.

Systematic uncertainties on the jet-counting background estimation using the extrapolation method are determined directly from the data as part of the background validation. In contrast, systematic uncertainties on the signal predictions are determined from several sources of modeling uncertainties. The largest systematic uncertainties are those on the background yield, the jet energy scale uncertainties on the signal yield (10–20% for most signal regions), and the uncertainty in $b$-tagging efficiencies for many signal regions that require the presence of $b$-tagged jets (between 15–20% for signal regions requiring at least two $b$-tags).

An additional systematic uncertainty is included in these estimates in order to cover possible contamination of signal in the control regions for the extrapolation. The analysis is repeated with signal injected into the control regions and the backgrounds are re-computed. The resulting bias depends on the signal model and is found to be less than 5% in all cases.

Given the good agreement between the data and the predictions from the jet-counting background estimation, there is no evidence of new physics.
Simulation studies show that $M_T^2$ provides greater sensitivity than variables such as $H_T$, the scalar sum of jet $p_T$: the masses contain angular information about the events by definition, whereas a variable like $H_T$ simply describes the energy (or transverse momentum) in the event. A large $M_T^2$ implies not only high energy, but also rich angular structure. Previous studies at the Monte Carlo event generator level have demonstrated the power of the $M_T^2$ variable in the high-multiplicity events that this analysis targets [67, 68].

Figure 6 presents examples of the discrimination that the $M_T^2$ observable provides between the background (represented here by SHERPA multi-jet MC simulation) and several signal samples, as well as the comparison of the data to the SHERPA multi-jet background. Three signal samples, each with $m_{\tilde{g}} = 175$ GeV and several gluino masses $m_{\tilde{g}}$ in the range $0.6 - 1.4$ TeV are shown. In each case, the discrimination in the very high $M_T^2$ region is similar and is dictated primarily by the gluino mass, but is also sensitive to the mass splitting, $m_{\tilde{g}} - m_{\tilde{\chi}_1^0}$. Larger $m_{\tilde{g}}$ results in larger $M_T^2$, as expected. However, for the same $m_{\tilde{g}}$, $M_T^2$ is largest for $m_{\tilde{\chi}_1^0} \approx m_{\tilde{g}}/2$. This is due to the partitioning of the energy in the final state. For very large $m_{\tilde{\chi}_1^0}$, with $m_{\tilde{\chi}_1^0} < m_{\tilde{g}}$, the two quarks from the decay of the $\tilde{g}$ are very soft and the partons from the decay of the $\tilde{\chi}_1^0$ are relatively isotropic, slightly reducing the efficacy of the approach. For very low $m_{\tilde{\chi}_1^0}$, $m_{\tilde{\chi}_1^0} \ll m_{\tilde{g}}$, the opposite occurs: the two quarks from the gluino decay have very high $p_T$ and the neutralino is Lorentz-boosted, often to the point that the decay products merge completely, no longer overlapping with quarks from other parts of the event, and the mass of the jet is substantially reduced.\(^3\) In both cases, although the

\(^3\)While the complete merging of the decay products of a $\tilde{\chi}_1^0$ into a single jet may suggest that the most effective variable for low $m_{\tilde{g}}$ might be the jet mass itself, typically only the lightest $\tilde{\chi}_1^0$ have enough $p_T$ to be strongly collimated. Such jets thereby have very
sensitivity of $M_{\Sigma J}$ is reduced, the overall approach still maintains good sensitivity.

Another discriminating variable that is independent of $M_{\Sigma J}$ is necessary in order to define suitable control regions for the analysis. As in the jet-counting analysis, the signal is characterized by a considerably higher rate of central jet events as compared to the primary multi-jet background. This is expected due to the difference in the production processes that is predominantly $s$-channel for the signal, while the background can also be produced through $u$- and $t$-channel processes. Figure 6 additionally shows the distribution of the pseudorapidity difference between the two leading large-$R$ jets, $|\Delta \eta|$. The discrimination between the signal samples and the background is not nearly as significant for $|\Delta \eta|$ as for $M_{\Sigma J}$. However, the lack of significant correlation (Pearson linear correlation coefficient of approximately 1%) between the two observables makes $|\Delta \eta|$ effective as a means to define additional control regions in the analysis. It is also observed that the shape of the distribution is relatively independent of the $\tilde{g}$ and $\tilde{\chi}^0_1$ masses and mass splittings.

The ability of several other observables to discriminate between signal and background was also tested. In particular, the possibility of using more detailed information about the substructure of jets (e.g., the subjet multiplicity or observables such as $N$-subjettiness, $\tau_{32}$ [71, 72]) was investigated. Although some additional discrimination is possible using more observables, these significantly complicated the background estimation techniques and only marginally increase the sensitivity of the analysis.

low jet masses. These low jet masses similar to what is expected from QCD radiation, making discrimination very difficult, and so the nominal total-jet-mass technique is maintained even in these regions.
The key assumption in this approach is that the jet kinematics factorize and are independent of the other jets in the event. Deviations from this approximation may occur due to effects that are not included in the derivation of the jet mass templates. In particular, the composition of quarks and gluons can vary across different samples [73], and quark and gluon jets have been observed any input from MC simulation. A template method is adopted in which an expected \( M_{j}^{\Sigma} \) distribution is constructed using individual jet mass templates. Single-jet mass templates are extracted jet-by-jet from a signal-depleted 3-jet control region (3jCR), or training sample. These jet mass templates are binned in jet \( p_T \) and \( \eta \), which effectively provides a probability density function that describes the relative probability for a jet with a given \( p_T \) and \( \eta \) to have a certain mass. This template is randomly sampled 2500 times for a single jet \( p_T \) and \( \eta \), and a precise predicted distribution of possible masses for the given jet is formed.\(^4\) For an event with multiple jets, the jet mass templates are applied to each jet and the resulting predicted mass distributions are combined to predict the total-jet-mass \( M_{J}^{\Sigma} \) for that ensemble of jets.

Jet mass templates are applied to jets in events in orthogonal regions, typically with at least four large-\( R \) jets – the control (4jCR), validation (4jVR), and signal regions (4jSR) – but also in the 3jCR to test the method. Samples used in this way are referred to as the kinematic samples. The only information used is the jet \( p_T \) and \( \eta \), which are provided as inputs to the templates. The result is referred to as a dressed sample, which provides an SM prediction of the individual jet mass distributions for the jets in the kinematic sample. An SM prediction for the total-jet-mass can then be formed by combining the individual dressed jet mass distributions. The normalization of the \( M_{J}^{\Sigma} \) prediction – the dressed sample – is preserved such that the total expected yield is equal to the number of events in the kinematic sample. The procedure can be summarized as [69]:

1. Define a control region to obtain the training sample from which jet mass templates are to be constructed;
2. Derive a jet mass template binned in jet \( \eta \) and \( p_T \) using a smoothed Gaussian kernel technique;
3. Define a kinematic sample as either another control region or the signal region;
4. Convolve the jet mass template with the kinematic sample using only the jet \( p_T \) and \( \eta \);
5. Obtain a sample of dressed events which provides the data-driven background estimate of \( M_{J}^{\Sigma} \).

\(^4\)2500 times was found to be the best balance between the precision of the result and computational time.

\[ M_{j}^{\Sigma} \text{ for fixed } m_{\chi_{1}^{0}} = 175 \, \text{GeV} \]

\[ |\Delta \eta| \text{ for fixed } m_{\chi_{1}^{0}} = 175 \, \text{GeV} \]
to have different radial energy distributions [74]. Other experimental affects, arising from close-by or overlapping jets, can also have an effect. For this reason, extensive tests are performed in the 4jCR and 4jVR, as defined in Sec. VII B, to estimate the size of the correction factors needed to account for any sample dependence, and to assess systematic uncertainties. The entire procedure is tested first in SHERPA multi-jet MC simulation, which shows minimal differences between the template prediction and observed mass spectrum.

| Region   | $n_{\text{jet}}$ | $|\Delta \eta|$ | $p^3_T$ [GeV] | $p^4_T$ [GeV] | $M^2_\Sigma$ [GeV] |
|----------|------------------|-----------------|---------------|---------------|-------------------|
| 3jCR     | $n_{\text{jet}} = 3$ | -               | -             | -             | -                 |
| 4jCR     | $n_{\text{jet}} \geq 4$ | > 1.40          | > 100         | > 100         | -                 |
|          |                  | > 250           |               |               |                   |
| 4jVR     | $n_{\text{jet}} \geq 4$ | 1.0–1.40        | > 100         | > 100         | -                 |
|          |                  | > 250           |               |               |                   |
| SR1      | $n_{\text{jet}} \geq 4$ | < 0.7           | > 250         | > 625         |                   |
| SR100    | $n_{\text{jet}} \geq 4$ |                 | > 100         | > 100         | > 350 (binned)    |
| SR250    | $n_{\text{jet}} \geq 4$ |                 | > 250         | > 350 (binned)|                   |

Table I. Control (CR), validation (VR), and signal regions (SR) used for the analysis. $p^3_T$ and $p^4_T$ represent the transverse momentum of the third and fourth jet in $p_T$, respectively.

B. Signal and control region definitions

The $M^2_\Sigma$ and $|\Delta \eta|$ observables form the basis for the signal region definition for the analysis, where $|\Delta \eta|$ is used to define control regions for testing the background estimation in data. A requirement of $|\Delta \eta| < 0.7$ is found to have the best signal sensitivity over the entire plane of $(m_\tilde{g}, m_\chi^0)$. In this optimization, the background contribution is modeled by multi-jet events simulated with SHERPA.

An optimization study indicated that when using a single $M^2_\Sigma$ selection, $M^2_\Sigma > 625$ GeV provides the best sensitivity to many signal hypotheses, and gives the best expected sensitivity at high $m_\tilde{g}$. A single-bin signal region (SR1) is therefore defined with $M^2_\Sigma > 625$ GeV and a 250 GeV $p_T$ threshold applied to the third leading in $p_T$ large-$R$ jet. This region has an acceptance of 0.26% for the $m_\tilde{g} = 600$ GeV, $m_\chi^0 = 50$ GeV signal point. This acceptance grows rapidly with gluino mass to 11% for the point $m_\tilde{g} = 1000$ GeV, $m_\chi^0 = 600$ GeV, and is only weakly dependent on the neutralino mass.

A second set of signal regions is used to further improve the power of the analysis by making use of the shape of the $M^2_\Sigma$ distribution. Two selections on the third leading jet in $p_T$ ($p^3_T$) are used, $p^3_T > 100$ GeV (SR100) and $p^3_T > 250$ GeV (SR250). This provides better sensitivity to the full range of gluino masses considered, compared to SR1. The lower $p_T$ region, SR100, has better sensitivity for lower gluino masses, whereas SR250 has improved sensitivity for higher masses. All other selections are unchanged. In this case, a lower threshold of $M^2_\Sigma > 350$ GeV is used and the observed data are compared to the template predictions in bins of $M^2_\Sigma$. The improvements in the sensitivity obtained by adding these additional signal regions and using the shape of the $M^2_\Sigma$ spectrum are described below. The full set of selection criteria is listed in Tab. I.
the control regions is chosen to be larger than an inverse
4jVR. In the remaining control and validation regions,
the difference between template prediction and the data ob-
tained in the 4jCR is shown in green.

Figure 8. Total-jet-mass in the 4jSR (a) using \( p_T^3 > 100 \) GeV
(SR100) and (b) using \( p_T^3 > 250 \) GeV (SR250). For the SR100
selection, the reweighted template (built in the 3jCR, and
rewighted jet-by-jet in the 4jCR) is shown in the hatched
blue histogram. The total systematic uncertainty due to the
smoothing procedure, finite statistics in control regions, and
the difference between template prediction and the data ob-
served in the 4jCR is shown in green.

The jet multiplicity and \( |\Delta\eta| \) are used to define the
control regions. The 3jCR, with exactly three jets, is
used to train the background templates previously dis-
cussed. In the remaining control and validation regions,
each requiring \( \geq 4 \) jets, the \( |\Delta\eta| \) selection suppresses
the signal contribution and is used to define the 4jCR and
4jVR. In the \( \geq 4 \)-jet regions, the \( |\Delta\eta| \) selection value for
the control regions is chosen to be larger than an inver-
sion of the signal region selection, resulting in the selections
presented in Tab. I. These control region definitions
permit studies of the full \( M_T^2 \) spectrum as well as com-
parisons of data and SM predictions without significant
signal contamination.

C. Validation and systematic uncertainties

Many tests are performed using the 3jCR as both the
training sample and the kinematic sample in order to
determine the robustness of the method. The selection
requires that there be exactly three large-\( R \) jets in the
event, as described in Tab. I. The dependence of the tem-
plate on the jet in question (leading, subleading, etc) is
tested, as well as the dependence of the template on the
jet kinematics. It is determined that it is optimal to
define separate templates for each of the three jet cate-
gories (leading, subleading, and third jet) and to bin the
templates according to the jet \( p_T \) and \( \eta \).\(^5\) In the 4-jet
regions, the fourth jet uses the template derived for the
third jet in the 3jCR: tests in the 4jCR and 4jVR in-
dicate very good agreement between this template and
the observed spectrum. As a first test, the \( M_T^2 \) template
constructed from the 3-jet kinematic sample is compared
to the actual \( M_T^2 \) distribution in 3-jet events, and very
good agreement is observed.

There are two intrinsic sources of systematic uncer-
tainty associated with the template procedure: the uncer-
tainty due to finite statistics in the 3jCR training sample
(the variance), and the uncertainty due to the smooth-
ing procedure in the template derivation (the bias). The
former is estimated by generating an ensemble of \( M_T^2 \)
templates and taking the \( \pm 1\sigma \) deviations (defined as the
\( \pm 34\% \) quantile) with respect to the median of those vari-
ations as the uncertainty, bin by bin. The systematic un-
certainty due to the smoothing procedure is determined
using the fact that a Gaussian kernel smoothing is ap-
plied to the template. The full difference between the
nominal template and a template constructed using a
leading-order correction for the bias, derived analytically
in Ref. [69], is taken as the systematic uncertainty. The
systematic uncertainty due to finite control region statist-
ics is chosen to be larger (by setting the size of the kernel
smoothing) than that due to the smoothing procedure
since the former is more accurately estimated.

Figure 7 presents the total-jet-mass \( M_T^2 \) in the 4jVR
using \( p_T^3 > 100 \) GeV. A small level of disagreement is
observed when comparing the observed mass to the pre-
dicted mass in the 4jCR: a reweighting derived in the
4jCR (as a function of the jet mass) is then applied to
the individual jet masses prior to the construction of the
\( M_T^2 \) for each event. After the reweighting the agreement
is substantially improved at high total-jet-mass. The
rewighted template agrees very well with the observed

\(^5\)It is observed that the difference between the leading and sub-
leading jet templates is minimal, but that the third jet exhibits
qualitatively different masses as function of the jet \( p_T \).
$M_{\Sigma}^2$ distribution in the 4jVR, validating both the template method and the reweighting. The full magnitude of the reweighting on the total-jet-mass distribution is taken as a systematic uncertainty of the method. The total systematic on the background prediction therefore includes both the intrinsic systematic uncertainty given by the variance and the bias, as well as the difference observed in the 4jCR. The $M_{\Sigma}^2$ distribution is also shown for the 4jVR for the case in which $p_{T}^{1} > 250$ GeV. No reweighting is required when using the significantly higher $p_{T}^{1}$ selection since the observed effects due to topological differences in the training sample compared to the kinematic sample are suppressed. In order to account for any remaining disagreement, the difference between the data and template prediction in the 4jCR is applied as a further systematic. The total uncertainty therefore includes again both the intrinsic background estimation uncertainties and the disagreement observed in the 4jCR.

One possible concern for the template technique is that it assumes that the same mechanism is responsible for generating the individual jet masses in both the control and signal regions. In order to test the extent to which a different composition of processes may affect the derived templates, the assumption that multi-jet events are the only background in the 3jCR and 4j regions is modified by injecting separately a sample of SHHERPA $t\bar{t}$ MC simulation events (assuming SM cross-sections) into the full procedure. The resulting background estimates are fully consistent with the prediction without the injection – indicating that the technique is not sensitive to contamination from top quark production – and thus no additional systematic uncertainty is assessed for the potential presence of specific background processes. A similar procedure is performed for signal processes (assuming standard $g$ production cross-sections) and again no impact of signal contamination on the constructed background templates is observed.

Figure 8 shows the total-jet-mass in the 4jSR compared to the template prediction. For both SR100 and SR250, the total systematic error on the template method is also shown in the ratio plot in the lower panel of each distribution. The template predictions are clearly consistent with the observed data. Thus there is no indication of new physics in these results.

Systematic uncertainties associated with the scale and resolution of large- $R$ jet mass and energy [65] are significantly reduced by the use of a data-driven background estimate: residual effects may remain due to differences between the 3jCR and the 4j regions, and these are reflected in the systematic uncertainties assessed by the difference between the template prediction and observed spectrum in the 4jCR. The uncertainties due to the background estimation method are dominated by propagation of the statistical uncertainty from the 3jCR: these are typically 5–10%, except in the highest $M_{\Sigma}^2$ bins of SR100 and SR250, where they can extend to 20–40%. In addition, the observed difference systematic uncertainty from the 4jCR varies from 5% to 15%. Signal reconstruction – both in terms of selection efficiency and the $M_{\Sigma}^2$ spectrum predicted for a given $m_{\tilde{g}}, m_{\tilde{\chi}^{0}_{1}}$ combination – is sensitive to the kinematic uncertainties associated with the final state jets in the analysis. The impacts of these systematic uncertainties are directly assessed by varying the kinematics within the uncertainties and reported in Sec. VIII. Jet mass scale uncertainties have the largest effect, which for SR1 range from 30% for very low $m_{\tilde{g}}$ to 15% for very high $m_{\tilde{g}}$. In the cases of SR100 and SR250, the impact of the jet mass scale uncertainty also dominates, and varies across the $M_{\Sigma}^2$ spectrum from 10–20% at lower $M_{\Sigma}^2$ up to 50% for the very highest $M_{\Sigma}^2$ bin in the spectrum for low $m_{\tilde{g}}$. The luminosity uncertainty of 3% also affects the signal only.

VIII. RESULTS AND INTERPRETATIONS

As no significant excess is observed in data in either analysis, a procedure to set limits on the models of interest is performed. A profile likelihood ratio combining Poisson probabilities for signal and background is computed to determine the confidence level (CL) for consistency of the data with the signal-plus-background hypothesis (CL$_{s+b}$). A similar calculation is performed for the background-only hypothesis (CL$_{b}$). From the ratio of these two quantities, the confidence level for the presence of signal (CL$_{s}$) is determined [75]. Systematic uncertainties are treated via nuisance parameters assuming Gaussian distributions. In all cases, the nominal signal cross-section and uncertainty are taken from an envelope of cross-section predictions using different PDF sets and factorization and renormalization scales, as described in Ref. [76]. As discussed in Sec. IV, the region with $(m_{\tilde{g}} - m_{\tilde{\chi}^{0}_{1}}) < 100$ GeV is not considered in this analysis in order to ensure that the results are insensitive to the effects of ISR, since the uncertainties cannot be assessed for the UDD decays considered here.

The total-jet-mass analysis is designed to be agnostic to the flavor composition of the signal process and to remove any reliance on MC simulations of these complex hadronic final states. The jet-counting analysis provides the opportunity to enhance sensitivity to specific heavy-flavor compositions in the final state and to explore various assumptions on the branching ratios of the benchmark signal processes studied in this paper. The results obtained from the total-jet-mass analysis in the inclusive final state are presented first, and then the specific sensitivity provided by the jet-counting analysis to the full branching ratio space is presented.

A. Total-jet-mass analysis

The observed and expected event yields are presented in Tab. II, III, and IV for the three signal regions SR1, SR100 and SR250 respectively. The single-bin signal region selection (SR1) is reported in addition to the binned
Table II. Table showing the predicted in the SM and observed number of events in SR1 as well as three representative signal scenarios. Acceptances (including efficiency) of the various signals are listed in parentheses. The background uncertainties are displayed as statistical + systematic; the signal uncertainties are displayed as statistical + systematic + theoretical.

<table>
<thead>
<tr>
<th>$M_{ij}^2$ Bin</th>
<th>Expected SM</th>
<th>Obs.</th>
<th>$m_\tilde{g} = 600$ GeV $m_{\chi^0_i} = 50$ GeV</th>
<th>$m_\tilde{g} = 1$ TeV $m_{\chi^0_i} = 600$ GeV</th>
<th>$m_\tilde{g} = 1.4$ TeV $m_{\chi^0_i} = 900$ GeV</th>
</tr>
</thead>
<tbody>
<tr>
<td>&gt; 625 GeV</td>
<td>160±9.7 $^{+40}_{-34}$</td>
<td>176</td>
<td>200±2.2±22±35 (0.20%)</td>
<td>55±0.51±8.6±14 (11%)</td>
<td>6.3±0.07±0.46±2.5 (35%)</td>
</tr>
</tbody>
</table>

Table III. Table showing the predicted in the SM and observed number of events in SR100 as well as three representative signal scenarios. The background uncertainties are displayed as statistical + systematic; the signal uncertainties are displayed as statistical + systematic + theoretical.

Summary yield table for SR100

<table>
<thead>
<tr>
<th>$M_{ij}^2$ Bin</th>
<th>Expected SM</th>
<th>Obs.</th>
<th>$m_\tilde{g} = 600$ GeV $m_{\chi^0_i} = 50$ GeV</th>
<th>$m_\tilde{g} = 1$ TeV $m_{\chi^0_i} = 600$ GeV</th>
<th>$m_\tilde{g} = 1.4$ TeV $m_{\chi^0_i} = 900$ GeV</th>
</tr>
</thead>
<tbody>
<tr>
<td>350 - 400 GeV</td>
<td>4300±78 $^{+510}_{-500}$</td>
<td>5034</td>
<td>200±7.2±22±35 (0.20%)</td>
<td>5.8±0.17±1.3±1.5</td>
<td>0.19±0.01±0.04±0.07</td>
</tr>
<tr>
<td>400 - 450 GeV</td>
<td>2600±49 $^{+380}_{-380}$</td>
<td>2474</td>
<td>200±7.1±9.5±35 (0.20%)</td>
<td>9.7±0.21±2.2±2.5</td>
<td>0.31±0.02±0.07±0.12</td>
</tr>
<tr>
<td>450 - 525 GeV</td>
<td>2100±42 $^{+360}_{-360}$</td>
<td>1844</td>
<td>280±8.4±13±49 (0.20%)</td>
<td>26±0.35±4.3±6.7</td>
<td>0.88±0.03±0.14±0.34</td>
</tr>
<tr>
<td>525 - 725 GeV</td>
<td>960±25 $^{+200}_{-200}$</td>
<td>1070</td>
<td>280±8.4±57±49 (0.20%)</td>
<td>77±0.60±3.2</td>
<td>3.6±0.05±0.36±1.4</td>
</tr>
<tr>
<td>&gt; 725 GeV</td>
<td>71±7.0 $^{+32}_{-27}$</td>
<td>79</td>
<td>35±2.9±18±6.0 (0.20%)</td>
<td>35±0.40±9.9±9.0</td>
<td>4.8±0.06±0.61±1.9</td>
</tr>
</tbody>
</table>

Figure 9. Expected and observed exclusion limits in the $(m_\tilde{g}, m_{\chi^0_i})$ plane for the ten-quark model given by the total-jet-mass analysis. Limits are obtained by using the signal region with the best expected sensitivity at each point. The dashed black lines show the expected limits at 95% CL, with the light (yellow) bands indicating the 1σ excursions due to experimental and background-only theory uncertainties. Observed limits are indicated by medium dark (maroon) curves, where the solid contour represents the nominal limit, and the dotted lines are obtained by varying the signal cross-section by the renormalization and factorization scale and PDF uncertainties.

$M^2_{ij}$ results in SR100 and SR250 in order to provide yields that can be easily reinterpreted for other signal hypotheses. In the case of the binned $M^2_{ij}$ signal regions, a binned fit (where the number and size of the bins were optimized) is performed that takes into account the predictions for each $M^2_{ij}$ range. This approach provides greater sensitivity to small deviations from the template predictions. The correlation of the uncertainties in the bins of the $M^2_{ij}$ spectrum are accounted for by evaluating the full correlation matrix. The result leads the analysis to treat the different bins as fully uncorrelated for the variance, which is the largest component of the background uncertainties. All other uncertainties treat the bins of the $M^2_{ij}$ spectrum as fully correlated.

Figure 9 shows both the expected and observed 95% CL limits in the $(m_\tilde{g}, m_{\chi^0_i})$ mass plane when the signal region that provides the best expected exclusion is used for each mass combination. The dashed black line shows the expected exclusion limits, and the yellow band represents the experimental uncertainties on this limit. The solid line shows the observed limit, with the finely dashed lines indicating the ±σ variations due to theoretical uncertainties on the signal production cross-section given by renormalization and factorization scale and PDF uncertainties. All mass limits are reported conservatively assuming the $-1\sigma_{\text{theory}}$ signal production cross-section. At low $m_{\chi^0_i}$, the region with gluino mass $m_\tilde{g} \lesssim 750$ GeV is excluded. Excluded $m_\tilde{g}$ masses rise with increasing $m_{\chi^0_i}$, up to a maximum exclusion of approximately $m_\tilde{g} \lesssim 870$ GeV at $m_{\chi^0_i} = 600$ GeV. No models with $m_{\chi^0_i} > 650$ GeV are excluded.
Table IV. Table showing the predicted in the SM and observed number of events in SR250 as well as three representative signal scenarios. The background uncertainties are displayed as statistical + systematic; the signal uncertainties are displayed as statistical + systematic + theoretical.

Figure 10. Expected and observed cross-section limits for the six-quark gluino models for (a) the case where no gluinos decay into heavy-flavor quarks, and (b) the case where every gluino decays into a b-quark in the final state.

Figure 11. Expected and observed cross-section limits for the six-quark gluino models for (a) the case where each gluino is required to decay into a top quarks, and (b) the case where every gluino decays into a b-quark and a top quark.
Figure 12. Expected and observed mass exclusions at the 95% CL in the BR($t$) vs. BR($b$) space for BR($c$)=0%. Each point in this space is individually optimized and fit. Masses below these values are excluded in the six-quark model. Bin centers correspond to evaluated models.

B. Jet-counting analysis

In order to set limits on individual branching ratios, it is necessary to refer to the structure of the couplings that are allowed. From Eq. (1), it is clear that each RPV decay produces exactly two down-type quarks of different flavor and one up-type quark. Since the cross-section for gluino production is not dependent upon the $\lambda''_{ijk}$ parameters, it is not possible to directly probe or set limits upon any individual $\lambda''_{ijk}$ parameter. Instead, results are categorized based upon the probability for an RPV decay to produce a $t$-quark, a $b$-quark, or a $c$-quark. These branching ratios are denoted by BR($t$), BR($b$), and BR($c$), respectively. These branching ratios are partially constrained. The branching ratios for decays including $u$-, $c$-, and $t$-quarks (all given by the flavor index $i$ in the $\lambda''_{ijk}$ couplings) must sum to one and must therefore satisfy $\text{BR}(t) + \text{BR}(c) \leq 1$. The branching ratios to decays including each down-type quark (as given by the flavor indices $j$ and $k$ in the $\lambda''_{ijk}$ couplings) are independent of the up-type branching ratios. At most, one $b$-quark can be produced in such an RPV decay. Simultaneous nonzero $\lambda''_{ijk}$ values can result in nontrivial branching ratio combinations.

Results using the jet-counting analysis are determined for different hypotheses on the branching ratios of RPV
decays to \( t, b, c \), and light-flavor quarks. The selection requirements for the signal regions are optimized separately for each of these hypotheses. When running the optimization, the full limit-setting procedure is performed under the assumption that the expected number of background events is observed in the data, taking all statistical and systematic uncertainties into account. The results of this optimization are provided in Tab. \( V \). The first portion of Tab. \( V \) shows the optimization results and the comparison of the data with background predictions for the six-quark signal models under the assumption that \( (\text{BR}(t), \text{BR}(b), \text{BR}(c))=(0\%, 0\%, 0\%) \). In this simple model, it is equivalent to say that only the term given by \( \lambda_{ij}^{ij} \) being nonzero. Explicitly, this flavor hypothesis forces the RPV decays to result only in light quarks. Below this, the table shows the same comparisons under the assumption that \( (\text{BR}(t), \text{BR}(b), \text{BR}(c))=(0\%, 100\%, 0\%) \) corresponding to only RPV terms given by \( \lambda_{ij}^{ij} \) and \( \lambda_{ij}^{ij} \). The second half of Tab. \( V \) is analogous to the first, only with \( \text{BR}(t)=100\% \). The signal acceptance is largely affected by \( \text{BR}(t) \) and \( \text{BR}(b) \) due to the presence of signal regions with \( b \)-tagged jets. Because this search requires many high-\( p_T \) jets, increased \( \text{BR}(t) \) results in a lower.
acceptance from larger energy sharing in a higher multiplicity of final state objects. For this reason, the corners of the BR(\(t\)) vs. BR(\(b\)) space are shown here. Since the sensitivity to increased BR(\(c\)) comes from \(b\)-tagging configurations that are designed to efficiently select \(b\)-jets, the effect on the signal acceptance is dominated by BR(\(b\)). For this reason, the focus of this discussion is on the BR(\(b\)) degree of freedom. However, several results with various values of BR(\(c\)) are presented below.

The results of performing the limit-setting procedure on the data in the signal regions are shown in Fig. 10 and 11 for various flavor branching ratio hypotheses as a function of gluino mass for the six-quark model. These results show both the expected and observed cross-section limits in comparison to the predicted cross-section from the theory. Under the assumption that all RPV decays are to light-flavor quarks (BR(\(b\))=BR(\(t\))=BR(\(c\))=0%), gluino masses of \(m_{\tilde{g}} < 853\) GeV (expected) and \(m_{\tilde{g}} < 917\) GeV (observed) are excluded at the 95% CL. Alternatively for the scenario where BR(\(b\))=100% while the other heavy-flavor branching ratios are zero, exclusions of \(m_{\tilde{g}} < 921\) GeV (expected) and \(m_{\tilde{g}} < 929\) GeV (observed) are found. Similarly, for the case where BR(\(b\))=BR(\(t\))=100%, exclusions of \(m_{\tilde{g}} < 938\) GeV (expected) and \(m_{\tilde{g}} < 874\) GeV (observed) are found. More generally, excluded masses as a function of the branching ratios of the decays are presented in Fig. 12 and 13 where each bin shows the maximum gluino mass that is excluded for the given decay mode.

The event selection is optimized separately for the ten-quark model. Table VI shows the results for the ten-quark model with all UDD couplings allowed, as in the total-jet-mass analysis, when the number of \(b\)-tagged jets is also used as a variable in the optimization procedure. For the flavor-agnostic model where all couplings are equal, Fig. 14(a) shows both the expected and observed limits in the \((m_{\tilde{g}}, m_{\tilde{\chi}_1^0})\) mass plane when the signal region that provides the best expected exclusion is used for each mass point, not including signal regions containing \(b\)-tagged jets. The shapes of the contours are given by discontinuous changes in the optimized signal regions and fluctuations well within the given uncertainties. At \(m_{\tilde{\chi}_1^0} \sim 100\) GeV, models with \(m_{\tilde{g}} \lesssim 700\) GeV are excluded. Figure 14(b) shows the exclusion when signal regions with \(b\)-tagged jets are considered as part of the optimization and increase the sensitivity up to \(m_{\tilde{g}} \lesssim 1\) TeV for moderate \(m_{\tilde{g}} - m_{\tilde{\chi}_1^0}\) mass splittings. In the ten-quark model, there is a significant probability that the cascade decays of the gluinos produce at least one \(b\)- or \(t\)-quark, and so the requirement of a \(b\)-tagged jet improves the sensitivity of the analysis.

### C. Comparisons

Model-independent upper limits on non-SM contributions are derived separately for each analysis, using the SR1 signal region for the total-jet-mass analysis. A generic signal model, which contributes only to the sig-

<table>
<thead>
<tr>
<th>Sample ((m_{\tilde{g}}, m_{\tilde{\chi}_1^0}))</th>
<th>Jet (p_T) req.</th>
<th># jets</th>
<th># (b)-tagged jets</th>
<th>Signal (Acceptance)</th>
<th>Background</th>
<th>Data</th>
</tr>
</thead>
<tbody>
<tr>
<td>((400) GeV, (50) GeV)</td>
<td>80</td>
<td>7</td>
<td>2</td>
<td>1900±400 (0.5%)</td>
<td>1670±190</td>
<td>1558</td>
</tr>
<tr>
<td>((400) GeV, (300) GeV)</td>
<td>80</td>
<td>7</td>
<td>2</td>
<td>2500±600 (0.7%)</td>
<td>1670±290</td>
<td>1558</td>
</tr>
<tr>
<td>((600) GeV, (50) GeV)</td>
<td>120</td>
<td>7</td>
<td>1</td>
<td>180±40 (0.7%)</td>
<td>138±26</td>
<td>178</td>
</tr>
<tr>
<td>((600) GeV, (300) GeV)</td>
<td>80</td>
<td>7</td>
<td>2</td>
<td>2200±350 (8.3%)</td>
<td>1670±300</td>
<td>1558</td>
</tr>
<tr>
<td>((800) GeV, (50) GeV)</td>
<td>120</td>
<td>7</td>
<td>1</td>
<td>95±16 (3.0%)</td>
<td>138±26</td>
<td>178</td>
</tr>
<tr>
<td>((800) GeV, (300) GeV)</td>
<td>120</td>
<td>7</td>
<td>1</td>
<td>172±28 (5.4%)</td>
<td>138±26</td>
<td>178</td>
</tr>
<tr>
<td>((1000) GeV, (50) GeV)</td>
<td>220</td>
<td>6</td>
<td>1</td>
<td>7.0±1.3 (1.4%)</td>
<td>3.8±3.0</td>
<td>5</td>
</tr>
<tr>
<td>((1000) GeV, (300) GeV)</td>
<td>120</td>
<td>7</td>
<td>1</td>
<td>67±8 (14%)</td>
<td>138±26</td>
<td>178</td>
</tr>
<tr>
<td>((1000) GeV, (600) GeV)</td>
<td>120</td>
<td>7</td>
<td>1</td>
<td>101±13 (20%)</td>
<td>138±26</td>
<td>178</td>
</tr>
<tr>
<td>((1000) GeV, (900) GeV)</td>
<td>120</td>
<td>7</td>
<td>1</td>
<td>33±4 (6.7%)</td>
<td>138±26</td>
<td>178</td>
</tr>
<tr>
<td>((1200) GeV, (50) GeV)</td>
<td>220</td>
<td>6</td>
<td>1</td>
<td>3.8±0.7 (4.3%)</td>
<td>3.8±3.0</td>
<td>5</td>
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<tr>
<td>((1200) GeV, (300) GeV)</td>
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<td>7</td>
<td>1</td>
<td>2.01±0.32 (2.3%)</td>
<td>2.3±1.0</td>
<td>1</td>
</tr>
<tr>
<td>((1200) GeV, (600) GeV)</td>
<td>140</td>
<td>7</td>
<td>1</td>
<td>18.9±2.3 (21%)</td>
<td>41±12</td>
<td>45</td>
</tr>
<tr>
<td>((1200) GeV, (900) GeV)</td>
<td>140</td>
<td>7</td>
<td>1</td>
<td>12.6±1.5 (14%)</td>
<td>41±12</td>
<td>45</td>
</tr>
</tbody>
</table>

Table VI. Requirements as optimized for the ten-quark model under a variety of mass hypotheses when all \(\lambda^v\) couplings are nonzero and equal and \(b\)-tagging requirements are considered as part of the optimization procedure. The optimized signal region selection requirements are shown along with the resulting background and signal expectations and the number of observed data events. The nominal signal acceptance (including efficiency) is also shown for each result. Quoted errors represent both the statistical and systematic uncertainties added in quadrature.
Table VII. Table showing upper limits on the number of events and visible cross sections in various signal regions. Columns two and three show the expected and observed numbers of events. The uncertainties on the expected yields represent systematic and statistical uncertainties. Column four shows the probabilities, represented by the $p_0$ values, that the observed numbers of events are compatible with the background-only hypothesis (the $p_0$ values are obtained with pseudo-experiments). Columns five and six show respectively the expected and observed 95% CL upper limit on non-SM events ($N_{\text{non-SM}}$), and columns seven and eight show respectively the 95% CL upper limit on the visible signal cross-section ($\sigma_{\text{vis}} = \sigma_{\text{prod}} \times A \times \epsilon = N_{\text{non-SM}} / \mathcal{L}$). In the case where $N_{\text{expected}}$ exceeds $N_{\text{observed}}$, $p_0$ is set to $\geq 0.5$.

The interpretations of the results of the jet-counting and total-jet-mass analyses are displayed together in Fig. 15 for the ten-quark model. This figure allows for the direct comparison of the results of the various analyses. Without $b$-tagging requirements, the jet-counting analysis sets slightly lower expected limits than the total-jet-mass analysis. With $b$-tagging requirements, the limits are stronger for the jet-counting analysis. The observed limits from the total-jet-mass analysis and jet-counting analysis with $b$-tagging requirements are also comparable.

IX. CONCLUSIONS

A search is presented for heavy particles decaying into complex multi-jet final states using an integrated luminosity of $20.3 \pm 0.6 \text{ fb}^{-1}$ of $\sqrt{s} = 8 \text{ TeV}$ $pp$ collisions with the ATLAS detector at the LHC. Two strategies are used for both background estimation and signal discrimination. An inclusive data-driven analysis using the total-jet-mass with a template method for background estimation is performed as well as a jet-counting analysis that includes exclusive heavy-flavor signal regions and provides limits on different branching ratios for the benchmark SUSY RPV UDD decays. For the ten-quark model, results from both analyses are presented with comparable conclusions. When the jet-counting analysis includes sensitivity to heavy flavor given by $b$-tagging requirements, mass exclusions are further increased.

Exclusion limits at the 95% CL are set extending up to $m_{\tilde{g}} = 917 \text{ GeV}$ in the case of pair-produced gluino decays to six light quarks and up to $m_{\tilde{\chi}_1^0} = 1 \text{ TeV}$ in the case of cascade decays to ten quarks for moderate $m_{\tilde{g}} - m_{\tilde{\chi}_1^0}$ mass splittings. Limits are also set on different branching ratios by accounting for all possible decay modes allowed by the $\lambda_{ijk}$ couplings in full generality in the context of $R$-parity.
parity-violating supersymmetry. These results represent the first direct limits on many of the models considered as well as the most stringent direct limits to date on those models previously considered by other analyses.

ACKNOWLEDGMENTS

We thank CERN for the very successful operation of the LHC, as well as the support staff from our institutions without whom ATLAS could not be operated efficiently.

We acknowledge the support of ANPCyT, Argentina; YerPhI, Armenia; ARC, Australia; BMWFW and FWF, Austria; ANAS, Azerbaijan; SSTC, Belarus; CNPq and FAPESP, Brazil; NSERC, NRC and CFI, Canada; CERN; CONICYT, Chile; CAS, MOST and NSFC, China; COLCIENCIAS, Colombia; MSMT CR, MPO CR and VSC CR, Czech Republic; DNRF, DNRSC and Lundbeck Foundation, Denmark; EPLANET, ERC and NSRF, European Union; IN2P3-CNRS, CEADSM/IRFU, France; GNSF, Georgia; BMBF, DFG, HGF, MPG and AvH Foundation, Germany; GSRT and NSRF, Greece; RGC, Hong Kong SAR, China; ISF, MINERVA, GIF, I-CORE and Benoziyo Center, Israel; INFN, Italy; MEXT and JSPS, Japan; CNRST, Morocco; FOM and NWO, Netherlands; BRF and RCN, Norway; MNISW and NCN, Poland; GRICES and FCT, Portugal; MNE/IFA, Romania; MES of Russia and ROSATOM, Russian Federation; JINR; MSTD, Serbia; MSSR, Slovakia; ARRS and MIZS, Slovenia; DST/NRF, South Africa; MINECO, Spain; SRC and Wallenberg Foundation, Sweden; SER, SNSF and Cantons of Bern and Geneva, Switzerland; NSC, Taiwan; TAEK, Turkey; STFC, the Royal Society and Leverhulme Trust, United Kingdom; DOE and NSF, United States of America.

The crucial computing support from all WLCG partners is acknowledged gratefully, in particular from CERN and the ATLAS Tier-1 facilities at TRIUMF (Canada), NDGF (Denmark, Norway, Sweden), CC-IN2P3 (France), KIT/GridKA (Germany), INFN-CNAF (Italy), NL-T1 (Netherlands), PIC (Spain), ASGC (Taiwan), RAL (UK) and BNL (USA) and in the Tier-2 facilities worldwide.

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