THREE-DIMENSIONAL CHARACTER OF SEMIMETALLIC InAs–GaSb SUPERLATTICES

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High-field, far-infrared magneto-absorption experiments are performed in semimetallic InAs–GaSb superlattices. The spectra exhibit extensive oscillations of cyclotron resonance and interband absorptions from valence to conduction subbands. Transitions at both the center and the boundary of the superlattice zone are observed, from which the width of the ground conduction subband is obtained, demonstrating directly its three-dimensional character.

A CHARACTERISTIC FEATURE of the InAs–GaSb superlattice is the occurrence of a semiconductor-semimetal transition when the InAs layer thickness becomes ~ 100 Å. This transition arises from the peculiar band alignment of the basic materials; the bottom of the InAs conduction band being 150 meV below the top of the GaSb valence band. Another inherent feature of this superlattice is associated with the extremely light electron mass of InAs. Its de Broglie wavelength is so long that, even for GaSb layer thickness in excess of 100 Å, there is considerable interaction between electrons in successive InAs layers which leads to conduction subbands with a substantial width in the range of tens of millivolts. This subband width manifests the quasi-three-dimensional character of a superlattice, as opposed to the situation arising from a simple quantum size effect.

The band structure of such a semimetallic superlattice is schematically shown in Fig. 1(a) along $k_z$, where $z$ is the direction perpendicular to the layers. The ground conduction subband $E_1$ is below the ground valence subband $H_1$. The conduction states are mainly localized in the InAs layers, and the valence states in the GaSb layers [1, 2]. The width of $E_1$ is here $\Delta E_1$ but that of $H_1$ is essentially zero [2, 3]. In the semimetallic samples, electrons transfer from $H_1$ to $E_1$, namely from GaSb to InAs, and the Fermi level $E_F$ is close to $H_1$.

Under magnetic fields, both $E_1$ and $H_1$ exhibit a series of Landau levels, which move upward and downward, respectively, with an increase in the field. Clearly, each Landau level of $H_1$ gives rise to a single peak in the density of states. The $E_1$ subband, on the other hand, being flat at the superlattice zone center, $k_z = 0$, and the zone boundary, $k_z = \pm \pi/d$, where $d$ is the superlattice periodicity, results in a doublet or two peaks in the density of states for each Landau level as shown in Fig. 1(b). If the selection rules for interband transitions are taken to be [4] $\Delta k_z = 0$ and $\Delta N = 0$, where $N$ is the Landau level index, two sets of transitions are thus possible at these two extremal points. Note that such interband transitions can occur because the electron and hole wavefunctions overlap.

We wish to present in this communication far-infrared magneto-absorption experiments in semimetallic InAs–GaSb superlattices, similar to those reported earlier in establishing the negative energy gaps [4]. With the use of a high magnetic field and an optically pumped laser to provide a large number of infrared wavelengths, we have observed extensive transitions associated with both cyclotron resonance and interband absorptions with Landau indices covering the range of $N = 1$ to 7. These results not only substantiated the semimetallic property of the superlattice but provided accurate determinations of the subband energies of $E_1$ and $H_1$ at $k_z = 0$. What is more significant is the observation of the transition between Landau levels at $k_z = \pm \pi/d$. The width of the $E_1$ subband has for the first time been

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Table 1. Thickness of the InAs (d1) and GaSb (d2) layers for samples S1 and S2. Also given are the experimental and theoretical values of E1, H1 and ΔE

<table>
<thead>
<tr>
<th>Samples</th>
<th>d1 (Å)</th>
<th>d2 (Å)</th>
<th>Theory (LCAO)</th>
<th>Experiment</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td></td>
<td></td>
<td>E1 (meV) ΔE1</td>
<td>E1 (meV) ΔE1</td>
</tr>
<tr>
<td>S1</td>
<td>120</td>
<td>80</td>
<td>87.5 21</td>
<td>100 ± 15</td>
</tr>
<tr>
<td>S2</td>
<td>200</td>
<td>100</td>
<td>64.5 16</td>
<td>70 ± 10</td>
</tr>
</tbody>
</table>

Fig. 1. (a) Schematic band structure of a semimetallic InAs–GaSb superlattice along kx. The dashed curves are without magnetic field, the solid curves are the corresponding Landau levels under magnetic field, and EF is the Fermi level. Transitions noted 1, 2 correspond to transitions at kx = 0 from H1 Landau levels up to E1 Landau levels with the same index, namely N = 1, 2. Those noted 0', 1' correspond to similar transitions at kx = π/d, with N = 0, 1. (b) Density of states associated with the E1 and H1 subbands under magnetic field. The hatched area corresponds to states occupied by electrons.

measured experimentally, which indicates directly that the electron system in a superlattice possesses a three-dimensional character, deviating from strict two-dimensionality.

The samples (S1 and S2) used here were grown [1] by molecular-beam epitaxy on (100) GaSb substrates, the total thickness of the superlattice being typically ~2 μm. The thicknesses of the InAs and GaSb layers are given in Table 1 for both samples. Experimentally, the FIR transmission of these superlattices is studied at fixed photon energies as a function of the magnetic field B. The infrared radiation is propagating parallel to B (Faraday configuration), which is applied perpendicular to the plane of the layers. The field was provided by a Bitter magnet and could be varied continuously from 0 to 20 T. Several FIR wavelengths were generated using an optically pumped FIR laser with CH3OH as the active medium (λ = 1217, 699, 570, 471, 394, 294, 254, 233, 203, 193, 170, 118, 96 and 70 μm). The transmission signal was measured with a Ge bolometer cooled at liquid helium temperature, and normalized to the incident radiation intensity with a reference signal detected with a Golay cell to eliminate fluctuations of laser instabilities.

Typical transmission spectra obtained at liquid helium temperature are presented in Fig. 2 for sample S1, where it can be seen that, for each infrared wavelength, the transmission signal as a function of B exhibits several minima. In Fig. 3 are presented the infrared energy positions of the transmission minima (or absorption maxima) vs. B. As shown below from theoretical analyses, the energies corresponding to the transmission minima depend almost linearly on B. Extrapolation to zero field results in hν = 0 for the line marked CR in Fig. 3(a), an energy of −39 meV for the family of lines...
Fig. 3. Position of the transmission minima (see Fig. 2) as a function of the infrared photon energy and magnetic field \( B \) (crosses and full dots). The solid lines correspond to theoretical fits using the model presented in the text. The inset shows schematically the geometry of the experiment.

designated 1, 2, 3, . . . in Figs. 3(a) and 3(b), and an energy of \(-16\) meV for the single line which is denoted as \( 0' \) in the same figures. The CR line is interpreted as being due to electron cyclotron resonance, i.e. to transitions from the last filled to the first empty Landau level of \( E_1 \). The curves which converge to the most negative energy are attributed to interband transitions from \( H_1 \) to \( E_1 \) Landau levels at \( k_x = 0 \), such as those noted 1 and 2 in Fig. 1(a). The \( 0' \) line is also attributed to similar interband transitions, but it occurs at \( k_x = \pi/d \) as illustrated in Fig. 1(a). These interpretations in terms of both cyclotron resonance and interband transitions are consistent with those reported earlier [4]. The observations of additional transitions associated with the 1 and \( 0' \) branches are made possible by the application of high fields in the present experiments.

Quantitatively the \( E_1 \) and \( H_1 \) Landau levels are calculated as were done previously [4, 5], taking into account the InAs conduction band non-parabolicity on the basis of the two-band \( k \cdot p \) model due to Kane [6]. For the \( E_1 \) subband one obtains for the \( N \)th Landau level:

\[
E_{1,N} = -\frac{E_G}{2} + \left( \frac{E_G}{2} + E_G D_N \right)^{1/2}
\]  
(1)

with \( D_N = (N + 1/2)\hbar\omega_c + E_1(1 + E_1/E_G) \) and \( \omega_c = eB/m_e^* \) where \( E_G \) and \( m_e^* \) are respectively the band gap and band edge mass of bulk InAs. For the \( H_1, N \) Landau level, we take simply \( H_{1,N} = H_1 - (N + 1/2)\hbar\omega_c \), with \( \omega_c = eB/m_h^* \) where \( m_h^* \) is the GaSb heavy hole effective mass. All the energies used here are measured from the bulk InAs conduction band edge.

For electron cyclotron resonance transitions, \( h\nu = E_{1,N+1} - E_{1,N} \), where \( N \) is such that \( E_{1,N} \) is below, and \( E_{1,N+1} \) above, the Fermi level \( E_F \). Interband transitions occurring at \( k_x = 0 \) from \( H_1 \) Landau levels up to \( E_1 \) Landau levels correspond to \( h\nu = E_{1,N} - H_{1,N} \), taking also here \( E_F = H_1 \) and the same selection rules as in [4]. Fits of our experimental data to this theoretical model are shown in Fig. 3 for sample S1, with \( m_e^* = 0.023 m_0 \), \( E_G = 410 \) meV and \( m_h^* = 0.33 m_0 \) [7]. The agreement between experiment and theory is quite good and, from these fits, we obtain the values of \( E_1 \) and \( H_1 \) at \( B = 0 \) which are listed [8] in Table 1. Similar studies were done in sample S2, and the corresponding values of these parameters are also given in Table 1. We can, in addition, determine the superlattice electron cyclotron mass \( m_e^* \) from the CR data, which is found to be [8] \( 0.0385 m_0 \) and \( 0.0375 m_0 \) in samples S1 and S2, respectively, with an uncertainty of \( \pm 0.0015 m_0 \).

Having established the values of \( E_1 \) and \( H_1 \), we can calculate the transition energies at \( k_x = \pi/d \) from the same theoretical model, replacing \( E_1 \) by \( E_1 + \Delta E_1 \) in equation (1). Figure 3 shows the results fitted to the data points from which the Landau index is identified, \( N = 0' \), and the bandwidth is obtained, \( \Delta E_1 = 23 \) meV. This value together with that obtained from sample S2 is also listed in Table 1. To observe the transition at \( k_x = \pi/d \) requires that the subband broadening from
scattering be smaller than the subband width itself. This is borne out from the scattering time of $\sim 5 \times 10^{-13}$ sec as estimated from the cyclotron resonance linewidth, which corresponds to a level broadening of $\sim 1.2$ meV. That transitions associated with higher Landau indices at this zone boundary are not observed experimentally can be understood from considerations of wavefunction overlap between electrons and holes [9]. For a given energy, the $E_2$ component at $k_z = \pi/d$ is higher than that at $k_z = 0$ by the amount of $\Delta E_1$. This brings the former closer to the valence band edge of GaSb as such its associated electron wavefunction is more localized in InAs. For a given magnetic field, transitions at $\pi/d$ are expected to be weaker than at 0, so that they can be resolved only in regions where transitions at $k_z = 0$ are not present. It is clear from Table 1, where calculated values of $E_1$, $H_1$ and $\Delta E_1$ by the LCAO method are also included, that the experimental and theoretical results compare quite favorably in all cases.

The systematic deviation around 8 T of the data points from the calculated curve for the $N = 1$ transition, as can be seen in Fig. 3, is not understood at present. This may be due to polaron effects, which have been observed for interband transitions [10]. The effects become important at magnetic field values when the energy separation between the $N = 0$ and the $N = 1$ Landau levels, for example, approaches the longitudinal optical phonon energy. That the LO-phonon energy of InAs (and GaSb) is [7] about 30 meV is consistent with our data. Recent calculations [11] have shown that the magneto-optical anomalies arising from electron–phonon interactions are considerably enhanced in superlattices.

To conclude, we have observed in semimetallic InAs–GaSb superlattices cyclotron resonance and interband transitions at $k_z = 0$, from Landau levels of the ground valence subband $H_1$ up to those of the ground conduction subband $E_1$. We have obtained extensive experimental data, corroborating earlier results reported previously [4]. In addition, we have determined the width $\Delta E_1$ of the ground conduction subband, demonstrating directly the quasi-three-dimensional character of these superlattices. Finally, we have obtained from these investigations values of $E_1$, $H_1$ and $\Delta E_1$ which compare favorably with those calculated by the LCAO method [2].

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REFERENCES
1. For a recent review see, for example, L.L. Chang & L. Esaki, Surf. Sci. 98, 70 (1980).
3. Note that $H_1$ corresponds to heavy holes (see, for example, [11]).
8. The values of $E_1$, $H_1$ and $m^*$ obtained here are somewhat different from those reported in [4]. This is due to different values of the InAs band gap used in the theoretical fits. Indeed, the fits shown in [4] were done with a gap of 420 meV, not 410 meV as erroneously written in the text.