A POMDP Model of Eye-Hand Coordination

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Abstract
This paper presents a generative model of eye-hand coordination. We use numerical optimization to solve for the joint behavior of an eye and two hands, deriving a predicted motion pattern from first principles, without imposing heuristics. We model the planar scene as a POMDP with 17 continuous state dimensions. Belief-space optimization is facilitated by using a nominal-belief heuristic, whereby we assume (during planning) that the maximum likelihood observation is always obtained. Since a globally-optimal solution for such a high-dimensional domain is computationally intractable, we employ local optimization in the belief domain. By solving for a locally-optimal plan through belief space, we generate a motion pattern of mutual coordination between hands and eye: the eye’s saccades disambiguate the scene in a task-relevant manner, and the hands’ motions anticipate the eye’s saccades. Finally, the model is validated through a behavioral experiment, in which human subjects perform the same eye-hand coordination task. We show how simulation is congruent with the experimental results.

1 Introduction
Eye-hand coordination is an integral part of many human activities, and has been the subject of scientific inquiry for more than a century. This domain poses an interesting challenge of motor intelligence: the uncertainty inherent to the world’s state requires active disambiguation; with foveal vision being a limited resource, effective behavior requires task-dependent allocation of information-gathering activity (gaze shift) and goal-directed behavior (hand reaching).

When trying to predict the eye’s motion, a common null hypothesis is to assume the gaze is directed to visually-salient features of the scene (Koch and Ullman 1985). However, here we consider tasks whose goal is the motion of the hand, with the eye playing a supportive role. In this case, the assumption that only image heuristics (such as saliency) account for the eye’s movement seems unlikely. The top-down effects of the motor task on visual behavior are an active area of study (Peters and Itti 2008; Rothkopf, Ballard, and Hayhoe 2007). Here we step away from neuroscientific investigation of visual processing, and abstract the eye’s effect

as a localized reduction in observation noise (section 3.2). This allows us to take a broader perspective on tasks which require coordination of information-seeking behaviors.

Todorov and Jordan (2002) propose the paradigm of optimal control as a framework for the study of motor coordination, and normative models (Körding 2007) harness simulation and numerical optimization for the study of neural mechanisms. Algorithms of optimal control often rely on the principle of certainty equivalence (Stengel 1994), which posits a separation between estimation and control: given an estimate of the current state of the world, the best action can be identified by considering a deterministic, fully-observable system in the same state. This separation allows for efficient computation, because optimal control can focus only on the deterministic system, and estimation can be safely ignored during motion planning. However, this separation does not hold in tasks which involve information-seeking behavior.

In order to capture the coupling between perception and action inherent to eye-hand coordination, we model this domain as a continuous-state partially-observable Markov decision processes (POMDP) (Sondik 1971; Kaelbling, Littman, and Cassandra 1998). The POMDP framework is designed to tackle domains with state uncertainty, and allows us to consider goal-directed actions and task-relevant information-pickup in a single optimization problem. The continuous POMDP model is described in section 3. High-dimensional, continuous POMDPs are notoriously hard to solve; here we use a deterministic belief update heuristic, described in section 2.

The domain of eye-hand coordination exhibits a large degree of task-specific behavioral diversity (Carpenter 1977) — some circumstances elicit the use of saccades, while others elicit smooth pursuit. This is a modeling challenge, because we must allow for the emergence of a variety of possible solutions, depending on the specific instantiation of task parameters. Our POMDP model meets this requirement, as different parameter settings generate different motion patterns. In section 4 we discuss the role of the various parameters in shaping the resulting behavior.

Our model finds an optimal motion pattern of the hands and the eye, allowing for the emergence of coordination from first principles, without imposing heuristics. In order to test the model, we present a behavioral experiment in
which human subjects perform the same eye-hand coordination task. The experiment and results are described in section 5; we find that simulation and experimental results are mostly congruent, demonstrating the validity of the model.

2 Solving high-dimensional, continuous POMDPs

In POMDP terminology, the agent is said to occupy a belief state, which is a distribution over all possible states, representing the agent’s ambiguous sense of the world. For the most part, the POMDP literature focuses on finding globally-optimal solutions for discrete domains. Previous studies of continuous POMDPs (Porta et al. 2006; Brunskill et al. 2008; Brooks 2009) focus on finding a globally-optimal solution for domains with only one or two dimensions. Several recent studies (Prentice and Roy 2009; Erez and Smart 2010; Miller, Harris, and Chong 2009) propose an alternative approach to continuous POMDP optimization — finding the optimal behavior by planning deterministic trajectories through belief-space. In this paper, we use the Nominal-Belief heuristic (Miller, Harris, and Chong 2009), replacing the stochastic observation with its maximum-likelihood counterpart (Erez and Smart 2010) during planning. The resulting belief dynamics are deterministic, and therefore amenable to efficient optimization algorithms. However, since planning takes place in the belief domain, the optimization still accounts for the state’s ambiguity (as this information is represented by the various belief states). Therefore, the resulting behavior strikes a balance between information-seeking and goal-directed action, despite the marginalization of the stochastic processes.

2.1 Definitions

Formally speaking, we consider a discrete-time POMDP defined by a tuple \( \langle S, A, Z, T, O, R, N \rangle \), where: \( S, A \) and \( Z \) are the state space, action space and observation space, respectively; \( T(s', s, a) = \Pr (s' | s, a) \) is a transition function describing the probability of the next state given the current state and action; \( \Omega(z, s, a) = \Pr (z | s, a) \) is the observation function, describing the probability of an observation given the current state and action; and \( R(s, a) \) is a reward function, and a terminal reward \( R^N (s) \). In this paper we consider an undiscounted optimality criterion, where the agent’s goal is to maximize the expected cumulative reward within a fixed time horizon of \( N \) time steps.

The belief state \( b \in B \) is a probability distribution over \( S \), where \( b(s) \) is the likelihood of the true state being \( s \) at time \( t \). Ignoring the effect of feedback control, the reward associated with a belief is simply the expected value over this state distribution:

\[
R^t (b, a) = \mathbb{E}_s [R^t (s, a)] .
\]  

(1)

Given the current belief \( b \), an action \( a \) and observation \( z \), the updated belief \( \hat{b} \) can be calculated by applying Bayes’s rule. However, in the continuous case \( B \) is infinite-dimensional, and therefore the belief update must be approximated by some estimation filter.

2.2 The deterministic belief update heuristic

We study continuous stochastic dynamics of the form \( ds = f(s, a)dt + q(s, a)d\zeta \), where \( \zeta \) represents continuous-time Brownian motion. For a given state \( s \) and action \( a \), integrating this continuous dynamics over a small time-step \( \tau \) results in a normal distribution over the next state \( s' \):

\[
T(s', s, a) = \mathcal{N}(s'|F(s, a), Q(s, a)),
\]

where the mean is propagated with the Euler integration

\[
F(s, a) = s + \tau f(s, a),
\]

(2)

and the covariance \( Q = \tau q^T q \) is a time-scaling of the continuous stochastic process \( q d\zeta \).

Similarly, we focus on observation distributions of the form \( \Omega(z, s, a) = \mathcal{N}(z | w(s), W(s, a)) \), where \( w \) is a deterministic observation function, and \( W \) describes how the current state and action affect the observation noise.

Given a Gaussian prior on the initial state, we approximate the infinite-dimensional \( b \) by a single Gaussian: \( \hat{b}(s) = \mathcal{N}(s | \Sigma, \hat{\Sigma}) \), where the covariance \( \hat{\Sigma} \) belongs to the space of symmetric, positive-semidefinite matrices \( \mathcal{M} \subset \mathbb{R}^{nxn} \). Therefore, the belief space \( \hat{B} \) is parameterized in this case by the product space \( \nu \in S \times \mathcal{M} \). In the limit of \( \tau \rightarrow 0 \), and given a Gaussian prior, this approximation is accurate.\(^1\)

In order to approximate the belief update, we use the Extended Kalman Filter (EKF) (Stengel 1994). Given the current belief \( \hat{b} \), action \( a \) and observation \( z \), we calculate the partial derivatives of the dynamics and the observation functions around \( \hat{s} : w_s = \partial w / \partial s \) and \( F_s = \partial F / \partial s \). We find the uncorrected estimation uncertainty \( H = F_s \Sigma F_s^T + Q(\hat{s}, a) \) and calculate the new mean \( \hat{s}' \) by the innovation process:

\[
\hat{s}' = F(\hat{s}, a) - K(z - w(\hat{s})),
\]

(3)

where \( K = Hw_s(w_s^T Hw_s + W(\hat{s}, a))^{-1} \) is the Kalman gain. Finally, the new covariance \( \Sigma' \) is given by:

\[
\Psi(\hat{s}, \Sigma, a) = H - Hw_s(w_s^T Hw_s + W(\hat{s}, a))^{-1} w_s^T H^T .
\]

(4)

The deterministic belief update is obtained by taking the expectation of equations (3) and (4) with respect to the observation variable \( z \). Since equation (3) is linear in \( z \), the expectation operator replaces \( z \) with its mean \( w(\hat{s}) \), causing the second term of equation (3) to vanish. Therefore, the maximum-likelihood estimate of the next belief’s mean is reduced to the deterministic dynamics (2). By virtue of the EKF being a first-order filter, the calculation in (4) is independent of \( z \), and so the next belief’s covariance is the same, regardless of the value of \( z \). In summary, the maximum-likelihood estimate for the next belief is formed by combining (2) and (4): \( \hat{b}'(s) = \mathcal{N}(s | F(\hat{s}, a), \Psi(\hat{s}, \Sigma, a)) \).

2.3 Planning in the belief domain

The belief update heuristic of the previous section (together with equation 1) define a problem of deterministic optimal control in a high-dimensional continuous space,

\(^1\)Note that this single-Gaussian approximation fails when the domain includes discontinuities and unilateral constraints (e.g., joint limit constraints, or confining walls); in such cases, a different formulation of the belief is needed (Erez and Smart 2010).
with non-linear dynamics and non-quadratic reward. To find a locally-optimal solution, we may use trajectory optimization; here we use Differential Dynamic Programming (DDP), a second-order algorithm that has been successfully applied to high-dimensional, non-linear control domains (Abbeel and Ng 2005; Tassa, Erez, and Smart 2008).

3 A POMDP model of eye-hand coordination

We model the position of the gaze target in the frontal plane, as well as the position of the hands’ end-effectors in that plane. In addition, the model’s state includes the (a priori unknown) planar positions of a target and four obstacles. The agent’s task is to guide both hands to the target while passing between a pair of obstacles, using the eye’s gaze to locally disambiguate portions of the scene (figure 4.2). By solving for an optimal motion plan, we generate a coordinated movement of hands and eye through the scene. The model and the resulting motion are best illustrated by a short movie, available at youtube.com/?v=PxvLIaoLn2o.

3.1 State, action, and transition function

The system’s state is the concatenation of the planar positions of the agent’s state and the environment’s state. The agent has kinematic control of gaze fixation point \( s_e \in \mathbb{R}^2 \) and two hands \( (s_{h_1}, s_{h_2}) \in \mathbb{R}^2 \); the agent’s state also includes a scalar time-lag variable \( \sigma_k \), which measures the time from the last saccade (section 3.2). The environment’s state specifies the positions of the target \( s_T \) and obstacles \((s_{b_i}, i = 1 \ldots 4)\). This leads to a 17-dimensional state space.

The state update is subject to process noise whose magnitude is constant in time but varies between the elements of the scene. For example, the state update equation for the target position is:

\[
s'_{T} = s_T + \sigma c \xi,
\]

with \( \xi \) being a two-element vector of zero-mean normally-distributed random variables with unit variance (same equation holds for \( s_{h_i} \), the state dimensions describing the positions of the obstacles). The parameter \( \sigma \) scales the process noise for the target and obstacles (see discussion in section 4.2).

The agent controls six continuous action variables, specifying the displacement of the hands and eye at every time step. For example, the state update equation for the hand’s position is:

\[
s'_{h_i} = s_{h_i} + a_{h_i} + \sigma h \xi,
\]

where \( \sigma h \) is a model parameter that sets the magnitude of the process noise affecting the hand; the same equation holds for \( s_{h_2} \) and \( s_{h} \), and their corresponding controls. We eliminate any uncertainty in the eye’s position by not subjecting it to process noise \( \sigma e = 0 \).

It is known that the brain’s processing of visual information is impaired (even if not completely inhibited) during a saccade. Furthermore, it has been shown (Thorpe, Fize, and Marlot 1996) that even after the eye’s gaze settles on the new target, it takes some time before visual information is available for some tasks. We model this effect with an auxiliary state variable \( s_k \), which measures the time elapsed from the last saccade. This variable integrates linearly when the eye’s velocity is zero, and becomes very low otherwise:

\[
s'_{k} = \tau + \frac{s_k}{1 + \alpha \| a_e \|},
\]

where \( \tau \) is the time-step length, and \( \alpha \) is some large coefficient (we use \( \alpha = 1000 \)). Like the eye’s position, this auxiliary variable is also not subject to any process noise, and therefore needs no estimation.

3.2 Observation

In a POMDP, the agent receives stochastic observations, through which it infers the true state of the system. Here, the agent may observe the state of all the scene’s elements, and the observation of every element’s position is randomly drawn from a normal distribution centered at the true underlying value; the agent has accurate observation of the eye’s position, as well as the time since the last saccade.

The covariance of the observation of each scene element depends on its position relative to the eye’s gaze. Let \( d_e = \| s_e - s_e \| \) be the Euclidean (planar) distance between a scene element and the eye’s gaze point \( * \) standing for either a hand, a target or an obstacle), and let \( g(d) \) be a function that scales the width of this element’s observation distribution; this function models foveated vision, so it is low around \( d = 0 \), and high farther away. We chose to model \( g \) as a sigmoid: given a width parameter \( \eta \) and a slope parameter \( l \), we look at the scaled distance

\[
\tilde{d}(s_e, s_e) = \frac{\| s_e - s_e \| - \eta}{l_d},
\]

and compute:

\[
g(\tilde{d}) = \sigma_o \left( 0.5 + \frac{\tilde{d}}{2\sqrt{d^2 + 1}} \right),
\]

with \( \sigma_o \) being the maximal observation covariance due to peripheral vision (see discussion in section 4). The width of the human fovea is about 2 degrees; in our experimental setup, this translates to 7% of the scene’s width, and so we set \( \eta = 0.035 \), and \( l_d = 0.005 \).

Modeling post-saccadic perceptual delay. In order to model the time delay due to processing of visual information, we added a term to the observation’s covariance that is sigmoidal in the elapsed time since the last saccade. We scale the elapsed time \( s_k \); \( t = (\mu - s_k)/l_k \), and compute

\[
k(s_k) = \alpha \left( 0.5 + \frac{t}{2\sqrt{t^2 + 1}} \right).
\]

We set \( \mu = 150 \text{ms} \) and \( l_k = 30 \text{ms} \) following Thorpe, Fize, and Marlot (1996), and \( \alpha \) is some large coefficient (we use \( \alpha = 1000 \)). Therefore, the observation’s covariance remains high for the first 120 ms after a saccade; at 150 ms this term drops, allowing the elements within the fovea to be observed accurately. Put together, the distribution of the observation for any scene element \( * \) (target or obstacles) is:

\[
\omega(\alpha_v | s_e, s_e, s_k) = \mathcal{N} \left( s_e, l_2 \cdot (k(s_k) + g(\tilde{d}(s_e, s_e)) \right)
\]
Proprioception. Proprioception is an independent channel of observation for the hands’ positions. We model this by bounding from above the covariance of the hands’ observation (as given by equation (8)) by a fixed value $\sigma_p$, the observation noise of proprioceptive observations. Therefore, the distribution of observations for the hands is:

$$\omega(s_e | s_s, s_c, s_b) = \mathcal{N}(s_e, I_2 \cdot \max(\sigma_p, k(s_e)) + g(d(s_e, s_c)))$$

(9)

3.3 The reward function

The reward function has two parts: running reward and terminal reward. The terminal reward is a penalty (cost) that is quadratic in the distance of the hands from the target:

$$R(s) = c_T (\|s_{h_1} - s_T\|^2 + \|s_{h_2} - s_T\|^2).$$

The running reward has two cost terms:

$$R(s, a) = -c_b \sum_{i=1}^{2} \sum_{j=1}^{4} \delta(s_{h_i}, s_{b_j}) - a^T M a$$

(10)

where $\delta$ is the delta function penalizing collision between hand and obstacle, and the quadratic action cost is given by the second term, with $M$ being a diagonal matrix assigning weight 1 to the hands’ displacement, and 0.01 to the eye’s displacement.

The only non-quadratic term is the obstacle cost. In a deterministic system, there is no delta-function, as the hand might pass at epsilon distance from the obstacle. However, since we plan in belief space, we use the belief cost function (1). The obstacle-related belief cost is the expectation of this delta-function under the normal distribution describing the joint uncertainty in the positions of the hand and the obstacle. Therefore, the belief-cost due to the obstacles is a Gaussian, which can be computed in closed form.

4 Exploring the model’s behavioral diversity

As mentioned in section 1, the domain of eye-hand coordination exhibits a diverse array of behaviors, and a candidate model should allow for an equally-diverse array of solutions. Our model employs three categories of parameters: the coefficients of the cost function, the coefficients describing the process noise, and parameters that determine the state-dependent observation noise. In this section, we discuss the model’s parameters, and the behavioral diversity they enable.

4.1 The cost function parameters

Our simulations suggest that the cost parameters are simple to choose, as the wrong value often leads to absurd behavior: for example, if the target cost parameter $c_T$ is not big enough compared to the hands’ action cost, the hands do not reach the target; increasing the target cost fixes the problem, and increasing it even more makes no difference (because the residual is already zero). The obstacle cost parameter $c_b$ leads to interesting behavioral diversity — when it is very big (relative to the hand action cost), the hands increase their velocity as they pass between the obstacles, and if it is very small, the hands choose a shorter path that gets dangerously close to the obstacle. Such behaviors are conceivable in certain scenarios, but the human subjects in our experiment (section 5) exhibited neither.

4.2 Process noise

While the observation noise is state-dependent, the process noise in equation (2) is constant. Two values need to be determined — $\sigma_b$, the process noise associated with the hands, and $\sigma_e$, the process noise associated with the static elements of the scene (target and obstacles). When the hands are not subject to process noise ($\sigma_b = 0$), the eye only looks at the obstacles, and when the static scene elements are not subject to noise ($\sigma_e = 0$), the eye’s gaze shifts preemptively (before the hand reaches the obstacles), as one glance is enough to perfectly and permanently disambiguate their position.

In contrast, when the hands are subject to a significant process noise, the eye performs smooth pursuit, following each hand along its path as it approaches the obstacles. This allows the agent to be certain of the hand’s position at the mission-critical moment, when it is near the obstacles. Similarly, applying some process noise to the static scene elements causes the eye’s gaze to remain fixed on the obstacles until the hand passed through the obstacle pair, so as to ensure that no uncertainty accumulates before the hand reaches the obstacle.

Another two parameters of behavioral relevance are $\sigma_p$ (the maximal observation covariance of the hands’ positions) and $\sigma_o$ (the maximal observation covariance of the static scene elements), appearing in equations (8) and (9). When the first is small, no smooth pursuit will emerge, as the agent has a reliable source of information of the hands’ positions. When the second is small, saccades will be inhibited, as peripheral vision provides observations that are good enough.

5 Comparing the model’s solution to human subjects’ behavior

In order to conflate simulation results with human motor behavior, we tested six subjects in an eye-hand coordination task. Subjects were equipped with a game controller consisting of two thumbsticks to move a left and right virtual hand in a two-dimensional scene projected on a large screen. Subjects were asked to move each virtual hand through a pair of obstacles and reach a common goal within 3 seconds. The position of the two gates changed at every trial, randomly rotating between 12 different arrangements (each scene was repeated thirty times). The scene was presented to the subjects at a field-of-view of 45 degrees. Before each trial, subjects had to fixate at the center of the screen. No instructions were given regarding eye movements during a trial. Eye movements were recorded using the double magnetic induction method (Bour et al. 1984).

The first row of panels in figure 1 shows the results of subject S5 for a single trial. The blue and red line represents the subject’s trajectory of the left and right virtual hand, respectively. Gaze fixations are represented by green dots. The obstacles and target are depicted as black squares and a star,
respectively. The subsequent panels show a snapshot of the subject’s behavior at the onset of a new fixation. The first panel shows that the subject initially fixates at the center of the screen, with the hands at the starting position at the bottom of the scene. After 348 ms, the gaze saccades toward the right obstacle pair to assist the right hand in passing the obstacles (second panel). Before the right hand has reached the obstacle pair, gaze already jumps to the left obstacle pair at \( t = 854 \) ms (third panel). Note that this jump consists of one large saccade (from the right to the left gate) followed by a small, so-called correction saccade which is a well-known phenomenon for large saccades (Carpenter 1977). When the right hand approached the gate, a saccade is made toward a new location between the left gate and target (fourth panel) to guide both hands to the final goal, which was reached after 1.85 s from the beginning of the trial (last panel).

In the second row with panels, we plotted the hand trajectories and gaze trajectory as solved by the POMDP model. In order to compare the subject’s behavior with the model predictions, we set the model’s time limit equal to the subject’s trial duration. The first panel shows the initial state of gaze and hand position. After 74 ms, gaze saccades to the right gate (second panel), which is earlier than the corresponding saccade of subject S5. Since the initial fixation was not preceded by a saccade, the model did not include a post-saccadic perceptual delay during the initial fixation, resulting in a short fixation duration. When the right hand reached the gate at \( t = 817 \) ms (third panel), gaze moved to the left gate to guide the left hand through the obstacles. At \( t = 1411 \) ms the left hand had passed the gate and gaze jumps toward the target (fourth panel) and stayed there until the end of the trial (last panel). Note that the timing of the second and third saccade is well in accordance with the subject’s behavior.

We compared the predictions of the POMDP model with the experimental results of all trials and subjects on three criteria: (1) the order and location of fixations, (2) the trajectory of left and right hand, and (3) the relative timing of gaze and hands. Figure 2 shows the trial average of all subjects for the same scene. The variability in hand position is represented by the shaded area (one standard deviation). Clusters of gaze fixations are represented by colored ellipses (two standard deviations). For this scene, the subjects’ order of fixations (i.e., initial fixation, right obstacle pair, left obstacle pair, target) is in agreement with the model predictions. However, when the gates were located close to the initial fixation location at the center of the screen, or when the gates were sufficiently large, subjects do not direct their gaze to the relevant obstacles in the scene, but instead use their peripheral vision to perform the task. This behavior was found in two of the twelve scenes (17%), except for subject S3, which showed this behavior in nine scenes (75%).

The subjects fixate approximately between an obstacle pair, in agreement with the model predictions. The precise fixation location differs slightly between subject and model. Some subjects make slightly smaller saccades than the model. This undershoot is a known phenomenon (Carpenter 1977) and is thought to reflect properties of the human saccadic system, which were not included in our model. In 62% of the scenes, the predicted fixation locations lay within the cluster of measured gaze fixations.

The right hand’s trajectory predicted by the model matches the measured path for subjects S3, S5 and S6 almost perfectly, whereas the left hand shows a slightly curved trajectory. For the other subjects, both hands reach the target via a more curved trajectory than predicted by the model. For all subjects and scenes, the predicted hand trajectory was located within one standard deviation of the measured hand trajectories for 72% of the time. A control experiment revealed that even in absence of any obstacles, subjects tend to move the hands in an inward-curved trajectory whereas the model predicts a straight line (i.e., the shortest path).
that case subjects fixate at positions in the middle, between both hands. A plausible explanation for this behavior is that subjects use their peripheral vision to guide both hands to the target, relying on the heightened capacity to perceive motion through peripheral vision (McKee and Nakayama 1984) (a feature which we did not try to model).

In addition to correctly predicting the spatial location of eye fixations and hand positions, the model also predicts the timing of gaze relative to hand position. This is illustrated in figure 1, which shows that gaze jumps from the initial gaze position at the start of each trial to the right obstacle pair, and from there to the left pair of obstacles after 0.9 s, when the right hand approached the obstacles. After another 0.6 s, gaze jumps from the left pair of obstacles to the target. By tuning the value of the parameter describing the obstacles’ process noise, we recover this temporal pattern in our model.

6 Conclusion

This paper presents a POMDP model of hand-eye coordination, and demonstrates that the optimal solution is congruent with the behavior of human subjects performing the same task even with minimal assumptions on the actual parametric forms and numerical values. However, it is important to note that we do not argue for the biological plausibility of the computational techniques; instead, this normative model may allow us to test our understanding of what (we believe) the brain “should” do.

Experiments of eye-hand coordination tasks yield a diverse set of behaviors, according to the particular experimental setup. Our model captures this feature, as it can produce qualitatively-different behavior when the values of these parameters change (as explained in section 4). Here, we demonstrate how the model can be congruent with one particular experimental setup; this naturally guided our choice of parameter values to a particular region.

References


