Planet or Brown Dwarf? Inferring the Companion Mass in HD 100546 from the Wall Shape using Mid-Infrared Interferometry.

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ABSTRACT

Context. Giant planets form in protoplanetary disks while these disks are still gas-rich, and can reveal their presence through the annular gaps they carve out. HD 100546 is a gas-rich disk with a wide gap between between a radius of ~1 and 13 AU, possibly cleared out by a planetary companion or planetary system.

Aims. We want to identify the nature of the unseen companion near the far end of the disk gap.

Methods. We use mid-infrared interferometry at multiple baselines to constrain the curvature of the disk wall at the far end of the gap. We use 2D hydrodynamical simulations of embedded planets and brown dwarfs to estimate viscosity of the disk and the mass of a companion close to the disk wall.

Results. We find that the disk wall at the far end of the gap is not vertical, but rounded-off by a gradient in the surface density. Such a gradient can be reproduced in hydrodynamical simulations with a single, heavy companion (≥30...80 MJup) while the disk has viscosity of at least α ≥ 5 × 10⁻³. Taking into account the changes in the temperature structure after gap opening reduces the lower limit on the planet mass and disk viscosity to 20MJup and α = 2 × 10⁻³.

Conclusions. The object in the disk gap of HD 100546 that shapes the disk wall is most likely a 60α−1MJup brown dwarf, while the disk viscosity is estimated to be at least α = 2 × 10⁻³. The disk viscosity is an important factor in estimating planetary masses from disk morphologies: more viscous disks need heavier planets to open an equally deep gap.

Key words. Radiative transfer - hydrodynamics - planet-disk interactions - protoplanetary disks - Stars: individual: HD 100546 - turbulence

1. Introduction

Giant planets need to form before the gas in protoplanetary disks is dispersed, thus making some of these disks not only planet-forming, but most likely also planet-hosting. Current planet-finding techniques have difficulties in detecting planets around these young stars: transits are blocked from view by the disk, whereas radial velocity measurements are disturbed by variability of the stellar photosphere (Setiawan et al. 2008, Huelamo et al. 2008), though (interferometric) imaging has identified a few possible companions (Kraus & Ireland 2012, Quanz et al. 2013).

However, planets can also reveal themselves in an indirect way, through their dynamical impact on the protoplanetary disk (e.g. Lin & Papaloizou 1979, 1986). A gap carved by a single planet has a minimal impact on the SED, but could be identified by imaging of the disk (Steinacker & Henning 2003, Varnière et al. 2006, Wolf et al. 2007). Nonetheless, a class of so-called transitional disks have been identified on the basis of their low near-infrared excess, apparently caused by depleted inner regions (Strom et al. 1989, Muzerolle et al. 2004, Calvet et al. 2005). Long-wavelength imaging has confirmed that most of these indeed have enlarged inner holes or annular gaps (Brown et al. 2009, Andrews et al. 2011), their size suggestive that multiple planets must be responsible (Dodson-Robinson & Salvaterra 2011, Zhu et al. 2011), or an additional clearing mechanism is at work, such as dust filtration or grain growth (Zhu et al. 2013, Birnstiel et al. 2012). However, how these transitional disks manage to sustain a substantial accretion rate with a depleted inner region remains a mystery, as well as the underlying architecture of their planetary systems.

If present, the properties of an underlying planetary system may be inferred from the disk geometry. Giant planets will carve out deep and wide gaps in the gas and dust, and a whole suite of codes exists to study disk-planet interactions (see de Val-Borro et al. 2006 for a comparison of such codes). Comparing these results to observational constraints on the surface density profile allows to estimate the mass and location of a planet (e.g. Tatulli et al. 2011).

In this work, we will study the disk-planet interaction in the disk of HD 100546. It was identified by Bouwman et al. (2003) as a transitional disk on basis of its SED even before the term existed, with an estimated companion mass of ~ 10MJup. The gap was later confirmed using mid-infrared nulling interferometry (Liu et al. 2008), UV spectroscopy (Grady et al. 2005), near-infrared CO spectroscopy (Brittain et al. 2009, Van Der Plas et al. 2009) and mid-infrared
interferometry \cite{Panic2013}, all consistent with a gap outer radius in the range of 10 to 15 AU. The inner disk is depleted in dust by a few orders of magnitude \cite{Benisty2010,Mulders2011}, and is less than 0.7 AU in size \cite{Panic2012}. Hydrodynamical modelling of the surface density profile inferred from the SED by Tatulli et al. \cite{2011ApJ...730L..19T} yields a planet of at least one Jupiter mass at 8 AU. Recent interferometric imaging has revealed a (different) planetary candidate further out in the disk, at 70 AU \cite{Quanz2013}.

However, the surface density profile around the gap can also be studied using mid-infrared interferometric data, providing additional constraints on the nature of a (planetary) companion. Using inclined ring models, Panic et al. \cite{Panic2012} have shown that the mid-infrared visibilities could not be reproduced by a sudden jump in intensity at the location of the disk wall at 13 AU, but that the emission from the edge increases smoothly over a few AU. This may indicate that the surface density does not show a sharp increase at 13 AU leading to a vertical wall, but gradually increases with radius. In this case the optical depth - which determines the height of the disk surface - also increases smoothly with radius, producing a more rounded-off wall. In this paper, we will explore the observational appearance of such surface density profiles, and how they can be explained by the gravitational and hydrodynamic interaction between a disk and a planet.

Such rounded-off walls are a natural outcome of hydrodynamical models of disk-planet interaction, where the detailed shape of the radial surface density profile depends on planet mass, disk thickness and viscosity \cite{Crida2006,Lubow2006}. The mass of the planet will therefore be reflected in the shape of the disk wall, that can be constrained with MIDI, the mid-infrared interferometer on the Very Large Telescope. We will explain this in more detail in Section 2. Besides the planets mass, the visibility in the disk wall is a critical parameter in determining the gap shape.

We will use a 2D radiative transfer code to model both SED and mid-infrared visibilities to determine the shape of the surface density profile in the disk wall at the far end of the gap (Section 3). We then try to reproduce this surface density profile with a hydrodynamical code to constrain the planet mass and disk viscosity (Section 4). We will discuss the companion mass and robustness of our result in Section 5 and summarize our results in the conclusion.

2. Interferometric signature of a disk wall

The visibility versus baseline curve is a Fourier transform of the surface brightness profile. Therefore, the visibility curve of a continuous disk decreases monotonously with baseline (gray dotted line in figure 1), as contributions from different radii add up to a smooth curve. In this case, the visibility is a direct measure of the spatial extent of a source.

However, in a disk with a gap, the situation is much more complex. The material at the far end of the gap (‘disk wall’) intercepts a much larger fraction of the stellar light than in a continuous disk, creating a peak in the surface brightness at that location, (red line in figure 2 and 3). The flux contribution from this radius will then dominate over that of the other radii, both in the SED and visibilities. Its Bessel function will contribute more to the visibilities than those from other radii, resulting in the characteristic gap signature in the visibility curve, showing multiple minima (‘bounces’ or ‘nulls’) and maxima (‘sidelobes’) (Figure 1 red line).

The detailed shape of the visibility curve of a gapped disk depends on the structure of the disk wall: A vertical wall (defined as a step function in the surface density) will create a narrow peak in the surface brightness profile with a typical width of a few AU. This non-zero width is due to inclination and optical depth effects caused by the vertical structure. It has much more power in the sidelobes, making the gap structure visible at very long baselines (red lines in figure 1 and 3). If the surface density increases gradually over a few AU (Fig. 2 blue line), the optical depth will increase more slowly, giving a surface height in the disk wall that slowly increases with radius, round-
In this section we will constrain the shape of the surface density profile in the disk wall from the visibilities presented by Panić et al. (2012) and Leinert et al. (2004). To do so, we need to first calculate the density and temperature structure in the disk wall for a given surface density profile. Because the structure of a rounded disk wall can strongly deviate from that of a geometrically thin disk, this is a job especially well suited for 2D radiative transfer codes - also because the disk wall near the midplane is completely shadowed by the inner disk, while the upper part is fully illuminated. In addition, we need to calculate the vertical structure in the disk wall, which strongly deviates from that of a continuous disk due to radial and vertical temperature gradients.

We use MCMax (Min et al. 2009), a 2D radiative transfer code that self-consistently calculates the temperature and vertical density structure for a given surface density profile in an axisymmetric geometry. We assume the gas is in vertical hydrostatic equilibrium, and because the SED shows no sign of dust settling of small grains (Mulders et al. 2011), we assume the dust and gas distributions to be equal. The SED and visibilities are calculated using ray-tracing to compare them to the observations. We will use the SED fit with a vertical wall presented in Mulders et al. (2011) as a starting point, refine it using the constraints from Panić et al. (2012), and fit the SED and visibilities simultaneously to constrain the surface density in the disk wall. For completeness, all model parameters are displayed in Table 1.

To generate visibilities from the observed correlated fluxes, we need to divide them by an observed total flux. Because the total flux measured with MIDI is affected by flux losses from the MIDI slit (see Panić et al. 2012), we use the flux measured with ISO to generate visibilities. The larger field of view of ISO also includes more large-scale PAH emission, with narrow features around 7.9, 8.6 and 11.3 µm, which are inversely imprinted in the visibilities, but which we do not model. These visibilities, together with those presented by Leinert et al. (2004), are shown in Figure 5. We will use the position angle of 145° and inclination of 53° derived by Panić et al. (2012) to compute visibilities from our disk models.

3. Deriving the wall shape

In this section we will constrain the shape of the surface density profile in the disk wall from the visibilities presented by Panić et al. (2012) and Leinert et al. (2004). To do so, we need to first calculate the density and temperature structure in the disk wall for a given surface density profile. Because the structure of a rounded disk wall can strongly deviate from that of a geometrically thin disk, this is a job especially well suited for 2D radiative transfer codes - also because the disk wall near the midplane is completely shadowed by the inner disk, while the upper part is fully illuminated. In addition, we need to calculate the vertical structure in the disk wall, which strongly deviates from that of a continuous disk due to radial and vertical temperature gradients.

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3.1. Inner disk

As shown by Panić et al. (2012), the inner disk is – at least in the small dust grains probed by MIDI – very compact, < 0.7 AU. This is perhaps best illustrated by plotting the correlated flux on the 41 meter baseline into the SED of figure 4. This baseline probes scales of order ~2...3 AU, and therefore filters out most of the emission from the outer disk. The correlated flux seems consistent with the 1700 K blackbody emission from the inner rim, with only little additional flux from colder material. We place the inner rim at 0.25 AU, consistent with the near-infrared interferometric constraints from Benisty et al. (2010) and Tatulli et al. (2011). Because the temperature behind the inner rim at 0.25 AU drops off very rapidly with radius, we find that the inner disk can not extend further out than 0.3 AU (in small grains), unless the surface density power law is steeper than $r^{-1}$. This tiny inner disk...
is similar to that in the transitional disk T Cha (Olofsson et al. 2013). The normalization of the surface density ($\Sigma_{\text{inner}}$) is fitted to the near-infrared excess.

In addition, there is a weak feature apparent at 10 micron, though it is not clear whether this is a mineralogical feature in the inner disk, or due to the structure of the outer disk. The outer disk wall also contributes to the correlated flux and creates similar features – which we will discuss extensively in the next section. If we treat the observed feature strength as an upper limit to the real feature strength, the feature is too weak to be consistent with a rim made out of the same small amorphous silicate grains as the outer disk wall. Because the temperature of the inner rim is above the crystallisation temperature of silicates – and possibly also above its sublimation temperature – we use a composition of pure iron, which also fits the SED (Figure 4). We can mix in a few percent of silicates or corundum (FeAl$_2$O$_3$, which has a higher sublimation temperature) to fit the weak 10 micron feature in the correlated spectrum, but this is not required for a good fit to the visibilities and has no effect on the results presented in this paper.

### 3.2. A vertical wall

As explained in section 2, the presence of a disk wall creates structures in the visibility as a function of baseline, which will be reflected in the spectrally resolved visibilities as well (Fig. 5). This is most clearly seen in the 14.9 m baseline, where a bounce is present at 10.5 $\mu$m. Bounces are also present around 8.5 $\mu$m in the 15.8 and 16.0 m baselines. The longer baselines do not show such pronounced structures.


<table>
<thead>
<tr>
<th>Parameter</th>
<th>Value</th>
<th>Reference</th>
</tr>
</thead>
<tbody>
<tr>
<td>$T_{\text{eff}}$ [K]</td>
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<td>[1]</td>
</tr>
<tr>
<td>$L_*$ [$L_\odot$]</td>
<td>33</td>
<td>[1]</td>
</tr>
<tr>
<td>$M_*$ [$M_\odot$]</td>
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<td>[1]</td>
</tr>
<tr>
<td>$d$ [pc]</td>
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<td>[2]</td>
</tr>
<tr>
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<td>[3]</td>
</tr>
<tr>
<td>$r_{\text{out,inner}}$ [AU]</td>
<td>0.3</td>
<td>†</td>
</tr>
<tr>
<td>$r_{\text{out,outer}}$ [AU]</td>
<td>400</td>
<td>[4]</td>
</tr>
<tr>
<td>$r_{\text{exp}}$ [AU]</td>
<td>29</td>
<td>†</td>
</tr>
<tr>
<td>$M_{\text{dust}}$ [$M_\odot$]</td>
<td>$5 \times 10^{-3}$</td>
<td>†</td>
</tr>
<tr>
<td>Vertical structure</td>
<td>hydrostatic</td>
<td></td>
</tr>
<tr>
<td>$\Sigma_{\text{inner}}(r)$ [g/cm$^2$]</td>
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<td>†</td>
</tr>
<tr>
<td>$\Sigma_{\text{exp}}(r)$ [g/cm$^2$]</td>
<td>0.0004 (r/AU)$^{-1}$</td>
<td>†</td>
</tr>
<tr>
<td>$\Sigma_{\text{wall}}(r)$ [g/cm$^2$]</td>
<td>see Eq [1]</td>
<td></td>
</tr>
<tr>
<td>$\Sigma_{\text{outer}}(r)$ [g/cm$^2$]</td>
<td>0.2 (r/AU)$^{-1}$</td>
<td>†</td>
</tr>
<tr>
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<td>[5]</td>
</tr>
<tr>
<td>$a_{\max}$ [$\mu$m]</td>
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<td>[5]</td>
</tr>
<tr>
<td>Shape</td>
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<tr>
<td>Silicate fraction [%]</td>
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<td>†</td>
</tr>
<tr>
<td>Carbon fraction [%]</td>
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<td>†</td>
</tr>
<tr>
<td>$i$ [°]</td>
<td>53</td>
<td>[6]</td>
</tr>
<tr>
<td>PA</td>
<td>145</td>
<td>[6]</td>
</tr>
</tbody>
</table>

A disk model with a vertical wall at 14 AU can reproduce the location of these bounces at the shortest baselines (Fig 5 red lines). However, this model overestimates the visibilities at these baselines. In addition, the vertical wall model predicts structures at the 41 and 74 meter baselines that are not observed. To fit the visibilities at all baselines, we have to round off the disk wall as described in section 2. This reduces the power in the side-lobes, thus reducing the visibilities at the shortest baselines and smoothing out structures at the longer baselines.

#### 3.3. A rounded-off wall

We round off the disk wall by modifying its surface density power law, using the following function:

$$\Sigma_{\text{wall}}(r < r_{\text{exp}}) = \Sigma_{\text{outer}} r^{-1} \exp \left( -\frac{1 - r/r_{\text{exp}}}{w} \right)$$

$$\Sigma_{\text{disk}}(r \geq r_{\text{exp}}) = \Sigma_{\text{outer}} r^{-1}$$

where $\Sigma_{\text{outer}}$ is the normalisation constant for the outer disk surface density fitted to the SED, $r_{\text{exp}}$ is the radius where the drop-off of the surface density sets in, and $w$ is a measure of how round
the disk wall is. This function is essentially a Gaussian similar to the vertical scale height, but with a different exponent of 3 as in \[ w = \exp[-(r - r_0)^3 / \lambda^3] \]

such that \( w \) is the face density profile in the vicinity of the planet. We model the disk around an embedded planet’s orbit. \textit{Fargo} is a solver to the Navier-Stokes and continuity equations in a differentially rotating disk in vertical hydrostatic equilibrium. It speeds up these calculations by removing the average azimuthal velocity component from these equations at each radius and at each time-step.

Because we focus on the steady-state wall shape, it is not necessary to follow the global evolution of the whole disk as \textit{Tatulli et al.} (2011) have done. Instead, we focus on the surface density profile in the vicinity of the planet. We model the disk within a factor 5 in radius of the planet (i.e., 2 to 50 AU for a planet at 10 AU) far enough from the grid edges so that their location do not affect the shape of the surface density in the vicinity of the planet. The planetary candidate discovered by \textit{Quanz et al.} (2013) lies outside this grid, and — assuming it is on a circular orbit — is therefore located too far away to influence the gap structure. We use square grid cells on a logarithmic grid, 384 in the azimuthal direction, and prevent mass from leaking out at the inner edge of the grid.

The model set-up is based on our best-fit radiative transfer model to the SED and visibilities. We use a surface density power law of \( r^{-1}\) for the initial surface density, similar to that of the outer disk. We use a pressure scale height derived from the scale height profile of our radiative transfer simulation from within the disk gap, i.e., between 0.3 and ~13 AU. Because our radiative transfer model is not vertically isothermal, the scale height is defined as the height above the midplane where the pressure drops off by \( e^{-1/2}\). The pressure scale height in this regime is well-fitted by a power law of the form \[ H_p(r) = 0.025 \, \rho^{1/39} \]

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4. Deriving planet mass and disk viscosity

In this section, we will show how a planet can explain the observed shape of the disk wall. The micron-sized dust grains observed with MIDI are a good tracer of the gas: they are well-coupled to the gas (\textit{Mulders et al.} 2013, their section 4.2), unlike millimeter sized grains that tend to pile up near pressure bumps in the midplane (\textit{Paardekooper & Mellema} 2004, \textit{Pinilla et al.} 2012). Therefore, the inferred surface density of the dust is equal to that of the gas, which we will reproduce using planet-disk interactions.

4.1. Gap opening

A planet embedded in a disk opens a gap by exerting a torque on the disk, pushing material outside of its orbit outwards and material inside of it inwards. However, gas flows back into the gap due to pressure gradients and viscous spreading, which tends to close the gap. Therefore, the shape of the surface density around a planet depends on its mass, the disk viscosity and scale height (\textit{Crida et al.} 2006, \textit{Lubow & D’Angelo} 2006). In general, a heavier planet can carve out a deeper and wider gap, while a more viscous or thicker disk (higher pressure scale height) will reduce the gap width and depth.

4.2. Hydrodynamical model

We use the freely-available 2D hydrodynamical code \textit{Fargo} (\textit{Masset} 2000) to model the surface density density of the gas disk around an embedded planet’s orbit. \textit{Fargo} is a solver to the Navier-Stokes and continuity equations in a differentially rotating disk in vertical hydrostatic equilibrium. It speeds up these calculations by removing the average azimuthal velocity component from these equations at each radius and at each time-step.

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3 With the exception of the model represented by the dotted line in figure 6, which uses the maximum accretion efficiency as defined in \textit{Kley} (1999).
If the gap is not deep enough, its emission will fill the gap in the SED around 8 micron and will over predict all visibilities. Because the inner disk is already depleted by a factor of a hundred, the gap needs to be depleted by about a factor of about ten more (See figure 2), depending on the dust opacities. This minimum gap depth is shown with the dashed line in figure 7 and only models below this line have gaps that are deep enough. It shows that the disk viscosity is a crucial parameter in opening a disk gap: a Jupiter mass planet may open a deep gap in an invisible disk, but for the most viscous disks it requires a 80 Jupiter mass planet to keep the gap deep enough. In general, we find that the planet mass needs to be scaled with the square root of viscosity to achieve a given gap depth.

There are two regions in this diagram which have a wall shape consistent with our observations, \( w \sim 0.33...0.40 \). One region lies at low planetary masses (\(<5M_{\text{Jup}}\)) and high viscosities (\( \alpha > 2 \times 10^{-2} \)). Although consistent with the planet mass estimate of Tatulli et al. (2011), the higher viscosity acts against gap opening, and these gaps are nowhere near deep enough to be consistent with observations, even if the planet would be allowed to accrete. Another region lies at very high masses (30...80 \( M_{\text{Jup}} \)) and moderately high viscosities (\( \alpha = 5 \times 10^{-3} ... 5 \times 10^{-2} \)), which seems consistent with the observed gap depth, and puts the planet between 8 and 10 AU. Our best fit-model has a planet of 60 \( M_{\text{Jup}} \) at 10 AU and a viscosity of \( \alpha = 2 \times 10^{-2} \), and is shown in figure 7. The dependence of these results on the assumed temperature profile is discussed in Section 5.3.

These estimates of \( \alpha \) are consistent with that of Mulders et al. (2013), who also find a high turbulent mixing strength of \( \alpha_{\text{turb}} > 0.01 \) by looking at the degree of dust settling in the disk wall.

### 4.4. Results

The results of our parameter study are presented in figure 7, showing the width over which the surface density in the disk wall is rounded off (\( w \) from equation 1) as a function of planet mass and disk viscosity. A global trend is visible, where lower planet masses and disk viscosities produce more vertical walls (\( w \sim 0.2 \)), whereas rounder walls are found at higher values (\( w \sim 0.35 \)). This trend can be understood from a balance between viscous spreading and planetary torques: a high viscosity makes material flow inward smoothing the surface density profile, while a heavier planet mass allows the torques to act over a wider range, allowing for a shallower profile. However, for intermediate shapes there is no linear trend (\( w \sim 0.25...0.3 \)).
5. Discussion

5.1. Planet or brown dwarf?

The shape of the disk wall points to a companion about thirty Jupiter masses or heavier, with a best fit around 60 Jupiter masses. According to the IAU definition, this object would be a brown dwarf, rather than a planet, making HD100546 a misinterpreted binary system with a disk like CoKu Tau/4 (Ireland & Kraus 2008), rather than a transitional disk.

Binaries are common around main sequence A stars and Herbig Ae/Be stars, with fractions over 70% (e.g. Baines et al. 2006; Kouwenhoven et al. 2007). The inferred period of around 20 years is consistent with the peak in the period distribution of binaries around sun like stars (e.g. Zinnecker 1984; Raghavan et al. 2010). Whether a mass ratio of $q \sim 0.02$ is uncommon for binaries is not clear, as detection limits typically go to $q \sim 0.1$, but Wheelwright et al. (2010) note that the companion distribution of Herbig Ae/Be companions is skewed towards higher masses than the interstellar mass function. However, we note that the companion candidate recently discovered around HD 142527 by Biller et al. (2012) has a very similar mass and orbital properties. In addition, there seems to be a trend from direct imaging that A type stars posses heavier planets than less massive stars (Marois et al. 2008; Lagrange et al. 2010; Carson et al. 2013), a trend also seen in radial velocity surveys (Lovis & Mayor 2007).

Whether to call a companion a planet or a brown dwarf should depend on how it forms, not on its mass. Young stars are found with masses below the deuterium burning limit (e.g. Luhman et al. 2005), while core-accretion models predict that planets can also form above it (Mordasini et al. 2009). A better definition would involve the formation process of the companion, in a disk or like a single star. The current gas mass of the disk is uncertain due to lack of resolved millimeter observations, but estimated to be in the range 0.0005...0.01$M_\odot$ (Panić et al. 2012; Thi et al. 2011), and therefore much lighter than the planet, making it unlikely that the planet recently formed out of the disk.

Observational limits exist on the mass and location of a possible binary companions of HD 100546. Baines et al. (2006) report no detection in a spectroastrometric survey for binary companions, with a contrast limit of 6 magnitudes and an separation of 0.1", excluding a companion with spectral type earlier than M6. Also plotted are the best fit profile in the gap (H$_p(r) = 0.025 r^{1.39}$, dotted line) and that of a disk without a gap (H$_p(r) = 0.02 r^{1.32}$, dashed line). Because the radiative transfer model is not vertically isothermal, the scale height is defined as the height where the pressure drops off with a factor $e^{-1/2}$ with respect to the mid-plane.

5.2. Gap Width

The width of the gap from the hydrodynamical simulations, about 6 AU, is inconsistent with the derived size for the inner disk of less than an AU. The planet itself is heavier than the disk and should not migrate, allowing it to act as a barrier for material from the outer disk to reach the inner disk. We have neglected the global evolution of the disk, so it is possible that in reality, the inner disk drains onto the central star as in Tatulli et al. (2011). The near-infrared interferometric data used by the authors, however, does not directly constrain the outer radius of the inner disk, which they place at 4 AU. The MIDI data do require the inner disk to be much smaller than the 4 AU previously assumed (see also Panić et al. 2012). Therefore, an additional mechanism might be necessary for clearing the inner regions.

Additional planets closer to the star could explain the extent of the gap, depleting the inner regions (Dodson-Robinson & Salys 2011; Zhu et al. 2011). Because the torques on the disk are strongest close to a planet, we expect only the outermost planet in the gap to shape the disk wall. Another mechanism could be dust filtration at the outer edge, blocking dust particles from crossing the gap together with the gas and reducing the dust to gas ratio of the inner disk (Zhu et al. 2012). However, the high viscosities we infer are less favorable for trapping dust in the outer disk wall (Pinilla et al. 2012). In addition, grain growth could contribute to depleting the inner disk of small grains (Birnstiel et al. 2012). Resolved millimeter observations of the gap, such as can be delivered with the Atacama Large Millimeter Array, would be crucial to investigate this.

5.3. Pressure scale height

As mentioned in section 4.1, the disk thickness – set by the pressure scale height and thus by temperature – is an important factor in determining the wall shape because it controls how much material flows back into the gap. The pressure scale height is
an input parameter of Fargo, and remains fixed during the simulation. This is a highly idealized situation, and in reality, the scale height will change during gap opening when the disk wall heats up (Turner et al. 2012). This will, in turn, influence the gap structure, but coupling the hydrodynamical simulations to radiation transfer is far from trivial. In this section we will describe how this coupling may affect our results and suggest directions for future work.

Because we are looking for a steady state solution of the wall shape after many orbits, we can derive the scale height profile corresponding to this wall shape from our best-fit radiative transfer model to the SED and visibilities. This profile is shown in figure 8. In the region up to ∼12 AU, i.e., within the disk gap, the vertical optical depth is so low that the midplane is not shielded, increasing the temperature by a factor of two and the pressure scale height by about 50% with respect to a disk without a gap (dashed line, see also Turner et al. 2012). Between ∼12 and 30 AU, the gradual increase in optical depth starts shielding the midplane, leading to lower temperatures and scale height. Outside 30 AU, the scale height profile is close to that of a continuous disk.

In the parameter study, we have used a parameterized scale height of the form \( H_p(r) = 0.025 r^{1.39} \) (Fig. 8 dotted line). This parameterization describes the profile accurately up to ∼12 AU, i.e., in most of the region modelled with Fargo. In addition, in the region where the intensity profile peaks (see Fig. 3) and where our observations are most sensitive to, it is closer to the scale height of the best-fit radiative transfer model than that of a continuous disk. However, the slope of the scale height profile after the peak in intensity at ∼12 AU is very different. In a steady-state viscous disk without a gap, it is this slope that sets the surface density distribution (e.g., Andrews et al. 2009). To see how this assumption affects our results, we designed the following test.

We perform one iteration on the hydrodynamical structure of the disk, to take into account the change in temperature structure of the disk after gap opening. We start with a subset of the hydrodynamical models presented in the previous section, shown in Table 2 and indicated by triangles in figure 7. These models span the entire range of wall shapes, from steep to rounded-off, and were initially calculated using the parameterized scale height profile. For each wall shape \( w \), we calculate the temperature structure using our radiative transfer code, as described in section 3. The radial location of the wall depends – apart from on the planets location – also on the planet mass, because more massive planets carve out wider gaps. Therefore we adjust the location of the planet \( r_{pl} \) – and hence that of the disk wall \( r_{exp} \) (Eq. 1) – to make sure that the radial intensity profile peaks at 12-13 AU for each wall shape, as in figure 3. This is equivalent to fitting the SED (but not the visibilities), since that only depends on the wall location, not its shape.

From these temperature structures we can calculate the scale height profiles, similar to figure 8. We use these (non-parameterized) profiles to rerun the hydrodynamical simulations, and measure the new wall shapes of these iterated models using equation 1. If the resulting radial location of the wall differs from that of the radiative transfer simulation, we rerun the hydrodynamical simulation with the planet at a different radius, to make sure that the wall location between both simulations is self-consistent. The wall shapes and location before and after iteration are shown in Table 2.

<table>
<thead>
<tr>
<th>Model</th>
<th>before iteration</th>
<th>RT</th>
<th>after iteration</th>
</tr>
</thead>
<tbody>
<tr>
<td>( M_{pl} )</td>
<td>( \alpha )</td>
<td>( w )</td>
<td>( r_{exp} ) [AU]</td>
</tr>
<tr>
<td>2</td>
<td>( 10^{-4} )</td>
<td>0.17</td>
<td>1.6</td>
</tr>
<tr>
<td>5</td>
<td>( 5 \cdot 10^{-4} )</td>
<td>0.20</td>
<td>1.8</td>
</tr>
<tr>
<td>10</td>
<td>( 10^{-3} )</td>
<td>0.23</td>
<td>2.0</td>
</tr>
<tr>
<td>20</td>
<td>( 2 \cdot 10^{-3} )</td>
<td>0.26</td>
<td>2.3</td>
</tr>
<tr>
<td>40</td>
<td>( 10^{-2} )</td>
<td>0.35</td>
<td>2.9</td>
</tr>
<tr>
<td>60</td>
<td>( 2 \cdot 10^{-2} )</td>
<td>0.36</td>
<td>3.0</td>
</tr>
</tbody>
</table>

**Table 2.** Wall shape and location, before and after iterating on the temperature structure. The wall shape \( w \) and its location \( r_{exp} \) are defined in equation 1. The location of the planet \( r_{pl} \) follows from comparing the fitted wall location in the radiative transfer code \( r_{exp} \) (in column RT) to that of the hydrodynamical simulation. This subset of models is highlighted by triangles in the parameter study of figure 7.
cretion across the gap. Ideally, one would also take into account the 3D structure of the wall, though this might take a considerable computational effort due to the long integration times necessary to reach a steady state.

5.4. Gap eccentricity

Throughout this work, we have assumed azimuthal symmetry for the disk. However, towards the highest companion masses in our simulations, the gap starts to become eccentric (see also Casassus et al. 2012). In addition, the chromatic phases measured with MIDI also show indications for an asymmetric outer disk (Panić et al. 2012). Taking an azimuthal average over an eccentric gap can lead to a rounder surface density profile, however, we will show that this is not the effect we observe or measure in our simulations.

From a modelling point of view, making a gap eccentric contributes to the roundness measured from an azimuthally averaged surface density profile under certain conditions. For example, an elliptical gap ($e = 0.4$) with a vertical wall has an azimuthally averaged surface density profile that appears slightly rounded-off (we fit $w = 0.05$). This is much less round than the lowest roundness we measure in our simulations, which is $w = 0.17$ (for a circular gap). To investigate if the eccentricity may contribute to the inferred roundness we compare a radial cuts of the surface density profile to azimuthally averaged ones. An example is shown in figure 10 for our best-fit model, which has an eccentricity of $e \approx 0.6$. The radial cut is significantly more noisy – motivating the use of azimuthally averaged profiles – but the shape of the wall does not change significantly, though it is radially displaced by a few AU.

From an observational perspective, the eccentricity of the gap does not change the roundness of the disk wall as inferred from the visibilities. Each visibility is measured along a particular baseline orientation, and is therefore sensitive to the radial gradient of the surface density along that baseline, without any azimuthal averaging. The radial displacement of the disk wall due to eccentricity is measurable, but unfortunately this effect is degenerate with disk inclination and position angle, increasing the uncertainties on these parameters.

It may be possible to constrain the eccentricity from the chromatic phases, hence providing an extra diagnostic on the companion mass, though this will require in-depth modeling of a more extended data set.

6. Conclusion

We have studied the gap shape in the disk of HD 100546. By comparing 2D radiative transfer models to the mid-infrared interferometric data presented in Panić et al. (2012), we find that:

- The disk wall at the far end of the gap is not vertical, but rounded off over a significant radial range. This shape can be explained by a gradual increase in the surface density over a range of $\sim 10$ to $\sim 25$ AU, creating a broad peak in the surface brightness profile around 12 AU that was also seen by Panić et al. (2012).
- The inner dust disk is extremely small in small grains. We confirm the upper limit on its size of 0.7 AU found by Panić et al. (2012), and use our 2D radiative transfer model to constrain it even further, with no measurable contribution outside of 0.3 AU.
- The roundness or spatial extent of a disk wall can be inferred from spectrally resolved visibilities beyond the first null.

By comparing these results to hydrodynamical simulations of planet-disk interactions, we find that:

- The shape of the surface density profile in the disk wall of HD 100546 can be explained by a massive planet ($\gtrsim 30\ldots80$ $M_{Jup}$) in a viscous ($\alpha \gtrsim 5 \cdot 10^{-6}$) disk between 8 and 10 AU.
- The roundness of a disk wall in hydrodynamical simulations depends on the temperature structure in the disk wall: iterating on the scale height profile using radiative transfer changes this roundness.
- The disk viscosity is a crucial parameter in estimating planet masses from a derived surface density profile, acting against gap opening by the planet. For a given depth, the gap-opening mass of a planet increases with the square root of the disks viscosity.
- The effect of a single planet is not enough to explain the full width of the disk gap in HD 100546. Either an additional clearing mechanism, or a multi-planet system is required to explain its extent.
- The object shaping the disk wall is most likely a brown dwarf, suggesting HD100546 might be a binary system rather than a transitional disk object.

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References


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