Measurement of $D_s^+$ and $D_s^{*+}$ production in $B$ meson decays and from continuum $e^+e^-$
annihilation at $\sqrt{s} = 10.6$ GeV

B. Aubert,1 D. Boutigny,1 J.-M. Gaillard,1 A. Hicheur,1 Y. Karyotakis,1 J. P. Lees,1 P. Robbe,1 V. Tisserand,1 A. Palano,2
A. Pompli,2 G. P. Chen,3 J. C. Chen,3 N. D. Qi,3 G. Kong,3 P. Wang,3 Y. S. Zhu,3 G. Eigen,4 B. Stugu,4
G. S. Abrams,5 W. Bogorland,5 A. B. Breon,5 D. N. Brown,5 J. Button-Shafer,5 R. N. Cahn,5 A. R. Clark,5 M. S. Gill,5
M. T. Ronan,5 G. V. Shelkov,5 A. V. Telnov,5 W. A. Wenzel,5 P. G. Bright-Thomais,5 T. J. Harrison,6 C. M. Hawkes,6
D. J. Knowles,6 S. W. O. Neale,6 R. C. Perry,6 A. T. Watson,6 T. Deppermann,6 K. Goetzen,6 H. Koch,6
M. Kunze,7 B. Lewandowski,7 K. Peters,7 H. Schmuecker,7 M. Steinke,7 J. C. Andress,8 N. R. Barlow,8 W. Bhimji,8
N. Chevalier,8 P. J. Clark,8 W. N. Cottingham,8 N. Dyce,8 B. Foster,8 C. Mackay,8 D. Wallom,8 F. F. Wilson,8 K. Abe,9
C. Hearty,9 T. S. Mattison,9 J. A. McKenna,9 D. Thiessen,9 S. Jolly,10 A. K. McKemy,10 V. E. Blinov,11 A. D. Bukanin,11
M. Chao,12 A. J. Lankford,12 M. Mandelkern,12 S. McMahon,12 D. P. Stoker,12 K. Arisaka,13 C. Buchanan,13 S. Chun,13
D. B. MacFarlane,14 S. Prell,14 Sh. Rahatlou,14 G. V. Sharma,14 C. Campagnari,15 B. Duhmes,15 P. A. Hart,15
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D. C. Williams,16 M. G. Wilson,16 E. Chen,17 G. P. Dubois-Felsmann,17 A. Dvoretskii,17 D. G. Hitlin,17 S. Metzler,17
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W. Kozanecki,21 M. Langer,21 G. W. London,21 B. Mayer,21 B. Serfass,21 G. Vasseur,21 Ch. Yeeche,21 M. Zito,21
T. Brandt,22 J. Brose,22 T. Colberg,22 M. Dickopp,22 R. S. Dubitzky,22 A. Hauke,22 E. Malý,22 R. Müller-Pfefferkorn,22
C. Borean,24 C. Bozzi,24 S. Dittongo,24 L. Piemontese,24 E. Treadwell,24 F. Anulli,28 R. Baldini-Ferroli,28
A. Calcaterra,28 R. de Sangro,28 D. Falciai,28 G. Finocchiaro,28 P. Patteri,28 M. Piccolo,28 Y. Xie,28
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New measurements of $D_s^+$ and $D_s^{*+}$ meson production rates from $B$ decays and from $qar{q}$ continuum events near the $Y(4S)$ resonance are presented. Using 20.8 fb$^{-1}$ of data on the $Y(4S)$ resonance and 2.6 fb$^{-1}$ off-resonance, we find the inclusive branching fractions $\mathcal{B}(B \to D_s^+ X) = (10.93 \pm 0.19 \pm 0.58 \pm 2.73)\%$ and $\mathcal{B}(B \to D_s^{*+} X) = (7.9 \pm 0.8 \pm 0.7 \pm 2.0)\%$, where the first error is statistical, the second is systematic, and the third is due to the $D_s^+ \to \phi \pi^+$ branching fraction uncertainty. The production cross sections $\sigma(e^+ e^- \to D_s^+ X) \times \mathcal{B}(D_s^+ \to \phi \pi^+) = 7.55 \pm 0.20 \pm 0.34$ pb and $\sigma(e^+ e^- \to D_s^{*+} X) \times \mathcal{B}(D_s^{*+} \to \phi \pi^+) = 5.8 \pm 0.7 \pm 0.5$ pb are measured at center-of-mass energies about 40 MeV below the $Y(4S)$ mass. The branching fractions $\Sigma \mathcal{B}(B \to D_s^{(*)+} D_s^{(*)}) = (5.07 \pm 0.14 \pm 0.30 \pm 1.27)\%$ and $\Sigma \mathcal{B}(B \to D_s^{(*)+} D^{(*)}) = (4.1 \pm 0.2 \pm 0.4 \pm 1.0)\%$ are determined from the $D_s^{(*)+}$ momentum spectra. The mass difference $m(D_s^{(*)}) - m(D^*) = 98.4 \pm 0.1 \pm 0.3$ MeV/c$^2$ is also measured.

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I. INTRODUCTION

The decay of $B$ mesons into final states involving a $D^{*(s)^+}$ provides an opportunity to study the production mechanisms for $c\bar{s}$ quark pairs. Although several diagrams can lead to $D^{*(s)^+}$ production in $B$ decays, the dominant source [1] is expected to be external $W^+\rightarrow c\bar{s}$ emission [Fig. 1]. A precise knowledge of this production rate remains interesting in light of continuing theoretical difficulties [2] in accounting for the measurements of both the semileptonic branching fraction and the inclusive charm production rate in $B$ decays. Indeed, it has been noted that an enhanced $B$ decay rate to charm would help explain the small observed semileptonic rate [3].

It is possible to produce $D^{*(s)^+}$ mesons in $q\bar{q}$ events from continuum $e^+e^-$ annihilation. The process of fragmentation (i.e., formation of hadrons) is nonperturbative and can only be modeled phenomenologically. The ratio of vector to pseudoscalar production rates is of particular interest for testing such models. The $D^+_s$ system is well suited to measure this quantity because the $c\bar{s}$ states with $L=1$ have not been observed to decay to either $D^+_s$ or $D^{*(s)^+}$ mesons.

In this Rapid Communication, measurements of $B \rightarrow D^+_s X$ and $B \rightarrow D^{*(s)^+}_s X$ production rates and momentum spectra are presented. We also determine the production cross section for $D^+_s$ and $D^{*(s)^+}_s$ mesons in continuum events.

II. THE BABAR DETECTOR AND DATA SET

The data used for this analysis were collected with the BABAR detector [4] at the PEP-II asymmetric-energy collider [5] at the Stanford Linear Accelerator Center. An integrated luminosity of 20.8 fb$^{-1}$ was recorded in 1999 and 2000 at the $Y(4S)$ resonance (“on-resonance”) corresponding to about $22.7 \times 10^6$ produced $B\bar{B}$ pairs, and 2.6 fb$^{-1}$ at an energy of about 40 MeV below the $Y(4S)$ mass (“off-resonance”). A detailed description of the BABAR detector can be found in Ref. [4]. Only the components of the detector most crucial to this analysis are summarized below.

A five-layer double-sided silicon vertex tracker (SVT) and a 40-layer central drift chamber (DCH) filled with helium-based gas are used to measure the momenta of charged particles. The tracking system covers 92% of the solid angle in the center-of-mass frame and lies within a 1.5-T solenoidal magnetic field. For charged-particle identification, ionization-energy loss ($dE/dx$) in the DCH and SVT, and Cherenkov radiation detected in a ring-imaging device (DIRC) are used. Photons are identified and measured by a CsI(Tl) electromagnetic calorimeter.

III. THE $D^+$ AND $D^{*(s)^+}$ SELECTION

Only the decay mode $D^+_s \rightarrow \phi \pi^+$ with $\phi \rightarrow K^+K^-$ is used since it has the best signal-to-background ratio. Charged tracks are required to originate within $\pm 10$ cm of the interaction point along the beam direction and $\pm 1.5$ cm in the transverse plane, and to leave at least 12 hits in the DCH.

Positive kaon identification is required for the tracks forming the candidate $\phi$ meson. This is based on $dE/dx$ information from the DCH and SVT, and the Cherenkov angle and the number of photons measured with the DIRC. The kaon selection is based on the likelihood calculated for each detector component and uses, for each track, the ratio of likelihoods for the pion and the kaon mass hypotheses, $L_\pi/L_K$. If this ratio is less than unity for at least one of the detector subsystems, the particle is selected as a “loose” kaon candidate. A “tight” identification criterion is also used in the analysis, based on the product of the likelihoods for each detector component. In this case, the track is considered a kaon if the ratio of the product likelihoods for the pion- and kaon-mass hypotheses is less than unity.

Three charged tracks originating from a common vertex are combined to form a $D^+$ candidate. Two oppositely charged tracks must be identified as kaons with the “loose” criterion, and at least one of them must pass the “tight” criterion. No identification criteria are applied to the pion from $D^+_s$ decay. The reconstructed invariant mass of the $K^+K^-$ candidates must be within 8 MeV/$c^2$ of the nominal $\phi$ mass [6]. In the decay $D^+_s \rightarrow \phi \pi^+$, the $\phi$ meson is polarized longitudinally and therefore the angular distribution of the kaons has a $\cos^2 \theta_{\phi}$ dependence, where $\theta_{\phi}$ is the angle between the $K^+$ and $D^+_s$ in the $\phi$ rest frame. We require $|\cos \theta_{\phi}| > 0.3$, which Monte Carlo studies show retains 97% of the signal while rejecting about 30% of the background.

With these requirements, signals for $D^+_s \rightarrow \phi \pi^+$ and the Cabibbo-suppressed decay $D^+ \rightarrow \phi \pi^+$ are readily observed [Fig. 2(a)]. The $D^+_s$ and $D^+$ peaks are both fit with single Gaussian distributions with a common width. We model the combinatorial background with an exponential function. From the fit a $D^+_s$ signal of 47 794 ± 311 events is found with a mass difference $m(D^+_s) - m(D^+)$ of 98.4 ± 0.1 ± 0.3 MeV/$c^2$. The first error on the latter is statistical, and the second is systematic, obtained from a study of the mass difference as a function of momentum in both data and Monte Carlo simulation. Although the uncertainties in the absolute mass scale are on the order of several MeV/$c^2$, the systematic error in the determination of the $D^+_s$ and $D^+$ mass difference is much smaller, since many sources of error cancel.

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1 Reference in this paper to a specific decay channel or state also implies the charge-conjugate decay or state. The notation $D^{*(s)^+}$ means either $D^+_s$ or $D^{*(s)^+}$. $B \rightarrow D^{*(s)^+}\bar{D}^{*(s)}$ is a general representation for any of the modes with $c\bar{s}$ and $c\bar{q}$ states including their excited states. The notation $B \rightarrow D^{*(s)^+}_s X$ also implies $B \rightarrow D^{*(s)^+}_s X$.

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**FIG. 1.** The main spectator diagram leading to the production of $D^{*(s)^+}_s$ mesons in $B$ decays.
with a Crystal Ball function [7], which incorporates a Gaussian core with a power-law tail toward lower masses. For the background, a threshold function

$$f(\Delta M) = p_1(\Delta M - p_2)^{p_3}e^{p_4(\Delta M - p_5)}$$

is used, where the four parameters $p_i$ are free in the fit. After ensuring that the connection point between the Gaussian and power-law tail does not depend on momentum and agrees with Monte Carlo simulation, this parameter has been fixed to 0.89σ in the final fit. A signal with $14392\pm376$ $D_s^+$ events is observed.

IV. EXTRACTION OF $D_s^{(*)+}$ MOMENTUM SPECTRA

The momentum spectrum of $D_s^+$ mesons in the $e^+e^-$ center-of-mass frame is extracted by fitting the $\phi\pi$-invariant mass distribution for 24 ranges of $D_s^+$ candidate momentum. These ranges are 200 MeV/c wide, which is much larger than the momentum resolution ($\approx 6$ MeV/c). The same function with two single Gaussians described above for the fit to the full mass distribution is used as well for the individual momentum bins. Since there are many more events in the on-resonance data sample, the number of $D_s^+$ in the off-resonance data is extracted with the Gaussian parameters ($M_{D_s^+}$, $M_{D_s^+}$, and $\sigma$) fixed to the values obtained from the on-resonance data.

The center-of-mass momentum spectrum for $D_s^{(*)+}$ mesons is extracted by fitting the $\Delta M$-invariant mass distribution in 250 MeV/c-wide $D_s^{(*)+}$ momentum ranges. We use a larger range because the $D_s^{(*)+}$ yield is lower. The $\Delta M$ distributions are modeled with a Crystal Ball function for the signal and a threshold function for the background as described above for the fit to the full distribution. The off-resonance data are again fit with the Gaussian parameters ($\bar{\lambda}$ and $\sigma$) fixed to the values obtained from the on-resonance data.

The efficiency $\epsilon$, obtained from Monte Carlo simulation of $B\bar{B}$ and $c\bar{c}$ events, varies as a function of the $D_s^{(*)+}$ center-of-mass momentum $p^*$. The efficiency ranges from 20% (5%) when the $D_s^+$ ($D_s^{(*)+}$) is at rest to 40% (20%) for $p^* = 5$ GeV/c. The efficiency-corrected momentum spectra of $D_s^+$ and $D_s^{(*)+}$ are shown in Fig. 3.

V. INCLUSIVE BRANCHING FRACTIONS

The $D_s^+$ and $D_s^{(*)+}$ production cross sections in $q\bar{q}$ continuum are obtained by integrating the momentum spectra obtained from the off-resonance data. This gives

$$\sigma(e^+e^-\rightarrow D_s^{(*)+}X)\times \mathcal{B}(D_s^{(*)+}\rightarrow \phi\pi) = 7.55\pm0.20\pm0.34 \text{ pb},$$

$$\sigma(e^+e^-\rightarrow D_s^+X)\times \mathcal{B}(D_s^+\rightarrow \phi\pi) = 5.8\pm0.7\pm0.5 \text{ pb},$$

where the first error is statistical and the second systematic. Sources of systematic error are listed in Table I. These include the statistical precision of the Monte Carlo determination of the efficiency, the luminosity uncertainty, and contributions from residual uncertainties on tracking (1.2% per track), and particle identification efficiencies, which are de-
FIG. 3. Efficiency-corrected center-of-mass momentum spectra for (a) $D_s^+$ and (b) $D_s^{*+}$ for on-resonance (filled circles) and scaled off-resonance data (open circles).

terminated from control samples in data. In addition, for the $D_s^{*+}X$ measurement, there are contributions from the uncertain signal shape, and residual uncertainties on the photon and $\pi^0$ veto efficiencies, again determined with control samples.

In order to determine the momentum spectra for $D_s^{(*)+}$ mesons from $B$ meson decays, the off-resonance data are scaled by the on- to off-resonance luminosity ratio and then subtracted bin by bin from the on-resonance data. Integrating the resulting spectrum after continuum subtraction and efficiency correction gives a total $D_s^+$ yield from $B$ meson decays of $87711 \pm 1485$ events. This corresponds to an inclusive branching fraction of

$$B(B \rightarrow D_s^+X) = \left[ \frac{(3.6 \pm 0.9)\%}{B(D_s^+ \rightarrow \phi \pi^+)} \right] \text{GeV}/c.$$  

Likewise, the total $D_s^{*+}$ yield from $B$ meson decays is $60047 \pm 6201$ events, leading to the inclusive branching fraction of

$$B(B \rightarrow D_s^{*+}X) = \left[ \frac{(7.9 \pm 0.8 \pm 0.7)\%}{B(D_s^{*+} \rightarrow \phi \pi^+)} \right] \text{GeV}/c.$$  

In the results above, the first error is statistical and the second is systematic. The dominant error, due to the uncertainty in the $D_s^{*+} \rightarrow \phi \pi^+$ branching fraction of $(3.6 \pm 0.9)\%$ [6], is shown separately. It is important to note that, with this method, the result is independent of any assumption regarding the shape of the fragmentation function. The various contributions to the systematic error are listed in Table I. In addition to the sources already noted above, the uncertainty in the shape of the background impacts this measurement, particularly in the lower momentum bins. This contribution is estimated with the use of different parametrizations for the background shape and different methods for handling the continuum subtraction. The efficiency variation over the width of the momentum bins is also included as an additional systematic error.

VI. FITS TO $D_s^{(*)+}$ MOMENTUM SPECTRA

By fitting the $D_s^{(*)+}$ momentum spectrum, relative branching fractions of $B$ decays to different final states containing $D_s^{(*)+}$ mesons are obtained. In the $Y(4S)$ rest frame, two-body $B$ decays produce $D_s^{(*)+}$ mesons with a momentum spectrum about 300 MeV/c wide. In $B$ decays, the $D_s^{(*)+}$ momentum spectrum is essentially governed by the production of direct $D_s^{(*)+}$. Other $c\bar{s}$ states (with $L=1$), such as $D_{s1}^+$ (2536) and $D_{s2}^+$ (2573), primarily decay to $D^{(*)}K$. Because $D_s^{(*)+}$ decays to $D_s^+ \gamma$ or $D_s^+ \pi^0$, the $D_s^+$ momentum distribution is slightly broader and shifted downward compared to direct production from $B \rightarrow D_s^+X$.

Three different sources of $D_s^{(*)+}$ mesons in $B$ decays are considered for the fits to the momentum spectra.

1. $B \rightarrow D_s^{(*)+}\bar{D}(*)$ decays. The relative branching frac-
tions of the individual channels can be taken either from existing measurements [8] or from predictions that assume factorization [9–11]. The fit is performed for both cases, with the assumption \( f_{D^s(*)} = f_{D^s} \) for the theoretical models, where \( f_{D^s(*)} \) are the \( D^s(*) \) decay constants.

(2) \( B \to D^{s(*)+} \bar{D}^{**} \) decays. Four \( \bar{D}^{**} \) states are considered: \( \bar{D}^{s0}_0(j = \frac{1}{2}), \bar{D}^{s0}_1(2420), \bar{D}^{s0}_2(j = \frac{1}{2}), \) and \( \bar{D}^{s2}_2(2460) \). Observation of \( B \to D^{s(*)+} \bar{D}^{**} \) decays was recently reported by CLEO [12].

(3) Three-body \( B \to D^{(*)+} \bar{D}^{(*)} \pi/\rho/\omega \) decays. Since little is known about these decays, they are attributed equal weights, and the momentum distributions are generated according to phase space.

Minimum-\( \chi^2 \) fits to the \( D^{s(*)+} \) momentum spectra are performed, where the total number of \( D^{s(*)+} \) events and the fractions of the source (1) and (2) contributions are free parameters. From the fits to the \( D_s^+ \) and \( D_s^{(*)+} \) spectra, the ratios of two-body modes [source (1)] to the total inclusive rate are determined to be

\[
\frac{\Sigma B(B \to D^{s(*)+} \bar{D}^{(*)})}{B(B \to D_s^+ X)} = (46.4 \pm 1.3 \pm 1.4 \pm 0.6)\% ,
\]

\[
\frac{\Sigma B(B \to D^{s(*)+} \bar{D}^{(*)})}{B(B \to D_s^+ X)} = (53.3 \pm 3.7 \pm 3.1 \pm 2.1)\% .
\]

The first error is statistical. The second error represents the systematic error due to the limited Monte Carlo statistics and the background parametrization.

The last error is due to the model uncertainty. It is obtained by varying the relative fractions of the modes contributing to each source of \( D^{s(*)+} \) listed above. The fit is performed with alternative assumptions for the relative contributions of the modes in source (1) taken from theoretical predictions and measurements. Different weights for \( B \to D_s^+ \bar{D}^{**} \) and \( B \to D_s^{(*)+} \bar{D}^{**} \), as well as different relative branching fractions of the four modes within source (2), are used. For source (3), either \( B \to D_s^{(*)+} \bar{D}^{(*)} \pi \), or \( B \to D_s^{(*)+} \bar{D}^{(*)} \rho/\omega \) is assumed to be dominant. The \( \chi^2 \) of the fit for the inclusive \( D_s^{(*)+} \) momentum spectrum is lowest when the contribution of \( B \to D_s^{(*)+} \bar{D}^{(*)} \rho/\omega \) is dominant compared to \( B \to D_s^{(*)+} \bar{D}^{(*)} \pi \). Uncertainty in source (3) is the main contribution to the error due to model dependence. The results of the fits to the \( D_s^{(*)+} \) momentum spectra are shown in Fig. 4 under the assumption of equal weights for the individual contributions within sources (2) and (3), and with the weights of the individual modes of source (1) taken from [11].

The sum of branching fractions for the two-body \( B \to D^{s(*)+} \bar{D}^{(*)} \) decays are obtained from the fits to the \( D_s^{(*)+} \) momentum spectra, where the yield from each source is a free parameter. We find

\[
\Sigma B(B \to D_s^{(*)+} \bar{D}^{(*)}) = (5.07 \pm 0.14 \pm 0.30 \pm 1.27)\% ,
\]

\[
\Sigma B(B \to D_s^{(*)+} \bar{D}^{(*)}) = (4.1 \pm 0.2 \pm 0.4 \pm 1.0)\% ,
\]

where the first error is statistical, the second is systematic, and the third is due to the \( D_s^+ \to \phi \pi^+ \) branching fraction uncertainty. The systematic error includes contributions from the \( B \to D_s^{(*)+} X \) branching fractions, the relative contributions of source (1), and the model dependence of the source spectra. The sum of the two-body modes is reasonably separated in the momentum spectra from the other components. Therefore, the fractional error on the sum of the two-body
modes is smaller than the fractional error on the $B \to D_s^{(*)} X$ branching fraction or the relative two-body branching ratio.

VII. SUMMARY

In summary, the branching fractions for inclusive $B \to D_s^{(*)} X$ production have been determined as well as the $D_s^{(*)}$ production cross-sections from continuum events at center-of-mass energies about 40 MeV below the $Y(4S)$ mass. Our more precise results for the $D_s^{*}$ are in agreement with previous measurements [8,13], while the $D_s^{*}$ measurements are new. In contrast to previous results, our measurements do not rely on any assumptions regarding the shape of the fragmentation function. Finally, fits to the $D_s^{(*)}$ momentum spectra provide relative yields and branching fractions for two-body $B \to D_s^{(*)} \bar{D}(s)_{(*)}$ and $B \to D_s^{(*)} \bar{D}(s)_{(*)}$ decays. The mass difference $m(D_s^+) - m(D^+)$ has also been measured.

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[7] The $\Delta M$ distribution for the $D_s^* \gamma$ signal is fit with the Crystal Ball function

$$f(x) = N \times \begin{cases} \frac{\exp\left(-\frac{(x-x)^2}{2\sigma^2}\right)}{(x-x)/\sigma < \alpha} & 
\text{ for } (x-x)/\sigma \geq \alpha,
\end{cases}$$

where $A = (n!/\alpha!)^2 \times \exp(-|\alpha|^2/2)$ and $B = (n!/\alpha!)|\alpha|$. $N$ is a normalization factor, $x$ and $\sigma$ are the peak position and width of the Gaussian portion of the function, $\alpha$ is the point at which the function changes to the power function, and $n$ is the exponent of the power function. $A$ and $B$ are defined so that the function and its first derivative are continuous at $\alpha$. More details can be found in D. Antreasyan, Crystal Ball Note 321 (1983).