Search for the Rare Leptonic Decay $B^+ \rightarrow \mu^+ \nu_\mu$


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(BABAR Collaboration)

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We have performed a search for the rare leptonic decay $B^+ \rightarrow \ell^+ \nu_\ell$ with data collected at the $Y(4S)$ resonance by the BABAR experiment at the PEP-II storage ring. In a sample of $8.8 \times 10^6 B\bar{B}$ pairs, we find no significant evidence for a signal and set an upper limit on the branching fraction $\mathcal{B}(B^+ \rightarrow \ell^+ \nu_\ell) < 6.6 \times 10^{-6}$ at the 90% confidence level.

The study of the purely leptonic decays $B^+ \rightarrow \ell^+ \nu_\ell$ ($\ell = e, \mu, \tau$) can provide sensitivity to poorly constrained standard model (SM) parameters and also act as a probe of new physics. In the SM, these decays proceed by annihilation to a $W$ boson with a branching fraction given by

$$\mathcal{B}(B^+ \rightarrow \ell^+ \nu_\ell) = \frac{G_F^2 m_B^2 m_\ell^2}{8 \pi} \left(1 - \frac{m_\ell^2}{m_B^2}\right)^2 f_{B^+}^2 |V_{ub}|^2 \tau_{B^+},$$

where $G_F$ is the Fermi coupling constant, $m_\ell$ and $m_B$ are the lepton and $B$ meson masses, and $\tau_{B^+}$ is the $B^+$ lifetime. The decay rate is sensitive to the product of the Cabibbo-Kobayashi-Maskawa matrix element $|V_{ub}|$ and the $B$ decay constant $f_{B^+}$, which is proportional to the wave function for zero separation between the quarks. Currently, our best understanding of $f_{B^+}$ comes from lattice gauge calculations where the theoretical uncertainty is roughly 15% [1]. This uncertainty is a significant limitation on the extraction of $|V_{ub}|$ from precision $B^+\bar{B}^0$ mixing measurements [1]. Observation of $B^+ \rightarrow \ell^+ \nu_\ell$ could provide the first direct measurement of $f_{B^+}$.

In this Letter, we present a search for the decay $B^+ \rightarrow \mu^+ \nu_\mu$ (charge conjugation is implied throughout this paper). This decay is highly suppressed due to the dependence on $|V_{ub}|^2$ and $m_\mu^2$ (helicity suppression). The SM prediction for the $B^+ \rightarrow \mu^+ \nu_\mu$ branching fraction is roughly $2 \times 10^{-7}$ while the current best published limit is $\mathcal{B}(B^+ \rightarrow \mu^+ \nu_\mu) < 2.1 \times 10^{-5}$ at the 90% C.L. [2]. Although the expected branching fraction for $B^+ \rightarrow \tau^+ \nu_\tau$ is larger by a factor of 225 due to the increased lepton mass, the additional neutrinos produced in the tau decay make the search more challenging experimentally. The current best limit is $\mathcal{B}(B^+ \rightarrow \tau^+ \nu_\tau) < 5.7 \times 10^{-4}$ [3].

The $B^+ \rightarrow \ell^+ \nu_\ell$ decay modes are also potentially sensitive to physics beyond the SM. For example, in two-Higgs-doublet models such as the minimal supersymmetric standard model (MSSM), these decays can proceed at tree level via an intermediate $H^\pm$, providing a possible enhancement up to current experimental limits [4]. Similarly, in $R$-parity violating extensions of the MSSM, $B^+ \rightarrow \ell^+ \nu_\ell$ may be mediated by scalar supersymmetric particles [5]. Hence, upper limits on the $B^+ \rightarrow \ell^+ \nu_\ell$ branching fractions constrain the $R$-parity violating couplings.

The data used in this analysis were collected with the BABAR detector at the PEP-II storage ring. The data sample consists of an integrated luminosity of $81.4 \text{ fb}^{-1}$ accumulated at the $Y(4S)$ resonance (“on-resonance”) and $9.6 \text{ fb}^{-1}$ accumulated at a center-of-mass (C.M.) energy about 40 MeV below the $Y(4S)$ resonance (“off-resonance”). The on-resonance sample corresponds to $8.8 \times 10^6 B\bar{B}$ pairs.

The BABAR detector is optimized for the asymmetric collisions at PEP-II and is described in detail elsewhere [6]. Charged particle trajectories are measured with a five-layer double-sided silicon vertex tracker (SVT) and a 40-layer drift chamber (DCH), which are contained in the 1.5 T magnetic field of a superconducting solenoid. A detector of internally reflected Cherenkov radiation provides identification of charged kaons and pions. The energies of neutral particles are measured by an electromagnetic calorimeter (EMC) consisting of 6580 CsI(Tl) crystals. The flux return of the solenoid is instrumented with resistive plate chambers to provide muon identification (IFR). A Monte Carlo (MC) simulation of the BABAR detector based on GEANT4 [7] was used to optimize the signal selection criteria and evaluate the signal efficiency.

The $B^+ \rightarrow \mu^+ \nu_\mu$ decay produces a monoenergic muon in the $B$ rest frame with $p_\mu = m_B/2$. Since the neutrino goes undetected, we assume that all remaining particles are associated with the decay of the other $B$ in the event, which we denote the “companion” $B$. Signal events are selected using the kinematic variables $\Delta E = E_B - E_\mu$ and energy-substituted mass, $m_{ES} = \sqrt{E_\mu^2 + p_\mu^2}$, where $p_\mu^2$ ($E_\mu$) is the momentum (energy) of the reconstructed companion $B$ and $E_\mu$ is the beam energy, all in the $Y(4S)$ rest frame. We require $m_{ES}$ to be consistent with the $B$ meson mass, and the energy of the companion $B$ to be consistent with $E_\mu$ resulting in $\Delta E \approx 0$.

To reduce nonhadronic backgrounds, we select events that contain at least four charged tracks and have a normalized second Fox-Wolfram moment [8] less than 0.98. Muon candidates are required to penetrate at least 2.2 interaction lengths of material in the IFR, have a measured penetration within 0.8 interaction lengths of that expected for a muon, and have an associated energy in the EMC consistent with that of a minimum-ionizing particle. The muon track must have at least 12 DCH hits, momentum transverse to the beam axis $p_{T} > 0.1 \text{ GeV/c}$, and a point of closest approach to the interaction point that is within 10 cm along the beam axis and less than 1.5 cm in the transverse plane. For each muon candidate with momentum between 2.25 and 2.95 GeV/c...
in the C.M. frame, we attempt to reconstruct the companion \( B \).

The companion \( B \) is formed from all charged tracks satisfying the above criteria regarding the distance of closest approach to the interaction point. It also includes all calorimeter clusters with energy greater than 30 MeV that are not associated with a charged track. Particle identification is applied to the charged tracks to identify electrons, muons, kaons, and protons while the remaining unidentified tracks are assumed to be pions. The resulting mass hypotheses are applied to improve the \( \Delta E \) resolution. Events with additional identified leptons are discarded since they typically arise from semileptonic \( B \) or charm decays and indicate the presence of additional neutrinos.

Once the companion \( B \) is reconstructed, we calculate the muon momentum in the rest frame of the signal \( B \). We assume the signal \( B \) travels in the direction opposite to that of the companion \( B \) momentum in the \( Y(4S) \) rest frame with a momentum determined by the two-body decay \( Y(4S) \to B^+ B^- \). For signal muons, the \( p_\mu \) distribution peaks at 2.64 GeV/c with an rms of about 100 MeV/c.

The two most significant backgrounds are \( B \) semileptonic decays involving \( b \to u \mu \bar{\nu} \) transitions where the end point of the muon spectrum approaches that of the signal, and nonresonant \( q \bar{q} \) (‘continuum’) events where a charged pion is mistakenly identified as a muon. Using a pion control sample obtained from \( e^+e^- \to \tau^+\tau^- \) events in the data, the misidentification probability is estimated to be 2% in the momentum and polar angle region relevant for \( B^+ \to \mu^+ \nu_\mu \). The muon candidate momentum spectrum of the background decreases with increasing momentum so we apply an asymmetric cut about the signal peak, \( 2.58 < p_\mu < 2.78 \) GeV/c.

In order for continuum events to populate the signal region of \( \Delta E \) and \( m_{ES} \), there must be significant missing energy due to particles outside the detector acceptance, unreconstructed neutral hadrons, or additional neutrinos. Therefore, we require \( |\cos \theta_\mu| < 0.88 \) so that the polar angle of the missing momentum vector in the laboratory frame, \( \theta_\mu \), is directed into the detector’s fiducial volume. Furthermore, these events tend to produce a jetlike event topology, whereas \( B \bar{B} \) events tend to be spherical. We define a variable, \( \theta_T \), which is the angle between the muon candidate momentum and the thrust axis of the companion \( B \) in the C.M. frame. By requiring \( |\cos \theta_T| < 0.55 \), we remove approximately 98% of the continuum background while retaining 54% of the signal decays.

We select \( B^+ \to \mu^+ \nu_\mu \) signal candidates with simultaneous requirements on \( \Delta E \) and \( m_{ES} \), thus forming a “signal box” defined by \( -0.75 < \Delta E < 0.5 \) GeV and \( m_{ES} > 5.27 \) GeV/c\(^2\). The dimensions of the signal box, as well as the above requirements on \( p_\mu \), \( |\cos \theta_\mu| \), and \( |\cos \theta_T| \), were determined using an optimization procedure that finds the combination of cuts that maximizes the quantity \( S/\sqrt{S + B} \), where \( S \) and \( B \) are the signal and background yields in the MC simulation, respectively. The signal branching fraction was set to the SM expectation during the optimization procedure. After applying all selection criteria, the \( B^+ \to \mu^+ \nu_\mu \) efficiency is determined from the simulation to be \( (2.24 \pm 0.07)\% \).

In addition to the signal box, we have defined a slightly larger blinding box and three sideband regions. The boundaries of these regions in the \( \Delta E, m_{ES} \) plane are listed in Table 1. The data within the blinding box was kept hidden until the analysis was completed in order to avoid the introduction of bias in the event-selection process.

We estimate the background in the signal box assuming that the \( m_{ES} \) distribution is described by the ARGUS function [9]. This assumption is consistent with the observed distributions in the MC simulation as well as the data in the \( \Delta E \) sidebands. The shape parameter of the ARGUS function \( (\xi) \) is determined from an unbinned maximum likelihood fit using the data in the fit sideband defined in Table 1. The ARGUS shape \( (A) \) is extrapolated through the signal box and constrained to be zero at the end point, which is fixed at \( E_h^* = 5.29 \) GeV/c\(^2\). Figure 1 shows the results of the fit. The expected background is

<table>
<thead>
<tr>
<th>Region</th>
<th>( \Delta E ) (GeV)</th>
<th>( m_{ES} ) (GeV/c(^2))</th>
</tr>
</thead>
<tbody>
<tr>
<td>Signal box</td>
<td>[−0.75, 0.5]</td>
<td>&gt;5.27</td>
</tr>
<tr>
<td>Blinding box</td>
<td>[−1.30, 0.70]</td>
<td>&gt;5.24</td>
</tr>
<tr>
<td>Fit sideband</td>
<td>[−0.75, 0.5]</td>
<td>[5.10, 5.24]</td>
</tr>
<tr>
<td>( \Delta E ) sideband (bottom)</td>
<td>[−3.00, −1.30]</td>
<td>&gt;5.10</td>
</tr>
<tr>
<td>( \Delta E ) sideband (top)</td>
<td>[0.70, 1.50]</td>
<td>&gt;5.10</td>
</tr>
</tbody>
</table>

![Figure 1](image-url)
calculated using
\[ N_{\text{bkg}} = N_{\text{fit}} \times \frac{\int_{m_{ES}} A(m_{ES}) dm_{ES}}{\int_{m_{ES}} A(m_{ES}) dm_{ES}} = N_{\text{fit}} \times R_{\text{ARGUS}}, \]

where \( N_{\text{fit}} \) is the number of events contributing to the fit. The result is \( N_{\text{bkg}} = 5.0_{-1.4}^{+1.8} \) events. The uncertainty is determined by varying \( \zeta \) by the \( \pm 1\sigma \) uncertainty from the fit. In the MC simulation (scaled to the on-resonance luminosity), we find \( 5.7 \pm 0.5 \) background events in the signal box, in agreement with the data extrapolation. The simulation indicates that the background is primarily continuum, consisting of 57\% light-quark (\( u\bar{u}, d\bar{d}, s\bar{s} \)), 23\% \( c\bar{c} \), and 20\% \( B\bar{B} \) events.

By using the ARGUS function to describe the background \( m_{ES} \) distribution, we would underestimate the contribution of backgrounds that peak within the blinded region. The simulation indicates that only the relatively small component of background from \( B\bar{B} \) events exhibits a mildly peaking \( m_{ES} \) distribution. When the background extrapolation is applied to the simulation, the resulting background estimate is \( 5.2 \pm 0.5 \) events, in agreement with the 5.7 events actually found in the signal box. Although neglecting peaking backgrounds could enhance an apparent signal, here the result would be a more conservative upper limit.

We have evaluated the systematic uncertainty in the signal efficiency which includes the muon candidate selection as well as the reconstruction efficiency of the companion \( B \). Using a muon control sample obtained from \( e^+e^- \rightarrow e^+e^- \mu^+\mu^- \) events in the data, the muon identification efficiency has been measured in bins of momentum, polar angle, and charge, and the results are incorporated into the nominal MC simulation. Averaged over the momentum and polar angle distributions of muons from \( B^+ \rightarrow \mu^+\nu_\mu \), we estimate that the muon identification efficiency for this data sample is 61\% with a systematic uncertainty of 4.2\%. From the fraction of tracks reconstructed in the SVT that are also found in the DCH, we find that the tracking efficiency of the muon candidate is overestimated in the simulation by 0.8\%, which is applied as a correction to the signal efficiency. The associated systematic error is 2\%. An additional systematic error of 1\% is included due to the requirement that the event contain at least four charged tracks.

The companion \( B \) reconstruction efficiency has been studied using a control sample of fully reconstructed \( B^+ \rightarrow D^{(*)0}\pi^+ \) events. These are also two-body decays in which the \( \pi^+ \) momentum spectrum is similar to that of the \( \mu^+ \) in signal events. Once reconstructed, the pion can be treated as if it were the signal muon and the \( D^{(*)0} \) decay products can be removed from the event to simulate the unobserved neutrino. Then the companion \( B \) is reconstructed in the control sample as it would be for signal. We then compare the efficiencies for each of our companion \( B \) selection cuts in the \( B^+ \rightarrow D^{(*)0}\pi^+ \) data and MC simulation. Figure 2 shows a comparison of on-resonance data and simulation for the \( \Delta E \) and \( m_{ES} \) distributions in the \( B^+ \rightarrow D^{(*)0}\pi^+ \) control sample.

FIG. 2. The distributions of \( \Delta E \) and \( m_{ES} \) of the companion \( B \) in the \( B^+ \rightarrow D^{(*)0}\pi^+ \) control sample after all previous cuts have been applied. The points are the on-resonance data while the histogram is the MC simulation normalized to the number of reconstructed \( B^+ \rightarrow D^{(*)0}\pi^+ \) decays. The observed discrepancies between data and simulation are accounted for by correcting the signal efficiency obtained from the simulation.

In the on-resonance data, we find 11 events in the signal box where \( 5.0_{-1.4}^{+1.8} \) background events are expected. The distribution of the data in the \( (\Delta E, m_{ES}) \) plane is shown in Fig. 3. Using a Monte Carlo technique [10], we determine the 90\% C.L. upper limit on the signal to be \( n_{UL} = 12.1 \) events. Systematic uncertainties are included following the prescription given in Ref. [11]. The probability of a

<table>
<thead>
<tr>
<th>Source</th>
<th>Correction</th>
<th>Uncertainty</th>
</tr>
</thead>
<tbody>
<tr>
<td>Tracking efficiency</td>
<td>0.992</td>
<td>2.0%</td>
</tr>
<tr>
<td>Muon</td>
<td></td>
<td></td>
</tr>
<tr>
<td>Companion ( B )</td>
<td></td>
<td>1.0%</td>
</tr>
<tr>
<td>Muon identification</td>
<td></td>
<td>4.2%</td>
</tr>
<tr>
<td>Companion ( B ) resc.</td>
<td>0.94</td>
<td>4.3%</td>
</tr>
<tr>
<td>Total</td>
<td>0.932</td>
<td>6.4%</td>
</tr>
</tbody>
</table>
We are grateful for the excellent luminosity and machine conditions provided by our PEP-II colleagues, and for the substantial dedicated effort from the computing organizations that support BABAR. The collaborating institutions wish to thank SLAC for its support and kind hospitality. This work is supported by DOE and NSF (U.S.A.), NSERC (Canada), IHEP (China), CEA and CNRS-IN2P3 (France), BMBF and DFG (Germany), INFN (Italy), FOM (The Netherlands), NFR (Norway), MIST (Russia), and PPARC (United Kingdom). Individuals have received support from the A.P. Sloan Foundation, Research Corporation, and Alexander von Humboldt Foundation.

[9] The ARGUS function is defined by \( \mathcal{A}(m_{ES}) \propto m_{ES} \left[ 1 - m_{ES}^2/E_b^2 \right] \exp[-\xi(1 - m_{ES}^2/E_b^2)] \). ARGUS Collaboration, H. Albrecht et al., Phys. Lett. B 241, 278 (1990).