Measurement of Branching Fractions and Search for CP-Violating Charge Asymmetries in Charmless Two-Body B Decays into Pions and Kaons

We present measurements, based on a sample of approximately $23 \times 10^6 B\bar{B}$ pairs, of the branching fractions and a search for $CP$-violating charge asymmetries in charmless hadronic decays of $B$ mesons into two-body final states of kaons and pions. We find the branching fractions $\mathcal{B}(B^0 \to K^+ \pi^-) = (4.1 \pm 1.0 \pm 0.7) \times 10^{-6}$, $\mathcal{B}(B^0 \to K^+ \pi^-) = (16.7 \pm 1.6 \pm 1.3) \times 10^{-6}$, $\mathcal{B}(B^+ \to K^0 \pi^0) = (10.8^{+2.1}_{-1.9} \pm 1.0) \times 10^{-6}$, $\mathcal{B}(B^+ \to K^0 \pi^+ ) = (18.2^{+3.3}_{-3.1} \pm 2.0) \times 10^{-6}$, $\mathcal{B}(B^0 \to K^0 \pi^0) = (8.2^{+3.2}_{-2.3} \pm 1.2) \times 10^{-6}$. We also report 90% confidence level upper limits for $B$ meson decays to the $\pi^+ \pi^0$. 

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The study of $B$ meson decays into charmless hadronic final states plays an important role in the understanding of CP violation, which, in the standard model, is a consequence of the phase in the Cabibbo-Kobayashi-Maskawa (CKM) quark-mixing matrix [1]. Recently, the BABAR and Belle Collaborations published measurements [2,3] of the angle $\beta$ of the CKM unitarity triangle from the study of $B$ decays into final states containing charmonium. Measurements of the rates and charge asymmetries for $B$ decays into the charmless final states $\pi\pi$ and $K\pi$ can be used to constrain the angles $\alpha$ and $\gamma$ [4] of the unitarity triangle.

In this Letter we present new measurements of the branching fractions for $B$ meson decays to the charmless hadronic final states $\pi^{+}\pi^{-}$, $K^{+}\pi^{-}$, $K^{+}\pi^{0}$, $K^{0}\pi^{+}$, and $K^{0}\pi^{0}$ [5]. In addition, we search for charge asymmetries in the modes $B^{0}\rightarrow K^{+}\pi^{-}$, $B^{+}\rightarrow K^{+}\pi^{0}$, and $B^{+}\rightarrow K^{0}\pi^{+}$. Measurements [6,7] of these decays were first reported by the CLEO Collaboration.

The data sample used in these analyses was collected with the BABAR detector [8] at the PEP-II $e^{+}e^{-}$ collider at the Stanford Linear Accelerator Center. It corresponds to an integrated luminosity of 20.6 fb$^{-1}$ taken on the $Y(4S)$ resonance (“on-resonance”), amounting to $(22.57 \pm 0.36) \times 10^{6} B\bar{B}$ pairs, and 2.61 fb$^{-1}$ taken at a center-of-mass (CM) energy 40 MeV below the $Y(4S)$ resonance (“off-resonance”), which are used for continuum background studies. The collider is operated with symmetric beam energies, producing a boost ($\beta\gamma = 0.56$) of the $Y(4S)$ along the collision axis ($z$). The boost increases the momentum range of two-body $B$ decay products from a narrow distribution centered near 2.6 GeV/$c$ to a broad distribution extending from 1.7 to 4.3 GeV/$c$.

The BABAR detector is a spectrometer of charged and neutral particles and is described in detail in Ref. [8]. Charged particle (track) momenta are measured in a tracking system consisting of a 5-layer, double-sided, silicon vertex detector and a 40-layer drift chamber (DCH) filled with a gas mixture of helium (80%) and isobutane (20%), both operating within a 1.5 T superconducting solenoidal magnet. Photons are detected in an electromagnetic calorimeter (EMC) consisting of 6580 CsI(Tl) crystals. Charged hadron identification is based on the Cherenkov angle $\theta_{c}$ measured by a unique, internally reflecting Cherenkov ring imaging detector (DIRC).

Hadronic events are selected based on track multiplicity and event topology. Backgrounds from nonhadronic events are reduced by requiring the ratio of Fox-Wolfram moments $H_{2}/H_{0}$ [9] to be less than 0.95 and the sphericity [10] of the event to be greater than 0.01. All tracks (except $K_{S}^{0}$ decay products) are required to have a polar angle within the tracking fiducial region $0.41 < \theta < 2.54$ radians and a Cherenkov measurement from the DIRC with a minimum of six photons above background, where the average is approximately 30 for both pions and kaons. The efficiency of requiring a $\theta_{c}$ measurement is 91% per track, and 97% of such tracks satisfy the minimum photon requirement. We reject tracks with a $\theta_{c}$ within $3\sigma$ of the expected value for a photon. Electrons are rejected based on specific ionization $(dE/dx)$ in the DCH system, shower shape in the EMC, and the ratio of shower energy to track momentum.

Candidate $K_{S}^{0}$ mesons are reconstructed from pairs of oppositely charged tracks that form a well-measured vertex and have an invariant mass within $3\sigma$ of the nominal $K_{S}^{0}$ mass [11]. The measured proper decay time of the $K_{S}^{0}$ candidate is required to exceed 5 times its error.

Candidate $\pi^{0}$ mesons are formed from pairs of photons with an invariant mass within $3\sigma$ of the nominal $\pi^{0}$ mass. Photons are defined as showers in the EMC that have the expected lateral shape, are not matched to a track, and have a minimum energy of 30 MeV. The $\pi^{0}$ candidates are then kinematically fitted with their mass constrained to the nominal $\pi^{0}$ mass.

$B$ meson candidates are reconstructed in four topologies: $h^{+}h^{-}$, $h^{+}\pi^{0}$, $K_{S}^{0}h^{+}$, and $K_{S}^{0}\pi^{0}$, where the symbols $h$ and $h'$ refer to $\pi$ or $K$. The kinematic constraints provided by the $Y(4S)$ initial state and relatively precise knowledge of the beam energies are exploited to efficiently identify $B$ candidates. We define a beam-energy substituted mass $m_{ES} = \sqrt{E_{b}^{2} - p_{b}^{2}}$, where $E_{b} = (s/2 + p_{1} \cdot p_{B})/E_{t}$, $E_{t}$ and $E_{i}$ are the total energies of the $e^{+}e^{-}$ system in the CM and lab frames, respectively, and $p_{1}$ and $p_{B}$ are the momentum vectors in the lab frame of the $e^{+}e^{-}$ system and the $B$ candidate, respectively. To improve the resolution in modes containing $\pi^{0}$ mesons, the $B$ candidate is kinematically fitted with the energy constrained to the CM beam energy. For all modes, the $m_{ES}$ resolution is dominated by the beam energy spread and is approximately 2.5 MeV/$c^{2}$. Candidates are selected in the range $5.2 < m_{ES} < 5.3$ GeV/$c^{2}$.

We define an additional kinematic parameter $\Delta E$ as the difference between the energy of the $B$ candidate and half the energy of the $e^{+}e^{-}$ system, computed in the CM system, where the pion mass is assumed for all charged decay products of the $B$. The $\Delta E$ distribution is peaked near zero for modes with no charged kaons and shifted on average $-45$ MeV ($-91$ MeV) for modes with one (two) kaons, where the exact separation depends on the laboratory kaon momentum. For modes with no $\pi^{0}$ mesons the $\Delta E$ resolution is about 26 MeV; with $\pi^{0}$ mesons the resolution is about 42 MeV and asymmetric due to underestimation of the $\pi^{0}$ energy in the EMC. Candidates are accepted in the following $\Delta E$ ranges (given in GeV): $[-0.15, 0.15]$.
The distributions of $\mathcal{F}$ for Monte Carlo simulated $B^0 \rightarrow h^+ h^-$ decays and background events in the $m_{ES}$ sideband region $5.20 < m_{ES} < 5.27$ GeV/c$^2$ are displayed in Fig. 1(a).

The final reconstruction efficiencies range from 31% to 45%, depending on the mode. Table I shows the overall detection efficiencies, which include the branching fractions of $K^0 \rightarrow K^0 \rightarrow \pi^+ \pi^-$ and $\pi^0 \rightarrow \gamma \gamma$ [11].

Signal yields are determined from an unbinned maximum likelihood fit that uses $m_{ES}$, $\Delta E$, $\mathcal{F}$, and $\theta_i$ (where applicable). Separate fits are performed for each of the four topologies, where the likelihood for a given candidate $j$ is obtained by summing the product of event yield $n_i$ and probability $\mathcal{P}_j$ over all possible signal and background hypotheses $i$. The $n_i$ are determined by maximizing the extended likelihood function $\mathcal{L}$:

$$\mathcal{L} = \exp \left( - \sum_{i=1}^{M} n_i \right) \prod_{j=1}^{N} \left[ \sum_{i=1}^{M} n_i p_i(\tilde{x}_j; \tilde{\alpha}_i) \right].$$

The probabilities $\mathcal{P}_j(\tilde{x}_j; \tilde{\alpha}_i)$ are evaluated as the product of probability density functions (PDFs) for each of the independent variables $\tilde{x}_j$, given the set of parameters $\tilde{\alpha}_i$. Monte Carlo simulation is used to validate the assumption that the fit variables are uncorrelated. The exponential factor in the likelihood accounts for Poisson fluctuations in the total number of observed events $N$. For the $K^0 \pi^0$, $\pi^0 \pi^0$, $K^0 \pi^\pm$, $K^\pm \pi^0$, $K^\pm \pi^\mp$, and $K^0 \pi^\pm$ terms, the yields are rewritten in terms of the sum $n_f + n_\gamma$ and the asymmetry $A = (n_\gamma - n_f)/(n_\gamma + n_f)$, where $n_f$ ($n_\gamma$) is the fitted number of events in the mode $B \rightarrow f$ ($B \rightarrow \gamma \gamma$). The number of events, $N$, entering the maximum likelihood fit for each topology are 16032 ($h^+ h^-$), 16452 ($h^+ \pi^0$), 3623 ($K_S^0 h^+ - h^-$), and 1503 ($K_S^0 \pi^0$).

The parameters for background $m_{ES}$ and $\Delta E$ PDFs are determined from events in on-resonance $\Delta E$ sideband regions. The signal $m_{ES}$ and $\Delta E$ PDF parameters

![Figure 1](image-url)
are determined from fully reconstructed $B^+ \rightarrow D^0 \pi^+$ and $B^+ \rightarrow D^0 \rho^+ (\rho^+ \rightarrow \pi^+ \pi^- \pi^0)$ decays. Events in on-resonance $m_{ES}$ sideband regions and Monte Carlo simulated signal decays are used to parametrize the Fisher discriminant PDFs for background and signal, respectively [see Fig. 1(a)]. Alternative parametrizations obtained from off-resonance data and Monte Carlo simulation are used as cross-checks and for determination of systematic uncertainties. The $\theta_s$ PDFs are derived from kaon and pion tracks in the momentum range of interest from approximately 42 000 $D^{*+} \rightarrow D^0 \pi^+$ ($D^0 \rightarrow K^- \pi^+$) decays. This control sample is used to parametrize the $\theta_s$ resolution $\sigma_{\theta_s}$ as a function of track polar angle. The resulting $K\pi$ separation, defined as $|\theta^K_c - \theta^\pi_c|/\sigma_{\theta_s}$, where $\theta^K_c$ (or $\theta^\pi_c$) is the expected Cherenkov angle for a kaon (pion), is shown as a function of momentum in Fig. 1(b).

The results of the fit are summarized in Table I, where the statistical error for each mode corresponds to a 68% confidence interval and is given by the change in signal yield $n_i$ that corresponds to a $-2\ln L$ increase of one unit. Signal significance is defined as the square root of the change in $-2\ln L$ with the corresponding signal yield fixed to zero. For the three modes that have statistical significance less than 4$\sigma$ we report Bayesian 90% confidence level upper limits. In addition, for the purpose of combining with measurements from other experiments, we report the branching fractions corresponding to the fitted signal yields. The upper limit on the signal yield for mode $i$ is given by the value of $n_i^0$ for which $\int_0^{n_i^0} L_{\text{max}} dn_i/\int_0^\infty L_{\text{max}} dn_i = 0.90$, where $L_{\text{max}}$ is the likelihood as a function of $n_i$, maximized with respect to the remaining fit parameters. Branching fraction upper limits are calculated by increasing the signal yield upper limit and reducing the efficiency by their respective systematic errors.

Figure 2 shows the distributions in $m_{ES}$ and $\Delta E$ for events passing the selection criteria, as well as requirements on likelihood ratios, which are used to increase the relative fraction of signal events of a given type. These likelihood ratios are defined for a given topology as $R_{\text{sig}} = \sum_i n_i P_i / \sum_i n_i P_i$ and $R_k = n_k P_k / \sum_i n_i P_i$, where $\sum_i$ denotes the sum over the probabilities for signal hypotheses only, $\sum_k$ denotes the sum over all the probabilities (signal and background), and $P_k$ denotes the probability for signal hypothesis $k$. These probabilities are constructed from all the PDFs except that describing the displayed variable. The likelihood fit projections, scaled by the relative efficiencies for the likelihood ratio requirements, are overlaid on each distribution.

Systematic uncertainties arise from imperfect knowledge of the PDF shapes, which affects both branching fraction and charge asymmetry measurements; uncertainties in the detection efficiencies; and potential charge bias in track reconstruction and particle identification.

The largest source of systematic error is due to uncertainty in the PDF shapes, except in $B^+ \rightarrow K^+ \pi^0$ where it is due to the 5% uncertainty on $\pi^0$ reconstruction efficiency. Systematic errors due to PDF shapes are estimated either by varying the parameters within 1 standard deviation, or by substituting alternative parameter sets obtained from off-resonance data, or $B^+ \rightarrow D^0 \pi^+ (\rho^+ \rightarrow \pi^+ \pi^- \pi^0)$ decays in the on-resonance sample. Systematic errors in the signal yields due to PDF uncertainties depend on decay mode as shown in Table I.

The $D^{*+}$ control sample of kaon and pion tracks is used to estimate systematic uncertainties in the asymmetries arising from possible charge biases in the $\theta_s$ quality requirements and from differences in $\theta_s$ reconstruction for different charge species. From these studies we conservatively assign a systematic uncertainty of $\pm 0.01$ on $A$ for all modes. Charge asymmetries in the detector and track reconstruction chain are shown to be less than 0.005 with high statistics samples of charged tracks in multihadron events. We assign an overall systematic uncertainty of $\pm 0.01$ on $A$ for possible charge-correlated biases in track reconstruction and particle identification. All measured background asymmetries are consistent with zero with
statistical uncertainties less than 0.03. The fitted signal yields and asymmetries for off-resonance data and on-resonance $\Delta E$ sidebands are also consistent with zero.

The overall systematic errors on the branching fractions and charge asymmetry measurements are computed by adding in quadrature the PDF systematic uncertainties and the systematic uncertainties on the efficiencies or because of possible charge biases, respectively.

In summary, we have measured branching fractions for the rare charmless decays $B^0 \to \pi^+ \pi^-$, $B^0 \to K^+ \pi^-$, $B^+ \to K^+ \pi^0$, $B^+ \to K^0 \pi^+$, and $B^0 \to K^0 \pi^0$, and set upper limits on $B^0 \to K^+ K^-$, $B^+ \to \pi^+ \pi^0$, and $B^+ \to K^0 K^+$. We find no evidence for direct $CP$ violation in the observed decays and set 90% confidence level intervals. These measurements are in good agreement with existing results [6,7,13].

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[5] Charge conjugate states are assumed throughout, except where explicitly noted.