Topological Search for the Production of Neutralinos and Scalar Particles

The OPAL Collaboration

Abstract

A search for scalar particles and neutralinos such as those predicted by supersymmetric models has been performed using a data sample of 4.4 million hadronic \( Z^0 \) decays recorded by the OPAL detector at the \( e^+e^- \) collider LEP. The production of such particles typically leads to event topologies consisting of an acoplanar pair of jets, or of a mono-jet, accompanied by sizeable missing energy owing to neutrinos and other undetectable neutral particles. Limits are obtained, at the 95% confidence level, on the masses and production rates of scalar particles produced in association with the \( Z^0 \). Limits are also placed on neutralino production, for which an additional possible signature is also studied, events containing a single observed photon. Within the Minimal Supersymmetric Standard Model, the mass of the lightest neutralino is found to be larger than 12.5 GeV/c\(^2\) at 95% C.L., provided that \( \tan\beta \) is larger than 1.5.
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1 Introduction

The data collected with the OPAL detector during the years 1990-1995, amounting to approximately 4.4 million hadronic \( Z^0 \) decays, were analysed in order to look for events with large missing energy, containing either a single jet ("mono-jet") or an "acoplanar" pair of jets, i.e. jets which are not back-to-back in the transverse plane. Such topologies are characteristic of several interesting processes involving the production of scalar or supersymmetric particles. The events observed with such topologies are compatible with expected backgrounds from standard processes, and our results may be used to place limits on the production of a scalar particle produced in association with a virtual \( Z^0 \) boson (\( Z^* \)), where the scalar decays either into quarks or into invisible neutral particles. Limits are also placed on neutralino production, for which data on single photon production and on the \( Z^0 \) width are also used.

In the Standard Model [1] (SM) of electroweak interactions, a complex doublet of scalar fields is introduced in order to endow the \( W^\pm \) and \( Z^0 \) gauge bosons with mass [2]. This leads to the prediction that a scalar Higgs boson (\( H^0 \)) should exist, of unspecified mass, but well-defined couplings. Any extension of the Standard Model with two or more complex doublets leads to additional scalar Higgs particles. The lightest of these particles would typically couple to the \( Z^0 \) with a smaller coupling than the SM Higgs. In a large class of models it decays in a manner similar to that of a SM Higgs [3], mostly to a pair of heavy quarks. Such scalars should be produced in association with a virtual \( Z^* \) which decays to neutrinos with branching fraction \( \approx 20\% \). A clear signature for scalar production would therefore be hadronic events with unbalanced momentum and large missing energy.

A similar topology may occur if the \( Z^0 \) boson decays into a pair of neutralinos, which are predicted in supersymmetric (SUSY) theories [4]. The fermionic partners of the \( \gamma \) (photinos), the \( Z^0 \) boson (zinos), and the neutral Higgs boson (neutral Higgsinos) mix to form mass eigenstates (\( \tilde{\chi}_i^0 \)) called neutralinos. The sign of the mass eigenvalues corresponds to the product of their charge-conjugation and parity (CP) quantum numbers. In the present analysis the lightest neutralino \( \tilde{\chi}_1^0 \) is assumed to be the lightest supersymmetric particle and is therefore stable and invisible if R-parity [5] is conserved. The pair production of \( \tilde{\chi}_2^0 \tilde{\chi}_1^0 \) or \( \tilde{\chi}_2^0 \tilde{\chi}_2^0 \), where \( \tilde{\chi}_2^0 \) is the second lightest neutralino, followed by the decay of \( \tilde{\chi}_2^0 \rightarrow \tilde{\chi}_1^0 Z^\pm \), with \( Z^\pm \rightarrow q\bar{q} \), leads to the topology of an acoplanar pair of jets, or a mono-jet. Neutralino pairs (\( \tilde{\chi}_i^0 \tilde{\chi}_j^0 \)) can be produced through s-channel \( Z^0 \) boson decay or by t-channel selectron (\( \tilde{e} \)) exchange. The latter diagram gives a significant constructive contribution to the production rate if the selectron is light. However, in that case, the decay of \( \tilde{\chi}_2^0 \) to \( \tilde{\nu} \nu \) may dominate for certain values of the SUSY parameters, leading to unobserved final states.

The simplest supersymmetric extension of the SM is the Minimal Supersymmetric Standard Model [6] (MSSM), which involves the addition of only one complex doublet of scalar fields to the SM. In the MSSM there might be a large branching ratio for the decay \( \tilde{\chi}_2^0 \rightarrow \tilde{\chi}_1^0 \gamma \) [7]. Therefore events in which a single photon is detected are also included in the present study.

Finally we consider the case of an invisible scalar which couples to the \( Z^0 \) with some fraction of the coupling of the SM Higgs boson, produced in association with a virtual \( Z^* \). Such a scenario could occur, for example, in the MSSM, where the light scalar Higgs might decay to a pair of invisible neutralinos. Invisible scalar particles also appear in other models, such as Majoron models ([8] to [11]). Some of these models are suggested for the generation of the cosmological baryon asymmetry at the electroweak scale [12]. In all of these models the scalar boson could decay predominantly into invisible Majorons [10]-[13]. In order to search for invisible scalars.
produced in association with a virtual $Z^*$, one can exploit the 70% decay branching fraction of the $Z^0$ boson to a quark pair. The experimental signature is therefore essentially the same as for a scalar decaying to quarks recoiling against a $Z^*$ decaying to neutrinos.

In this paper we report on a direct search for events with acoplanar jets, mono-jets or single photons, using the OPAL detector at centre-of-mass energies around the $Z^0$ mass. In section 2 we outline the detector, and the data and Monte Carlo samples used for the analysis. In section 3 the analysis procedure is described, in section 4 the efficiencies and systematic errors are discussed, and in section 5 the results are interpreted in terms of limits on particle production rates within the framework of some of the models mentioned above.

2 The OPAL Detector, Data Selection and Simulation

The OPAL detector is described in detail in Ref. [14]. It is a multipurpose apparatus having nearly complete solid angle coverage. The central detector consists of a system of tracking chambers providing charged particle tracking over 96% of the full solid angle inside a 0.435 T solenoidal magnetic field. A lead-glass electromagnetic calorimeter located outside the magnet coil covers the full azimuthal range with excellent hermeticity in the polar angle range $|\cos \theta| < 0.82$ for the barrel region and $0.81 < |\cos \theta| < 0.984$ for the endcap region. The magnet return yoke is instrumented for hadron calorimetry, and consists of barrel and endcap sections along with pole tips that together cover the region $|\cos \theta| < 0.99$. Calorimeters close to the beam axis measure the luminosity using small angle Bhabha scattering events and complete the geometrical acceptance down to 26 mrad. These include the forward detectors (FD) which are lead-scintillator sandwich calorimeters and at smaller angles, silicon-tungsten calorimeters (SW) [15] located on both sides of the interaction point.

The data sample used for the present analysis includes about 4.4 million hadronic $Z^0$ decays collected at energies around the $Z^0$ peak, corresponding to a total integrated luminosity of approximately 160 pb$^{-1}$. Standard quality requirements on tracks and energy clusters in the calorimeters were imposed, as described in Ref. [16]. In brief, the tracks used in this study were required to originate at the interaction point, to have greater than some minimum number of hits in the main tracking chamber and to have a transverse momentum with respect to the beam direction greater than 0.1 GeV/$c$. Energy clusters in the calorimeters were required to exceed minimum energy thresholds and those coming from noisy channels were excluded.

The detection efficiency for signal events depends on the mass of the scalar in the $S^0Z^*$ process. In the neutralino case it depends on the $\tilde{\chi}_2^0$ mass, on the mass difference $\Delta M^0 = (m_{\tilde{\chi}_2^0} - m_{\tilde{\chi}_1^0})$ and on the $\tilde{\chi}_2^0$ decay modes. There is also a small dependence on the relative CP phase of the neutralinos, which affects the cross-sections and angular distributions. Monte Carlo simulations were used in order to estimate the efficiency. For the simulation of the scalar production process $e^+e^-\rightarrow Z^0\rightarrow Z^*S^0$ the Monte Carlo generator PYTHIA [18] was used in its $e^+e^-\rightarrow Z^0\rightarrow Z^*\tilde{\tau}\tilde{\tau}$ generation mode. In the case of a visible scalar the decay modes were $Z^*\rightarrow \nu\tilde{\nu}$, $S^0\rightarrow q\bar{q}$. Event samples were generated for scalar masses in the range 5–70 GeV/$c^2$. For the invisibly decaying $S^0$ boson, only $Z^*$ decays to $q\bar{q}$ were considered. Event samples were generated for invisible scalar masses in the range 1–70 GeV/$c^2$. Neutralino events were

\footnote{A right-handed coordinate system is adopted, where the $x$-axis points to the centre of the LEP ring, and positive $z$ is along the electron beam direction. The angles $\theta$ and $\phi$ are the polar and azimuthal angles, respectively.}
simulated using SUSYGEN [19], based on the formulae of Ref. [20]. The processes considered were $e^+ e^- \rightarrow \tilde{\chi}_2^0 \tilde{\chi}_1^0$ where $\tilde{\chi}_2^0 \rightarrow \tilde{\chi}_1^0 q\bar{q}$ and $e^+ e^- \rightarrow \tilde{\chi}_2^0 \tilde{\chi}_2^0$ where one of the neutralinos was forced to decay to $\tilde{\chi}_1^0 q\bar{q}$ and no restriction was placed on the decay mode of the other. Events were generated corresponding to different points in the $(m_{\tilde{\chi}_2^0}, m_{\tilde{\chi}_1^0})$ plane and for both values of their relative CP phase (CP$_{\chi_2^0}$CP$_{\chi_1^0} = \pm 1$). The regions where $\Delta M^0 \lesssim 3$ GeV/c$^2$ were not considered in the present analysis. The Lund fragmentation scheme does not reliably describe this region due to large non-perturbative QCD effects, and the experimental analysis was not designed to have good acceptance in this region.

To study the reaction $e^+ e^- \rightarrow \tilde{\chi}_2^0 \tilde{\chi}_1^0$, with $\tilde{\chi}_2^0 \rightarrow \tilde{\chi}_1^0 \gamma$, a simple generator was constructed. In the laboratory system this effectively produced an isotropic angular distribution of photons with a flat energy spectrum within the region allowed by kinematics. The known experimental acceptance and resolution for photons was then taken into account.

There are several possible sources of background to the signal topology, for which Monte Carlo simulations are needed:

- In the case of acoplanar events with large visible energy (corresponding to the cases of large $\Delta M^0$, heavy visible scalar or light invisible scalar), the most important background arises from multi-jet hadronic events originating from $Z^0 \rightarrow q\bar{q}$ decays, in which one or more jet momenta are poorly determined. A sample of approximately 7.5 million $Z^0 \rightarrow q\bar{q}$ events was generated using the JETSET [18] generator, with parameters tuned to OPAL data [21]. The most common reasons for poor determination of jet momenta are the production of heavy quarks decaying into energetic neutrinos, or the production of energetic neutrons or $K_L^0$'s which could be poorly measured in the hadron calorimetry. A further sample of $Z^0$ decays was therefore generated using JETSET, applying a preselection to enhance such events before detailed simulation. This sample was equivalent to 33 million inclusive hadronic $Z^0$ decays.

- The process $e^+ e^- \rightarrow \tau^+ \tau^- (\gamma)$ may involve highly energetic neutrinos, yielding two acoplanar jets with large missing energy. Such events were generated with the KORALZ [22] event generator.

- In the cases where a visible scalar is light or an invisible scalar is heavy or when $\Delta M^0$ is small, the events would be characterised by large missing energy. In this case, an important background can arise from two-photon scattering events in which energy escapes detection close to the beam direction. Such events were generated with PYTHIA [18], including both point-like $\gamma \gamma \rightarrow q\bar{q}$ processes and a vector meson dominance component.

- A further background to the present search arises from other four-fermion processes in which at least one of the fermions is a neutrino. Although the cross-section for these processes is small at centre-of-mass energies below the $W^+ W^-$ or $Z^0 Z^0$ threshold, their event topology is similar to that of the signal. To simulate these events we used a generator based on helicity amplitude calculations, which takes into account all the relevant diagrams and their interference, and includes initial state radiation [23].

- Finally in the case of single photon events, the main irreducible background comes from $e^+ e^- \rightarrow \nu \bar{\nu} \gamma$ events. These events were produced with a generator based on Ref. [24].

Generated signal and background events were processed through the full simulation of the OPAL detector [25], and the same event analysis chain was applied to simulated events as to the data.
3 Analysis

3.1 Acoplanar jets and mono-jets

An accurate measurement of energy and of jet directions is crucial in order to distinguish between signal and background. The measurement of visible energy, missing momentum, visible mass and total transverse momentum of the events, and of jet angles, was performed by the method described in Ref. [16]. Four-momentum vectors were formed for each track and calorimeter cluster, and then summed. The tracks were assigned the pion mass, unless identified as electrons or muons, and the calorimeter clusters were treated as massless particles. In order to reduce the effects of double counting, four-vectors based on the average expected energy deposition in the calorimeters for each charged track were then subtracted. This average energy deposition was parametrised as a function of track momentum and polar angle.

In most cases the signal consists of multi-jet events. However, if the invisible scalar is heavy, or both $\chi_0^0$ and $\chi_1^0$ are light, the expected topology is often that of a mono-jet. In order to classify events as mono- or di-jets, each event was divided into two hemispheres by the plane orthogonal to the thrust direction. If there were no tracks and clusters passing the quality cuts in one of the hemispheres, the event was classified as a mono-jet. In the remaining events, classified as di-jets, the momentum sums in the two hemispheres were taken to define the two jets. In the following description, all cuts were applied to both classes unless otherwise specified.

The first group of cuts was applied as a preselection on the data:

- The numbers of charged tracks and of electromagnetic clusters were each required to be $\geq 5$. The cut was set to a low value in order to accept events where the mass difference between $\chi_2^0$ and $\chi_1^0$ is small, or the mass of the invisibly decaying scalar is large, leading to a small visible energy and low multiplicity.
- The fraction of tracks pointing to the interaction point was required to exceed 20% (50%) of the total number of tracks in the event in di-jet (mono-jet) events. This cut serves to eliminate background from off-momentum particles interacting in the beam pipe or low-multiplicity events containing hadronic interactions in the beam pipe or detector material.
- To reduce the number of hadronic $Z^0$ decays in the event sample, di-jet events were required to satisfy $\cos \theta_{acoll} < 0.98$ where $\pi - \theta_{acoll}$ is the three-dimensional angle between the two jets. This cut rejected about 98% of the initial data sample.
- In order to ensure good energy containment, events with large energy flow near the beam direction were eliminated by the following cuts:
  - The energies deposited in the forward (FD and SW) calorimeters were required to be less than 2 GeV and 5 GeV respectively.
  - The polar angle of the missing momentum vector was required to lie in the range $|\cos \theta| < 0.94$.
  - The forward energy flow divided by the total observed energy was required to be less than 10. The forward energy flow [17] is the sum of the energies observed in forward and backward cones (defined by $|\cos \theta| > 0.8$), weighted by $1/\sin^2 \theta$.
  - The $z$ component of the total event momentum was required to be less than 20 GeV/c.
Table 1: Numbers of events in data and Monte Carlo (scaled to the luminosity in the data) at various stages in the cuts, for mono-jet and di-jet events combined.

<table>
<thead>
<tr>
<th>Cuts</th>
<th>Data</th>
<th>$Z^0 \rightarrow q\bar{q}$</th>
<th>Two-photon</th>
<th>$Z^0 \rightarrow \tau^+\tau^-$</th>
<th>four-fermion</th>
<th>Total MC</th>
</tr>
</thead>
<tbody>
<tr>
<td>Preselection</td>
<td>34998</td>
<td>32561</td>
<td>3370</td>
<td>96</td>
<td>2.6</td>
<td>36030</td>
</tr>
<tr>
<td>$p_T$ cut</td>
<td>31536</td>
<td>32547</td>
<td>30</td>
<td>92</td>
<td>2.4</td>
<td>32671</td>
</tr>
<tr>
<td>$\tau$ cuts</td>
<td>31412</td>
<td>32518</td>
<td>30</td>
<td>18</td>
<td>2.3</td>
<td>32567</td>
</tr>
<tr>
<td>non-spherical</td>
<td>11461</td>
<td>12467</td>
<td>30</td>
<td>17</td>
<td>2.1</td>
<td>12516</td>
</tr>
<tr>
<td>$\theta_{acol}$ and $\theta_{acop}$</td>
<td>20</td>
<td>16</td>
<td>0</td>
<td>2</td>
<td>1.5</td>
<td>19.5</td>
</tr>
<tr>
<td>All cuts</td>
<td>2</td>
<td>0.54</td>
<td>0</td>
<td>0.35</td>
<td>1.41</td>
<td>2.30</td>
</tr>
</tbody>
</table>

After these preselection cuts, the number of events selected in data and the expectations from the Monte Carlo simulations are shown in Table 1.

In Fig. 1(a) we plot, for the di-jet events in the data, $p_T$ against $M_{vis}/E_{c.m.}$, where $M_{vis}$ is the visible mass, $E_{c.m.}$ the centre-of-mass energy and $p_T$ the total transverse momentum of the event, i.e. the magnitude of the vector sum of the transverse momenta. The clear cluster of events at low $p_T$ and $M_{vis}$ is associated with two-photon interactions. This background was effectively eliminated by rejecting di-jet events having $M_{vis}/E_{c.m.} < 0.27$ and $p_T < 10$ GeV/c. Fig. 1(b) shows the $p_T$ distribution for di-jet events having $M_{vis}/E_{c.m.} < 0.27$ for data, in comparison with Monte Carlo. Mono-jet events were required to satisfy $p_T > 4$ GeV/c. The value of $p_T$ was calculated with and without the hadronic calorimeter information, and the minimum of the two values was taken. The value using the hadron calorimeter gave the minimum in only a few cases; however, this procedure was adopted in order to ensure optimal rejection of two-photon events. The observed and expected numbers of events after these cuts are again shown in Table 1.

The next group of cuts was designed to reject $Z^0 \rightarrow \tau^+\tau^-$ events:
- For events with less than 10 tracks the thrust value was required to be smaller than 0.95.
- Some $\tau$-pairs show a mono-jet-like signature and therefore an additional requirement that the mass of the highest energy hemisphere exceed 2 GeV/c$^2$ was imposed.
- To remove radiative $\tau$ events, an additional requirement was imposed on events containing less than 10 charged tracks. Events containing an unassociated electromagnetic cluster of energy greater than 10 GeV or a converted photon of energy greater than 6 GeV were rejected, provided that the events were planar (specifically, the aplanarity $A < 0.02$ where $A = \frac{3}{2}Q_1$ and $Q_1$ is the smallest eigenvalue of the sphericity tensor [26]). The observed and expected numbers of events after these cuts are again given in Table 1.

The remaining cuts are applied to di-jet events only. At this stage, the principal background is $Z^0 \rightarrow q\bar{q}$ events. In order to search for acoplanar events within the remaining data (which are dominated by the back-to-back topology of the hadronic decays of the $Z^0$), we cut in the distributions of acollinearity ($\theta_{acol}$) and acoplanarity ($\theta_{acop}$, where $\pi - \theta_{acop}$ is the angle between the two jets in the $x$-$y$ plane). To ensure that the events have a non-spherical topology, so that $\theta_{acol}$ and $\theta_{acop}$ are well defined, events with thrust $<0.7$ were eliminated. In addition, events were rejected if the average hemisphere mass, $m_{hem}^{acol}$, was greater than 20 GeV/c$^2$ or if the minimum of the hemisphere thrust, $T_{hem}^{min}$ (calculated in the centre-of-mass of each hemisphere separately) was less than 0.7. The observed and expected numbers of events after these cuts are compared in Table 1.

The cuts on $\theta_{acol}$ and $\theta_{acop}$ need to take account of the angular resolution, which depends on...
the topological nature of the events and also on the different geometrical regions of the detector. The remaining events were divided into two classes A and B, for which different acollinearity and acoplanarity cuts were applied. The class B events have broader jets, and thus the resolution on the angles is poorer. The cuts are given in Table 2. They are tighter than we used in Ref. [17], because Monte Carlo studies indicated that, with the present larger data sample, significant background would have been expected with the old cuts. The distributions of $\theta_{\text{acol}}$ for classes A and B are shown in Figs. 1(c,d) for data and Monte Carlo, and the observed and expected numbers of events after these cuts are again shown in Table 1.

<table>
<thead>
<tr>
<th>Class</th>
<th>$T^\text{min}_{\text{hemi}}$</th>
<th>$m^{\text{avg}}_{\text{hemi}}$</th>
<th>region</th>
<th>$\cos \theta_{\text{acol}}$</th>
<th>$\cos \theta_{\text{acop}}$</th>
</tr>
</thead>
<tbody>
<tr>
<td>A</td>
<td>0.85 – 1.00</td>
<td>0 – 11 GeV/c$^2$</td>
<td>barrel</td>
<td>$&lt; 0.95$</td>
<td>$&lt; 0.98$</td>
</tr>
<tr>
<td></td>
<td></td>
<td></td>
<td>endcap</td>
<td>$&lt; 0.90$</td>
<td>$&lt; 0.95$</td>
</tr>
<tr>
<td>B (excluding class A)</td>
<td>0.70 – 1.00</td>
<td>0 – 20 GeV/c$^2$</td>
<td>both</td>
<td>$&lt; 0.70$</td>
<td>$&lt; 0.5$</td>
</tr>
</tbody>
</table>

Table 2: Class definitions and values of the cuts on the acollinearity and the acoplanarity angle. The barrel region is defined by $|\cos \theta| < 0.71$ and the endcap region by $|\cos \theta| \geq 0.71$.

The background events which survive the above cuts consist mainly of poorly measured multi-jet events, and thus the missing momentum generally lies close to one of the jets. These events are eliminated by demanding that the sum of charged track and cluster energies in the calorimeters in a cone of half-angle $45^\circ$ around the missing momentum vector be less than 2 GeV. The observed and expected numbers of events after this final cut are presented in the last row of Table 1.

Two events from the full data sample survive all the selection cuts; their properties are summarised in Table 3. The two observed candidates are consistent with the background expectation of $2.30 \pm 0.43$ events, consisting of $0.54 \pm 0.24$ events from hadronic decays of the $Z^0$, $0.35 \pm 0.35$ events from $\tau^+\tau^-$, and $1.41 \pm 0.04$ events from four-fermion processes. Fewer than 0.6 events are expected with $M_{\text{vis}}$ exceeding 50 GeV/c$^2$. Although the remaining events exhibit no apparent deviation from expectations based on SM processes, both events are conservatively taken as signal candidates when interpreting the results of the search. Fig. 2(a) shows the distribution of $M_{\text{vis}}/E_{\text{c.m.}}$ for the surviving data and the background expectations. In Fig. 2(b) the Monte Carlo predictions for the signal after all cuts are shown for some typical cases: for a 60 GeV/c$^2$ visible or a 70 GeV/c$^2$ invisible scalar particle or a pair of neutralinos with masses of $(m_{\chi^0_2}, m_{\chi^0_1}) = (30,0)$ GeV/c$^2$. The predicted mass resolutions of these signals are taken into account when calculating limits.

### 3.2 Single photon events

The selection of single photon events followed closely the analysis of Ref. [27], which reported a measurement of the process $e^+e^-\rightarrow\nu\bar{\nu}\gamma$. The analysis was modified in order to concentrate on the search for high-energy photons. In particular, it was required that the scaled transverse energy of the photon, $x_T = 2E\sin\theta/E_{\text{c.m.}}$, exceed 0.2. The angular region considered was $|\cos \theta| < 0.7$. A total of 31 single photon events was observed, consistent with the expectation from known processes of $27.1 \pm 2.1$, dominated by $\nu\bar{\nu}\gamma$ events. The observed spectrum of $x_T$ is compared with $\nu\bar{\nu}\gamma$ Monte Carlo in Fig. 2(c). The expected number of events depends strongly on the photon energy. Since the expected energy spectrum from radiative neutralino decay is
determined by the neutralino masses, we select an optimal cut on $x_T$ (above $x_T=0.2$) for each point in the $(m_{\tilde{\chi}^0_2}, m_{\tilde{\chi}^0_1})$ plane so as to achieve maximal sensitivity to the existence of neutralinos. We parametrised the expected background from $\nu\bar{\nu}\gamma$ and evaluated the acceptance for radiative neutralino decay for each value of the $x_T$ cut. The value of the $x_T$ cut was chosen so that if there were no signal, and if observed events were produced at the rate expected for background events, the resulting upper limit on the signal process would be minimised. At each point in the $(m_{\tilde{\chi}^0_2}, m_{\tilde{\chi}^0_1})$ plane the observed number of events is consistent with the expected background and thus 95% C.L. upper limits on the product branching ratio $\text{BR}(Z^0\rightarrow\tilde{\chi}^0_2\tilde{\chi}^0_1)\text{BR}(\tilde{\chi}^0_2\rightarrow\tilde{\chi}^0_1\gamma)$ were evaluated taking into account the expected background contribution.

### 4 Efficiencies and Systematic Errors

#### 4.1 Signal Efficiencies

The detection efficiencies for scalar particles depend mainly on the mass and the decay modes. The efficiency for a heavy visible scalar produced in association with a $Z^*$ which decays into a pair of neutrinos is comparable to that of a light invisible scalar produced in association with a $Z^*$ which decays to a pair of quarks. The efficiency for a visible scalar (not including the $Z^*$ branching ratio) reaches 50% at a scalar mass of around 40 GeV/$c^2$. It falls to 15% at 65 GeV/$c^2$ because the jets originating from a heavy scalar decay become more collinear, and falls to 30% for a 12 GeV/$c^2$ scalar owing to the low mass and $p_T$ of the observed system. Likewise the efficiency for an invisible scalar was found to be about 26% for a very light invisible scalar, rising to 55% at 50 GeV/$c^2$, and falling to 22% at 70 GeV/$c^2$.

For neutralinos produced through the reaction $\tilde{\chi}^0_2\rightarrow\tilde{\chi}^0_1Z^*$, with $Z^*\rightarrow q\bar{q}$, the detection efficiency at a given point in the $(m_{\tilde{\chi}^0_2}, m_{\tilde{\chi}^0_1})$ plane depends on the value of $\cos\theta^{\tilde{\chi}^0_2}$ and $\cos\theta^{\tilde{\chi}^0_1}$. The lower of the two efficiencies was used for the limit calculation. The efficiencies were found to lie between 3% and 51% in the direct search for $e^+e^-\rightarrow\tilde{\chi}^0_2\tilde{\chi}^0_1$, and between 2% and 43% in the direct search for $e^+e^-\rightarrow\tilde{\chi}^0_2\tilde{\chi}^0_2$. The lower ends of these ranges of efficiencies correspond to the case of small $\Delta M^0$. In the case of radiative neutralino decay, $\tilde{\chi}^0_2\rightarrow\tilde{\chi}^0_1\gamma$, the efficiencies varied between 20 to 70% (within the fiducial region $|\cos\theta| < 0.7$).
4.2 Systematic Errors

The integrated luminosity was determined by counting multihadronic decays of the $Z^0$ and using the published OPAL hadronic cross-sections [28]. The systematic error from this procedure was 0.5%, common to all channels.

The SM Higgs production cross-section serves as a convenient reference for the scalar particle search, and its uncertainty was taken to be 1.0% [29], taking into account the absolute cross-section and its dependence on the centre-of-mass energy.

The uncertainty associated with modelling of signal and background using Monte Carlo was evaluated taking account of Monte Carlo statistics, the effect of fragmentation, the uncertainty on $\alpha$, and the variation of selection cuts. The latter was accomplished by varying each of the selection cuts by approximately one standard deviation of the experimental resolution on the corresponding quantity, and determining the consequent change in the efficiency. It was found that the Monte Carlo statistical error dominated the uncertainties in all signal channels. The total Monte Carlo error varied between 1.8% and 5.0% for the visible scalar, between 3.1% and 6.1% for the invisible scalar, and between 3.0% and 18.0% for the neutralinos, depending on the masses.

The systematic and statistical errors were summed quadratically and subtracted from the signal selection efficiency.

5 Results

5.1 Limits on Scalar Particle Production Rates and Masses

The production rate of a scalar particle of mass $m_{S^0}$ in association with a $Z^*$, normalised to that of a SM Higgs boson of the same mass $m_{H^0}$, is given by the ratio of the corresponding cross-sections. To set upper bounds on the normalised production rates of visible or invisible scalar particles, the following expression was used:

$$
\frac{B \cdot \sigma(e^+e^-\rightarrow S^0Z^*)}{\sigma(e^+e^-\rightarrow \bar{H}_{SM}Z^*)} = \frac{N(m_{S^0})}{\text{BR}(Z^*\rightarrow \bar{f}f) \cdot \sum_{E_i} e(E_i, m_{S^0}) \cdot \sigma(e^+e^-\rightarrow \bar{H}_{SM}Z^*)(E_i, m_{H^0}) \cdot \mathcal{L}(E_i)},
$$

(1)

where $\bar{f}f = \bar{q}q$ or $\bar{f}f = \nu\bar{\nu}$ for an invisible or a visible scalar respectively, and $B$ is 1 or $\text{BR}(S^0\rightarrow q\bar{q})$ respectively. The $\sigma$'s are the production cross-sections, $e$ is the selection efficiency, and $\mathcal{L}$ is the integrated luminosity at an energy $E_i$. The function $N(m_{S^0})$ is the minimum number of expected events needed in order to set an upper bound at the 95% C.L. It was calculated using Poisson statistics and taking into account the mass resolution of the observed candidates [30].

The exclusion curves are shown in Fig. 3. Shoulders appear at masses corresponding to the candidate events passing the selection cuts. Degrading the mass resolution by up to 50% has only a minor effect on the curves. Fig. 3(a) shows that a visible scalar particle decaying entirely to quarks can be excluded for masses up to 60.8 GeV/$c^2$ at the 95% C.L. for a coupling strength to the $Z^0$ equivalent to that of the SM Higgs boson. A scalar with the expected decay branching ratios of the SM Higgs boson would be excluded up to 60.6 GeV/$c^2$. In a forthcoming publication, this result will be used together with other search channels to place limits on the SM Higgs boson. From Fig. 3(b) one can see that a massless invisible scalar particle is excluded.
if its production rate is larger than $2.8 \cdot 10^{-4}$ that of the SM Higgs Boson, while for the same production rate as that predicted for the SM Higgs, an invisible scalar is excluded if its mass is less than 67.5 GeV/c².

5.2 Limits on Neutralino Production

We obtain upper limits at the 95% C.L. on the $Z^0 \to \tilde{\chi}_2^0 \tilde{\chi}_1^0$ branching ratio, assuming specific decay modes. These limits do not depend on the details of SUSY models. The limit is computed as:

$$\frac{N(m_{\tilde{\chi}_2^0}, m_{\tilde{\chi}_1^0})}{\sum E_i \epsilon(m_{\tilde{\chi}_2^0}, m_{\tilde{\chi}_1^0}, E_i) \cdot \sigma(e^+e^- \to Z^0)(E_i) \cdot \mathcal{L}(E_i)},$$

where $N(m_{\tilde{\chi}_2^0}, m_{\tilde{\chi}_1^0})$ is the minimum number of events needed to set a 95% C.L. upper limit, $\epsilon(m_{\tilde{\chi}_2^0}, m_{\tilde{\chi}_1^0}, E_i)$ is the detection efficiency at energy $E_i$, and $\sigma(e^+e^- \to Z^0)(E_i) \cdot \mathcal{L}(E_i)$ gives the number of $Z^0$ decays in the sample at energy $E_i$. The contours of the upper limits for the $Z^0 \to \tilde{\chi}_2^0 \tilde{\chi}_1^0$ process are shown for two cases: $\tilde{\chi}_2^0 \to \tilde{\chi}_1^0 Z^+$ with 100% branching fraction (Fig. 4(a)), or $\tilde{\chi}_2^0 \to \tilde{\chi}_1^0 \gamma$ with 100% branching fraction (Fig. 4(b)). The Standard Model branching fractions were used for the $Z^+$ decay. The dark region in Fig. 4(a) corresponds to $\Delta M^0 < 3$ GeV/c², and was not considered in this analysis. The right-hand border of the triangular shape is the kinematic limit $m_{\tilde{\chi}_2^0} + m_{\tilde{\chi}_1^0} = m_{Z^0}$, where $m_{Z^0}$ is the $Z^0$ mass. One may infer, for example, from Fig. 4(a) that if $\Delta M^0 > 10$ GeV/c² and the decay of the $\tilde{\chi}_2^0$ occurs purely via a $Z^+$ boson, then the branching fraction of $Z^0 \to \tilde{\chi}_2^0 \tilde{\chi}_1^0$ is smaller than $20 \cdot 10^{-6}$ at the 95% C.L. independent of the neutralino masses. Similarly from Fig. 4(b) one can conclude that if $m_{\tilde{\chi}_2^0}/m_{\tilde{\chi}_1^0} > 1.2$ and the $\tilde{\chi}_2^0$ decay is purely radiative, then the branching fraction of $Z^0 \to \tilde{\chi}_2^0 \tilde{\chi}_1^0$ is smaller than $100 \cdot 10^{-6}$ at the 95% C.L., independent of the neutralino masses.

The results of the above searches can be interpreted within the framework of the MSSM where the physics of the gaugino-higgsino sector of the theory is completely determined by three parameters: $M_2$, the mass of the supersymmetric partner of the W-boson at the weak scale when it is assumed that all the gauginos have a common mass at the grand-unification scale; $\mu$, the mass coupling strength between the two Higgs superfields, and $\tan \beta$, the ratio of the vacuum expectation values of the two Higgs doublets. The scanned regions of the parameter space were $0 \leq M_2 \leq 1500$ GeV/c² and $-400 \leq \mu \leq 400$ GeV/c² for two values of $\tan \beta$: $\tan \beta = 1.5$, a small value interesting for infrared fixed-point predictions for the top quark [31], and $\tan \beta = 35$, approximately equal to the ratio of the top quark mass to the b quark mass favoured by Yukawa coupling unification at a large mass scale [32].

Two values were considered for the common mass scale of the sfermions, $m_0$: either $m_0 = 1000$ GeV/c² or the smallest $m_0$ consistent with present limits on the $\ell$ and $\nu$ masses, namely $m_\ell > 45.0$ GeV and $m_\nu > 41.8$ GeV [33]. Although a small $m_0$ enhances neutralino production at energies close to the $Z^0$ pole owing to constructive interference between s-channel and t-channel exchange diagrams, the decay of $\tilde{\chi}_2^0$ to $\tilde{\nu}\tilde{\nu}$, leading to unobserved final states, may be important for certain values of the other SUSY parameters, and thus may lead to less stringent limits. A careful consideration of both scenarios is therefore required.

Further constraints were imposed using experimental limits on the mass of the lightest chargino [34] and from limits on the excess in the width of the $Z^0$ ($\Delta \Gamma < 13.9$ MeV at the 95% C.L.) [35]. Points in the SUSY parameter space where either $m_{\tilde{\chi}_1^\pm} < 47$ GeV/c² provided $m_{\tilde{\chi}_1^\pm} < 41$ GeV/c² or $m_{\tilde{\chi}_1^\pm} < 45.2$ GeV/c², or where $\Gamma(Z^0 \to \tilde{\chi}_1^0 \tilde{\chi}_1^0) + \Gamma(Z^0 \to \tilde{\chi}_2^0 \tilde{\chi}_1^0) + \Gamma(Z^0 \to \tilde{\chi}_2^0 \tilde{\chi}_2^0) >$
The limits from the direct searches for $Z^0 \rightarrow \tilde{\chi}^0_2 \tilde{\chi}^0_1$ and $Z^0 \rightarrow \tilde{\chi}^0_2 \tilde{\chi}^0_2$ and the constraints from the $Z^0$ width and from the experimental bounds on the mass of the lightest chargino are combined to form exclusion regions in the $(m_{\tilde{\chi}^+_2}, m_{\tilde{\chi}^0_2})$ and $(\mu, M_2)$ planes, as shown in Figs. 4 and 5. The exclusion domain in the $(m_{\tilde{\chi}^0_2}, m_{\tilde{\chi}^0_1})$ plane is shown in Fig. 4(c) for $\tan \beta = 1.5$ and 4(d) for $\tan \beta = 35$. The regions bounded by the solid lines are excluded at the 95% C.L. The regions outside the dotted lines are not accessible within the scanned parameter space. The dashed line on the left side of each triangle is the $\Delta M^0 = 0$ line, which is accessible only via the $Z^0$ width constraint. The right dashed line is the kinematic limit for $\tilde{\chi}_2^0 \tilde{\chi}_1^0$ production ($m_{\tilde{\chi}_2^0}^2 + m_{\tilde{\chi}_1^0}^2 = m_{Z^0}$). Sensitivity to the region beyond this line comes only from the $Z^0$ width constraints. The following lower limits can be set on the neutralino masses: $m_{\tilde{\chi}_1^0} > 12.5$ GeV/c$^2$ and $m_{\tilde{\chi}_2^0} > 33.0$ GeV/c$^2$ for $\tan \beta = 1.5$, and $m_{\tilde{\chi}_1^0} > 26.0$ GeV/c$^2$ and $m_{\tilde{\chi}_2^0} > 51.5$ GeV/c$^2$ for $\tan \beta = 35$. Taking $m_0 = 1000$ GeV/c$^2$, the lower limit on the lightest neutralino becomes $m_{\tilde{\chi}_1^0} > 16.3$ GeV/c$^2$ for $\tan \beta = 1.5$.

The exclusion domain in the $(\mu, M_2)$ plane is shown in Fig. 5(a) for $\tan \beta = 1.5$ and in Fig. 5(b) for $\tan \beta = 35$. The region bounded by the solid lines is excluded at the 95% C.L. Note that the measurement of the $Z^0$ width allows the limits to be extended beyond the kinematically accessible region for $\tilde{\chi}_2^0 \tilde{\chi}_1^0$ production (represented by the dashed lines). Finally it should be noted that the case of a smaller $\tan \beta$ was also studied. We find that if $1 < \tan \beta < 1.3$, the $Z^0$ width cannot exclude neutralinos with a small $\Delta M^0$ and one cannot set a limit on the masses of neutralinos.

These results update a previous OPAL publication [36] and can be compared with other LEP publications [37].

6 Summary and Conclusions

We have analysed a data sample corresponding to an integrated luminosity of 160 pb$^{-1}$, collected around the $Z^0$ peak with the OPAL detector, to search for aoplanar jets or mono-jets motivated by supersymmetry and other theories. Two events remained after the selection, consistent with the background expectation of $2.30 \pm 0.43$ events from hadronic, $\tau^+\tau^-$ and four-fermion processes.

Limits have been placed on the production, in association with a $Z^*$, of invisible scalar particles and of visible scalars decaying to quarks. A massless invisible scalar is excluded if its production rate is more than $2.8 \cdot 10^{-4}$ that of the SM Higgs boson. A scalar particle whose
production rate is the same as the SM Higgs boson can be excluded at the 95% C.L. for masses up to 67.5 GeV/c² (or 60.8 GeV/c²) if it decays entirely into invisible final states (or entirely into quarks).

In placing limits on neutralino production, single photon events and information on the $Z^0$ width are also included in the analysis. At 95% C.L., lower limits on the lightest and next to lightest neutralino masses within the Minimal Supersymmetric Standard Model are set at 12.5 GeV/c² and 33.0 GeV/c² respectively for $\tan \beta > 1.5$. Taking $m_0=1000$ GeV/c², the lower limit on the lightest neutralino becomes $m_{\tilde{\chi}_1^0} > 16.3$ GeV/c².

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Figure 1: (a) $p_T$ vs. $M_{vis}/E_{c.m.}$ for di-jet data after the preselection cuts. The cut used to remove two-photon events is indicated. (b) Distribution of $p_T$ for $M_{vis}/E_{c.m.} < 0.27$ for di-jet data, compared with Monte Carlo. The two-photon contribution is shown shaded. The cut applied is indicated by an arrow. (c) Distribution of $\theta_{acop}$ for class A for data (points) compared with Monte Carlo. The full points and open histogram are before the $\theta_{acol}$ cut is made, and the open points and hatched histogram are after the $\theta_{acol}$ cut is applied. The dotted histogram illustrates the expected distribution for neutralino pair production with masses of $(m_{\chi_2}, m_{\chi_1})=(30,0)$ GeV/$c^2$. (d) Distribution of $\theta_{acop}$ for class B, using the same notation as (c).
Figure 2: (a) The scaled reconstructed mass, $M_{vis}/E_{c.m.}$, of the events in the mono-jet/di-jet search, after all cuts as described in the text. The events selected in data are shown as solid points, and the histogram shows backgrounds from multihadron (diagonal hatched), $\tau^{+}\tau^{-}$ (horizontal hatched) $\nu\bar{\nu}q\bar{q}$ (cross-hatched) and $e\nu q\bar{q}'$ (open). (b) The signals expected from Monte Carlo for a 60 GeV/$c^2$ visible scalar (open), a 70 GeV/$c^2$ invisible scalar (cross-hatched) and a pair of neutralinos with masses of $(m_{\tilde{\chi}_2^0},m_{\tilde{\chi}_1^0})=(30,0)$ GeV/$c^2$ (horizontal hatched). (c) Distribution of $x_T = 2E\sin\theta/E_{c.m.}$ for the 31 selected single photon events (points). The expected contributions from $\nu\bar{\nu}\gamma(\gamma)$ and $\ell^{+}\ell^{-}\gamma$ ($\ell = \mu, \tau$) are shown by the histograms; the non-$\nu\bar{\nu}\gamma(\gamma)$ contribution is hatched.
Figure 3: The 95% C.L. exclusion limits on the production rates of (a) a visible scalar decaying to quarks and (b) an invisibly decaying scalar.
Figure 4: Upper limits at 95\% C.L. on product branching ratios for neutralino production:
(a) BR(Z$^0$→$\tilde{\chi}_2^0\tilde{\chi}_1^0$)BR($\tilde{\chi}_2^0$→$\tilde{\chi}_1^0Z^+$). The curves show the contours corresponding to product branching ratios of 2, 3, 4, 5, 10, 20$\cdot$10$^{-6}$. (b) BR(Z$^0$→$\tilde{\chi}_2^0\tilde{\chi}_1^0$)BR($\tilde{\chi}_2^0$→$\tilde{\chi}_1^0\gamma$). The curves show the contours corresponding to product branching ratios of 1.2, 2, 3, 4, 5, 10, 100$\cdot$10$^{-6}$.

The results are interpreted in the framework of the MSSM in the ($m_{\tilde{\chi}_2^0}$,$m_{\tilde{\chi}_1^0}$) plane for (c) tan\(\beta\)=1.5 and (d) tan\(\beta\)=35.0. The regions bounded by the solid lines are excluded at the 95\% C.L. The regions outside the dotted lines are not accessible within the scanned parameter space. The dashed line on the left side of the triangle is the $\Delta M^0 = 0$ line which is accessible only via the Z$^0$ width constraint. The right dashed line is the kinematic boundary ($m_{\chi_1^0}+m_{\chi_0^0} = m_{Z^0}$). The region outside this line is also accessible only via the Z$^0$ width constraint. The shaded region in (c) is excluded for $m_0$=1000 GeV/c$^2$, but not for a light $m_0$. 
Figure 5: The exclusion domain in the \((M_2, \mu)\) plane in the framework of the MSSM for (a) \(\tan \beta = 1.5\) and (b) \(\tan \beta = 35\). The regions bounded by the solid lines are excluded at the 95\% C.L. The dashed lines represent the limits of the kinematically accessible region for \(\chi^0_2\chi^0_1\) production. The shaded region is excluded for \(m_0=1000\) GeV/c\(^2\), but not for a light \(m_0\).