Study of heavy-flavor quarks produced in association with top-quark pairs at $\sqrt{s} = 7$ TeV using the ATLAS detector

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Using a sample of dilepton top-quark pair ($t\bar{t}$) candidate events, a study is performed of the production of top-quark pairs together with heavy-flavor (HF) quarks, $t\bar{t} + b + X$ or $t\bar{t} + c + X$, collectively referred to as $t\bar{t} + HF$. The dataset used corresponds to an integrated luminosity of 4.7 fb$^{-1}$ of proton–proton collisions at a center-of-mass energy of 7 TeV recorded by the ATLAS detector at the CERN Large Hadron Collider. The presence of additional HF quarks in the $t\bar{t}$ sample is inferred by looking for events with at least three $b$-tagged jets, where two are attributed to the $b$-quarks from the $t\bar{t}$ decays and the third to additional HF production. The dominant background to $t\bar{t} + HF$ in this sample is $t\bar{t} + j$ events in which a light-flavor jet is misidentified as a heavy-flavor jet. To determine the heavy- and light-flavor content of the additional $b$-tagged jets, a fit to the vertex mass distribution of $b$-tagged jets in the sample is performed. The result of the fit shows that 79 ± 14 (stat.) ± 22 (syst.) of the 105 selected extra $b$-tagged jets originate from HF quarks, three standard deviations away from the hypothesis of zero $t\bar{t} + HF$ production. The result for extra HF production is quoted as a ratio ($R_{HF}$) of the cross section for $t\bar{t} + HF$ production to the cross section for $t\bar{t}$ production with at least one additional jet. Both cross sections are measured in a fiducial kinematic region within the ATLAS acceptance. $R_{HF}$ is measured to be $[6.2 ± 1.1 \text{(stat.)} ± 1.8 \text{(syst.)}]%$ for jets with $p_T > 25$ GeV and $|\eta| < 2.5$, in agreement with the expectations from Monte Carlo generators.


I. INTRODUCTION

In order to characterize the recently observed Higgs-like particle ($H$) [1, 2], quantities such as the Yukawa coupling of the top quark and the Higgs boson need to be measured with precision. For a Standard Model (SM) Higgs boson with a mass of 125 GeV, the decay mode with the largest branching ratio is $H \to bb$. Thus, the channel with the largest yields for studying $t\bar{t} + H$ production is $t\bar{t} + H \to b\bar{b}$. Production of top-quark pair ($t\bar{t}$) events featuring additional heavy-flavor (HF) $b$- and $c$-quarks, $t\bar{t} + b + X$ and $t\bar{t} + c + X$, referred to as $t\bar{t} + HF$, is the main irreducible background to $t\bar{t} + H \to b\bar{b}$. A study of $t\bar{t} + HF$ production is useful to constrain models of heavy-flavor quark production at the scale of the top-quark mass. This analysis is also of interest because of the many potential phenomena beyond the SM, such as composite Higgs models [3] and processes leading to final states with four top quarks [4–9], that could produce additional heavy-flavor quarks in the $t\bar{t}$ candidate sample.

This paper describes a study of $t\bar{t} + HF$ production. Within the SM, heavy-flavor quark pairs, $c\bar{c}$ and $b\bar{b}$, are expected to be produced in association with $t\bar{t}$ mainly via gluon splitting from initial- and final-state radiation [10]. In addition, the heavy-flavor content of the proton could lead to $t\bar{t}$ final states with at least one additional HF quark, $t\bar{t} + c$ and $t\bar{t} + b$. The data analyzed correspond to an integrated luminosity of 4.7 fb$^{-1}$ at a center-of-mass energy of $\sqrt{s} = 7$ TeV produced at the Large Hadron Collider (LHC) and recorded in 2011 with the ATLAS detector.

This analysis is performed on $t\bar{t}$ dilepton candidate events in which each top quark decays to a $b$-quark and a $W$ boson, which subsequently decays to a neutrino and an isolated, charged lepton. The dilepton signature is selected for this measurement because it is relatively background free and precludes a third $b$-tagged jet from a hadronically decaying $W$ boson, predominantly via $W \to s\bar{c}$. The $t\bar{t} + HF$ signal region is the subset of these events with three or more jets identified as containing HF quarks ($b$-tagged jets, or $b$-tags). However, jets without HF quarks may also be $b$-tagged, so that care must be taken to properly identify the flavor composition of the $b$-tagged jets in the sample. Two $b$-tagged jets from each event are presumed to originate from the $b$-quarks from top-quark decays, $t\bar{t} \to W^+bW^-\bar{b}$. Therefore, all events in the signal region have at least one additional $b$-tag either from a $b$- or $c$-quark jet, or from a light-quark or gluon jet that was misidentified. The latter are referred to as light-flavor or LF jets.

Due to limited data statistics and discrimination between $b$- and $c$-jets, the sum of $b$-quark and $c$-quark jet rates is measured. Information about the composition of $t\bar{t} + b + X$ and $t\bar{t} + c + X$ in $t\bar{t} + HF$ is nevertheless required for the total correction due to acceptance, which is different for $b$- and $c$-quark jets. The composition is estimated with Monte Carlo simulation and tested in the data.

From the measurement of the fraction of jets with heavy flavor content, the cross section for $t\bar{t}$ production with at least one additional HF jet can be extracted. To reduce some systematic uncertainties, the result is quoted as a ratio, termed $R_{HF}$, of the cross section for $t\bar{t}$ production with at least one additional HF jet to the cross section for $t\bar{t}$ production with at least one additional jet ($t\bar{t} + j$), regardless of flavor. The measurement of $t\bar{t} + j$ production is performed in dilepton $t\bar{t}$ candidate events with at least three jets, at least two of which are $b$-tagged and assumed to come from top-quark decays.

The paper is organized as follows. The ATLAS
detector is briefly described in Sec. II. The data and Monte Carlo samples used in the analysis are described in Sec. III, followed by a description of the event selection in Sec. IV. The definition of the fiducial phase space used in the measurement of $R_{HF}$, and the calculation of acceptances and efficiencies are presented in Sec. V. In Sec. VI, observed and expected numbers of events with $≥3$ $b$-tagged jets are shown. Section VII describes a fit to the vertex mass distribution of $b$-tagged jets in these data events to extract the fraction of HF jets produced in association with $t\bar{t}$. A discussion of the systematic uncertainties of the measurement is presented in Sec. VIII. Section IX shows the result of the measurements, followed by conclusions in Sec. X.

II. THE ATLAS DETECTOR

A detailed description of the ATLAS detector can be found elsewhere [11]. The innermost part of the detector is a tracking system that is immersed in a 2 T axial magnetic field and that measures the momentum of charged particles. The inner detector comprises a silicon pixel detector, a silicon microstrip detector, and a transition radiation tracker, providing tracking capability within the pseudorapidity range $|\eta| < 2.5$ [12]. The tracking system is also used to identify the displaced secondary vertex that is formed by hadrons containing a $b$- or $c$-quark. Calorimeter systems, which measure the electron, photon, and hadron energies, reside outside the inner detector and cover the region $|\eta| < 4.9$. Outside the calorimeters there is a muon spectrometer that is used to identify and measure the momentum of muons in an azimuthal magnetic field in the region $|\eta| < 2.7$. To reduce the data rate, a three-level trigger system selects the potentially interesting events that are recorded for offline analysis.

III. DATA AND MONTE CARLO SAMPLES

The total integrated luminosity for the analyzed data sample is $4.7 \text{ fb}^{-1}$ at a center-of-mass energy of $\sqrt{s} = 7 \text{ TeV}$. During the 2011 data-taking period the instantaneous luminosity of the LHC increased, causing the average number of simultaneous inelastic $pp$ interactions per beam crossing (pile-up) at the beginning of a $pp$ fill to increase from about 6 to 17. Multiple $pp$ interactions can occur either in the same bunch crossing as the primary vertex (termed "in-time pile-up") or in an adjacent bunch crossing (termed "out-of-time pile-up"). To account for these effects, all Monte Carlo simulated events are overlaid with additional inelastic events generated with the PYTHIA AMBT1 tune [13], and the distribution of the number of vertices in the simulation is reweighted to match the distribution of the number of additional interactions per bunch crossing measured in the data.

Monte Carlo simulation is used to study signal and background processes. Inclusive $t\bar{t}$ production and dedicated $t\bar{t} + \text{HF}$ samples are simulated using the multi-leg matrix-element generator ALPGEN v2.13 [14] with the CTEQ6L1 [15] parton distribution function (PDF) set. Parton showering and hadronization are performed by HERWIG v6.520 [16]. Effects due to the mass of the heavy-flavor quarks are included by default in ALPGEN. In these samples, additional jets (including heavy-flavor) can also be produced in the parton shower. The MLM [14] parton–jet matching scheme is applied to avoid double counting of configurations generated by both the parton shower and the leading-order (LO) matrix-element (ME) calculation. In addition, overlap between $t\bar{t}$ events with HF quarks that originate from ME production and those that originate from the parton shower is removed. This heavy flavor overlap removal (HFOR) is based on the \( \Delta R_{qq} > 0.4 \) event selection. In this sample the $t\bar{t}$ process is described at next-to-leading order (NLO), while the extra jets are described at LO. For each sample showered with HERWIG, JIMMY v4.31 [18] and the AUET1 tune [19] are used to simulate the underlying event and to model various soft interactions. To assess the effect of different parton shower models, a sample is generated using ALPGEN v2.14 with the PYTHIA v6.425 [20] parton shower and hadronization, using the CTEQ5L PDF set [21]. The uncertainty associated with the CTEQ6L1 PDF set is evaluated with an envelope calculated using the uncertainty set from the NLO PDF MTSW2008nlo68cl [22], and an additional term to account for the difference between the central values of the LO and NLO calculations.

Initial- and final-state radiation (ISR/FSR) variations are studied using samples generated with ACERMC v2.0 [23] interfaced with PYTHIA v6.2. In these samples the parameters that control the amount of ISR/FSR are set to points consistent with the PEGNIA Hard/Soft tune [24] in a range constrained by current experimental data [25].

In all samples the top-quark mass is set to $m_t = 172.5 \text{ GeV}$. The cross section for Standard Model $t\bar{t}$ production at this mass is calculated using the approximate next-to-next-to-leading-order (NNLO) QCD calculation described in [26].

Background samples from the production of $W$ and $Z$ bosons are generated using the CTEQ6L1 PDFs with
ALPGEN, which is interfaced to HERWIG for parton showering and hadronization; the ALPGEN matrix elements include diagrams with up to five additional partons. Separate samples of \(W + b\bar{b}\) and \(Z + b\bar{b}\) events are generated. The overlap between jets from the parton-shower and the matrix-element in the \(n\) and \(n+1\) jet multiplicity samples is removed for the \(W+\)jets and \(Z+\)jets samples in the same manner as for the \(t\bar{t}\) samples. Single top-quark production is modeled using ACERMC in the \(t\)-channel and MC@NLO v3.41 [27] for the \(Wt\)- and \(s\)-channels. Diboson (\(WW, WZ,\) and \(ZZ\)) production is modeled using ALPGEN interfaced with HERWIG. Less than 0.5% of the expected yield in the \(t\bar{t} + \) HF sample comes from the associated production of \(t\bar{t} + W/Z\) and \(t\bar{t} + H\), and these processes are thus neglected in this analysis.

The resulting generated samples are passed through a Geant4 simulation [28] of the ATLAS detector [29]. Events are then reconstructed in the same manner as the data.

IV. EVENT SELECTION

Events for the analysis are selected by at least one of the high-\(p_T\) [12] single-electron or single-muon triggers, as described in Refs. [30] and [31]. The single-electron triggers are based on calorimeter energy deposits, shower shape, and matching track quality constraints, while the single-muon triggers are based on a reconstructed track in the muon spectrometer that matches a track found in the inner detector. To ensure a final trigger rate that is compatible with the ATLAS data acquisition system, a minimum \(p_T\) threshold for the electron and muon triggers is used. The \(p_T\) threshold for the muon trigger is 18 GeV. For the electron trigger, the threshold is 20 GeV or 22 GeV, depending on the data-taking period due to varying LHC luminosity conditions.

The selected events are required to contain a reconstructed primary vertex with at least five associated tracks with \(p_T > 0.4\) GeV. Event reconstruction makes use of electrons (\(e\)), muons (\(\mu\)), jets, and missing transverse momentum (\(E_T^{\text{miss}}\)). Electrons are reconstructed by matching energy deposits in the electromagnetic calorimeter with tracks in the inner detector, and are required to have \(p_T > 25\) GeV and \(|\eta| < 2.47\), excluding the transition region between the barrel and end-cap calorimeters at \(1.37 < |\eta| < 1.52\) [32]. Muons are reconstructed by matching tracks in the inner detector with tracks measured in the muon spectrometer, and are required to have \(p_T > 20\) GeV and \(|\eta| < 2.5\).

Tight isolation cuts are applied to both the electron and muon candidates to reduce the number of identified leptons (\(e, \mu\)) that come from non-prompt (non-\(W/Z\)) sources and from misidentified hadrons. For electrons, the \(E_T\) deposited in the calorimeter cells in a cone in \(\phi\) space of radius \(\Delta R = 0.2\) around the electron position is summed, and the \(E_T\) due to the electron is subtracted. The scalar sum of track transverse momenta in a cone of \(\Delta R = 0.3\), excluding the electron, is also measured. Cuts parametrized by the electron \(\eta\) and \(E_T\) are made on these two isolation variables to ensure a constant efficiency over the entire \((\eta, E_T)\) range. For muons, the corresponding calorimeter isolation energy in a cone of \(\Delta R = 0.2\) is required to be less than 4 GeV, and the scalar sum of track transverse momenta in a cone of \(\Delta R = 0.3\) is required to be less than 2.5 GeV after subtraction of the muon \(p_T\).

Jets are reconstructed from clustered energy deposits in the calorimeters with the anti-\(k_t\) [33] algorithm with a radius parameter \(R = 0.4\) [34]. Jets selected for the analysis are required to have \(p_T > 25\) GeV and \(|\eta| < 2.5\). In order to reduce the background from jets originating from pile-up interactions, additional selection criteria are applied to the fraction of the jet’s \(p_T\) (\(JVF\)) carried by tracks originating from the primary vertex, \(JVF > 0.75\).

The transverse momentum of neutrinos produced in the top-quark decays, measured as \(E_T^{\text{miss}}\), is inferred by balancing the vector sum of all visible transverse momenta. Specifically, the \(E_T^{\text{miss}}\) is constructed from the vector sum of all calorimeter cell energies contained in topological clusters [34] with \(|\eta| < 4.5\), projected onto the transverse plane. Contributions to the \(E_T^{\text{miss}}\) from the calorimeter cells associated with jets are taken at the corrected energy scale that is used for jets, while the contribution from cells associated with electrons is substituted by the calibrated transverse momentum of the electron. The contribution to the \(E_T^{\text{miss}}\) from the \(p_T\) of muons passing the selection requirements is also included.

The \(b\)-tagging algorithm [35, 36] employed for this analysis uses impact parameter and vertex position measurements from tracks in the inner detector as inputs to a neural network. The \(b\)-tagging efficiency was calibrated in a multi-jet data sample where at least one jet contains a muon [36]. The \(c\)-tagging efficiency was calibrated in a data sample with reconstructed \(D^-\) mesons [37]. For this analysis, \(b\)-tagged jets are required to satisfy a selection that is 75\% efficient for \(b\)-quark jets, approximately 30\% efficient for \(c\)-quark jets, and rejects light-flavor jets by a factor of approximately 35 in simulated \(t\bar{t}\) events. In this paper, a ‘\(b\)-tag’ (or a ‘\(b\)-tagged jet’) refers to any jet passing this selection, regardless of flavor. A ‘\(b\)-jet’, by contrast, refers to a jet (which may or may not be \(b\)-tagged) which contains a \(b\)-quark. Similarly, ‘\(c\)-jet’ and ‘\(HF\) jet’ are statements of the flavor composition of the jet, not whether the jet is \(b\)-tagged. Three distinct subsets of the selected \(b\)-tagged jets with different \(b\)-jet purity are used in the measurement of \(\sigma_{bd}(t\bar{t} + \text{HF})\), as described in Sec. VII.

Dilepton \(t\bar{t}\) candidate events are selected by requir-
ing exactly two opposite-sign leptons and at least two jets. To reduce the background from $Z\gamma^*$ processes, events with like-flavor leptons are required to have $E_T^{miss}$ above 60 GeV and a dilepton invariant mass satisfying $|m_{e^+e^-} - m_Z| > 10$ GeV. For events with one electron and one muon, the scalar sum of the lepton and jet transverse momenta is required to be above 130 GeV to reduce the backgrounds from $Z\gamma^* \rightarrow \tau^+\tau^-$, as well as $WW$, $WZ$, and $ZZ$ processes. This set of selection criteria is termed the 'nominal' $t\bar{t}$ selection criteria. The measurement of $t\bar{t}$ + HF production is carried out in the subset of these events that contain three or more $b$-tagged jets, whereas the measurement of $t\bar{t}$ production with at least one additional jet is performed in the subset with at least three jets, at least two of which are $b$-tagged.

Using the nominal selection criteria described above, data and Monte Carlo events are compared in three control regions: dilepton $t\bar{t}$ candidate events with zero, one, or two $b$-tagged jets. Data-to-simulation normalization corrections are applied to Monte Carlo simulation samples when calculating acceptance to account for observed differences in predicted and observed trigger and lepton reconstruction efficiencies, jet flavor tagging efficiencies and mistag rates, as well as jet and lepton energy scales and resolutions. In Fig. 1, the jet multiplicity distributions in the three regions are compared to Monte Carlo predictions. Agreement is observed within uncertainties.

### V. Definition of the Fiducial Phase Space and Calculation of Correction Factors

To allow comparison of the analysis results to theoretical predictions, the measurement is made within a fiducial phase space. The fiducial volume is defined in Monte Carlo simulation by requiring two leptons ($e$, $\mu$) from the $t \rightarrow Wb \rightarrow \ell b$ decays (including electrons and muons coming from $\tau \rightarrow \ell \nu\nu$) with $p_T > 25$ (20) GeV for $e$ ($\mu$), and $|\eta| < 2.5$ as well as three or more jets with $p_T > 25$ GeV and $|\eta| < 2.5$.

In the simulation, jets are formed by considering all particles with a lifetime longer than 10 ps, excluding muons and neutrinos. Particles arising from pile-up interactions are not considered. For the determination of the $t\bar{t}$ + HF fiducial cross section, $\sigma_{fid}(t\bar{t} + \text{HF})$, three or more jets are required to match a $b$- or $c$-quark, two of which must match a $b$-quark from top-quark decay. All simulated $b$- and $c$-quarks that were generated with $p_T > 5$ GeV are considered for the matching, and are required to satisfy $\Delta R(\text{quark}, \text{jet}) < 0.25$. Jets that match both a $b$- and a $c$-quark are considered as $b$-jets. For the calculation of $\sigma_{fid}(t\bar{t} + j)$ three or more jets are required, two of which must contain a $b$-quark from top-quark decay.

Each fiducial cross section is determined using measured quantities from the data, and a correction factor derived from the Monte Carlo simulation. The ratio of cross sections is defined as:

$$R_{HF} = \frac{\sigma_{fid}(t\bar{t} + \text{HF})}{\sigma_{fid}(t\bar{t} + j)}$$

The fiducial cross section for $t\bar{t}$ + HF production is determined from:

$$\sigma_{fid}(t\bar{t} + \text{HF}) = \frac{N_{\text{HF}}}{\int L \, dt \, \epsilon_{\text{HF}}}$$

where $N_{\text{HF}}$ is the number, after background subtraction, of $b$-tags from HF jets observed in the data, in addition
to the two $b$-jets from top-quark decays. The integrated luminosity of the sample is denoted as $\int \mathcal{L} dt$, and $\epsilon_{HF}$ is a correction factor taken from Monte Carlo simulation that converts the number of observed $b$-tags from additional HF jets to the number of events in the signal fiducial volume. This correction factor includes the acceptance within the fiducial region, the reconstruction efficiency, and a factor to account for the multiplicity of extra $b$-tagged HF jets per $t\bar{t}$+HF event in the signal region. This correction factor is different for $t\bar{t}$ + $b$ + $X$ ($\epsilon_b$) and $t\bar{t}$ + $c$ + $X$ ($\epsilon_c$), and thus $\epsilon_{HF}$ is determined as a weighted sum of these two contributions. The weight used to form the sum is the fraction of $t\bar{t}$ + HF events in the fiducial volume which contain additional $b$-jets as opposed to $c$-jets. This fraction is termed $F_{b/HF}$. The total correction factor ($\epsilon_{HF}$) is calculated as:

$$\epsilon_{HF} = F_{b/HF} \cdot \epsilon_b + (1 - F_{b/HF}) \cdot \epsilon_c$$

The denominator for $R_{HF}$, $\sigma_{fid}(t\bar{t} + j)$, is computed using a similar prescription:

$$\sigma_{fid}(t\bar{t} + j) = \frac{N_j}{\int \mathcal{L} dt \cdot \epsilon_j}$$

where $N_j$ is the yield of dilepton events in data with at least three jets, at least two of which are $b$-tagged, and $\epsilon_j$ is the $t\bar{t} + j$ acceptance factor calculated from the Monte Carlo simulation. The acceptance calculation for each fiducial cross section assumes that all $b$-tagged jets are from real HF quarks. Events with $b$-tagged jets from LF quarks are treated as a background, and subtracted when computing both $N_{HF}$ and $N_j$.

The ALPGEN + HERWIG Monte Carlo sample predicts $\epsilon_b = 0.19$, $\epsilon_c = 0.06$, and $F_{b/HF} = 0.31$. The total correction factor is thus predicted to be $\epsilon_{HF} = 0.106 \pm 0.005$ (stat.) for $\sigma_{fid}(t\bar{t} + HF)$. For $\sigma_{fid}(t\bar{t} + j)$ the acceptance factor is calculated to be $\epsilon_j = 0.129 \pm 0.001$ (stat.).

The prediction for $R_{HF}$ from the ALPGEN + HERWIG Monte Carlo sample is 3.4%. The value obtained from the POWHEG v1.01 [38] generator showered with HERWIG [16] is $R_{HF} = 5.2\%$, with $F_{b/HF} = 0.34$. While this $R_{HF}$ value is different to that from ALPGEN + HERWIG, the predicted $F_{b/HF}$ values are similar. Furthermore, a parton-level study using MAdGRAPH5 v1.47 [39] gives $F_{b/HF} = 0.29$. The value of $F_{b/HF}$ is also stable when different showering algorithms are used: the ALPGEN + PYTHIA Monte Carlo sample predicts a value of $F_{b/HF} = 0.32$, in good agreement with the prediction when HERWIG is used. Based on comparison of these predictions for $F_{b/HF}$, a symmetric 10% Monte Carlo systematic uncertainty is assigned, $F_{b/HF} = 0.31 \pm 0.03$. The prediction of $F_{b/HF}$ is also tested in data (see Sec. IX).

VI. EXPECTED SIGNAL AND BACKGROUND YIELDS

Table I shows the number of events with $\geq 3 \ b$-tagged jets expected in the Monte Carlo simulation from dilepton $t\bar{t}$ production and from various background sources. At this point, no distinction is made between events with a true additional HF jet and those containing a mistagged LF jet. The number of observed events is also shown. While Monte Carlo simulation is used to estimate $t\bar{t}$ + HF event rates and kinematic features, data-driven methods and Monte Carlo simulation are both used to estimate background processes, as detailed below.

Background processes containing real $b$-jets and leptons, such as single top-quark, $Z/\gamma* +$ jets, and diboson ($WW$, $WZ$, and $ZZ$) production, are estimated using Monte Carlo simulation. Contributions from diboson production are found to be negligible.

A major source of background comes from $t\bar{t}$ events in which one or more of the $b$-tagged jets is from a mistagged LF jet. This background is estimated using Monte Carlo simulation for the measurement of $t\bar{t}$ + HF. In the measurement of $\sigma_{fid}(t\bar{t} + HF)$, the final $t\bar{t}$ + LF background is determined by a fit to the vertex mass distribution of $b$-tagged jets in data, as explained in Sec. VII.

Background from events in which at least one of the leptons is either non-prompt (originating from e.g. a photon conversion or $b$-quark decay) or is a misidentified hadron, is estimated using data and Monte Carlo simulation. For instance, $W +$ jets, multi-jet, and $t\bar{t}$ events with one hadronically decaying $W$ boson can contribute in this way. This contribution is determined by scaling the yield of events in the data with a pair of same-sign leptons by the ratio of opposite-sign to same-sign yields ($R_{OS/SS}$) obtained in Monte Carlo simulation. The opposite-sign to same-sign ratio is determined separately for the three dilepton channels, and found to be $1.3 \pm 0.1$ (stat.) $\pm 1.5$ (syst.) for $e^+e^-$ events, $1.2 \pm 0.1$ (stat.) $\pm 0.7$ (syst.) for $\mu^+\mu^-$ events, and $1.2 \pm 0.1$ (stat.) $\pm 0.5$ (syst.) for events with one electron and one muon. The systematic uncertainty takes into account the unknown relative mixture of fake-lepton sources (photon conversions, $b$- and $c$-hadron decays, or misidentified hadrons) in the $R_{OS/SS}$ calculation. Since the central value of the prediction for this background is zero events, only variations in $R_{OS/SS}$ that lead to larger background predictions are considered in the systematic uncertainty calculation. This method for estimating the background due to events with fake leptons is validated in a control sample of dilepton events with less restrictive lepton identification requirements and no isolation criteria.

The dominant uncertainties on the total yield in Table I come from the jet energy scale, $b$-tagging efficiency, parton showering model, and initial- and final-
TABLE I: Observed and expected number of events in the signal region (i.e. with \( \geq 3 \) \( b \)-tagged jets). Uncertainties on individual components are statistical only. For the total expectation, systematic uncertainties are included.

<table>
<thead>
<tr>
<th>Process</th>
<th>Number of events</th>
</tr>
</thead>
<tbody>
<tr>
<td>( t\bar{t} )</td>
<td>( 106.7 \pm 3.4 )</td>
</tr>
<tr>
<td>Single top</td>
<td>( 2.2 \pm 0.5 )</td>
</tr>
<tr>
<td>( Z + \text{jets} )</td>
<td>( 0.2 \pm 0.1 )</td>
</tr>
<tr>
<td>Fake leptons</td>
<td>( 0 \pm ^{+5}_{-0} )</td>
</tr>
<tr>
<td>Total expectation</td>
<td>( 106 \pm ^{35 \text{(stat.)}}_{-35 \text{(syst.)}} )</td>
</tr>
<tr>
<td>Data</td>
<td>106</td>
</tr>
</tbody>
</table>

state radiation.

VII. TEMPLATE FIT

For the measurement of \( \sigma_{\text{fid}}(t\bar{t} + \text{HF}) \), the fraction of heavy-flavor jets produced in association with \( t\bar{t} \) is extracted by performing a binned maximum-likelihood fit on the displaced-vertex mass distribution using all \( b \)-tagged jets in the events with \( \geq 3 \) \( b \)-tagged jets. Although the final result is for both flavors combined, the fit includes separate \( b \)- and \( c \)-quark components to improve the determination of the LF fraction, and to test the Monte Carlo prediction for \( F_{b/\text{HF}} \), which is used for the calculation of the correction factor described in Sec. V. This displaced-vertex mass is constructed from the inner detector tracks associated with the secondary vertex using the algorithm described in Ref. [40]. While the presence of a displaced vertex is an indication that a jet contains a \( b \)-quark, a jet may be \( b \)-tagged even if no vertex is reconstructed. In this case, the vertex mass is undefined. These jets are assigned a mass value of \( -1 \) GeV and they are included in the fit to the displaced-vertex mass distribution. Keeping the events without a reconstructed vertex improves the discrimination between heavy-flavor and light-flavor jets.

While the vertex mass is a powerful discriminant, Monte Carlo studies indicate that the sensitivity on the fitted fraction of LF jets increases when the jet \( p_T \) is used as an additional discriminant. Considering only the statistical uncertainty, it is seen that a fit with both jet \( p_T \) and vertex mass is approximately half a standard deviation more sensitive than a fit with only the vertex mass. It was thus decided to define a two-dimensional probability density function, termed a ‘template,’ for the fit using the vertex mass and jet \( p_T \).

The fit is performed simultaneously in three mutually exclusive bins of \( b \)-jet purity, defined by different ranges of the \( b \)-tagging neural network output value. Certain values of the neural network output, termed ‘operating points’, are defined by the average \( b \)-jet selection efficiency resulting from the applied selection.

TABLE II: Summary of the \( b \)-tagging efficiencies for \( b \)-jets, \( c \)-jets, and light-flavor jets for the three mutually exclusive \( b \)-tagging selections used in the vertex mass template fit.

<table>
<thead>
<tr>
<th>( b )-purity</th>
<th>( b )-jet efficiency</th>
<th>( c )-jet efficiency</th>
<th>light-flavor efficiency</th>
</tr>
</thead>
<tbody>
<tr>
<td>High</td>
<td>60%</td>
<td>17%</td>
<td>0.43%</td>
</tr>
<tr>
<td>Medium</td>
<td>10%</td>
<td>7%</td>
<td>1.00%</td>
</tr>
<tr>
<td>Low</td>
<td>5%</td>
<td>6%</td>
<td>1.33%</td>
</tr>
</tbody>
</table>

In this analysis, operating points of 60%, 70% and 75% efficiency are used to define the boundaries of the \( b \)-jet purity bins.

The first bin uses only the tightest calibrated operating point (60%), contains the highest-purity sample of \( b \)-jets (referred to as ‘high purity’), and has a \( b \)-tagging efficiency of 60% for \( b \)-jets. The second bin (referred to as ‘medium purity’) requires a \( b \)-tag selection between the tightest and second tightest (70%) operating points, and contains a larger fraction of LF jets and \( c \)-jets. The efficiency for this bin is 10% for \( b \)-jets, i.e. the difference between the 70% and 60% operating points. The final bin ('low purity') requires a \( b \)-tag selection between the second (70%) and third operating point (75%), and contains the largest fraction of LF jets. The efficiency for this bin is 5% for \( b \)-jets. The \( b \)-tagging efficiencies for \( b \)-jets, \( c \)-jets, and light-flavor jets for each selection are given in Table II.

All three classes of \( b \)-tag purity are used in the analysis so that a jet is considered ‘\( b \)-tagged’ if it satisfies any of these criteria. The discrimination power between LF and \( c \)-jets is greatly improved by using three (as opposed to one) classes of \( b \)-purity. The vertex mass distributions for all \( b \)-tagged jets in events passing the nominal \( t\bar{t} \) selection criteria are shown in Fig. 2 to confirm that (a) the data are well described by the Monte Carlo simulation, (b) and the \( b \)-jet, \( c \)-jet and LF-jet fractions are different in the three purity selections. For the purpose of illustration, the normalization of the \( b \)-jet, \( c \)-jet, and LF-jet components is taken from Monte Carlo simulation.

The template fit has five components: \( b \)-jets from top-quark decays, non-\( t\bar{t} \) background, extra \( b \)-tagged jets from \( b \)-quarks, extra \( b \)-tagged jets from \( c \)-quarks, and light-flavor \( b \)-tagged jets. The template for \( b \)-jets from top-quark decays is obtained from the data in \( t\bar{t} \) dilepton events with exactly two \( b \)-tags. Monte Carlo simulation indicates that 97% of \( b \)-tagged jets in \( t\bar{t} \) dilepton events with exactly two \( b \)-tags come from the decay of the top quark. To account for this in the shape of the data template, a template for \( b \)-tags not from the top-quark decays is derived from the \( t\bar{t} \) Monte Carlo simulation, and subtracted with a 3% relative normalization from the data template. In the fit, the normalization for the template for \( b \)-jets from the top-quark decays is fixed assuming it contributes two of the three or more \( b \)-tags per observed event.
Background events from non-dilepton $t\bar{t}$ processes are included using Monte Carlo simulation, and enter the fit with a fixed normalization. Monte Carlo simulation is used to obtain templates for additional (non-$t \rightarrow Wb$) $b$-jets, $c$-jets, and LF jets.

In the fit to determine the number of $b$-tags from HF jets in addition to the two $b$-jets from top-quark decay, $N_{HF},$ separate templates for each category of jet in each of the three purity classes (high, medium, and low) are used. The $b$-tagging efficiencies (Table II) for each flavor of jet are used to relate the number of jets in each purity bin. After the application of all constraints, the fit has two floating parameters: the fraction of LF jets and the fraction of additional $b$-jets. The fraction of additional $c$-jets makes up the remainder.

Monte Carlo pseudo-experiments show that the fitting method is unbiased in both best-fit values and estimated uncertainties. The fit strategy (including estimates of statistical and systematic uncertainties) was verified using 10% of the full data sample as well as Monte Carlo pseudo-experiments before the fit was performed on the full data sample. These studies indicated that the fit could achieve only a 1$\sigma$ separation of $b$- vs. $c$-jets based on the expected statistical uncertainty alone. Inclusion of the systematic uncertainty would further reduce the sensitivity. However, the LF-jet fraction is expected to be measured with sufficient precision to give a statistically significant measurement of the total HF content, defined as the fraction of additional $b$-tagged jets not coming from LF jets. In the fit, the individual fractions are not constrained to be positive or below unity.

VIII. SYSTEMATIC UNCERTAINTIES

Systematic uncertainties may affect the shape of the vertex mass and $p_T$ templates as well as the acceptance calculations. For the systematic uncertainties on the template shapes, the fit to the data is re-evaluated using new templates, derived by varying the relevant parameters by their systematic uncertainties, and a new fit to the data is performed. Major uncertainties that affect the fit are the jet energy scale and resolution, the tagging efficiencies for $b$-, $c$- and LF jets, the parton-shower and hadronization models, and the Monte Carlo event generators.

The template for $b$-jets from top-quark decays is nominally taken from the data with exactly two $b$-tags. To account for kinematic biases due to additional heavy-flavor jets in the event, a systematic uncertainty on the shape of this template is assessed using $b$-jets
from top-quark decays from Monte Carlo inclusive $t\bar{t}$ events with three or more $b$-tagged jets.

The vertex mass of additional $b$- and $c$-jets is sensitive to the number of HF quarks contained in a jet (for instance, for $b\bar{b}$ or $c\bar{c}$ produced via gluon splitting). The dominant uncertainty from this effect would manifest itself as a difference in the shape of the template for additional $b$-jets. To assess this uncertainty, the template for additional $b$-jets is replaced by the template for $b$-jets from top-quark decays.

By default, the normalization of the template for $b$-jets from top-quark decays is fixed to two per event. A systematic uncertainty on this normalization is assessed by using the predicted normalization from Monte Carlo simulation, which includes events with less than two $b$-tags from top-quark decays, due to $b$-tagging inefficiency. The total uncertainty due to specific template shape variations is referred to as ‘additional fit uncertainties’ for the rest of this paper.

Systematic uncertainties also affect the overall event reconstruction efficiency. Dominant sources of uncertainty for this category are: the tagging efficiencies for $b$-, $c$- and LF jets, the jet energy scale and resolution, and the Monte Carlo event generator. Uncertainties on the lepton identification efficiency, $E_T^{miss}$ reconstruction, and fragmentation modeling are negligible. In general, systematic uncertainties are evaluated on the full data sample, with each uncertainty being taken as the difference between the nominal and the varied resulting values of $R_{HF}$.

An important uncertainty in this analysis comes from the flavor composition in the fiducial volume, namely in the value of $F_{b/HF}$, the fraction of $t\bar{t}$ + HF events in the fiducial volume which contain $b$-jets, used to calculate the correction factor $\epsilon_{HF}$. As described in Sec. V, an uncertainty of 10% on $F_{b/HF}$ is estimated using different Monte Carlo generators. It is possible to evaluate $F_{b/HF}$ using the data, but with the present data set, significant discrimination between $b$- and $c$-jets is not possible, making such a comparison of limited use. Nonetheless, the result of this study is presented as a point of comparison to the result obtained from the Monte Carlo.

**IX. RESULTS**

In the 106 events in the signal sample (with $\geq 3$ $b$-tagged jets), there are 325 $b$-tagged jets. After subtracting the non-$t\bar{t}$ background component, and the contribution from the tagged jets from the $t\rightarrow Wb$ decay, the number of additional $b$-tags is found to be 105. As described in Sec. VII, a template fit to all $b$-tagged jets is performed to determine the flavor composition of these additional $b$-tagged jets. The result of the fit to all 325 $b$-tagged jets is shown in Fig. 3. The weighted sums of all fit templates are shown, with contributions for extra HF and mistagged LF jets shown separately. The fitted fractions of $b$-tags from LF jets and additional $b$-jets are given in Table III. Of the 105 additional $b$-tags, 79 ± 14 (stat.) ± 22 (syst.) are attributed to HF jets. A detailed breakdown of the systematic uncertainties on the total number of HF jets is shown in Table IV.

Using Eq. 1, the number of HF jets observed in data, and the quoted correction factor $\epsilon_{HF}$ derived from

![FIG. 3: The result of the template fit (solid line) to the vertex mass distribution in data (points). Data are divided into three groups depending on the purity of $b$-jets passing each selection, as described in the text. The first three bins are the vertex mass distributions for the high-purity $b$-tags, the middle three bins for the medium-purity $b$-tags, and the last three bins for the low-purity $b$-tags. Within each purity category, the fit contains jets with no reconstructed secondary vertex. The middle bin contains jets with ‘low’ mass: less than 2 GeV. The third bin contains jets with ‘high’ mass: greater than 2 GeV. The best fit is shown as a sum (labeled as ‘Combined fit’, which includes the $b$-jets from top-quark decay) with separate contributions from additional $b$- and $c$-jets (labeled as ‘Heavy flavor’), and LF jets (labeled as ‘Light flavor’).](image)

**TABLE III: Relative composition of $b$-tagged jets in the signal region, fitted in data and compared to the expectation from Monte Carlo (MC) simulation. In data, the fractions of LF and additional $b$-jets are determined by the fit. The fraction of $b$-jets from top-quark decays is fixed in the fit to two $b$-tags in each event. The contributions from $t\bar{t}$ events with a fake lepton, or non-$t\bar{t}$ events are fixed in the fit using the Monte Carlo simulation (those are labeled as ‘other sources’ in the table). The fraction of $c$-jets is determined from unitarity. All quoted errors are statistical.**

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<th>Type of $b$-tag, fractions</th>
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<th>MC expectation</th>
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<td>Additional LF jets, %</td>
<td>8 ± 4</td>
<td>20</td>
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<tr>
<td>Additional $b$-jets, %</td>
<td>2 ± 7</td>
<td>9</td>
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<td>Additional $c$-jets, %</td>
<td>26 ± 8</td>
<td>3.5</td>
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<tr>
<td>$b$-jets from $t\rightarrow Wb$, %</td>
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<td>–</td>
</tr>
<tr>
<td>$b$-jets from other sources, %</td>
<td>2.5</td>
<td>–</td>
</tr>
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</table>
the Monte Carlo simulation for $t\bar{t} +$ HF production, $\sigma_{\text{id}}(t\bar{t} + $ HF) is found to be $0.16 \pm 0.03$ (stat.) pb. ALPGEN interfaced with HERWIG predicts a value of $0.10$ pb.

The uncertainty on the fitted fraction of light-flavor jets is significantly smaller than the uncertainty on the fitted fraction of additional $b$-jets. This is understood as an effect of fitting in multiple $b$-purity bins: the low-purity bin is dominated by light-flavor jets and thus gives improved discrimination. The data resolve the total observed HF production rate with a significance of about $3\sigma$.

In the data, $1656$ $t\bar{t}$ dilepton candidate events are observed with at least three jets, at least two of which are $b$-tagged. The total background estimate, which is dominated by LF jets misidentified as $b$-jets from top-quark decay, is found to be $112 \pm 4$ (stat.), leading to a background-subtracted yield of $1544 \pm 41$ (stat.). Using Eq. 2, and the quoted acceptance factor for $t\bar{t} + j$ production, $\sigma_{\text{id}}(t\bar{t} + j)$ is found to be $2.55 \pm 0.07$ (stat.) pb, compared to $2.83$ pb predicted by ALPGEN and HERWIG. Taking into account the total uncertainty, it is found that $R_{\text{HF}} = 0.52 \pm 0.11$ (stat.) $\pm 0.18$ (syst.) \%. A full breakdown of the systematic uncertainties contributing to $R_{\text{HF}}$ is given in Table IV.

The extracted value of $\sigma_{\text{id}}(t\bar{t} + $ HF) is very sensitive to the value of $F_{b/\text{HF}}$. As indicated in Sec. V, the efficiency for $t\bar{t} + b + X$ events is approximately a factor of three higher than the corresponding efficiency for $t\bar{t} + c + X$ events, implying a potential change in $\sigma_{\text{id}}(t\bar{t} + $ HF) by a factor of three if $F_{b/\text{HF}}$ is allowed to vary over the full range $[0,1]$.

Using the fitted fraction of additional $b$-jets in data results in $F_{b/\text{HF}} = -0.02$, with one and two sigma statistical upper bounds of $F_{b/\text{HF}} = 0.09$ and $0.27$, respectively. This value is found to be compatible with the predicted value to within $1\sigma$ when systematic uncertainties are included. Figure 4 shows $R_{\text{HF}}$ as a function of $F_{b/\text{HF}}$. The predicted and data-driven ranges of $F_{b/\text{HF}}$ are overlaid. With $F_{b/\text{HF}} = -0.02$ the central value for $R_{\text{HF}}$ is determined as $10.7\%$.

X. CONCLUSIONS

A $4.7$ fb$^{-1}$ sample of $7$ TeV proton–proton collisions recorded by the ATLAS detector at the LHC was used to measure the ratio $R_{\text{HF}}$ of the fiducial cross section for the production of $t\bar{t}$ events with at least one additional HF quark jet ($t\bar{t} + b + X$ or $t\bar{t} + c + X$) to that for the production of $t\bar{t}$ events with at least one additional jet, regardless of flavor, each with $p_T > 25$ GeV and $|\eta| < 2.5$. A fit to the vertex mass distribution for $b$-tagged jets in $t\bar{t}$ candidate events with three or more $b$-tagged jets is performed to determine the heavy- and light-flavor content of the additional $b$-tagged jets. The result of the fit shows that $79 \pm 14$ (stat.) $\pm 22$ (syst.) of the $105$ selected $b$-tagged jets originate from HF quarks, three standard deviations away from the hypothesis of zero $t\bar{t} +$ HF production. A value of $R_{\text{HF}} = 0.52 \pm 0.11$ (stat.) $\pm 0.18$ (syst.) \% is extracted. This value of $R_{\text{HF}}$ is consistent with the leading order predictions of $3.4\%$ obtained from the ALPGEN Monte Carlo generator interfaced with HERWIG and $5.2\%$ from a calcu-
lation using POWHEG interfaced with HERWIG.

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[12] ATLAS uses a right-handed coordinate system with its origin at the nominal interaction point (IP) in the centre of the detector and the z-axis along the beam pipe. The z-axis points from the IP to the centre of the LHC ring, and the y-axis points upward. Cylindrical coordinates \( r, \phi \) are used in the transverse plane, \( \phi \) being the azimuthal angle around the beam pipe. The pseudorapidity is defined in terms of the polar angle \( \theta \) as \( \eta = -\ln \tan(\theta/2) \). Transverse momentum and energy are defined as \( p_T = p \sin \theta \) and \( E_T = E \sin \theta \), respectively.

[17] \( \Delta R = \sqrt{(\Delta \phi)^2 + (\Delta \eta)^2} \), where \( \Delta \eta \) is the separation in \( \eta \) between the quark and jet and \( \Delta \phi \) is the separation in \( \phi \).
18 School of Physics and Astronomy, University of Birmingham, Birmingham, United Kingdom
19 (a) Department of Physics, Bogazici University, Istanbul; (b) Division of Physics, Dogus University, Istanbul;
(c) Department of Physics Engineering, Gaziantep University, Gaziantep, Turkey
20 (a) INFN Sezione di Bologna; (b) Dipartimento di Fisica, Università di Bologna, Bologna, Italy
21 Physikalisches Institut, University of Bonn, Bonn, Germany
22 Department of Physics, Boston University, Boston MA, United States of America
23 Department of Physics, Brandeis University, Waltham MA, United States of America
24 (a) Universidade Federal do Rio De Janeiro COPPE/EE/IF, Rio de Janeiro; (b) Federal University of Juiz de Fora (UFJF), Juiz de Fora; (c) Federal University of Sao Joao del Rei (UFSJ), Sao Joao do Rei; (d) Instituto de Física, Universidade de Sao Paulo, Sao Paulo, Brazil
25 Physics Department, Brookhaven National Laboratory, Upton NY, United States of America
26 (a) National Institute of Physics and Nuclear Engineering, Bucharest; (b) University Politehnica Bucharest, Bucharest; (c) West University in Timisoara, Timisoara, Romania
27 Departamento de Física, Universidad de Buenos Aires, Buenos Aires, Argentina
28 Cavendish Laboratory, University of Cambridge, Cambridge, United Kingdom
29 Department of Physics, Carleton University, Ottawa ON, Canada
30 CERN, Geneva, Switzerland
31 Enrico Fermi Institute, University of Chicago, Chicago IL, United States of America
32 (a) Departamento de Física, Pontificia Universidad Católica de Chile, Santiago; (b) Departamento de Física, Universidad Técnica Federico Santa María, Valparaíso, Chile
33 (a) Institute of High Energy Physics, Chinese Academy of Sciences, Beijing; (b) Department of Modern Physics, University of Science and Technology of China, Anhui; (c) Department of Physics, Nanjing University, Jiangsu; (d) School of Physics, Shandong University, Shandong; (e) Physics Department, Shanghai Jiao Tong University, Shanghai, China
34 Laboratoire de Physique Corpusculaire, Clermont Université and Université Blaise Pascal and CNRS/IN2P3, Clermont-Ferrand, France
35 Nevis Laboratory, Columbia University, Irvington NY, United States of America
36 Niels Bohr Institute, University of Copenhagen, Kobenhavn, Denmark
37 (a) INFN Gruppo Collegato di Cosenza; (b) Dipartimento di Fisica, Università della Calabria, Rende, Italy
38 (a) AGH University of Science and Technology, Faculty of Physics and Applied Computer Science, Krakow; (b) Marian Smoluchowski Institute of Physics, Jagiellonian University, Krakow, Poland
39 The Henryk Niewodniczanski Institute of Nuclear Physics, Polish Academy of Sciences, Krakow, Poland
40 Physics Department, Southern Methodist University, Dallas TX, United States of America
41 Physics Department, University of Texas at Dallas, Richardson TX, United States of America
42 DESY, Hamburg and Zeuthen, Germany
43 Institut für Experimentelle Physik IV, Technische Universität Dortmund, Dortmund, Germany
44 Institut für Kern- und Teilchenphysik, Technical University Dresden, Dresden, Germany
45 Department of Physics, Duke University, Durham NC, United States of America
46 SUPA - School of Physics and Astronomy, University of Edinburgh, Edinburgh, United Kingdom
47 INFN Laboratori Nazionali di Frascati, Frascati, Italy
48 Fakultät für Mathematik und Physik, Albert-Ludwigs-Universität, Freiburg, Germany
49 Section de Physique, Université de Genève, Geneva, Switzerland
50 (a) INFN Sezione di Genova; (b) Dipartimento di Fisica, Università di Genova, Genova, Italy
51 (a) E. Andronikashvili Institute of Physics, Iv. Javakhishvili Tbilisi State University, Tbilisi; (b) High Energy Physics Institute, Tbilisi State University, Tbilisi, Georgia
52 II Physikalisches Institut, Justus-Liebig-Universität Giessen, Giessen, Germany
53 SUPA - School of Physics and Astronomy, University of Glasgow, Glasgow, United Kingdom
54 II Physikalisches Institut, Georg-August-Universität, Göttingen, Germany
55 Laboratoire de Physique Subatomique et de Cosmologie, Université Joseph Fourier and CNRS/IN2P3 and Institut National Polytechnique de Grenoble, Grenoble, France
56 Department of Physics, Hampton University, Hampton VA, United States of America
57 Laboratory for Particle Physics and Cosmology, Harvard University, Cambridge MA, United States of America
58 (a) Kirchhoff-Institut für Physik, Ruprecht-Karls-Universität Heidelberg, Heidelberg; (b) Physikalisches Institut, Ruprecht-Karls-Universität Heidelberg, Heidelberg; (c) ZITI Institut für technische Informatik, Ruprecht-Karls-Universität Heidelberg, Mannheim, Germany
59 Faculty of Applied Information Science, Hiroshima Institute of Technology, Hiroshima, Japan
60 Department of Physics, Indiana University, Bloomington IN, United States of America
<table>
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<td>Institut für Astro- und Teilchenphysik, Leopold-Franzens-Universität</td>
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Center for High Energy Physics, University of Oregon, Eugene OR, United States of America
LAL, Université Paris-Sud and CNRS/IN2P3, Orsay, France
Graduate School of Science, Osaka University, Osaka, Japan
Department of Physics, University of Oslo, Oslo, Norway
Department of Physics, Oxford University, Oxford, United Kingdom
(a) INFN Sezione di Pavia; (b) Dipartimento di Fisica, Università di Pavia, Pavia, Italy
Department of Physics, University of Pennsylvania, Philadelphia PA, United States of America
Petersburg Nuclear Physics Institute, Gatchina, Russia
(a) INFN Sezione di Pisa; (b) Dipartimento di Fisica E. Fermi, Università di Pisa, Pisa, Italy
Department of Physics and Astronomy, University of Pittsburgh, Pittsburgh PA, United States of America
(a) Laboratorio de Instrumentacion e Fisica Experimental de Particulas - LIP, Lisboa, Portugal; (b) Departamento de Física Teórica y del Cosmos and CAFPE, Universidad de Granada, Granada, Spain
Institute of Physics, Academy of Sciences of the Czech Republic, Praha, Czech Republic
Czech Technical University in Prague, Praha, Czech Republic
Faculty of Mathematics and Physics, Charles University in Prague, Praha, Czech Republic
State Research Center Institute for High Energy Physics, Protvino, Russia
Particle Physics Department, Rutherford Appleton Laboratory, Didcot, United Kingdom
Physics Department, University of Regina, Regina SK, Canada
Ritsumeikan University, Kusatsu, Shiga, Japan
(a) INFN Sezione di Roma I; (b) Dipartimento di Fisica, Università La Sapienza, Roma, Italy
(a) INFN Sezione di Roma Tor Vergata; (b) Dipartimento di Fisica, Università di Roma Tor Vergata, Roma, Italy
(a) INFN Sezione di Roma Tre; (b) Dipartimento di Matematica e Fisica, Università Roma Tre, Roma, Italy
(a) Faculté des Sciences Ain Chock, Réseau Universitaire de Physique des Hautes Energies - Université Hassan II, Casablanca; (b) Centre National de l’Energie des Sciences Techniques Nucleaires, Rabat; (c) Faculté des Sciences Semlalia, Université Cadi Ayyad, LPHEA-Marrakech; (d) Faculté des Sciences, Université Mohamed Premier and LPTPM, Oujda; (e) Faculté des sciences, Université Mohammed V-Agdal, Rabat, Morocco
DSM/IRFU (Institut de Recherches sur les Lois Fondamentales de l’Univers), CEA Saclay (Commissariat à l’Energie Atomique et aux Energies Alternatives), Gif-sur-Yvette, France
Santa Cruz Institute for Particle Physics, University of California Santa Cruz, Santa Cruz CA, United States of America
Department of Physics, University of Washington, Seattle WA, United States of America
Department of Physics and Astronomy, University of Sheffield, Sheffield, United Kingdom
Department of Physics, Shinsiu University, Nagano, Japan
Fachbereich Physik, Universität Siegen, Siegen, Germany
Department of Physics, Simon Fraser University, Burnaby BC, Canada
SLAC National Accelerator Laboratory, Stanford CA, United States of America
(a) Faculty of Mathematics, Physics & Informatics, Comenius University, Bratislava; (b) Department of Subnuclear Physics, Institute of Experimental Physics of the Slovak Academy of Sciences, Kosice, Slovak Republic
(a) Department of Physics, University of Johannesburg, Johannesburg; (b) School of Physics, University of the Witwatersrand, Johannesburg, South Africa
(a) Department of Physics, Stockholm University; (b) The Oskar Klein Centre, Stockholm, Sweden
Physics Department, Royal Institute of Technology, Stockholm, Sweden
Departments of Physics & Astronomy and Chemistry, Stony Brook University, Stony Brook NY, United States of America
Department of Physics and Astronomy, University of Sussex, Brighton, United Kingdom
School of Physics, University of Sydney, Sydney, Australia
Institute of Physics, Academia Sinica, Taipei, Taiwan
Department of Physics, Technion: Israel Institute of Technology, Haifa, Israel
Raymond and Beverly Sackler School of Physics and Astronomy, Tel Aviv University, Tel Aviv, Israel
Department of Physics, Aristotle University of Thessaloniki, Thessaloniki, Greece
International Center for Elementary Particle Physics and Department of Physics, The University of Tokyo, Tokyo, Japan
Graduate School of Science and Technology, Tokyo Metropolitan University, Tokyo, Japan
Department of Physics, Tokyo Institute of Technology, Tokyo, Japan
Department of Physics, University of Toronto, Toronto ON, Canada
TRIUMF, Vancouver BC; (b) Department of Physics and Astronomy, York University, Toronto ON, Canada
Faculty of Pure and Applied Sciences, University of Tsukuba, Tsukuba, Japan
Department of Physics and Astronomy, Tufts University, Medford MA, United States of America
Centro de Investigaciones, Universidad Antonio Narino, Bogota, Colombia
Department of Physics and Astronomy, University of California Irvine, Irvine CA, United States of America
(a) INFN Gruppo Collegato di Udine; (b) ICTP, Trieste; (c) Dipartimento di Chimica, Fisica e Ambiente, Università di Udine, Udine, Italy
Department of Physics, University of Illinois, Urbana IL, United States of America
Department of Physics and Astronomy, University of Uppsala, Uppsala, Sweden
Instituto de Física Corpuscular (IFIC) and Departamento de Física Atómica, Molecular y Nuclear and Departamento de Ingeniería Electrónica and Instituto de Microelectrónica de Barcelona (IMB-CNM), University of Valencia and CSIC, Valencia, Spain
Department of Physics, University of British Columbia, Vancouver BC, Canada
Department of Physics and Astronomy, University of Victoria, Victoria BC, Canada
Department of Physics, University of Warwick, Coventry, United Kingdom
Waseda University, Tokyo, Japan
Department of Particle Physics, The Weizmann Institute of Science, Rehovot, Israel
Department of Physics, University of Wisconsin, Madison WI, United States of America
Fakultät für Physik und Astronomie, Julius-Maximilians-Universität, Würzburg, Germany
Fachbereich C Physik, Bergische Universität Wuppertal, Wuppertal, Germany
Department of Physics, Yale University, New Haven CT, United States of America
Yerevan Physics Institute, Yerevan, Armenia
Centre de Calcul de l’Institut National de Physique Nucléaire et de Physique des Particules (IN2P3), Villeurbanne, France
Also at Department of Physics, King’s College London, London, United Kingdom
Also at Laboratorio de Instrumentacao e Fisica Experimental de Particulas - LIP, Lisboa, Portugal
Also at Faculdade de Ciencias and CFNU, Universidade de Lisboa, Lisboa, Portugal
Also at Particle Physics Department, Rutherford Appleton Laboratory, Didcot, United Kingdom
Also at TRIUMF, Vancouver BC, Canada
Also at Department of Physics, California State University, Fresno CA, United States of America
Also at Novosibirsk State University, Novosibirsk, Russia
Also at Department of Physics, University of Coimbra, Coimbra, Portugal
Also at Università di Napoli Parthenope, Napoli, Italy
Also at Institute of Particle Physics (IPP), Canada
Also at Department of Physics, Middle East Technical University, Ankara, Turkey
Also at Louisiana Tech University, Ruston LA, United States of America
Also at Dep Fisica and CEFITEC of Faculdade de Ciencias e Tecnologia, Universidade Nova de Lisboa, Caparica, Portugal
Also at Department of Physics and Astronomy, Michigan State University, East Lansing MI, United States of America
Also at Department of Physics, University of Cape Town, Cape Town, South Africa
Also at Institute of Physics, Azerbaijan Academy of Sciences, Baku, Azerbaijan
Also at Institut für Experimentalphysik, Universität Hamburg, Hamburg, Germany
Also at Manhattan College, New York NY, United States of America
Also at CPPM, Aix-Marseille Université and CNRS/IN2P3, Marseille, France
Also at School of Physics and Engineering, Sun Yat-sen University, Guanzhou, China
Also at Academia Sinica Grid Computing, Institute of Physics, Academia Sinica, Taipei, Taiwan
Also at Laboratoire de Physique Nucléaire et de Hautes Energies, UPMC and Université Paris-Diderot and CNRS/IN2P3, Paris, France
Also at School of Physical Sciences, National Institute of Science Education and Research, Bhubaneswar, India
Also at Dipartimento di Fisica, Università La Sapienza, Roma, Italy
Also at DSM/IRFU (Institut de Recherches sur les Lois Fondamentales de l’Univers), CEA Saclay (Commissariat à l’Energie Atomique et aux Energies Alternatives), Gif-sur-Yvette, France
Also at Section de Physique, Université de Genève, Geneva, Switzerland
Also at Departamento de Fisica, Universidade de Minho, Braga, Portugal
Also at Department of Physics, The University of Texas at Austin, Austin TX, United States of America
Also at Department of Physics and Astronomy, University of South Carolina, Columbia SC, United States of America
America

$^a$ Also at Institute for Particle and Nuclear Physics, Wigner Research Centre for Physics, Budapest, Hungary

$^b$ Also at DESY, Hamburg and Zeuthen, Germany

$^c$ Also at International School for Advanced Studies (SISSA), Trieste, Italy

$^d$ Also at LAL, Université Paris-Sud and CNRS/IN2P3, Orsay, France

$^e$ Also at Faculty of Physics, M.V.Lomonosov Moscow State University, Moscow, Russia

$^f$ Also at Nevis Laboratory, Columbia University, Irvington NY, United States of America

$^g$ Also at Department of Physics, Oxford University, Oxford, United Kingdom

$^h$ Also at Discipline of Physics, University of KwaZulu-Natal, Durban, South Africa

$^*$ Deceased