I. INTRODUCTION

This paper reports the results of a search for photons originating from a displaced vertex due to the decay of a neutral long-lived particle into a photon and an invisible particle. The search exploits the capabilities of the ATLAS liquid-argon (LAr) electromagnetic (EM) calorimeter to make precise measurements of the flight direction and the time of flight of photons. The analysis uses the full data sample of 8 TeV proton-proton ( pp ) collisions collected in 2012 with the ATLAS detector at the LHC, corresponding to an integrated luminosity of 20.3 fb$^{-1}$. The method used is an evolution of the ATLAS nonpointing photon analysis [1] using the full 2011 data sample of 7 TeV pp collisions, corresponding to an integrated luminosity of 4.8 fb$^{-1}$. This previous analysis based on 7 TeV pp collisions found no excess above the Standard Model (SM) background expectation.

Scenarios where neutral long-lived particles are produced in pairs arise naturally, for example, within models of supersymmetry (SUSY) [2–10]. SUSY predicts the existence of a new SUSY partner (sparticle) for each of the SM particles, with identical quantum numbers except differing by half a unit of spin. In R-parity-conserving SUSY models [11–15], pp collisions at the LHC could produce these sparticles in pairs, and they would then decay in cascades involving other sparticles and SM particles until the lightest SUSY particle (LSP) is produced, which is stable. This analysis investigates the diphoton plus large $E_T^{\text{miss}}$ final state, where $E_T^{\text{miss}}$ is the magnitude of the missing transverse momentum, and is therefore most sensitive to the pair production of long-lived particles.

In gauge-mediated supersymmetry breaking (GMSB) models [16–21], the gravitino ($\tilde{G}$) is the LSP and is predicted, for typical model parameter values, to be very light. While the recent discovery of a Higgs boson with a mass around 125 GeV [22,23] disfavors minimal GMSB within reach of the LHC, modifications to minimal GMSB can easily accommodate this Higgs mass value without changing the particle masses [24–26]. GMSB phenomenology is largely determined by the properties of the next-to-lightest supersymmetric particle (NLSP), since the decay chains of the sparticles with higher mass would terminate in the decay of the NLSP. Very weak coupling of the NLSP to the gravitino could lead to displaced decay vertices of the NLSP [20]. The NLSP lifetime ($\tau$) depends on the fundamental scale of SUSY breaking [27,28], and therefore provides important information about the SUSY-breaking mechanism.

The results of this analysis are presented within the context of the so-called Snowmass Points and Slopes parameter set 8 (SPS8) [29], which describes a set of minimal GMSB models with the lightest neutralino ($\tilde{\chi}^0_1$) as the NLSP. The free parameter in the GMSB SPS8 set of models is the effective scale of SUSY breaking, denoted $\Lambda$, which depends on details of how the SUSY breaking is communicated to the messenger sector of the theory.

For $\Lambda$ values below about 100 TeV, strong production of pairs of squarks and/or gluinos make a significant contribution to the production rate of SUSY events at the LHC. However, for most of the range of $\Lambda$ values relevant for this analysis.
analysis, SUSY production is dominated by electroweak pair production of gauginos, and in particular of \(\tilde{\chi}^0_2\tilde{\chi}^+_1\) and \(\tilde{\chi}^0_1\tilde{\gamma}\) pairs.

In the GMSB SPS8 models, the dominant decay mode of the NLSP is \(\tilde{\chi}^0_1 \rightarrow \gamma + \tilde{G}\), leading to a \(\gamma \gamma + E^{\text{miss}}_T + X\) final state, where the escaping gravitinos give rise to \(E^{\text{miss}}_T\), and \(X\) represents SM particles produced in the decay cascades. To minimize the dependence of the results on the details of the SUSY decays, the analysis requires only a pair of photons and large \(E^{\text{miss}}_T\), avoiding explicit requirements on the presence of leptons or jets or any other particular SM particles in the final state.

This analysis considers the scenario where the NLSP has a finite lifetime, at least 250 ps, and travels partway through the ATLAS detector before decaying. In the range of \(\Lambda\) values of interest, about 80–300 TeV, the NLSP mass lies in the range of about 120–440 GeV. In this case, the photons produced in the NLSP decays can either be “nonpointing” or “delayed” or both; namely, the photons can have flight paths that do not point back to the primary vertex (PV) of the event and arrive times at the calorimeter that are later than those expected for a photon produced promptly at the PV.

The search for nonpointing and delayed photons is performed using the excellent performance of the finely segmented LAr EM calorimeters. An EM shower produced by a photon is measured precisely with varying lateral segmentation in three different longitudinal (i.e. depth) segments, allowing a determination of the flight direction of the photon from the EM shower measurements. The flight direction can then be compared with the direction back toward the PV identified for the event. This method is employed to determine the value of the pointing-related variable used, namely \(\Delta z_\gamma\), defined as the separation, measured along the beam line, between the extrapolated origin of the photon and the position of the selected PV of the event. The LAr calorimeter also has excellent time resolution and the arrival time \(t_\gamma\) of a photon at the calorimeter (with zero defined as the expected value for a prompt photon from the hard collision) is also a sensitive measure, since positive and finite time values would be expected for photons arising from nonprompt NLSP decays.

In the 7 TeV analysis [1], the pointing measurement was used to extract the result, with the time measurement used only qualitatively as a cross-check. The 7 TeV analysis set exclusion limits within the context of GMSB SPS8 models and similar results were obtained in a CMS analysis [30] of their full 7 TeV data set, but investigating a final state with at least one photon, at least three jets, and \(E^{\text{miss}}_T\). The current analysis utilizes both the pointing and time measurements. As described in Sec. VII, the current analysis divides the sample into six exclusive categories, according to the value of \(\Delta z_\gamma\), and then simultaneously fits the \(t_\gamma\) distributions of each of the categories to determine the possible contribution from signal. The use of both variables greatly improves the sensitivity.

II. THE ATLAS DETECTOR

The ATLAS detector [31] covers nearly the entire solid angle around the collision point and consists of an inner tracking detector surrounded by a solenoid, EM and hadronic calorimeters, and a muon spectrometer incorporating three large toroidal magnet systems. The inner-detector system (ID) is immersed in a 2 T axial magnetic field, provided by a thin superconducting solenoid located before the calorimeters, and provides charged-particle tracking in the pseudorapidity range |\(\eta\)| < 2.5. The ID consists of three detector subsystems, beginning closest to the beam line with a high-granularity silicon pixel detector, followed at larger radii by a silicon microstrip tracker and then a straw-tube-based transition radiation tracker. The ID allows an accurate reconstruction of tracks from the primary pp collision and precise determination of the location of the PV.

This analysis relies heavily on the capabilities of the ATLAS calorimeter system, which covers the pseudorapidity range |\(\eta\)| < 4.9. Finely segmented lead/LAr EM sampling calorimeters cover the barrel (|\(\eta\)| < 1.475) and end cap (1.375 < |\(\eta\)| < 3.2) regions. An additional thin LAr presampler covering |\(\eta\)| < 1.8 allows corrections for energy losses in material upstream of the EM calorimeters. Hadronic calorimetry is provided by a steel/scintillator-tile calorimeter, segmented into three barrel structures within |\(\eta\)| < 1.7, and two copper/LAr hadronic end cap calorimeters. The solid angle coverage is completed with forward copper/LAr and tungsten/LAr calorimeter modules, optimized for EM and hadronic measurements, respectively. Outside the calorimeters lies the muon spectrometer, which identifies muons and measures their deflection up to |\(\eta\)| = 2.7 in a magnetic field generated by superconducting air-core toroidal magnet systems.

A. Pointing resolution

For |\(\eta\)| < 2.5, the EM calorimeter is segmented into three layers in depth that are used to measure the longitudinal profile of the shower. The first layer uses highly granular “strips” segmented in the \(\eta\) direction, designed to allow efficient discrimination between single photon showers and two overlapping showers, the latter originating, for example, from the decay of a \(\pi^0\) meson. The second layer...
search for nonpointing and delayed photons in...  

PHYSICAL REVIEW D 90, 112005 (2014)

Pointing Resolution [mm]  

FIG. 1 (color online). The pointing resolution (defined as the resolution of \(z_{\text{origin}}\)) obtained for EM showers in the LAr EM barrel calorimeter. The pointing resolution for photons from GMSB SPS8 signal MC samples is plotted as a function of \(|z_{\text{origin}}|\). The pointing resolution is also shown for \(Z \rightarrow ee\) data and MC events, for which the PV position, \(z_{\text{PV}}\), serves the role of \(|z_{\text{origin}}|\).

nominal center of the detector serves the role of \(z_{\text{origin}}\). In this case, the pointing resolution is obtained by fitting to a Gaussian the difference between \(z_{\text{PV}}\), obtained from reconstructed tracks, and the calorimeter measurement of the origin along the beam line of the electron. Figure 1 shows that a similar pointing performance is observed for photons and for electrons, as expected given their similar EM shower developments. This similarity validates the use of a sample of electrons from \(Z \rightarrow ee\) events to study the pointing performance for photons. The expected pointing performance for electrons in a MC sample of \(Z \rightarrow ee\) events is also shown on Fig. 1, and is consistent with the data. The level of agreement between MC simulation and data over the range of values that can be accessed in the data gives confidence in the extrapolation using MC simulation to the larger \(|z_{\text{origin}}|\) values characteristic of signal photons.

B. Time resolution

Photons from long-lived NLSP decays would reach the LAr calorimeter with a slight delay compared to prompt photons produced directly in the hard scatter. This delay results mostly from the flight time of the heavy NLSP, which would have a distribution of relativistic speed \((\beta = v/c)\) that peaks typically near 0.9 and has a tail to much lower values. In addition, the opening angle in the NLSP decay, which causes the photon to be nonpointing,
results in a longer geometrical path to the calorimeter, as compared to a prompt photon from the PV.

The EM calorimeter, with its novel “accordion” design, and its readout, which incorporates fast shaping, has excellent time resolution. Quality-control tests during production of the electronics required the clock jitter on the LAr readout boards to be less than 20 ps, with typical values of 10 ps [32]. Calibration tests of the overall electronic readout performed in situ in the ATLAS cavern show a time resolution of ≈70 ps [33], limited not by the readout but by the jitter of the calibration pulse injection system. Test-beam measurements [34] of EM barrel calorimeter modules demonstrated a time resolution of ≈100 ps in response to high-energy electrons.

The LAr energy and time for each calorimeter cell are reconstructed by applying the optimal filtering algorithm [35] to the set of five samples of the signal shape read out for each calorimeter channel, with successive samples on the waveform separated by 25 ns. More specifically, the deposited energy per cell and the time of the deposition are calculated using appropriately weighted linear combinations of the set of samples of the waveform:

\[
E = \sum_{i=0}^{4} a_i S_i \quad \text{and} \quad t = \frac{1}{E} \sum_{i=0}^{4} b_i S_i,
\]

where \( S_i \) denotes the five samples of the signal waveform. The parameters \( a_i \) and \( b_i \) are the optimal filter coefficients (OFC), the values of which are calculated, knowing the pulse shape and noise autocorrelation matrix, to deliver the best energy and time resolutions.

For this analysis, the arrival time of an EM shower is measured using the second-layer EM calorimeter cell with the maximum energy deposit. For the EM shower of an electron or photon with energy within the range of interest, this cell typically contains about 20%–50% of the total energy deposited in the EM shower. In principle, the times measured in neighboring cells could be used in a weighted time calculation to try to further improve the precision. However, some studies that investigated more complicated algorithms found no improvement in time resolution, likely due to the pulse shapes in the channels with lower deposited energies suffering some distortion due to crosstalk effects.

During 2012, the various LAr channels were timed-in online with a precision of order 1 ns. A large sample of \( W \rightarrow e\nu \) events in the 8 TeV data set was used to determine calibration corrections that need to be applied to optimize the time resolution for EM clusters. The calibration includes corrections of various offsets in the time of individual channels, corrections for the energy dependence of the time measurement, crosstalk corrections, and flight-path corrections depending on the PV position.

To cover the full dynamic range of physics signals of interest, the ATLAS LAr calorimeter readout boards [32] employ three overlapping linear gain scales, dubbed High, Medium and Low, where the relative gain is reduced by a factor of about ten for each successive scale. For a given event, any individual LAr readout channel is digitized using the gain scale that provides optimal energy resolution, given the energy deposited in that calorimeter cell. The calibration of the time was determined separately for High and Medium gain for each channel. The number of electron candidates from the \( W \rightarrow e\nu \) sample that were digitized using Low gain was insufficient to obtain statistically precise results for the calibration constants. Therefore, the analysis requires that selected photons be digitized using either High or Medium gain resulting in a loss in signal efficiency, which ranges from much less than 1%, for the lowest \( \Lambda \) values probed, to less than 5% for the highest \( \Lambda \) values. The majority of signal photons are digitized using Medium gain, the fraction rising with rising \( \Lambda \) from about 60% to about 90%, over the \( \Lambda \) range of interest.

An independent sample of \( Z \rightarrow ee \) events was used to validate the time calibration and determine the resolution obtained, by performing Gaussian fits to the time distributions in bins of cell energy. Figure 2 shows the time resolution for High and Medium gain cells with \( |\eta| < 0.4 \), as a function of the energy in the second-layer calorimeter cell used to calculate the time for the sample of \( Z \rightarrow ee \).
events. Similar results are obtained over the full coverage of the EM calorimeter.

The time resolution, \( \sigma(t) \), is expected to follow the form \( \sigma(t) = p_0/E \oplus p_1 \), where \( E \) is the cell energy, \( \oplus \) indicates addition in quadrature, and the fit parameters \( p_0 \) and \( p_1 \) are the coefficients of the so-called noise term and constant term, respectively. Superimposed on Fig. 2 are the results of fits to this expected form of the time resolution function. The fits yield values of \( p_1 \), which gives the time resolution in the limit of large energy deposits, of 256 ps (299 ps) for High (Medium) gain. The somewhat worse results for Medium gain are due to limited statistics in the \( W \rightarrow ev \) sample used to determine the time calibration constants. The time resolution includes a contribution of \( \approx220 \) ps, which is caused by the time spread in \( pp \) collisions for a given PV position due to the LHC bunch-spread along the beam line. Subtracting this contribution in quadrature implies the LAr contributions to the time resolution are \( \approx130 \) ps (\( \approx200 \) ps) for high (medium) gain.

The time resolution is not modeled properly in the MC simulation of the ATLAS detector and it is necessary to apply additional smearing to the MC events in order to match the time performance observed in data. To smear the MC events, the fits to the time resolution determined from \( Z \rightarrow ee \) data as a function of the energy of the most energetic cell in the second layer are used. The fits are parameterized in terms of the pseudorapidity of the cell and the gain scale used to reconstruct the time. To account for the impact of the beam-spread, the smearing includes a component with a Gaussian standard deviation of 220 ps that is applied in a correlated way to all photons in the same event. In addition, an uncorrelated component is applied separately to each photon to match its overall time resolution to that observed in data.

C. Measurements of delayed particles

The OFC values in Eq. (1) deviate from being optimal for signals that are early or delayed with respect to the time used to determine the OFC values. This effect can cause the reconstructed values of the energy and time to deviate from their true values.

A source of early and delayed particles can be obtained using so-called satellite bunches of protons that, due to the radio-frequency structure of the LHC accelerator and injection complex, are present in the LHC beams but separated from the main bunches by multiples of \( \pm5 \) ns. A study was made using \( W \rightarrow ev \) and \( Z \rightarrow ee \) events produced in collisions between pairs of such satellite bunches that occur at the center of the detector but are \( 5 \) ns early or late, compared to nominal collisions. These “satellite–satellite” collisions are suppressed in rate by a factor of about one million compared to collisions of the nominal bunches, since the typical population of a satellite bunch is about a factor of one thousand lower than that of the nearby nominal bunch. However, the 8 TeV data sample is sufficiently large that a statistically significant observation of these satellite–satellite collisions could be made.

The values of the mean times reconstructed for electrons produced in satellite–satellite collisions were determined to be \( \approx -5.1 \) ns (\( \approx 5.4 \) ns), for events that occurred \( 5 \) ns early (late), demonstrating that the use of fixed OFC values causes a bias for signals that are sufficiently early or late compared to the nominal time. In contrast to the time reconstruction, the studies show that the reconstructed energies are very insensitive to modest time shifts of the samples on the waveform, as expected due to the methods used to calculate the OFC values used in the energy calculation. For time shifts within \( \pm5 \) ns of the nominal time, the reconstructed energy decreases by less than 1%.

III. DATA AND MONTE CARLO SIMULATION SAMPLES

This analysis uses the full data set of \( pp \) collision events at a center-of-mass energy of \( \sqrt{s} = 8 \) TeV, recorded with the ATLAS detector in 2012. The data sample, after applying quality criteria that require all ATLAS sub-detector systems to be functioning normally, corresponds to a total integrated luminosity of 20.3 fb\(^{-1}\).

While all background studies, apart from some cross-checks, are performed with data, MC simulations are used to study the response to GMSB signal models, as a function of the free parameters \( \Lambda \) and \( \tau \). The other GMSB parameters are fixed to the following SPS8 model values: the messenger mass \( M_{\text{mess}} = 2 \Lambda \), the number of SU(5) messengers \( N_5 = 1 \), the ratio of the vacuum expectation values of the two Higgs doublets \( \tan \beta = 15 \), and the Higgs-sector mixing parameter \( \mu > 0 \) [29].

The full GMSB SPS8 SUSY mass spectra, branching fractions and decay widths are calculated from this set of parameters using ISAJET [36] version 7.80. The HERWIG++ generator, version 2.4.2 [37], was used to generate the signal MC samples, with MRST 2007 LO\(^{a} \) [38] parton density distributions (PDF). A total of 30 signal points, from \( \Lambda = 70 \) TeV to \( \Lambda = 400 \) TeV, were generated, with \( \tau \) values of 2 ns or 6 ns. For each signal point, 40,000 inclusive GMSB SUSY events were simulated. For each sample, the NLSP was forced to decay to a photon and gravitino, with the branching fraction \( BR(\tilde{\chi}_1^0 \rightarrow \gamma \tilde{G}) \) fixed to unity. Other \( \tau \) values were simulated by appropriately reweighting the events of these generated samples, with weights related to the decay times of the neutralinos, to mimic the expected decay time distributions.

Signal cross sections are calculated to next-to-leading order (NLO) in the strong coupling constant using PROSPINO2 [39].\(^2\) The nominal cross section and its uncertainty are taken from an envelope of cross-section

\(^2\)In addition a resummation of soft gluon emission at next-to-leading-logarithm accuracy (NLL) [39–43] is performed in the case of strong SUSY pair production.
predictions using different PDF sets and factorization and renormalization scales, as described in Ref. [44]. Uncertainties on the cross-section values range from 9% to 14%.

All MC samples used in this analysis were passed through a GEANT4-based simulation of the ATLAS detector and were reconstructed with the same algorithms used for the data. The effect of multiple pp interactions in the same or nearby bunch crossings (pileup) is taken into account in all MC simulations and the distribution of the number of interactions per bunch crossing in the MC simulation is reweighted to that observed in the data. During the 2012 data-taking period, the average number of pp collisions per bunch crossing varied between 6 and 40, with a mean value of 20.7.

IV. OBJECT RECONSTRUCTION AND IDENTIFICATION

The reconstruction and identification of electrons and photons are described in Refs. [47,48] and [49], respectively. The photon identification criteria described in Ref. [49] have been re-optimized for the expected pileup conditions of the 8 TeV run period. Shape variables computed from the lateral and longitudinal energy profiles of the EM showers in the calorimeter are used to identify photons and discriminate against backgrounds. A set of photon selection criteria, designed for high efficiency and modest background rejection, defines the so-called “loose” photon identification used in this analysis. The loose photon requirements use variables that describe the shower shape in the second layer of the EM calorimeter and leakage into the hadronic calorimeter. These selection criteria do not depend on the transverse energy of the photon \( E_T \), but do vary as a function of \( \eta \) in order to take into account variations in the calorimeter geometry and upstream material. The efficiency of these loose requirements, for the signal photons, is over 95% over the range \( |z_{\text{origin}}| < 250 \text{ mm} \) and steadily falls to approximately 75% at \( |z_{\text{origin}}| = 700 \text{ mm} \).

The measurement of \( E_T^{\text{miss}} \) [50] is based on the energy deposits in the calorimeter with \( |\eta| < 4.9 \) and the energy associated with reconstructed muons; the latter is estimated using the momentum measurement of its reconstructed track. The energy deposits associated with reconstructed objects (jets defined using the anti-\( k_t \) algorithm [51] with radius parameter 0.4, photons, electrons) are calibrated accordingly. Energy deposits not associated with a reconstructed object are calibrated according to their energy sharing between the EM and hadronic calorimeters.

V. EVENT SELECTION

The selected events were collected by an online trigger requiring the presence of at least two loose photons with \( |\eta| < 2.5 \), one with \( E_T > 35 \text{ GeV} \) and the other with \( E_T > 25 \text{ GeV} \). This trigger is insensitive to the time of arrival of photons that are relevant for the signal considered, but there may be a slight dependence of the trigger efficiency on the \( z_{\text{origin}} \) of the photon. This effect is discussed in Sec. VIII A. The trigger efficiency exceeds 99% for signal events that pass the offline selection cuts. To ensure the selected events resulted from a pp collision, events are required to have at least one PV candidate with five or more associated tracks, each with transverse momentum satisfying \( p_T > 400 \text{ MeV} \). In case of multiple vertices, the PV is chosen as the vertex with the greatest sum of the squares of the transverse momenta of all associated tracks.

The offline photon selection requires two loose photons with \( E_T > 50 \text{ GeV} \) and \( |\eta| < 2.37 \) (excluding the transition region between the barrel and end cap EM calorimeter at \( 1.37 < |\eta| < 1.52 \)). At least one photon is required to be in the barrel region \( |\eta| < 1.37 \). Both photons are required to be isolated, by requiring that the transverse energy deposition in the calorimeter in a cone of radius \( \Delta R = \sqrt{\Delta\eta^2 + \Delta\phi^2} \approx 0.4 \) around each photon candidate be less than 4 GeV, after corrections to account for pileup and the energy deposition from the photon itself [49]. To avoid collisions due to satellite bunches, both photons are required to have a time that satisfies \( |\tau| < 4 \text{ ns} \).

The selected diphoton sample is divided into exclusive subsamples according to the value of \( E_T^{\text{miss}} \). The subsample with \( E_T^{\text{miss}} < 20 \text{ GeV} \) is used to model the prompt backgrounds, as described in Sec. VII B. The events with \( 20 \text{ GeV} < E_T^{\text{miss}} < 75 \text{ GeV} \) are used as control samples to validate the analysis procedure and background model. Diphoton events with \( E_T^{\text{miss}} > 75 \text{ GeV} \) define the signal region.

Table I summarizes the total acceptance times efficiency of the selection requirements for examples of GMSB SPS8 signal model points with various \( \Lambda \) and \( \tau \) values. Strong SUSY pair production is only significant for \( \Lambda < 100 \text{ TeV} \). For \( \Lambda = 80 \text{ TeV} \) and \( \tau = 6 \text{ ns} \), the acceptance times efficiency is evaluated from MC samples to be \( 1.6 \pm 0.1\% \) and \( 2.1 \pm 0.1\% \) for weak and strong production.

### Table I. The total signal acceptance times efficiency, given in percent, of the event selection requirements, for sample GMSB SPS8 model points with various \( \Lambda \) and \( \tau \) values. The uncertainties shown are statistical only.

<table>
<thead>
<tr>
<th>( \tau ) [ns]</th>
<th>( \Lambda = 80 \text{ TeV} )</th>
<th>( \Lambda = 160 \text{ TeV} )</th>
<th>( \Lambda = 320 \text{ TeV} )</th>
</tr>
</thead>
<tbody>
<tr>
<td>0.5</td>
<td>8.4 ( \pm 0.6 ) &amp; 30 ( \pm 1 ) &amp; 46 ( \pm 2 )</td>
<td></td>
<td></td>
</tr>
<tr>
<td>2</td>
<td>5.1 ( \pm 0.3 ) &amp; 21 ( \pm 0.2 ) &amp; 33.0 ( \pm 0.3 )</td>
<td></td>
<td></td>
</tr>
<tr>
<td>6</td>
<td>1.7 ( \pm 0.1 ) &amp; 7.3 ( \pm 0.1 ) &amp; 12.5 ( \pm 0.2 )</td>
<td></td>
<td></td>
</tr>
<tr>
<td>10</td>
<td>0.86 ( \pm 0.03 ) &amp; 3.71 ( \pm 0.06 ) &amp; 6.45 ( \pm 0.09 )</td>
<td></td>
<td></td>
</tr>
<tr>
<td>40</td>
<td>0.089 ( \pm 0.004 ) &amp; 0.38 ( \pm 0.01 ) &amp; 0.70 ( \pm 0.02 )</td>
<td></td>
<td></td>
</tr>
<tr>
<td>100</td>
<td>0.016 ( \pm 0.001 ) &amp; 0.070 ( \pm 0.002 ) &amp; 0.129 ( \pm 0.004 )</td>
<td></td>
<td></td>
</tr>
</tbody>
</table>
respectively, corresponding to a total value of $1.7 \pm 0.1\%$. For fixed $\Lambda$, the acceptance falls approximately exponentially with increasing $\tau$, dominated by the requirement that both NLSP decay before reaching the EM calorimeter, so that the resulting photons are detected. For fixed $\tau$, the acceptance increases with increasing $\Lambda$, since the SUSY particle masses increase, leading the decay cascades to produce, on average, higher $E_T^{\text{miss}}$ and also higher $E_T$ values of the decay photons.

### VI. SIGNAL AND BACKGROUND MODELING

The analysis exploits both the pointing and time measurements. However, the measured properties of only one of the two photons are used, where the choice of which photon to use is made according to the location of the two photons. The selection requires at least one of the photons to be in the barrel region, since events with both photons in the end cap calorimeters are expected to contribute very little to the signal sensitivity. For events, referred to hereafter as BE events, where one photon is found in the barrel and one in the end cap calorimeter, the $\Delta z_\gamma$ and $t_\gamma$ measurements of the barrel photon are used in the analysis; this choice is made since, due to geometry, the $\Delta z_\gamma$ resolution in the barrel calorimeter is better. For so-called BB events, with both photons in the EM barrel calorimeter, the $\Delta z_\gamma$ and $t_\gamma$ measurements of the photon with the maximum value of $t_\gamma$ are used. Studies showed that this approach achieves a sensitivity very similar to that when using both photons, while avoiding the complexity of having to deal with the correlations between the measurements of the two photons within a single event.

#### A. GMSB SPS8 signal

The shape of the $\Delta z_\gamma$ and $t_\gamma$ distributions for signal events is obtained from the signal MC samples. For a given value of $\Lambda$, the distributions for any NLSP lifetime value can be obtained by appropriately reweighting the distributions of the existing MC samples.

Examples of $\Delta z_\gamma$ and $t_\gamma$ signal distributions for a few representative GMSB SPS8 models are shown in Fig. 3. The distributions are normalized to unity area within the displayed horizontal-axis range, in order to allow for an easier comparison between the various signal and background shapes. The upper two plots show signal shapes for some example NLSP lifetime ($\tau$) values, all with $\Lambda$ fixed to a value of 160 TeV. The lower two plots show signal shapes for some example $\Lambda$ values, all with $\tau$ fixed to a value of 1 ns. The signal shapes have some dependence on $\Lambda$ due to its impact on the SUSY mass spectrum, and therefore the event kinematics. However, the signal shapes vary most strongly with NLSP lifetime. For larger $\tau$ values, the signal shapes are significantly impacted by the diphoton event selection, which effectively requires that both NLSP decay before reaching the EM calorimeters, leading to a signal acceptance that falls rapidly with increasing time values. As a result, the signal shapes for $\tau$ values of 2.5 ns and 25 ns, for example, are quite similar, as shown in the upper plots of Fig. 3.

#### B. Backgrounds

The background is expected to be completely dominated by $pp$ collision events, with possible backgrounds due to cosmic rays, beam-halo events, or other noncollision processes being negligible. The source of the loose photons in background events contributing to the selected sample is expected to be either a prompt photon, an electron misidentified as a photon, or a jet misidentified as a photon. In each case, the object providing the loose photon signature originates from the PV.

The pointing and time distributions expected for the background sources are determined using control samples in data. In addition to avoiding a reliance on the precise MC simulation of the pointing and timing performance for the backgrounds, and particularly of the tails of their $\Delta z_\gamma$ and $t_\gamma$ distributions, using data samples naturally accounts for the influence of pile-up, the possibility of selecting the wrong PV, and any instrumental or other effects that might influence the background measurements.

Given their similar EM shower developments, the pointing and time resolutions for prompt photons are similar to those for electrons. The $t_\gamma$ distribution in each $\Delta z_\gamma$ category is modeled using electrons from $Z \rightarrow ee$ data events. The $Z \rightarrow ee$ event selection requires a pair of oppositely charged electron candidates, each of which has $p_T > 35$ GeV and $|\eta| < 2.37$ (excluding the transition region between the barrel and end cap calorimeters). Both electrons are required to be isolated, with the transverse energy deposited in the calorimeter in a cone of size $\Delta R = 0.2$ around each electron candidate being less than 5 GeV, after subtracting the energy associated with the electron itself. As for photons, electrons must be read out using either high or medium gain, and must have a time less than 4 ns. The dielectron invariant mass is required to be within 10 GeV of the $Z$ boson mass, yielding a sufficiently clean sample of $Z \rightarrow ee$ events. The electrons are used to construct $\Delta z_\gamma$ and $t_\gamma$ templates. The unit-normalized $Z \rightarrow ee$ templates are shown superimposed on the plots of Fig. 3.

Due to their wider showers in the EM calorimeter, jets have a wider $\Delta z_\gamma$ distribution than prompt photons and electrons. Events passing the diphoton selection with $E_T^{\text{miss}} < 20$ GeV are used as a data control sample that includes jets with properties similar to the background contributions expected in the signal region. The $E_T^{\text{miss}}$ requirement serves to render negligible any possible signal contribution in this control sample. The time resolution depends on the deposited energy in the calorimeter. Using the shape of the $E_T^{\text{miss}} < 20$ GeV template to describe events in the signal region, defined with $E_T^{\text{miss}} > 75$ GeV therefore implicitly relies on the kinematic distributions for
photons in both regions being similar. However, it is expected that there should be a correlation between the value of $E_{\text{miss}}$ in a given event, and the $E_T$ distribution of the physics objects in that event. This correlation is indeed observed in the low-$E_{\text{miss}}$ control region samples. Increasing to 60 GeV the minimum $E_T$ requirement on the photons in the $E_{\text{miss}} < 20$ GeV control sample selects photons with similar kinematic properties to the photons in the signal region. Therefore, the $E_{\text{miss}} < 20$ GeV sample requiring $E_T > 60$ GeV for the photons is used to model the background.

The selected diphoton sample with $E_{\text{miss}} < 20$ GeV should be dominated by jet–jet, jet–$\gamma$ and $\gamma\gamma$ events. Therefore, the associated $\Delta z_{\gamma}$ and $t_{\gamma}$ distributions include contributions from photons as well as from misidentified jets that satisfy the loose photon signature. The unit-normalized $E_{\text{miss}} < 20$ GeV templates are shown superimposed on the plots of Fig. 3. As expected, Fig. 3 shows

![Signal distributions for (left) $\Delta z_{\gamma}$ and (right) $t_{\gamma}$, for some example GMSB SPS8 model points. The upper two plots show signal shapes for NLSP lifetime ($\tau$) values of 0.25, 1, 2.5, and 25 ns, all with the effective scale of SUSY breaking ($\Lambda$) fixed to a value of 160 TeV. The lower two plots show signal shapes for $\Lambda$ values of 80, 160, and 300 TeV, all with $\tau$ fixed to a value of 1 ns. Superimposed on each of the plots are the corresponding data distributions for the samples used to model the backgrounds, namely $Z \rightarrow ee$ events and diphoton events with $E_{\text{miss}} < 20$ GeV. For all plots, the distributions are normalized to unity area within the horizontal-axis range displayed, and the uncertainties shown on the data distributions are statistical only.](image-url)
that the \( \Delta z_\gamma \) distribution is much wider for the \( E_T^{\text{miss}} < 20 \text{ GeV} \) sample than for the \( Z \to ee \) sample, while the \( t_\gamma \) distributions of these two background samples are very similar. Both backgrounds have distributions that are very different than those expected for GMSB SPS8 signal events, with larger differences observed for higher lifetime values.

**VII. STATISTICAL ANALYSIS**

The photon pointing and time measurements are each sensitive to the possible presence of photons from displaced decays of heavy, long-lived NLSP. In addition, the measurements of \( \Delta z_\gamma \) and \( t_\gamma \) are almost completely uncorrelated for prompt backgrounds. The lack of correlation results from the fact that \( \Delta z_\gamma \) uses the spread of the EM shower to precisely measure its centroids in the first two layers in the EM calorimeter, while \( t_\gamma \) uses the time reconstructed from the pulse-shape of only the second-layer cell with the maximum energy deposit. Using both variables to distinguish signal from background is therefore a powerful tool.

Since the \( \Delta z_\gamma \) distribution should be symmetric for both signal and background, the pointing distribution is folded by taking \( |\Delta z_\gamma| \) as the variable of interest instead of \( \Delta z_\gamma \). The inputs to the statistical analysis are, therefore, the values of \( |\Delta z_\gamma| \) and \( t_\gamma \) measured for the photon selected in each event.

A full two-dimensional analysis of \( |\Delta z_\gamma| \) versus \( t_\gamma \) would require populating a very large number of bins of the corresponding two-dimensional space with both the background and signal models. Since the background model is determined using data in control samples, which have limited numbers of events, this approach is impractical. Instead, the original two-dimensional analysis is transformed into a “\( N \times 1D \)” problem by using the \( |\Delta z_\gamma| \) values to define \( N \) mutually exclusive categories of photons, and then simultaneously fitting the \( t_\gamma \) spectra of each of the categories. To optimize the sensitivity of the analysis, the categories are chosen to divide the total sample of photons into categories with different signal-to-background ratios. This approach is similar to that followed in the ATLAS determination of the Higgs boson spin in the \( H \to \gamma \gamma \) decay channel [52].

An additional motivation for applying the “\( N \times 1D \)” approach is to simplify the task of modeling the overall background with an unknown mixture of the background templates measured using the \( Z \to ee \) and \( E_T^{\text{miss}} < 20 \text{ GeV} \) samples. As shown in Fig. 3, these samples used to model the various background contributions have different \( |\Delta z_\gamma| \) distributions, but very similar \( t_\gamma \) distributions. The minor \( t_\gamma \) differences can be handled, as described in Sec. VIII, by including a small systematic uncertainty on the \( t_\gamma \) background shape. However, the \( |\Delta z_\gamma| \) distribution of the total background depends sensitively on the background composition. By implementing the normalization of the background in each \( |\Delta z_\gamma| \) category as an independent, unconstrained nuisance parameter, the fitting procedure eliminates the need to predict the overall \( |\Delta z_\gamma| \) distribution of the total background, thereby avoiding the associated dependence on knowledge of the background composition.

The binning in both \( |\Delta z_\gamma| \) and \( t_\gamma \) was chosen to optimize the expected sensitivity. It was found that using six \( |\Delta z_\gamma| \) categories and six \( t_\gamma \) bins provides the analysis with good expected sensitivity, without undue complexity. While the optimized choice of bin boundaries has almost no dependence on \( \Lambda \), there is some dependence on NLSP lifetime. The analysis, therefore, uses two separate choices of binning, one for low lifetime values (\( \tau < 4 \text{ ns} \)) and one for high lifetime values (\( \tau > 4 \text{ ns} \)). The optimized category and bin boundaries for both cases are summarized in Tables II and III, respectively.

The one-dimensional fits of the \( t_\gamma \) distributions of the individual categories are performed simultaneously. The signal normalization is represented by a single unconstrained signal-strength parameter, \( \mu \), that is correlated between all categories and defined as the fitted signal cross section divided by the GMSB SPS8 prediction. Thus, there are seven unconstrained parameters in the fit, namely

### TABLE II. Values of the optimized ranges of the six \( |\Delta z_\gamma| \) categories, for both low and high NLSP lifetime (\( \tau \)) values.

<table>
<thead>
<tr>
<th>Lifetime</th>
<th>Cat. 1</th>
<th>Cat. 2</th>
<th>Cat. 3</th>
<th>Cat. 4</th>
<th>Cat. 5</th>
<th>Cat. 6</th>
</tr>
</thead>
<tbody>
<tr>
<td>( \tau &lt; 4 \text{ ns} )</td>
<td>0–40</td>
<td>40–80</td>
<td>80–120</td>
<td>120–160</td>
<td>160–200</td>
<td>200–2500</td>
</tr>
<tr>
<td>( \tau &gt; 4 \text{ ns} )</td>
<td>0–50</td>
<td>50–100</td>
<td>100–150</td>
<td>150–200</td>
<td>200–250</td>
<td>250–2000</td>
</tr>
</tbody>
</table>

### TABLE III. Values of the optimized ranges of the six \( t_\gamma \) bins, for both low and high NLSP lifetime (\( \tau \)) values.

<table>
<thead>
<tr>
<th>Lifetime</th>
<th>Bin 1</th>
<th>Bin 2</th>
<th>Bin 3</th>
<th>Bin 4</th>
<th>Bin 5</th>
<th>Bin 6</th>
</tr>
</thead>
<tbody>
<tr>
<td>( \tau &lt; 4 \text{ ns} )</td>
<td>4.0– + 0.5</td>
<td>0.5–1.1</td>
<td>1.1–1.3</td>
<td>1.3–1.5</td>
<td>1.5–1.8</td>
<td>1.8–4.0</td>
</tr>
<tr>
<td>( \tau &gt; 4 \text{ ns} )</td>
<td>4.0– + 0.4</td>
<td>0.4–1.2</td>
<td>1.2–1.4</td>
<td>1.4–1.6</td>
<td>1.6–1.9</td>
<td>1.9–4.0</td>
</tr>
</tbody>
</table>
six separate nuisance parameters, one for each category, describing the background normalization, and the signal strength $\mu$.

The analysis uses a likelihood model $\mathcal{L}(\mu, \theta)$ that is dependent on the signal strength $\mu$ and the values of the nuisance parameters $\theta$. The model incorporates a statistical Poisson component as well as Gaussian constraint terms for the nuisance parameters associated with systematic uncertainties. The statistical model and procedure are implemented within the HistFactory framework [53]. Two likelihood-based test statistics $q_0$ and $q_\mu$ are calculated to find the $p_0$ values for the background-only hypothesis and to set upper limits on the signal strength.

Asymptotic formulae based on Wilk’s theorem are used to approximate the $q_0$ and $q_\mu$ distributions following the procedures documented in Ref. [54]. Tests of the background model’s validity in the control regions and the signal region rely on the $p_0$ test statistic, calculated from the observed $q_0$. In the absence of any excess, the $CL_s$ exclusions for each signal type are calculated according to Ref. [55].

To validate the statistical model and asymptotic forms of $q_0$ and $q_\mu$, unconditional pseudo-experiment ensembles were generated from the background-only model and multiple signal-plus-background models. Although the number of data events in the signal region is not large, deviations from the asymptotic $\chi^2$ distribution of $q_\mu$ were shown to have a minimal impact on the exclusion. The model accurately reconstructed the signal and background normalization parameters and produced Gaussian distributions of the constrained nuisance parameters.

VIII. SYSTEMATIC UNCERTAINTIES

In the statistical analysis, the background normalization for each $|\Delta z_j|$ category is determined using an independent nuisance parameter. Therefore, it is not necessary to include systematic uncertainties regarding the normalization of the background, nor regarding its shape in the variable $|\Delta z_j|$. As a result, the various systematic uncertainties relevant for this analysis can be divided into two categories: so-called “flat” uncertainties are not a function of $|\Delta z_j|$ and $t_j$ and affect only the overall signal yield, while “shape” uncertainties are those that are related to the shapes of the unit-normalized $|\Delta z_j|$ and $t_j$ distributions for signal or to the shape of the background $t_j$ template.

A. Signal yield systematic uncertainties

The various flat systematic uncertainties affecting the signal yield are summarized in Table IV. The uncertainty on the integrated luminosity is $\pm 2.8\%$ and is determined with the methodology detailed in Ref. [56]. The uncertainty due to the trigger is dominated by uncertainties on the dependence on $|\Delta z_j|$ of the efficiency of the hardware-based level 1 (L1) trigger. The L1 calorimeter trigger [57] uses analog sums of the channels grouped within projective trigger towers. This architecture leads to a small decrease in L1 trigger efficiency for highly nonpointing photons, due to energy leakage from the relevant trigger towers. The uncertainty on the impact of this dependence is conservatively set to the magnitude of the observed change in efficiency in signal MC events versus $|\Delta z_j|$, and dominates the $\pm 2\%$ uncertainty on the trigger efficiency.

Following the method outlined in Ref. [58], uncertainties on the signal efficiency, arising from the combined impact of uncertainties in the photon energy scale and resolution and in the combined photon identification and isolation efficiencies, are determined to be $\pm 1\%$ and $\pm 1.5\%$, respectively. An additional $4\%$ is included as a conservative estimate of the uncertainty in the identification efficiency due to the nonpointing nature of the photons. This estimate is derived from studies of changes in the relevant variables measuring the shapes of the EM showers for nonpointing photons. An uncertainty on the signal yield of $\pm 1.1\%$ results from varying the $E_{T}^{\text{miss}}$ energy scale and resolution within their estimated uncertainties [50]. The uncertainty on the signal efficiency due to MC statistics lies in the range $\pm 0.8\%–3.6\%$ and the contribution due to the lifetime reweighting technique is in the range $\pm 0.5\%–5\%$, depending on the sample lifetime.

Variations in the calculated NLO signal cross sections times the signal acceptance and efficiency, at the level of $\pm 9\%–14\%$ occur when varying the PDF set and factorization and renormalization scales, as described in Sec. III. In the results, these uncertainties on the theoretical cross section are shown separately, as hashed bands around the theory prediction. Limits are quoted at the points where the experimental results equal the value of the central theory prediction minus one standard deviation of the theoretical uncertainty.

B. Signal shape systematic uncertainties

The expected signal distributions are determined using the GMSB SPS8 MC signal events. Therefore, limitations
in the MC simulation could lead to differences between data and MC events in the predicted signal behavior. Any such discrepancies in the shapes of the signal distributions must be handled by corresponding systematic uncertainties on the signal shapes. Since signal templates for both $|\Delta z_j|$ and $t_j$ are used in the statistical analysis, systematic uncertainties on the signal shapes of both must be taken into account in the fitting procedure.

The dominant systematic uncertainty on the shape of the signal $t_j$ distribution arises from the impact of the time reconstruction algorithm on the measurement of delayed signals. As discussed in Sec. II C, the use of fixed OFC values causes a bias in the energy and reconstructed time for signals that are sufficiently early or late compared to the nominal time. For time shifts within ±5 ns of the nominal time, the reconstructed energy decreases by less than 1% and, as a result, impacts on the measurements of the photon energy and pointing are negligible. However, for time shifts of ±5 ns, a bias in the time reconstruction of order 10% of the shift is observed in the analysis of satellite-satellite collisions. Since the optimal filtering approach is equivalent to a linearization of the optimization problem, the expected form of the time bias is expected to be dominated by the neglected quadratic terms in the Taylor expansion. Therefore, one expects deviations in the time measurement to be small for small time shifts, over a region where the linear approximation works well, and then to grow roughly quadratically for larger time shifts. As a conservative estimate of the systematic uncertainty on the time measurement due to these effects, a linear dependence is assumed for the deviations, with an amplitude of ±10% of the reconstructed time. This uncertainty is applied only to the signal time distribution, since the background time shape is determined directly from data and therefore already includes whatever impact is caused by the bias.

Another source of systematic uncertainty in the signal $|\Delta z_j|$ and $t_j$ shapes results from possible differences between the pileup conditions in data and signal MC events, even though the MC signal samples are reweighted to match the pileup distribution observed in the data. The PV in GMSB SPS8 signal events should be correctly identified with high efficiency, typically greater than 90%, due to the high $E_T$ values of the other SM particles produced in the SUSY decay chains. However, the presence of pileup could still increase the likelihood of incorrectly choosing the PV, potentially impacting both the pointing and time measurements. Nearby energy deposits that are not associated with the photon could also impact the photon measurements, though these should be moderated by the photon isolation requirements. As a conservative estimate of the possible influence of pileup, the signal shapes in the entire MC sample were compared with those in two roughly equally sized subsamples with differing levels of pileup, chosen as those events with less than, and those with greater than or equal to, 13 reconstructed PV candidates. The small differences observed are included as pileup-induced systematic uncertainties on the signal template shapes.

To investigate the possible impact of the imperfect knowledge of the material distribution in front of the calorimeter, one signal MC point was simulated with the nominal detector description as well as with a modified version that varies the material description within the uncertainties. The signal distributions using the two detector geometries are very similar, typically agreeing within a few percent. These variations are small compared to the other systematic uncertainties on the signal shapes, and are therefore neglected.

Typical values of the total systematic uncertainties on the signals shapes are around ±10%, dominated by the impact of the time reconstruction algorithm on the measurement of delayed signals. These uncertainties have a very small impact on the overall sensitivity of the analysis, which is dominated by statistical uncertainties due to the limited size of the data sample in the signal region.

C. Background shape systematic uncertainties

The dominant uncertainty in the knowledge of the background template shape arises from uncertainty in the background composition in the signal region. As described in Sec. VI B, and seen in Fig. 3, the EM shower development of electrons and photons differs from that of jets and gives rise to somewhat different $t_j$ shapes, and very different $|\Delta z_j|$ shapes. Therefore, the $t_j$ and $|\Delta z_j|$ shapes for the total background depend on the background composition.

The statistical analysis includes an independent normalization fit parameter for the total background in each of the $|\Delta z_j|$ categories. By this means, the fit result avoids any dependence on the $|\Delta z_j|$ distribution of the background and it is not necessary to account for systematic uncertainties on the background $|\Delta z_j|$ shape. However, the background $t_j$ shape is used in the fitting procedure, and therefore its associated systematic uncertainties must be taken into account.

Since the time measurement is performed using only the second-layer cell of the EM cluster with the maximum energy deposit, it is expected that the time should be rather insensitive to the details of the EM shower development and, therefore, one would expect very similar time distributions for prompt electrons, photons and jets. As seen in Fig. 3, this expectation is largely satisfied since the $Z \rightarrow ee$ and $E_T^{\text{miss}} < 20$ GeV $t_j$ distributions are indeed very similar. However, there are some effects that could cause a slight violation of the assumption that the $t_j$ distribution would be the same for all prompt background sources. Details of the EM shower development can indirectly impact the time measurement, for example, due to cross-talk from neighboring cells. In addition, the time measurement necessarily includes a correction for the
time of flight from the PV; therefore, misidentification of the PV can lead to shifts in the reconstructed time away from the true time, and different background sources can have different rates of PV misidentification. PV misidentification can also produce shifts in the pointing measurement, introducing a nonzero correlation between $t_\gamma$ and $|\Delta z_\gamma|$, even for prompt backgrounds.

The $t_\gamma$ template from the diphoton sample with $E_T^{\text{miss}} < 20$ GeV includes contributions from jets as well as EM objects and is taken as the nominal estimate of the background $t_\gamma$ shape. The difference between this distribution and that of the $Z \rightarrow ee$ sample, which has a higher purity of EM objects, is taken as an estimate of the uncertainty due to the background composition and is symmetrized to provide a symmetric systematic uncertainty on the background $t_\gamma$ shape. The uncertainty is small for low time values, but reaches almost $\pm 100\%$ in the highest $t_\gamma$ bin. However, this uncertainty has little impact on the overall sensitivity since the signal yield in the highest $t_\gamma$ bin is much larger than the background expectation, even when this large background uncertainty is taken into account.

Another uncertainty in the background $t_\gamma$ shape arises from uncertainties in the relative contributions of BB and BE events to the background in the signal region. The definition of $t_\gamma$ for BB events as the time of the photon with the maximum time value produces, as mentioned previously, a small shift toward positive time values for such events, which does not exist for BE events. Therefore, in constructing the total background $t_\gamma$ template, it is necessary to appropriately weight the $t_\gamma$ background templates measured separately for BB and BE events in order to match the background in the signal region. Since any signal can have a different BB/BE composition than the background, the rate of BB and BE events in the signal region cannot simply be used to determine the background composition. However, the background-dominated control regions can be used to make an estimation of the background BB/BE composition. Comparing the various samples with $E_T^{\text{miss}} < 75$ GeV, BB events are estimated to contribute $(61 \pm 4)$% of the total background in the signal region, where the uncertainty conservatively covers the variations observed among various samples. Therefore, the nominal $t_\gamma$ background template is formed by appropriately weighting the BB and BE background distributions to this fraction, with BB fractions varied by $\pm 4\%$ to generate the $\pm 1\sigma$ variations on this shape due to the uncertainty in the BB/BE background contributions. This systematic shape uncertainty reaches less than $\pm 10\%$ in the highest $t_\gamma$ bin and, therefore, is much smaller than the dominant uncertainty due to the background composition.

An additional systematic uncertainty on the background $t_\gamma$ shape arises from the event kinematics. As discussed in Sec. VI B, the minimum $E_T$ requirements on the photons are increased to 60 GeV for the $E_T^{\text{miss}} < 20$ GeV control sample, as opposed to 50 GeV for the signal region, in order for the $E_T^{\text{miss}} < 20$ GeV control sample to select photons with kinematic properties more similar to the background photons expected in the signal region. Systematic uncertainties on the $t_\gamma$ shape of the $E_T^{\text{miss}} < 20$ GeV sample are determined by varying the photon $E_T$ requirement up and down by 10 GeV. The three shapes agree quite well with each other, with the observed variations reaching about $\pm 40\%$ in the highest time bin.

### IX. RESULTS AND INTERPRETATION

Before examining the $|\Delta z_\gamma|$ and $t_\gamma$ distributions of the data in the signal region, the two control regions, CR1 with $20 < E_T^{\text{miss}} < 50$ GeV and CR2 with $50 < E_T^{\text{miss}} < 75$ GeV, are used to validate the analysis technique and background modeling. Since the control regions should be dominated by background, their data distributions are expected to be well described by the background-only fit. Table V summarizes the number of selected events in CR1 and CR2, as well as those in the signal region (SR), showing that the control region data sets are much larger than that of the signal region. It is of interest whether the background modeling, including the assigned systematic uncertainties, is adequate to describe the control region data within the statistical uncertainties of the data in the signal region. Therefore, the fitting procedure was applied separately to the measured data distributions in CR1 and CR2, scaled in each case to the total of 386 events of the signal region. The fit results for both control regions are in good agreement with the background-only model for all tested signal points, validating the analysis methodology.

Figure 4 shows the distributions of $|\Delta z_\gamma|$ and $t_\gamma$ for the 386 events in the signal region. The distributions of both variables are rather narrow, as expected for background. In particular, there is no evidence for events in the tail of the $t_\gamma$ distribution at positive times, as would be expected for a signal contribution due to delayed photons. The $|\Delta z_\gamma|$ distribution is quite symmetric around zero, as expected for both the signal and for physics backgrounds. The $|\Delta z_\gamma|$ and $t_\gamma$ distributions in the final, coarser binning are used as inputs to the final fitting procedure and statistical analysis.

Example results of fits to the signal region data are shown in Fig. 5, for the particular case of $\Lambda = 100$ TeV and $\tau = 19$ ns. The figures show the results of the signal-plus-background (with $\mu = 1$) and background-only ($\mu = 0$) fits to the six $|\Delta z_\gamma|$ categories. The signal-region data are in

<table>
<thead>
<tr>
<th>Sample</th>
<th>$E_T^{\text{miss}}$ range [GeV]</th>
<th>Number of events</th>
</tr>
</thead>
<tbody>
<tr>
<td>CR1</td>
<td>$20 &lt; E_T^{\text{miss}} &lt; 50$</td>
<td>50751</td>
</tr>
<tr>
<td>CR2</td>
<td>$50 &lt; E_T^{\text{miss}} &lt; 75$</td>
<td>3591</td>
</tr>
<tr>
<td>SR</td>
<td>$E_T^{\text{miss}} &gt; 75$</td>
<td>386</td>
</tr>
</tbody>
</table>

TABLE V. Numbers of selected events in the two control regions (CR1 and CR2) and in the signal region (SR).
FIG. 4 (color online). Distributions of (left) $\Delta z$ and (right) $t_{\gamma}$ for the 386 events in the signal region, defined with $E_{T}^{\text{miss}} > 75$ GeV. Superimposed are the data distributions for diphoton events with $E_{T}^{\text{miss}} < 20$ GeV, used to model the backgrounds, and the distributions for two example NLSP lifetime values in GMSB SPS8 models with $\Lambda = 160$ TeV. The background and MC signal distributions are scaled to the total number of data events in the signal region.

FIG. 5 (color online). Example fit to the signal-region data. The figures show the results of the signal-plus-background fits with $\mu = 1$ to the six $|\Delta z_j|$ categories, along with the background-only fit and the $\pm 1\sigma$ systematic shape variations (dashed lines). The signal model shown has $\Lambda = 100$ TeV and $\tau = 19$ ns. The ranges of the $t_{\gamma}$ bins are as defined in Table III.
good agreement with the background-only model, and there is no evidence for a signal-like excess.

Fits to the data were performed for τ values exceeding 250 ps, and for the range of relevant Λ values. The smallest $p_0$ value of 0.21, corresponding to an equivalent Gaussian significance of 0.81σ, was found for signal model parameters of Λ = 100 TeV and τ = 0.25 ns. Using ensembles of background-only pseudoexperiments, the probability of observing a $p_0$ value this small or smaller from any one of the 640 signal points in the Λ–τ plane was calculated to be 88%.

Figure 6 shows, for Λ = 200 TeV, the results of the signal-region fit interpreted as 95% confidence level (C.L.) limits on the number of signal events, as well as on the signal cross section, as a function of $\tau_{\chi^0_1}$ lifetime, for the case of Λ = 200 TeV. The regions above the limit curves are excluded at 95% C.L. The red bands show the GMSB SPS8 theory prediction, including its theoretical uncertainty.

FIG. 6 (color online). The observed and expected 95% C.L. limits on (left) the number of signal events and (right) the GMSB SPS8 signal cross section, as a function of $\tau_{\chi^0_1}$ lifetime, for the case of Λ = 200 TeV. The regions above the limit curves are excluded at 95% C.L. The red bands show the GMSB SPS8 theory prediction, including its theoretical uncertainty.

the subsequent limits in the two-dimensional GMSB signal space of $\chi^0_1$ lifetime versus Λ, and also versus the corresponding $\chi^0_1$ and $\chi^+_1$ masses in the GMSB SPS8 model. For example, $\chi^0_1$ lifetimes up to about 100 ns are excluded at 95% C.L. for Λ values in the range of about 80–100 TeV, as are Λ values up to about 300 TeV (corresponding to $\chi^0_1$ and $\chi^+_1$ masses of about 440 and 840 GeV, respectively) for $\chi^0_1$ lifetimes in the range of about 2–3 ns. For comparison,

FIG. 7 (color online). The observed and expected 95% C.L. limits in the two-dimensional GMSB signal space of $\chi^0_1$ lifetime versus Λ, and also versus the corresponding $\chi^0_1$ and $\chi^+_1$ masses in the GMSB SPS8 model. For example, $\chi^0_1$ lifetimes up to about 100 ns are excluded at 95% C.L. for Λ values in the range of about 80–100 TeV, as are Λ values up to about 300 TeV (corresponding to $\chi^0_1$ and $\chi^+_1$ masses of about 440 and 840 GeV, respectively) for $\chi^0_1$ lifetimes in the range of about 2–3 ns. For comparison,
results from the ATLAS analysis of the 7 TeV data set [1] are also shown in Fig. 7, indicating the significantly larger reach of the 8 TeV analysis.

X. CONCLUSIONS

A search has been made for evidence of nonpointing and delayed photons, such as would arise in the decays of long-lived heavy neutral particles. The search, in the $\gamma\gamma + E_T^{miss} + X$ final state, uses the full data sample collected by ATLAS in 2012, corresponding to an integrated luminosity of 20.3 fb$^{-1}$ of 8 TeV $pp$ collisions at the LHC.

The data are in good agreement with the background-only fit and no evidence for nonpointing and delayed photons is observed. The results are interpreted in the context of the GMSB SPS8 benchmark model, in the plane of $r$, the $\tilde{\chi}_1^0$ lifetime, versus $\Lambda$, the effective scale of SUSY breaking, and also versus the corresponding $\tilde{\chi}_1^0$ and $\tilde{\chi}_1^-$ masses. The resultant 95% C.L. exclusion limits include values of $r$ in the range from 0.25 ns to about 100 ns, and values of $\Lambda$ in the range from 80 to about 300 TeV.

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PHYSICAL REVIEW D 90, 112005 (2014)

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