B meson decays to $\omega K^*$, $\omega\rho$, $\omega\omega$, $\omega\phi$, and $\omega f_0$

We describe searches for $B$ meson decays to the charmless vector-vector final states $\omega K^*$, $\omega \rho$, $\omega \omega$, and $\omega \phi$ with $233 \times 10^6$ $\BB$ pairs produced in $e^+ e^-$ $\BB$ annihilation at $\sqrt{s} = 10.58$ GeV. We also search for the vector-scalar $B$ decay to $\omega f_0$. We measure the following branching fractions in units of $10^{-6}$: $\mathcal{B}(B^0 \to \omega K^{*0}) = 2.4 \pm 1.1 \pm 0.7 (<4.2)$, $\mathcal{B}(B^+ \to \omega K^{*+}) = 6.6^{+14.4}_{-12.0} (<3.4)$, $\mathcal{B}(B^0 \to \omega f_0) = 0.6 \pm 0.7^{+0.2}_{-0.3} (<1.5)$, $\mathcal{B}(B^+ \to \omega f^+) = 10.6 \pm 2.1^{+1.6}_{-1.0}$, $\mathcal{B}(B^0 \to \omega f^0) = 1.8^{+1.3}_{-0.5} \pm 0.4 (<4.0)$, $\mathcal{B}(B^0 \to \omega \phi) = 0.1 \pm 0.5 \pm 0.1 (<1.2)$, and $\mathcal{B}(B^0 \to \omega f_0) = 0.9 \pm 0.4^{+0.7}_{-0.3} (<1.5)$. In each case the first error quoted is statistical, the second systematic, and the upper limits are defined at the 90\% confidence level.

For $B^+ \to \omega \rho^+$ decays we also measure the longitudinal spin component $f_L = 0.82 \pm 0.11 \pm 0.02$ and the charge asymmetry $A_{CP} = 0.04 \pm 0.18 \pm 0.02$.

We reconstruct the $B$ mesons to pairs of light vector mesons (VV final states) have received less theoretical and experimental attention than decays to two pseudoscalar mesons (PP) or one pseudoscalar and one vector meson (PV). Early papers presented calculations for branching fractions, CP-violating asymmetries [1], and relative spin component contributions [2] for these decays. The measurement three years ago of an unexpectedly small value of the fraction of the longitudinal spin component $(f_L)$ in penguin-dominated $B \to \phi K^*$ decays [3,4] triggered new theoretical activity. There have been several attempts to understand the small value of $f_L$ within the standard model (SM) [5] and many papers suggested non-SM explanations [6]. Further information about these effects can come from both branching fraction and $f_L$ measurements in decays such as $B \to \omega K^*$ or $B \to \omega \phi$, which are conjugate to $B \to \phi K^*$ via an SU(3) rotation [7]. Information on these and related charmless decays can additionally be used to provide sensitivity to the Cabibbo-Kobayashi-Maskawa (CKM) angles $\alpha$ and $\gamma$ [8].

We have discussed above mostly penguin-dominated decays. There are also decays with the $K^*$ replaced by a $\rho$, $\omega$, or $\phi$ meson where tree diagrams are expected to be more important. These include $B$ decays to the final states $\rho\rho$, $\omega\rho$, and $\omega\omega$. The decay $B \to \rho\rho$ is known to be nearly fully longitudinally polarized [9,10] and these other predominantly tree decays are expected to behave similarly [11], with branching fractions as predicted in [1].

We report results of measurements of $B$ decays to the charmless VV final states $\omega V$, where $V$ represents a neutral or charged $K^*$ or $\rho$, or an $\omega$ or $\phi$ meson. We also measure the decay $B^0 \to \omega f_0(980)$ which shares the same final state as the $B^0 \to \omega \rho^0$ decay. Because of the current small signal samples, only the branching fractions and the fraction of the longitudinal spin component are measured, the latter by integrating over the azimuthal angles, for which the azimuthal acceptance is uniform. The angular distribution is

$$
\frac{1}{\Gamma} \frac{d^2 \Gamma}{d \cos \theta_1 d \cos \theta_2} = \frac{9}{4} \left[ (1-f_L) \sin^2 \theta_1 \sin^2 \theta_2 + f_L \cos^2 \theta_1 \cos^2 \theta_2 \right],
$$

where $\theta_k$ is the helicity angle in the $V_k$ rest frame with respect to the boost axis from the $B$ rest frame, and $f_L$ is the fraction of the longitudinal spin component. For $B^+ \to \omega \rho^+$, we also measure the direct CP-violating time-integrated charge asymmetry $A_{CP} = (\Gamma^- - \Gamma^+)/\Gamma^+$, where the superscript on the $\Gamma$ corresponds to the sign of the $B^\mp$ meson.

The results presented here are based on data collected with the BABAR detector [12] at the PEP-II asymmetric $e^+ e^-$ collider located at the Stanford Linear Accelerator Center. An integrated luminosity of 211 fb$^{-1}$, corresponding to 232.8 $\times 10^6$ $\BB$ pairs, was recorded at the $Y(4S)$ resonance (center-of-mass energy $\sqrt{s} = 10.58$ GeV).

Charged particles from the $e^+ e^-$ interactions are detected, and their momenta measured, by five layers of double-sided silicon microstrip detectors surrounded by a 40-layer drift chamber, both operating in the 1.5-T magnetic field of a superconducting solenoid. We identify photons and electrons using a CsI(Tl) electromagnetic calorimeter (EMC). Further charged particle identification (PID) is provided by the average energy loss $(dE/dx)$ in the tracking devices and by an internally reflecting ring-imaging Cherenkov detector (DIRC) covering the central region.

We reconstruct the $B$-daughter candidates through their decays $\rho^0 \to \pi^+ \pi^-$, $f_0(980) \to \pi^+ \pi^-$, $\rho^+ \to \pi^+ \pi^0$, $K^{*0} \to K^+ \pi^-$ (denoted $K^{*0}_{S,K^+\pi^-}$), $K^+ \to K^+ \pi^0(K^{*0}_{K^+\pi^0})$, $K^{*+} \to K^{*0}_{S,K^+\pi^-} \pi^+$, $\omega \to \pi^+ \pi^+ \pi^0$, $\phi \to K^+ K^-$, $\pi^0 \to \gamma \gamma$, and $K^{*0}_{S} \to \pi^+ \pi^-$ (charge-conjugate decay modes are implied throughout). Table I lists the requirements on the invariant mass of these particles’ final states. For the $\rho$, $K^*$, $\phi$, and $\omega$ invariant masses these requirements are set loose enough to include sidebands, as these
mass values are treated as observables in the maximum-likelihood fit described below. The \( \rho^0 \) and \( f_0 \) [we use \( f_0 \) as shorthand for \( f_0(980) \)] yields are extracted from a simultaneous fit to the same data sample. For \( K^0_S \) candidates we further require the three-dimensional flight distance from the event primary vertex to be greater than 3 times its uncertainty. Secondary pion and kaon candidates in \( \rho, K^*, \) and \( \omega \) candidates are rejected if their DIRC, \( dE/dx, \) and EMC PID signature satisfies tight consistency with protons or electrons, and the kaons (pions) must (must not) have a kaon signature.

Table 1 also gives the restrictions on the \( K^* \) and \( \rho \) helicity angles \( \theta \) [previously defined for Eq. (1)], imposed to avoid regions of rapid acceptance variation or combinatorial background from soft particles. To calculate \( \theta \) we take the angle relative to, for \( \omega, \) the helicity axis of the normal to the decay plane, for \( \rho \) and \( \phi, \) the positively charged (or only charged) daughter momentum, and for \( K^* \) the daughter kaon momentum.

A \( B \) meson candidate is characterized kinematically by the energy-substituted mass \( m_{ES} = \sqrt{(s/2) + p_0} \cdot p_B/E_0^2 - p_B^2 \) and the energy difference \( \Delta E = E^*_B - \frac{s}{2} \times \sqrt{\gamma} \), where \( (E_0, p_0) \) and \( (E_B, p_B) \) are four-momenta of the \( Y(4S) \) and the \( B \) candidates, respectively, \( s \) is the square of the center-of-mass energy, and the asterisk denotes the \( Y(4S) \) frame. The resolution on \( \Delta E \) \( (m_{ES}) \) is about 30 MeV (30 MeV). Our signal falls in the region \( |\Delta E| \leq 0.1 \text{ GeV} \) and \( 5.27 \leq m_{ES} \leq 5.29 \text{ GeV}, \) which is then extended to include sidebands that provide a good description of the background. The average number of candidates found per selected event in data is in the range 1.1 to 1.7, depending on the final state. We choose the candidate with the smallest value of \( x^2 \) constructed from the deviations of the \( B \)-daughter resonance masses (all particles in Table I except \( \pi^0, K^0_S, \) and \( f_0 \)) from their expected [13] values.

Backgrounds arise primarily from random combinations of particles in continuum \( e^+e^- \rightarrow q\bar{q} \) events \( (q = u, d, s, c) \). We reduce these by using the angle \( \theta_T \) between the thrust axis of the \( B \) candidate in the \( Y(4S) \) frame and that of the rest of the charged and neutral particles in the event. The distribution of \( |\cos\theta_T| \) is sharply peaked near 1.0 for \( q\bar{q} \) jet pairs, and nearly uniform for \( B \) meson decays. The requirements, chosen to reduce the sample size for the large background modes, are \( |\cos\theta_T| < 0.9 \) for the \( \omega\phi \) mode, \( |\cos\theta_T| < 0.8 \) for the \( \omega\omega \) and \( \omega K^* \) modes, and \( |\cos\theta_T| < 0.7 \) for the \( \omega\rho \) modes. In the maximum-likelihood fit described below, we also use a Fisher discriminant \( F \) that combines four variables defined in the \( Y(4S) \) frame: the polar angles with respect to the beam axis of the \( B \) momentum and \( B \) thrust axis, and the zeroth and second angular moments, \( L_0 \) and \( L_2 \), of the energy flow about the \( B \) thrust axis in the \( Y(4S) \) frame. The moments are defined by \( L_j = \sum_i p_i \times |\cos\theta_i|^j \), where \( \theta_i \) is the angle with respect to the \( B \) thrust axis of a charged or neutral particle \( i, p_i \) is its momentum, and the sum excludes the \( B \) candidate’s daughters.

From Monte Carlo (MC) simulation [14] we determine the most important charmless \( B\bar{B} \) backgrounds (typically about a dozen background modes for each signal final state). We include a variable yield for these in the fit described below. We also introduce a component for nonresonant \( \pi\pi \) and \( K\pi \) background. The magnitude of this component is fixed in the fit as determined from extrapolations from higher-mass regions.

We obtain yields and values of \( f_L \) and \( A_{CP} \) from extended unbinned maximum-likelihood fits with input observables \( \Delta E, m_{ES}, F \) and, for the vector meson \( k, \) the mass \( m_k \) and helicity angle \( \theta_k \). For each event \( i \) and hypothesis \( j \) (signal, \( q\bar{q} \) background, \( B\bar{B} \) background) we define the probability density function (PDF)

\[
P_j = P_j(m_{ES}^i)P_j(\Delta E)^iP_j(F)^iP_j(m_1^i, m_2^i, \theta_1^i, \theta_2^i). \tag{2}
\]

We check for correlations in the background observables beyond those accounted for in this PDF and find them to be small. For the signal component, we correct for the effect of small neglected correlations (see below). The likelihood function is

\[
L = \frac{e^{-\sum Y_j} N}{N!} \prod_{i=1}^N Y_j P_j^i, \tag{3}
\]

where \( Y_j \) is the yield of events of hypothesis \( j \) and \( N \) is the number of events in the sample.

The PDF factor for the resonances in the signal takes the form \( P_{1, sig}(m_1^i)P_{2, sig}(m_2^i)Q(\theta_1^i, \theta_2^i) \) with \( Q \) given by Eq. (1) modified to account for detector acceptance. For \( q\bar{q} \) background it is given for each resonance independently by \( P_{1, sig}(m_1^i, \theta_1^i)P_{1, sig}(m_2^i, \theta_2^i)P_{1, sig}(m_1^i, \theta_1^i)P_{1, sig}(m_2^i, \theta_2^i) \), distinguishing between true resonance \( (P_{1, sig}) \) and combinatorial \( (P_{c}) \) components. For the \( B\bar{B} \) background we assume that all four mass and helicity-angle observables are independent.

For the signal, \( B\bar{B} \) background, and nonresonant background components, we determine the PDF parameters.
from simulation. We study large control samples of $B \to D\pi$ decays of similar topology to verify the simulated resolutions in $\Delta E$ and $m_{ES}$, adjusting the PDFs to account for any differences found. For the continuum background we use $(m_{ES}, \Delta E)$ sideband data to obtain initial values, before applying the fit to data in the signal region, and leave them free to vary in the final fit.

The parameters that are allowed to vary in the fit include the signal, $B\bar{B}$ background, nonresonant background yields, and continuum background PDF parameters. For the three modes with signals of more than $2\sigma$ significance, we vary $f_L$ in the fit to properly account for the variation of efficiency with $f_L$. For $B^+ \to \omega\rho^+$ we also vary the signal and background charge asymmetries. For the fits with little signal, we fix $f_L$ to a value that is consistent with a priori expectations (see Table II), and account for the associated systematic uncertainty.

To describe the PDFs, we use the sum of two Gaussians for $\mathcal{P}_\text{sig}(m_{ES})$, $\mathcal{P}_\text{sig}(\Delta E)$, and the true resonance components of $\mathcal{P}(m_k)$; for $\mathcal{F}$ we use an asymmetric Gaussian for signal with a small Gaussian component for background to account for important tails in the signal region. The background $m_{ES}$ shape is described by the function $x\sqrt{1-x^2}\exp[-\xi(1-x^2)]$ (with $x=m_{ES}/E_k^0$) and the distributions of masses $m_k$ by second or third order polynomials. The background PDF parameters that are allowed to vary in the fit are $\xi$ for $m_{ES}$, slope for $\Delta E$, the polynomial describing the combinatorial component for $m_k$, and the peak position and lower and upper width parameters for $\mathcal{F}$.

We evaluate possible biases from our neglect of correlations among discriminating variables in the PDFs by fitting ensembles of simulated experiments into which we have embedded the expected number of signal events and $B\bar{B}$ background events, randomly extracted from the fully simulated MC samples. We give in Table II the yield bias $Y_0$ found for each mode. Since events from a weighted mixture of simulated $B\bar{B}$ background decays are included, the bias we measure includes the effect of this background.

The systematic uncertainties on the branching fractions arising from lack of knowledge of the PDFs have been included, in part, in the statistical error since model background parameters are free in the fit. For the signal, the uncertainties in PDF parameters are estimated from the consistency of fits to MC and data in large control samples of topology similar to signal. Varying the signal PDF parameters within these errors, we estimate yield uncertainties for each mode. The uncertainty in the yield bias correction is taken to be the quadratic sum of two terms: half the bias correction and the statistical uncertainty on the bias itself. Similarly, we estimate the uncertainty from modeling of the $B\bar{B}$ backgrounds as the change in the signal yield when the number of fitted $B\bar{B}$ events is fixed to be within one sigma of the expected number of $B\bar{B}$ events from MC. For the nonresonant $\pi\pi$ or $K\pi$ backgrounds, the uncertainty is taken as the change in the signal when the background yield is varied within the uncertainty of the fits to the higher-mass regions. For modes with fixed $f_L$, the uncertainty due to the dependence of signal efficiency on $f_L$ is evaluated as the measured change in the branching fraction when $f_L$ is varied by $\pm 0.3$ (up to a maximum of $f_L = 1$). These additive systematic errors are dominant for all modes; the PDF variation is always the smallest but the others are typically similar in size.

Uncertainties in our knowledge of the efficiency, found from studies of data control samples, include $0.8\% \times N_t$, $3.0\% \times N_{\omega\rho}$, and $1\%$ for a $K_0^0$ decay, where $N_t$ is the number of tracks, and $N_{\omega\rho}$ the number of $\pi^0$'s in a decay. We estimate the uncertainty in the number of $B$ mesons to be 1.1%. Published data [13] provide the uncertainties in the $B$-daughter product branching fractions ($1\%$--$2\%$). The uncertainties from the event selection are 1%--2% for the requirement on $\cos\theta_T$.

The systematic uncertainty on $f_L$ for $B^+ \to \omega\rho^+$ includes the effects of fit bias, PDF-parameter variation, and $B\bar{B}$ and nonresonant backgrounds, all estimated with the same method as for the yield uncertainties described above. From large inclusive kaon and $B$-decay samples,

\begin{table}[!h]
\centering
\caption{Signal yield $Y$ and its statistical uncertainty, bias $Y_0$, detection efficiency $\epsilon$, daughter branching fraction product $\prod \mathcal{B}_j$, significance $S$ (with systematic uncertainties included), measured branching fraction $\mathcal{B}$, 90\% CL. upper limit, measured or assumed longitudinal polarization, and $\mathcal{A}_{CP}$.}
\begin{tabular}{lccccccccc}
\hline
Mode  & $Y$ (events) & $Y_0$ (events) & $\epsilon$ ($\%$) & $\prod \mathcal{B}_j$ ($\%$) & $S$ ($\sigma$) & $\mathcal{B}$ ($10^{-6}$) & $\mathcal{B}$ U.L. ($10^{-6}$) & $f_L$ & $\mathcal{A}_{CP}$ \\
\hline
$\omega K^{+0}$ & $55^{+20}_{-19}$ & 11 & 13.2 & 59.2 & 2.4 & $2.4 \pm 1.1 \pm 0.7$ & 4.2 & $0.71^{+0.27}_{-0.24}$ & \ldots \\
$\omega K^{+0}$ & $-3.6^{+10}_{-8}$ & $-5$ & 12.5 & 20.3 & 0.1 & $0.2^{+1.1+1.5}_{-1.5-1.1}$ & 4.2 & 0.7 fixed & \ldots \\
$\omega K^{+0}$ & $12^{+14}_{-12}$ & 6 & 8.0 & 29.6 & 0.5 & $1.1^{+5.1+13}_{-2.1-12}$ & 5.7 & 0.7 fixed & \ldots \\
$\omega K^{+0}$ & $4^{+5}_{-3}$ & 0.4 & $0.6^{+1.4+1.1}_{-1.2-0.9}$ & 3.4 & 0.7 fixed & \ldots \\
$\omega K^{+0}$ & $-18^{+12}_{-7}$ & $-2$ & 11.6 & 89.1 & 0.6 & $-0.6 \pm 0.7 \pm 0.8$ & 1.5 & 0.9 fixed & \ldots \\
$\omega K^{+0}$ & $25^{+12}_{-17}$ & 4 & 15.2 & 59.4 & 2.8 & $0.9 \pm 0.4 \pm 0.1$ & 1.5 & \ldots & \ldots \\
$\omega K^{+0}$ & $156^{+33}_{-30}$ & 11 & 6.6 & 89.1 & 5.7 & $10.6 \pm 2.1 \pm 1.6$ & $\ldots$ & $0.82 \pm 0.11 \pm 0.02$ & 0.04 $\pm 0.18 \pm 0.02$ \\
$\omega K^{+0}$ & $48^{+24}_{-19}$ & 8 & 12.9 & 77.5 & 2.1 & $1.8^{+1.3+0.9}_{-1.0-0.3}$ & 4.0 & 0.79 $\pm$ 0.34 & \ldots \\
$\omega K^{+0}$ & $3.1^{+2.5}_{-1.8}$ & 1 & 19.0 & 43.2 & 0.3 & $0.1 \pm 0.5 \pm 0.1$ & 1.2 & 0.88 fixed & \ldots \\
\hline
\end{tabular}
\end{table}
we find a systematic uncertainty for $\mathcal{A}_{CP}$ of 0.02 due mainly
to the dependence of reconstruction efficiency on
the momentum of the charged $\rho$ daughter. We find for the
$B^+ \to \omega \rho^+$ background, $\mathcal{A}_{CP}^\omega = -0.010 \pm 0.007$,
confirming this estimate.

In Table II we also show for each decay mode the measured
branching fraction with its uncertainty and significance
together with the quantities entering into these
computations. The significance is taken as the square root
of the difference between the value of $-2 \ln L$ (with
systematic uncertainties included) for zero signal and the
value at its minimum. For all modes except for $B^+ \to \omega \rho^+$ we quote a 90% confidence level (C.L.) upper limit,
taken to be the branching fraction below which lies 90% of
the total of the likelihood integral in the positive branching
fraction region. In calculating branching fractions we
assume that the decay rates of the $Y(4S)$ to $B^+B^-$ and $B^0\bar{B}^0$
are equal [13]. For decays with $K^{*+}$, we combine the
results from the two $K^*$ decay channels, by adding their
values of $-2 \ln L$, taking into account the correlated and
uncorrelated systematic errors.

We present in Fig. 1 the data and PDFs projected onto
$m_{ES}$ and $\Delta E$, for subsamples enriched with a mode-
dependent threshold requirement on the signal likelihood
(computed without the PDF associated with the variable
plotted) chosen to optimize the significance of signal in the
resulting subsample. Figure 2 gives projections of $\cos \theta$
for the $B^+ \to \omega \rho^+$ decay.

The branching fraction value $\mathcal{B}$ given in Table II for
$B^+ \to \omega \rho^+$ comes from a direct fit with the free parame-
ters $\mathcal{B}$ and $f_L$, as well as $\mathcal{A}_{CP}$. This choice exploits the
feature that $\mathcal{B}$ is less correlated with $f_L$ than is either the
yield or efficiency taken separately. The behavior of $-2 \ln L(f_L, \mathcal{B})$
is shown in Fig. 3.

In summary, we have searched for seven charmless
hadronic $B$ meson decays. We observe $B^+ \to \omega \rho^+$ with a
significance of 5.7$\sigma$, and establish improved 90% C.L.
upper limits for the other modes, with the following branching fractions:

$$\mathcal{B}(B^+ \to \omega \rho^+) \times 10^{-6}$$

FIG. 1 (color online). Projections of $\Delta E$ (left panel) and $m_{ES}$
(right panel) of events passing a signal likelihood threshold for,
from top to bottom, $B^0 \omega K^0$, $B^+ \omega K^{*+}$, $B^0 \omega \rho^0$,
$B^+ \omega \rho^+$, $B^0 \omega \omega$, $B^0 \omega \phi$, and $B^0 \omega f_0$. The solid
curve is the fit function, the dashed curve is the signal contri-
bution, and the dot-dashed curve is the background contribution.

FIG. 2 (color online). Projections of helicity-angle cosines, of
events passing a signal likelihood threshold for $\omega$ (left panel)
and $\rho^+$ (right panel) from the fit for $B^+ \to \omega \rho^+$ decay. The solid
curve is the fit function, the dashed curve is the signal contri-
bution, and the dot-dashed curve is the background contribution.

FIG. 3. Distribution of $-2 \ln L(f_L, \mathcal{B})$ for $B^+ \to \omega \rho^+$ decay.
The solid dot gives the central value; curves give the contours in
1-sigma steps [$\Delta\sqrt{-2 \ln L(f_L, \mathcal{B})} = 1$].
\[ \mathcal{B}(B^0 \to \omega K^{*0}) = 2.4 \pm 1.1 \pm 0.7 \ (\text{<4.2}) \times 10^{-6}, \]
\[ \mathcal{B}(B^+ \to \omega K^{*+}) = 0.6^{+1.4+1.1}_{-1.2-0.9} \ (\text{<3.4}) \times 10^{-6}, \]
\[ \mathcal{B}(B^0 \to \omega \rho^0) = -0.6 \pm 0.7^{+0.8}_{-0.3} \ (\text{<1.5}) \times 10^{-6}, \]
\[ \mathcal{B}(B^+ \to \omega \rho^+) = 10.6 \pm 2.1^{+1.4}_{-1.0} \times 10^{-6}, \]
\[ \mathcal{B}(B^0 \to \omega \omega) = 1.8^{+3.3}_{-0.2} \pm 0.4 \ (\text{<4.0}) \times 10^{-6}, \]
\[ \mathcal{B}(B^0 \to \omega \phi) = 0.1 \pm 0.5 \pm 0.1 \ (\text{<1.2}) \times 10^{-6}, \]
\[ \mathcal{B}(B^0 \to \omega f_0) = 0.9 \pm 0.4^{+0.6}_{-0.1} \ (\text{<1.5}) \times 10^{-6}. \]

In each case the first error quoted is statistical, the second systematic, and the upper limits are taken at 90% C.L.

For \( B^+ \to \omega \rho^+ \) we also measure the longitudinal spin component \( f_L = 0.82 \pm 0.11 \pm 0.02 \) and charge asymmetry \( \mathcal{A}_{CP} = 0.04 \pm 0.18 \pm 0.02 \). The longitudinal spin component is dominant, as it is for \( B \to \rho \rho \) [9,10].

Assuming tree dominance we naively expect the branching fraction for \( B^+ \to \omega \rho^+ \) to be equal to that of \( B^+ \to \rho^+ \rho^0 \). However, the measured branching fraction for \( \mathcal{B}(B^+ \to \omega \rho^+) \) is more than 2 standard deviations smaller than the world average \( \mathcal{B}(B^+ \to \rho^+ \rho^0) = 26 \pm 6 \times 10^{-6} \) [13].

Our branching fraction results are in agreement with theoretical estimates [1,11].

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