Measurement of $J/\psi$ Production in Continuum $e^+e^-$ Annihilations near $\sqrt{s} = 10.6$ GeV

The production of \( J/\psi \) mesons in continuum \( e^+e^- \) annihilations has been studied with the BABAR detector at energies near the \( Y(4S) \) resonance. The mesons are distinguished from \( J/\psi \) production in \( B \) decays through their center-of-mass momentum and energy. We measure the cross section \( e^+e^- \rightarrow J/\psi X \) to be \( 2.52 \pm 0.21 \pm 0.21 \) pb. We set a 90\% C.L. upper limit on the branching fraction for direct \( Y(4S) \rightarrow J/\psi X \) decays at \( 4.7 \times 10^{-4} \).

The development of nonrelativistic QCD (NRQCD) represents a significant advance in the theory of the production of heavy quarkonium (q \( \bar{q} \)) states [1]. In particular, it provides an explanation [2] for the cross section for...
$\psi(2S)$ production observed by CDF [3], which is a factor of 30 larger than expected from previous models. The enhancement is attributed to the production of a $cc$ pair in a color octet state, which then evolves into the charmonium ($cc$) meson along with other light hadrons. A similar contribution is expected in NRQCD for $J/\psi$ production in $e^+e^-$ annihilation [4,5], but is absent in the color singlet model [6].

Significant continuum $J/\psi$ production—as distinct from production in $B$ decay at the $Y(4S)$ resonance—has not been observed previously in $e^+e^-$ annihilation below the $Z$ resonance. It therefore represents a good test of NRQCD. In particular, matrix elements extracted from different $J/\psi$ production processes should be consistent [7]. In addition, momentum, polarization, and particularly the angular distributions of the $J/\psi$ distinguish between theoretical approaches [8]. Despite NRQCD’s successes, it is not clear whether it correctly explains [9] the CDF theoretical approaches [8].

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The study reported here uses 20.7 fb$^{-1}$ of data collected at the $Y(4S)$ resonance (10.58 GeV) and 2.59 fb$^{-1}$ collected at 10.54 GeV, below the threshold for the $B\bar{B}$ creation. The luminosity-weighted center-of-mass (c.m.) energy is 10.57 GeV.

The data were collected with the BABAR detector [13] located at the PEP-II collider at the Stanford Linear Accelerator Center. PEP-II collides 9 GeV electrons with 3.1 GeV positrons to create a center of mass moving along the z axis with a Lorentz boost of $\beta\gamma = 0.56$.

The momenta and trajectories of charged particles are reconstructed with two detector systems located in a 1.5-T solenoidal magnetic field: a five-layer, double-sided silicon vertex tracker (SVT) and a 40-layer drift chamber (DCH). The fiducial volume covers the polar angular region $0.41 < \theta < 2.54$ rad, 86% of the solid angle in the c.m. frame.

The energies of electrons and photons are measured in a CsI(Tl) electromagnetic calorimeter (EMC) in the fiducial volume $0.41 < \theta < 2.41$ rad, 84% of the solid angle in the c.m. frame. The instrumented flux return is used to detect muons. The DIRC, a unique Cherenkov radiation detection device, distinguishes charged particles of different masses.

$J/\psi$ mesons are reconstructed via decays to electron or muon pairs. The leptons must match the visible energy and $R_2$ distributions for our signal—continuum-produced $J/\psi$ mesons and $J/\psi$ mesons from the decay of continuum-produced $\psi(2S)$ and $\chi_{cJ}$ mesons—and from other known sources. We apply additional selection criteria to suppress these other sources based on their kinematic properties.

The most copious background, $B \to J/\psi X$, is eliminated by requiring the $J/\psi$ momentum in the c.m. frame ($p^*$) to be greater than 2 GeV/c, above the kinematic limit for $B$ decays. This requirement is dropped for data recorded below the $Y(4S)$ resonance.

Other background sources include initial-state radiation (ISR) production of $J/\psi$ mesons, $e^+e^- \to \gamma J/\psi$, or of the $\psi(2S)$, with $\psi(2S) \to J/\psi X$. ISR production of lower-mass $Y$ resonances is negligible. Two photon production of the $\chi_{c2}$ can produce $J/\psi$ mesons via $\chi_{c2} \to \gamma J/\psi$. Because the out-going electron and positron are rarely reconstructed, this process, similar to the ISR $J/\psi$ production, contains only two tracks. Therefore we require three high-quality tracks with $0.41 < \theta < 2.54$ rad.

The remaining background is primarily ISR $\psi(2S)$ decays to $J/\psi \pi^+\pi^-$, plus some ISR $J/\psi$ events in which the ISR photon converts. To suppress these, we require the visible energy $E$ to be greater than 5 GeV, and the ratio of the second to the zeroth Fox-Wolfram moment [14], $R_2$, to be less than 0.5. Both are calculated from tracks and neutral clusters in the fiducial volume. Figure 1, which displays the visible energy and $R_2$ distributions for our signal and for simulated ISR background, motivates these criteria.

The ISR distributions in Fig. 1 are obtained from a full detector simulation. All selection criteria are applied, other than the one on the quantity being plotted. ISR kinematics ensures $E < 5$ GeV when the photon is outside the fiducial volume unless it interacts in material and deposits additional energy in the detector. The rate of such interactions is not accurately simulated and so is obtained by a...
show clear signals for both

e^+e^− and \( \mu^+\mu^- \) final states; the histogram is the predicted ISR background that has been subtracted from data; the filled histogram is the ISR component only. A requirement of \( >5 \) tracks is applied to the \( e^+e^- \) sample; applying it to the \( \mu^+\mu^- \) sample produces the dashed histogram. Event preselection requires \( E > 4 \) GeV and \( R_2 < 0.95 \).

comparison to data for \( E < 5 \) GeV. Approximately 3.5% of the \( J/\psi \) meson events that satisfy all criteria are from this background; an additional \( \sim 1.6\% \) are ISR events with the photon in the fiducial volume. Systematic errors on the remaining backgrounds are estimated from a comparison between simulation and data for \( E < 5 \) GeV and for events in which the ISR photon is reconstructed.

\( J/\psi \) production as a function of \( E \) is obtained in the data by fitting the dilepton mass distribution in 1-GeV wide energy intervals after applying all other selection criteria. The fit uses a polynomial function for the background distribution. The \( J/\psi \) mass function is obtained from a complete simulation of \( B \to J/\psi X \) events, convolved with a Gaussian distribution to match the resolution of 12 MeV/\( c^2 \) observed in data in a sample of approximately 14 000 \( B \to J/\psi X \) events. The signal distribution in \( E \) is obtained by subtracting the ISR backgrounds from the data distribution.

A similar process is used for \( R_2 \). Figures 1(c) and 1(d) show there is little signal above \( R_2 \) of 0.5. In this respect, the continuum \( J/\psi \) events are more similar to \( BB \) events, in which the energy is distributed spherically, than \( c\bar{c} \) events, which tend to be jetlike.

The mass distributions of the selected \( J/\psi \) candidates show clear signals for both \( e^+e^- \) and \( \mu^+\mu^- \) final states, both on and below resonance (Fig. 2).

to determine the production cross section, we perform mass fits in 15 \( p^*\cos\theta^* \) bins, where \( \theta^* \) is the polar angle of the candidate in the c.m. frame. This allows us to correct

\begin{align}
\sigma_{e^+e^−→J/\psi X} &= \sum_{ij} \epsilon_{ij}^R \cdot e^E \cdot \mathcal{B}_{j/\psi→e^+e^-} \cdot \mathcal{L}_i,
\end{align}

where the sum is over three \( p^* \) (i) and five \( \cos\theta^* \) (j) bins. \( N_{ij} \) is the number of \( J/\psi \) mesons in the bin, where electrons and muons are analyzed separately, but off- and on-resonance data are combined. The sum of the yields from the 15 fits agrees to within 1% with the yields in Fig. 2. \( B_{ij} \) is the ISR background, \( \mathcal{B}_{j/\psi→e^+e^-} \) is the \( J/\psi \to e^+e^- \) or \( \mu^+\mu^- \) branching fraction [15], and \( \mathcal{L}_i \) is the integrated luminosity—sum of on plus off-resonance for \( p^* > 2 \) GeV/\( c \), off resonance only for \( p^* < 2 \) GeV/\( c \).

The reconstruction efficiency \( \epsilon_{ij}^R \) (acceptance, track quality, and lepton identification) is calculated in each bin with simulated unpolarized \( J/\psi \) mesons uniformly distributed in \( p^* \) and \( \cos\theta^* \). The efficiency decreases with increasing \( p^* \) and \( \cos\theta^* \) due to acceptance. The average \( \epsilon_{ij}^R \) is 0.63 for \( J/\psi \to e^+e^- \) and 0.48 for \( J/\psi \to \mu^+\mu^- \), where the difference is due to lepton identification.

Particle identification efficiency is verified in data by comparing the number of \( J/\psi \) mesons in \( B \) decays in which one or both leptons satisfy the requirements. The efficiency of the track-quality selection is studied by comparing tracks found in the SVT and DCH.

The components of \( e^E \), the event selection efficiency, are determined as follows. We estimate the efficiency of the requirements on the number of high-quality tracks, primary vertex location, and total energy to be the average of simulated \( c\bar{c} \) and \( BB \) events, and the uncertainty to be one-half the difference. We use \( BB \) events for \( R_2 \).

The efficiency of the five track requirement applied to \( e^+e^- \) candidates is 0.67, obtained by comparing the net
\( J/\psi \) yield, in both \( e^+e^- \) and \( \mu^+\mu^- \) final states, in events passing and failing the requirement. Overall, \( e^+e^- = 0.59 \) for \( e^+e^- \) and 0.89 for \( \mu^+\mu^- \).

The calculations of the \( J/\psi X \) cross section from the \( e^+e^- \) and \( \mu^+\mu^- \) final states are consistent: the ratio \( \sigma(e^+e^-)/\sigma(\mu^+\mu^-) \) is 0.93 ± 0.11 for \( p^* > 2 \) GeV/c. The two values are combined, accounting for common systematic errors, to obtain

\[
\sigma_{e^+e^- J/\psi X} = 2.52 \pm 0.21 \pm 0.21 \text{ pb}, \tag{2}
\]

where the first error is statistical and the second systematic. With existing values for matrix elements, color singlet cross section estimates range from 0.45 to 0.81 pb [4–6], while NRQCD cross sections, including a color octet component, range from 1.1 to 1.6 pb [4,5].

The dominant component of the 8.3% systematic error is a 7.2% uncertainty on \( e^+e^- \) common to both the \( e^+e^- \) and \( \mu^+\mu^- \) cases and a 4.9% uncertainty due to the five track requirement. Other contributions include 2.4% due to track quality cuts; 1.5% from the luminosity; 1.8% (electrons) or 1.4% (muons) from particle identification; and 1.2% from the ISR background.

The statistical error is dominated by the uncertainty on the contribution below \( p^* > 2 \) GeV/c. Restricting the measurement to \( p^* > 2 \) GeV/c gives \( \sigma_{e^+e^- J/\psi X} = 1.87 \pm 0.10 \pm 0.15 \) pb.

In determining the cross sections, we assume that there are no \( J/\psi \) mesons from direct \( Y(4S) \) decays. We quantify this statement using the \( p^* > 2 \) GeV/c component. We scale the off-resonance event yield to the on-resonance luminosity and subtract it from the on-resonance yield. The excess, attributable to \( Y(4S) \) decays, is consistent with zero: \( -120 \pm 179 \) \( e^+e^- \) events and \( 176 \pm 138 \) \( \mu^+\mu^- \), in a sample of \( 22.7 \pm 0.4 \times 10^6 \) \( Y(4S) \) decays. Using the average reconstruction efficiency for \( p^* > 2 \) GeV/c (0.62 for \( e^+e^- \) and 0.45 for \( \mu^+\mu^- \)), we obtain \( \mathcal{B}_{Y(4S) \rightarrow J/\psi X} = (1.5 \pm 2.2 \pm 0.1) \times 10^{-4} \). A Bayesian 90% confidence level upper limit with a uniform prior above zero is

\[
\mathcal{B}_{Y(4S) \rightarrow J/\psi X} < 4.7 \times 10^{-4} \text{ (90% C.L.)}, \tag{3}
\]

for \( J/\psi \) with \( p^* > 2 \) GeV/c. This result disagrees with a previous publication [16]. In NRQCD, the expected partial width is similar to that for the \( Y(1S) \) [5,17], implying a branching fraction of a few \( \times 10^{-6} \). Note that a true branching fraction of \( 10^{-4} \) would correspond to an effective cross section of 0.10 pb.

Production and decay properties of the \( J/\psi \) have also been studied. The \( p^* \) distribution is obtained by dividing the sample into 500 MeV/c wide intervals, fitting the resulting mass distribution, subtracting predicted ISR backgrounds, correcting for the reconstruction efficiency, and normalizing for different luminosities (Fig. 3).

The distribution of the signal in \( \cos\theta^* \) has been extracted and fit with \( 1 + A \cdot \cos^2\theta^* \). Both NRQCD and color singlet calculations predict a flat distribution \( (A = 0) \) at low \( p^* \). At high momentum, NRQCD predicts \( 0.6 < A < 1.0 \)

\[ p^* < 3.5 \text{ GeV/c} \]

while the color singlet model predicts \( A = -0.8 \) [8]. We measure the distribution separately for low and high momentum mesons, selecting \( p^* > 3.5 \) GeV/c as the boundary. We proceed as for the \( p^* \) distribution, with mass fits performed in \( \cos\theta^* \) intervals of width 0.4. The distributions are then normalized to the unit area [Fig. 4(a)]. We find \( A = 0.05 \pm 0.22 \) for \( p^* < 3.5 \) GeV/c and \( A = 1.5 \pm 0.6 \) for \( p^* > 3.5 \) GeV/c, clearly favoring NRQCD.

Finally, we obtain the helicity angle \( \theta_H \) distribution for the two \( p^* \) ranges by fitting mass distributions in intervals of width 0.4 in \( \cos\theta_H \) [Fig. 4(b)]. The helicity is measured in the rest frame of the \( J/\psi \), between the positively charged lepton daughter and the direction of the \( J/\psi \) measured in the c.m. frame. Fitting the function \( 3(1 + \alpha \cos^2\theta_H)/(2(\alpha + 3)) \), we obtain a \( J/\psi \) polarization \( \alpha = -0.46 \pm 0.21 \) for \( p^* < 3.5 \) GeV/c and \( \alpha = -0.80 \pm 0.09 \) for \( p^* > 3.5 \) GeV/c. \( \alpha = 0 \) indicates an unpolarized distribution, \( \alpha = 1 \) transversely polarized, and \( \alpha = -1 \) longitudinally polarized.

In summary, we measure the cross section \( \sigma_{e^+e^- J/\psi X} = 2.52 \pm 0.21 \pm 0.21 \) pb. Restricting to \( p^* > 2 \) GeV/c, we find \( 1.87 \pm 0.10 \pm 0.15 \) pb. The total cross section and the angular distribution favor the NRQCD calculation over the color singlet model. We set a 90% C.L. upper limit on the branching fraction \( \mathcal{B}_{Y(4S) \rightarrow J/\psi X} = 4.7 \times 10^{-4} \).

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FIG. 3. Center-of-mass momentum distribution of \( J/\psi \) mesons produced in continuum \( e^+e^- \) annihilation.

FIG. 4. (a) Production angle (\( \cos\theta^* \)) distribution for \( J/\psi \) mesons produced in continuum \( e^+e^- \) annihilation; (b) helicity (\( \cos\theta_H \)) distribution. Solid curve is the fit to \( p^* < 3.5 \) GeV/c; dashed curve is for \( p^* > 3.5 \) GeV/c.
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