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Measurement of the spin-dependent structure function $g_1(x)$ of the proton

Spin Muon Collaboration


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Abstract

We have measured the spin-dependent structure function $g_1^p$ of the proton in deep inelastic scattering of polarized muons off polarized protons, in the kinematic range $0.003 < x < 0.7$ and $1 \text{GeV}^2 < Q^2 < 60 \text{GeV}^2$. Its first moment, $\int_0^1 g_1^p(x) \, dx$, is found to be $0.136 \pm 0.011$ (stat.) $\pm 0.011$ (syst.) at $Q^2 = 10 \text{GeV}^2$. This value is smaller than the prediction of the Ellis-Jaffe sum rule by two standard deviations, and is consistent with previous measurements. A combined analysis of all available proton, deuteron and neutron data confirms the Bjorken sum rule to within 10% of the theoretical value.
ton and for the neutron, under the assumptions that the strange sea is unpolarized and that SU(3) symmetry is valid for the baryon octet decays.

First measurements of $g_1^p$ were performed by experiments at SLAC (E80 and E130 [4]) and at CERN (EMC [5]). The analysis of these data [6,5] showed a deviation from the Ellis-Jaffe prediction, with the implications that the total contribution of quark spins to the nucleon spin is small and that the strange sea is negatively polarized. Recently, two experiments have measured $g_1^p$ from polarized muon-deuteron (SMC [7] at CERN) and $g_1^n$ from polarized electron-$^3$He scattering (E142 [8] at SLAC). The conclusions from these two experiments appeared to be at variance. However, combined analyses [9-12] showed that the experimental data agree in the kinematic region of overlap, and emphasized that the conclusions are very sensitive to the small-$x$ extrapolation of $g_1(x)$ and to higher order and higher twist QCD corrections. Additional data are required to provide a more stringent test of the sum rules and to clarify the contribution of the quark spins to the nucleon spin.

In this paper, we report the results of a new measurement of $g_1^p$ at CERN, where longitudinally polarized muons were scattered from longitudinally polarized protons in the kinematic range $1 \text{ GeV}^2 < Q^2 < 60 \text{ GeV}^2$ and $0.003 < x < 0.7$. The experiment is similar to the previous SMC experiment with a deuteron target [7].

The positive muon beam had an intensity of $4 \times 10^7$ muons/spill with a spill time of 2.4 s, a period of 14.4 s, and an average muon energy of 190 GeV. The beam polarization was determined from the shape of the energy spectrum of positrons from the decay $\mu^+ \rightarrow e^+\nu_\mu\bar{\nu}_\mu$. The polarimeter is described in Ref. [13]. The polarization was measured to be $P_\mu = -0.803 \pm 0.029$ (stat.) $\pm 0.020$ (syst.), in good agreement with Monte Carlo simulations of the beam transport [14].

A new polarized target was built for this experiment. Its design is similar to that used in the earlier EMC proton [5] and SMC deuteron [7] experiments. The target consists of an upstream and a downstream cell, each 60 cm long and 5 cm in diameter, separated by 30 cm, and with opposite longitudinal polarizations. The target material was butanol with about 5% of water, in which paramagnetic complexes [15] were dissolved, resulting in a concentration of $7.2 \times 10^{19}$ unpaired electrons per cm$^3$. The material was frozen into beads of about 1.5 mm diameter.

A new superconducting magnet system [16] and a new $^3$He/$^4$He dilution refrigerator were constructed. The magnet system consists of a solenoid, 16 correction coils, and a dipole. The solenoid provides a magnetic field of 2.5 T with its axis aligned along the beam direction and with an homogeneity of $2 \times 10^{-5}$ throughout the target volume. The dipole magnet provides a magnetic field of up to 0.5 T in the vertical direction. The dilution refrigerator achieved a temperature of about 0.3 K with a cooling power of 0.3 W when polarizing. The typical temperature in frozen spin operation was below 60 mK.

Protons were polarized by dynamic nuclear polarization (DNP). This was obtained by applying microwave power near the resonance frequency of the paramagnetic molecules. To achieve opposite proton polarizations in the two target cells simultaneously, we used slightly different microwave frequencies. In addition, frequency modulation of the microwaves reduced the polarization buildup time by about 20% and increased the maximum polarization by 6%. The mean polarization throughout the data-taking was 0.86, with a maximum value of 0.94.

The measurement of the proton polarization, $P_T$, was performed with 10 coils along the target using continuous-wave NMR with series Q-meter circuits [17,18]. The NMR signals were calibrated by measuring the thermal equilibrium signals at different temperatures around 1 K, where the natural polarization ($\sim 0.25\%$) is known from the Curie law. The thermal equilibrium signals were corrected for systematic effects including a small change in size with the field polarity and the contamination with background signals. The signals were also corrected for Q-meter non-linearity effects present at large polarizations. The relative accuracy of the polarization measurement was 3%.

The spin directions were reversed every 5 hours with only small losses of polarization and running time, by rotating the magnetic field direction using a superposition of the solenoid and the dipole fields. In addition, the spin polarization in each target cell was reversed via DNP once a week. During spin reversals by field rotation, the field was made slightly inhomogeneous to avoid depolarization due to superradiance [19].

The momentum of the incident muon was measured
using a bending magnet upstream of the target. Its track was reconstructed from hits in scintillator hodoscopes and proportional chambers. The trajectory and the momentum of the scattered muon were determined from hits in a total of 150 planes of proportional chambers, drift chambers and streamer tubes located upstream and downstream of the forward spectrometer magnet (FSM). The large number of planes minimized the effect of individual plane inefficiencies on the overall track reconstruction efficiency. The scattered muon was identified by having traversed a 2 m thick hadron absorber made of iron. Incident and scattered muon tracks determined the interaction vertex with an average resolution of 30 mm (0.3 mm) in the direction parallel (perpendicular) to the beam direction.

The readout of the apparatus was triggered by coincident hits in three large scintillator hodoscopes, one located just downstream of the FSM and two located downstream of the hadron absorber. A dedicated trigger for events with small scattering angles used hodoscopes with finer segmentation close to the beam and covered mainly the small x range.

Cuts were applied to minimize smearing effects, to limit the size of radiative corrections, to reject muons originating from the decay of pions produced in the target, to ensure that the beam flux was the same for both target cells and to ensure proper separation of events originating from the upstream and downstream target cells. After cuts, the data sample amounted to $3.1 \times 10^6$ events and $1.3 \times 10^6$ events for the large and small angle triggers, respectively.

The virtual-photon proton asymmetry $A_1^p$ is related to the measured muon-proton asymmetry $A_1^p = \frac{\sigma^{1/-} - \sigma^{1/+}}{\sigma^{1/+} + \sigma^{1/-}}$ by [1]

$$A_1^p = \frac{\sigma^{1/-} - \sigma^{3/-}}{\sigma^{1/+} + \sigma^{3/+}} = \frac{A_1^p}{D} - \eta A_2^p,$$

where 1/2 and 3/2 are the total spin projections in the direction of the virtual photon. The depolarization factor $D$ and the coefficient $\eta$ depend on the event kinematics. In addition, $D$ depends on the unpolarized structure function $R(x, Q^2)$, which was taken from a global fit of the SLAC data [20]. The asymmetry $A_2^p$ arises from the interference between transverse and longitudinal virtual photon polarizations and is constrained by the positivity limit $|A_2^p| \leq \sqrt{R}$. We have measured $A_2^p$ in a dedicated experiment, where the dipole field was used to hold the proton polarization in a direction perpendicular to the beam. We found $A_2^p$ to be compatible with zero within a statistical uncertainty of 0.20, which is a stronger constraint than the one imposed by the positivity limit. In addition, since the coefficient $\eta$ is small in the kinematic range covered by our experiment, we neglected the term $\eta A_2^p$ and included its possible effect in the systematic error.

The asymmetry $A_1^p$ is extracted from combinations of data sets taken before and after a polarization reversal. Each event is weighted with the corresponding values of $D$ and the dilution factor $f$, the fraction of the event yield from protons of hydrogen in the target ($f \approx 0.12$). Since we take data simultaneously with oppositely polarized cells, the incident muon flux, the amount of material in the target cells and the absolute value of the spectrometer acceptances, $a_u$ and $a_d$, cancel in the determination of $A_1^p$. The subscripts $u$ and $d$ refer to the upstream and downstream target cells, respectively. The only assumption in deriving $A_1^p$ is that the ratio $r = a_u/a_d$ remains constant within the typical period of time between two polarization reversals ($\Delta t \approx 5$ hours). A time dependence of $r$ leads to a false asymmetry of

$$\Delta A_1^p = \frac{1}{4fp_{p} P_{f} D} \frac{\Delta r}{r}.$$

In order to estimate the uncertainty due to this effect, we have studied the time dependences of all detector efficiencies; we then reprocessed the data after artificially imposing on the whole sample the largest of the variations observed within two polarization reversals. We also reanalyzed the data ignoring the information from a fraction of the planes in our chambers. In this way, we artificially reduced the redundancy of the spectrometer and became more sensitive to time dependences. Finally, we divided the data into different subsets according to a variety of criteria (e.g. data-taking periods, radial vertex position, events reconstructed in different parts of the spectrometer) and looked for disagreements between the different samples. From these studies we concluded that $\Delta r/r < 7 \times 10^{-4}$, corresponding to a false asymmetry $\Delta A_1^p < 7 \times 10^{-3}$.

Spin-dependent radiative corrections to $A_1^p$ were calculated using the approach of Ref. [21]. They were found to be small over the whole kinematic range. The
Table 1 Results on the virtual photon proton asymmetry $A_1^p$ and the spin structure function $g_1^p$ of the proton

<table>
<thead>
<tr>
<th>$x$-range</th>
<th>$\langle x \rangle$</th>
<th>$\langle Q^2 \rangle$ (GeV$^2$)</th>
<th>$A_1^p$</th>
<th>$g_1^p$</th>
<th>$g_1^p (Q^2=10\text{GeV}^2)$</th>
</tr>
</thead>
<tbody>
<tr>
<td>0.003-0.006</td>
<td>0.005</td>
<td>1.3</td>
<td>0.053±0.025±0.007</td>
<td>1.34±0.62±0.27</td>
<td>2.48±1.15±0.49</td>
</tr>
<tr>
<td>0.006-0.010</td>
<td>0.008</td>
<td>2.1</td>
<td>0.042±0.024±0.005</td>
<td>0.73±0.42±0.11</td>
<td>1.13±0.65±0.17</td>
</tr>
<tr>
<td>0.010-0.020</td>
<td>0.014</td>
<td>3.7</td>
<td>0.048±0.022±0.005</td>
<td>0.52±0.24±0.06</td>
<td>0.67±0.31±0.08</td>
</tr>
<tr>
<td>0.020-0.030</td>
<td>0.025</td>
<td>6.0</td>
<td>0.050±0.031±0.005</td>
<td>0.34±0.21±0.03</td>
<td>0.38±0.24±0.04</td>
</tr>
<tr>
<td>0.030-0.040</td>
<td>0.035</td>
<td>8.1</td>
<td>0.069±0.039±0.006</td>
<td>0.35±0.20±0.03</td>
<td>0.37±0.20±0.03</td>
</tr>
<tr>
<td>0.040-0.060</td>
<td>0.049</td>
<td>10.8</td>
<td>0.124±0.034±0.009</td>
<td>0.46±0.13±0.03</td>
<td>0.45±0.13±0.03</td>
</tr>
<tr>
<td>0.060-0.100</td>
<td>0.077</td>
<td>15.5</td>
<td>0.161±0.035±0.012</td>
<td>0.38±0.08±0.03</td>
<td>0.36±0.08±0.03</td>
</tr>
<tr>
<td>0.100-0.150</td>
<td>0.122</td>
<td>22.1</td>
<td>0.275±0.047±0.019</td>
<td>0.40±0.07±0.03</td>
<td>0.38±0.06±0.03</td>
</tr>
<tr>
<td>0.150-0.200</td>
<td>0.172</td>
<td>28.5</td>
<td>0.273±0.067±0.020</td>
<td>0.26±0.06±0.02</td>
<td>0.25±0.06±0.02</td>
</tr>
<tr>
<td>0.200-0.300</td>
<td>0.241</td>
<td>36.3</td>
<td>0.267±0.070±0.022</td>
<td>0.16±0.04±0.01</td>
<td>0.16±0.04±0.01</td>
</tr>
<tr>
<td>0.300-0.400</td>
<td>0.342</td>
<td>46.4</td>
<td>0.529±0.115±0.043</td>
<td>0.17±0.04±0.01</td>
<td>0.18±0.04±0.01</td>
</tr>
<tr>
<td>0.400-0.700</td>
<td>0.481</td>
<td>58.0</td>
<td>0.520±0.156±0.049</td>
<td>0.06±0.02±0.01</td>
<td>0.08±0.02±0.01</td>
</tr>
</tbody>
</table>

The first error is statistical, the second one is systematic. For the evaluation of $g_1^p (Q^2 = 10\text{GeV}^2)$, it has been assumed that $A_1^p$ does not depend on $Q^2$.

The spin structure function $g_1^p$ was evaluated from the average asymmetry $A_1^p$ in each $x$ bin using the relation

$$g_1^p (x, Q^2) = A_1^p (x, Q^2) \frac{F_2^p (x, Q^2)}{2x[1 + R(x, Q^2)]}.$$ (3)

The unpolarized structure function, $F_2^p (x, Q^2)$, was taken from the NMC parametrization [22]. The uncertainty is typically 3% to 5%. The lowest $x$ bin is outside the kinematic region covered by the NMC data, but we have verified that their parametrization extrapolates smoothly to the HERA data [23], and estimated the corresponding uncertainty to be 15%. The structure function $g_1^p$ is practically independent of $R$ due to cancellations between the implicit $R$ dependences in $D$ and $F_2$ and the explicit one in Eq. (3). Results for $g_1^p$ are given in Table 1 and Fig. 2.

To evaluate the integral $\int g_1^p (x, Q_0^2) \, dx$ at a fixed $Q^2$, we recalculated $g_1^p$ at $Q_0^2 = 10\text{GeV}^2$, which represents an average value for our data. Using Eq. 3, we obtained $g_1^p (x, Q_0^2)$ in each bin assuming $A_1 (x, Q_0^2)$ to be independent of $Q^2$. This assumption is consistent with our data, with previous experimental results for both the proton [5] and deuteron [7], and with recent theoretical calculations [11]. The values of $g_1^p (x, Q_0^2)$

Fig. 1. The virtual-photon proton cross section asymmetry $A_1^p$ as a function of the Bjorken scaling variable $x$. Only statistical errors are shown with the data points. The size of the systematic errors for the SMC points is indicated by the shaded area.
Fig. 2. The solid circles (right-hand axis) show the structure function $xg_1^p$ as a function of the Bjorken scaling variable $x$, at $Q_0^2 = 10\text{GeV}^2$. The open boxes (left-hand axis) show $\int_{x_m}^{1} g_1^p(x)dx$, where $x_m$ is the value of $x$ at the lower edge of each bin. Only statistical errors are shown. The solid square shows our result $\int_{x_m}^{1} g_1^p(x)dx$, with statistical and systematic errors combined in quadrature. Also shown is the theoretical prediction by Ellis and Jaffe [3].

are shown in Table 1.

The integral over the measured $x$ range is

$$\int_{x_m}^{0.7} g_1^p(x, Q_0^2)dx = 0.131 \pm 0.011 \pm 0.011. \quad (4)$$

Here, and in the following, the first error is statistical and the second is systematic. The contributions to the systematic error are detailed in Table 2.

To estimate the integral for $x > 0.7$, we take $A_1^p = 0.7 \pm 0.3$ for $0.7 < x < 1.0$, which is consistent with the bound $A_1 < 1$, and also with the result from perturbative QCD [24] that $A_1 \rightarrow 1$ as $x \rightarrow 1$. This contribution amounts to $0.0015 \pm 0.0007$. The integral $\int_{x_m}^{0.7} g_1^p(x)dx$ as a function of the lower integration limit, $x_m$, is shown in Fig. 3. The contribution to the integral of the unmeasured region $x < 0.003$ was evaluated assuming a Regge-type dependence $g_1^p(x) \propto x^\alpha$, with $0 < \alpha < 0.5$ [25]. Although $g_1$ shows a tendency to increase at low $x$, Table 1, we do not consider the trend significant enough to call into question the validity of Regge behavior.

The result for the first moment of $g_1^p(x)$ at $Q_0^2 = 10\text{GeV}^2$ is

<table>
<thead>
<tr>
<th>Source of the error</th>
<th>$\Delta \Gamma_1^p$</th>
</tr>
</thead>
<tbody>
<tr>
<td>Beam polarization</td>
<td>0.0057</td>
</tr>
<tr>
<td>Uncertainty on $F_2$</td>
<td>0.0052</td>
</tr>
<tr>
<td>Extrapolation at low $x$</td>
<td>0.0040</td>
</tr>
<tr>
<td>Target polarization</td>
<td>0.0039</td>
</tr>
<tr>
<td>Dilution factor</td>
<td>0.0034</td>
</tr>
<tr>
<td>Acceptance variation $\Delta r$</td>
<td>0.0030</td>
</tr>
<tr>
<td>Radiative corrections</td>
<td>0.0023</td>
</tr>
<tr>
<td>Neglect of $A_2$</td>
<td>0.0017</td>
</tr>
<tr>
<td>Momentum measurement</td>
<td>0.0020</td>
</tr>
<tr>
<td>Uncertainty on $R$</td>
<td>0.0018</td>
</tr>
<tr>
<td>Kinematic resolution</td>
<td>0.0010</td>
</tr>
<tr>
<td>Extrapolation at high $x$</td>
<td>0.0007</td>
</tr>
<tr>
<td>Total systematic error</td>
<td>0.0113</td>
</tr>
<tr>
<td>Statistics</td>
<td>0.0114</td>
</tr>
</tbody>
</table>
The Ellis-Jaffe sum rule, including first order QCD corrections [26], predicts $\Gamma^p = 0.176 \pm 0.006$ for $\alpha_s(10\text{GeV}^2) = 0.23 \pm 0.02$, corresponding to $\alpha_s(M_Z^2) = 0.113 \pm 0.004$ [27] and four quark flavors. Our measurement is two standard deviations below this value.

The first moment $\Gamma^p$ can be expressed in terms of the proton matrix element of the flavor singlet axial vector current $a_0$ [5] and the SU(3) coupling constants $F$ and $D$ [28]. We obtain $a_0 = 0.18 \pm 0.08 \pm 0.08$. In the quark-parton model, $a_0$ is proportional to $\Delta \Sigma = \Delta u + \Delta d + \Delta s$, the sum of the quark spin contributions to the nucleon spin. Our result corresponds to $\Delta \Sigma = 0.22 \pm 0.10 \pm 0.10$ (6) and $\Delta s = -0.12 \pm 0.04 \pm 0.04$ (7).

We thus find that only a small fraction of the nucleon spin is due to the helicity of the quarks, and that the strange sea is negatively polarized.

Our results are in good agreement with the previous measurements of E80/E130 and the EMC. A test of consistency of the experimental asymmetries $A^p(x)$ from all experiments yields $\chi^2 = 14.6$ for 15 degrees of freedom. To compare $g^p_1$, values we apply to the EMC asymmetries the same $F_2$ parametrization that we use in the present work. An evaluation of the integral over the $x$ range common to both experiments, at $Q_0^2 = 10\text{GeV}^2$, yields $\int_{0.01}^{0.7} g^p_1(x) dx = 0.124 \pm 0.013 \pm 0.019$ for the EMC and $\int_{0.01}^{0.7} g^p_1(x) dx = 0.118 \pm 0.010 \pm 0.009$ for our data. In the range $0 < x < 0.01$, the extrapolation of the EMC data gives $0.003 \pm 0.003$, while our two lowest $x$ points and our extrapolation give $\int_{0}^{0.01} g^p_1(x) dx = 0.017 \pm 0.006$.

For a common evaluation of $\Gamma^p_1$ from all existing data, we combine our results on $A^p_1(x)$ with those of E80/E130 and EMC. The extrapolations are recalculated from the combined asymmetries following the methods described above. The treatment of the systematic errors takes into account that some of them are correlated between the different experiments. This yields

$$\Gamma^p_1(10\text{GeV}^2) = 0.142 \pm 0.008 \pm 0.011$$

(All proton data), (8)

which is two standard deviations below the Ellis-Jaffe prediction. From this result, we obtain $\Delta \Sigma = 0.27 \pm 0.08 \pm 0.10$ and $\Delta s = -0.10 \pm 0.03 \pm 0.04$.

We now turn to a test of the Bjorken sum rule [2], using all available proton, neutron and deuteron data. We do this test at $Q^2 = 5\text{GeV}^2$ in order to avoid a large $Q^2$ evolution of the SLAC-E142 neutron data, which have an average $Q^2 = 2\text{GeV}^2$. A fit to $\Gamma^n_1$ (Eq. 8), $\Gamma^n_1$ [8] and $\Gamma_D^p$ [7], reevaluated at $5\text{GeV}^2$ under the assumption that the asymmetries $A_1$ are independent of $Q^2$, yields

$$\Gamma^p_1 - \Gamma^n_1 = 0.163 \pm 0.017 \quad (Q^2 = 5\text{GeV}^2),$$

(9)

where statistical and systematic errors are combined in quadrature. When one uses the available deuteron and proton data to replace the extrapolation on the neutron data, as discussed in Ref. [12], one obtains $\Gamma^p_1 = -0.069 \pm 0.025$ and

$$\Gamma^p_1 - \Gamma^n_1 = 0.204 \pm 0.029 \quad (Q^2 = 5\text{GeV}^2),$$

(10)

with a larger error due to the limited statistics in the deuteron experiment. The theoretical prediction, including perturbative QCD corrections up to third order in $\alpha_s$ [29], gives

$$\Gamma^p_1 - \Gamma^n_1 = 0.185 \pm 0.004 \quad (Q^2 = 5\text{GeV}^2),$$

(Theory)

(11)

which is in agreement with the above experimental results. Higher-twist effects are expected to contribute especially at low $Q^2$ [30,31], and have been estimated [11,31] to change $\Gamma^p_1 - \Gamma^n_1$ by about 2%, but the calculations are model dependent. We have therefore not taken these contributions into account.

In summary, we have presented a new measurement of the proton spin dependent structure function $g^p_1$. The measured asymmetries are in agreement with those of the earlier E80/E130 and EMC experiments, but systematic errors have been significantly reduced and the kinematic region has been extended down to $x = 0.003$. 

$$\int_0^1 g^p_1(x) dx = 0.136 \pm 0.011 \pm 0.011.$$ (5)
The first moment of the spin dependent structure function $g_1^p$, evaluated from our own data, is two standard deviations below the prediction of the Ellis-Jaffe sum rule. In the quark parton model, this result implies that the contribution of the quark spins to the proton spin is $0.22 \pm 0.14$. The Bjorken sum rule is now confirmed, at the one standard deviation level, to within 10% of its theoretical value.

References

J. Kodaira et al., Nucl. Phys. B159 (1979) 99;