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High-temperature quantum Hall effect in finite gapped HgTe quantum wells

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We report on the observation of the quantum Hall effect at high temperatures in HgTe quantum wells with a finite band gap and a thickness below and above the critical thickness \( d_c \), that separates a conventional semiconductor from a two-dimensional topological insulator. At high carrier concentrations, we observe a quantized Hall conductivity up to 60 K with energy gaps between Landau levels of the order of 25 meV, in good agreement with the Landau level spectrum obtained from \( k \cdot p \) calculations. Using the scaling approach for the plateau-plateau transition at \( ν = 2 \rightarrow 1 \), we find the scaling coefficient \( ν_s = 0.45 ± 0.04 \) to be consistent with the universality of scaling theory, and we do not find signs of increased electron-phonon interaction to alter the scaling even at these elevated temperatures. Comparing the high-temperature limit of the quantized Hall resistance in HgTe quantum wells with a finite band gap with room-temperature experiment in graphene, we find that the energy gaps at the breakdown of the quantization exceed the thermal energy by the same order of magnitude.

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I. INTRODUCTION

The quantum Hall effect (QHE) [1] is a universal phenomenon that occurs when two-dimensional (2D) metallic systems are subjected to a perpendicular magnetic field. The magnetic field condensates the constant density of states into discrete Landau levels (LLs), which are separated by energy gaps \( ΔE \). When the Fermi energy \( E_F \) is in the gapped regions, the Hall conductance is quantized to integer multiples of \( e^2/h \), where \( h \) is Planck’s constant and \( e \) is the electron charge. This quantization has been observed in a wide range of semiconductor heterostructures, such as GaAs/AlGaAs, which was discovered by Laughlin [12]. In this paper, we investigate the high-temperature QHE in HgTe quantum wells with a finite band gap, where the QHE can be explained on the basis of localized and extended states that occur in the spectrum of impurity-broadened LLs [5,6]. In the center of the LLs, extended states exist that lead to a metallic behavior, while in the vicinity of localized states the bulk behavior is insulating. Although bulk states in between LLs are localized, dissipationless 1D edge channels are formed that dominate the transport properties in this regime. The consequence is a quantized Hall resistance accompanied by a vanishing longitudinal resistance. To observe this quantization, low temperatures (\( T \lesssim 10 \) K) are, in general, necessary to prevent thermal occupation of extended states in higher LLs. This limit has recently been overcome by a new class of systems that exhibit a linear dispersion. One of the most famous systems with a linear dispersion is the zero-gap semiconductor graphene, where the QHE has been observed at room temperature using a magnetic field of 29 T [7]. The observation of a quantized resistance at these high temperatures is based on the peculiar nature of charge-carrier quantization in a magnetic field, which is given by \( E_N = ±v_F \sqrt{2eℏBN} \), where \( v_F \) is the Fermi velocity, \( B \) is the magnetic field, \( h \) is the reduced Planck constant, and \( N \) is the Landau level index. For a typical Fermi velocity in graphene of \( v_F \approx 10^6 \) m/s, the energy gap between the lowest LL (\( N = 0 \)) and the first excited one (\( N = 1 \)) is \( ΔE \approx 195 \) meV at 29 T, exceeding the thermal energy at room temperature (\( k_BT \approx 25 \) meV) by almost one order of magnitude. Unlike in conventional systems, where the second subband is relatively close to the first, the second subband in graphene is not occupied up to very high temperatures, thereby supporting the condition for the observation of the QHE.

Similar conditions are present in HgTe quantum wells (QWs). A remarkable property of these so-called type-III QWs is that by tuning the quantum-well thickness \( d_{QW} \) above a critical thickness \( d_c = 6.3 \) nm, a transition from a semiconductor to a topological insulator (TI) is achieved [8]. At \( d_{QW} = d_c \), the conduction and valence bands touch each other, which leads to a single-valley gapless 2D Dirac-fermion system [9,10], and the QHE can be observed up to nitrogen temperatures [11]. In contrast to conventional semiconductors, HgTe QWs with a finite (bulk) band gap also have a highly nonparabolic dispersion, approaching a linear energy-momentum relation at finite \( k \), and they are described by the Dirac Hamiltonian [12]. The presence of a small but finite bulk band gap affects the LL dispersion and consequently the energy gaps in the LL spectrum compared to zero-gap systems [11].

In this paper, we investigate the high-temperature QH regime of HgTe quantum wells with a finite band gap with \( d_{QW} \) below and above \( d_c \). The combination of the dispersion relation, leading to charge carriers that obey the Dirac equation, with a second subband that is more than 100 meV above \( E_F \) makes our system ideal to study the QHE up to high temperatures with only one occupied subband.

II. SAMPLE CHARACTERIZATION

Our samples were grown by molecular beam epitaxy (MBE) in the [001] direction, and they were structured into Hall bars of dimensions \( L \times W \) of (600 \( × \) 200) and (30 \( × \) 10) \( μm^2 \), respectively. The quantum-well thicknesses of the two samples are \( d_{QW} = 5.9 \) nm (sample 1) and \( d_{QW} = 11 \) nm (sample 2), respectively. The calculated energy dispersions \( E(k) \) using a

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$\mathbf{k} \cdot \mathbf{p}$ model with an $8 \times 8$ Kane Hamiltonian [13] are shown in Figs. 1(a) and 1(b), where the first ($E_1$) and second ($E_2$) electron- and holelike ($H_1$ and $H_2$) subbands are plotted. Both systems possess a finite bulk band gap, and while sample 1 is a trivial semiconductor with a direct band gap of 12 meV, sample 2 is a 2D TI with an indirect band gap of 3 meV and an inverted band ordering giving rise to helical edge states at zero magnetic field [8,14]. This difference can be seen experimentally when tuning the Fermi energy $E_F$ with the top gate through the band gap while measuring the low-temperature ($T = 4.2$ K) longitudinal resistance $R_{xx}$ [see Figs. 1(c) and 1(d)]. Compared to the expected insulating behavior of sample 1 ($R_{xx} \approx 1 \mathrm{M}\Omega$), sample 2 has a significantly reduced resistance ($R_{xx} \approx 27 \mathrm{k}\Omega$) when $E_F$ is in the bulk band gap. This value is above the expected quantization for a 2D TI due to the formation of charge puddles in larger samples ($L \gtrsim 1 \mu m$), which can lead to backscattering [8,15,16] as well as the thermal activation of bulk carriers over the narrow band gap of 3 meV.

To study the QHE at high temperatures, we tune the Fermi energy $E_F$ deep into the conduction band where the dispersion is nearly linear. We achieve this by applying gate voltages of $V_{g,1} = 1$ V (sample 1) and $V_{g,2} = 1.4$ V (sample 2), which yields almost equal charge-carrier concentrations of $n_{1,1} = 4.59 \times 10^{11}$ cm$^{-2}$ and $n_{1,2} = 4.66 \times 10^{11}$ cm$^{-2}$, respectively. In this regime, our samples have mobilities of $\mu_1 = 67,800$ cm$^2$/V s and $\mu_2 = 82,400$ cm$^2$/V s, as determined from the zero-field resistivity. For both carrier concentrations, $E_F$ is more than 100 meV below the second electronic subband $E_2$, as can be seen in Figs. 1(a) and 1(b), from which we exclude thermal excitation of higher subbands contributing to transport in our experiment. The nearly linear dispersion in combination with a single occupied subband up to high energies are perfect conditions for the observation of the QHE at high temperatures.

For the experiment, we used standard four-terminal lock-in techniques and carefully chose our excitation to prevent heating of the samples. We used a $^3\mathrm{He}$ system to access a temperature range from 0.3 to 80 K in magnetic fields up to 30 T.

III. RESULTS AND DISCUSSION

The main results of our measurements are summarized in Fig. 2, where we present data that represent the overall behavior of our samples. Figures 2(a) and 2(b) show measurements of $R_{xx}$ of the two samples at constant charge-carrier concentrations and different temperatures. From additional measurements of $R_{xy}$ and the known geometry of the Hall bars, we determine the corresponding resistivities $\rho_{xx}$ and $\rho_{xy}$ from which we calculate the Hall conductivities $\sigma_{xx} = \rho_{xx}/(\rho_{xx}^2 + \rho_{xy}^2)$ plotted in Figs. 2(c) and 2(d). The insets show a magnification of the region around filling factor $v = 1$, where $v$ is defined as $v = n_i/n_L = n_i h/e B$, where $n_i$ is the charge-carrier concentration and $n_L$ is the degeneracy of the Landau levels.

We observe pronounced Shubnikov–de Haas oscillations in the displayed temperature range accompanied by plateaus in $\sigma_{xx}$ at $v = 1$ up to 60 and 46.5 K for samples 1 and 2, respectively. From the temperature dependence of the minima in $R_{xx}$, we extract the activation gaps $\Delta E$ between adjacent LLs with a Fermi-Dirac fit, and we compare the results with theoretical calculations of the Landau level dispersions shown in Figs. 3(a) and 3(b). In contrast to the LL fan chart of the 5.9 nm quantum well where all LLs show a positive dispersion, the inverted sample exhibits a LL crossing of one electronlike and one holelike level at around 8 T, which is the hallmark of a 2D inverted system [9].

The experimentally and theoretically obtained energy gaps are in reasonably good agreement, as shown in Figs. 3(c) and 3(d), and the overall behavior of the sample is well described by our $\mathbf{k} \cdot \mathbf{p}$ model. While the calculations yield energy gaps of $\Delta E_{1,\nu=1} \approx 46$ meV at $B \approx 20$ T and $\Delta E_{2,\nu=1} \approx 39$ meV at $B \approx 21$ T for samples 1 and 2, respectively, the extracted activation energies are slightly smaller and determined to be $\Delta E_{1,\nu=1} \approx (42 \pm 1.5)$ meV and $\Delta E_{2,\nu=1} \approx (34 \pm 2.9)$ meV. This small difference can mainly be attributed to the simplicity of our calculations, where we assume an infinitely small LL width. In reality, scattering from impurities or dopants leads to a broadening of the LLs, resulting in smaller energy gaps than our theoretical estimates, as observed. Despite the broadened LLs, the energy gap for the lowest filling factor still exceeds the thermal energy at room temperature of $k_B T \approx 25$ meV. We note furthermore that the energy gaps are larger than in conventional 2D systems, but they are still almost an order of magnitude smaller than in graphene due to a smaller Fermi velocity $(\approx 5 \times 10^6$ m/s) [17–19] compared to graphene but with a large Zeeman splitting $\Delta E_Z = g^* \mu_B B$ of...
FIG. 2. Measurements of the longitudinal resistances $R_{xx}$ of the (a) 5.9-nm-thick and (b) 11-nm-thick QWs at constant electron densities $n_{s,1} = 4.59 \times 10^{11} \text{ cm}^{-2}$ and $n_{s,2} = 4.66 \times 10^{11} \text{ cm}^{-2}$ at different temperatures. The black arrows mark the position in magnetic field of filling factors $\nu = 1$ and 2. In (c) and (d), the corresponding Hall conductivities $\sigma_{xy}$ are shown. The insets show a magnification of $\sigma_{xy}$ at filling factor 1.

FIG. 3. Calculated LL dispersion for (a) a 5.9-nm-thick and (b) an 11-nm-thick HgTe quantum well. The position of the Fermi energy $E_F$ is marked by the orange line. In (c) and (d), the corresponding experimentally extracted and theoretical calculated energy gaps are plotted for the lowest four filling factors.

the LLs in HgTe, where $g^*$ is the effective Landé factor and $\mu_B$ is the Bohr magneton. Therefore, the energy gap for the filling factor $\nu = 1$ is $\Delta E_{\nu=1} = \nu v_F \sqrt{\hbar e B} - \Delta E_Z$, and for $\nu = 2$ it is $\Delta E_{\nu=2} = \Delta E_Z$. At the Fermi energy, the Landau-level dispersions are very similar, and $g^* \simeq 20$ for both samples. A further increase in charge-carrier densities and magnetic-field range would, due to the nature of the LL dispersion, only slightly increase the energy gaps, and the maximum $\Delta E$ remains in the order of 50 meV. Thus, the temperature range where we still observe the QHE is largely reduced compared to graphene. Interestingly, the ratio of the energy gap $\Delta E$ to the thermal energy where $\sigma_{xy}$ is still quantized is comparable to the ratio of $\Delta E/k_B T \approx 8$ measured in graphene.

Although our system has large energy gaps between adjacent LLs, a necessary but not sufficient condition for the observation of QHE at high temperatures, we need to consider the localization effects of charge carriers. In disordered systems, charge carriers in the tails of the LLs are localized, while extended states exist only at the center of each LL. Because of these localized states, the Fermi energy moves smoothly through the energy gap, and a plateaulike Hall resistance is observed in the measurements. A widely used approach to study localization is to investigate the scaling behavior of the unique insulator-metal transition, which occurs when the energy crosses from localized to delocalized states [20,21]. Within the finite-size scaling theory [20], it is possible to observe scaling behavior in the temperature dependence of the slope of the plateau transition; specifically, the maximum of the derivative of the Hall resistance scales with the temperature as

$$\left(\frac{dR_{xy}}{dB}\right)_{\text{max}} \propto T^{-\kappa},$$

with $\kappa = p/2\gamma$, with $\gamma$ the critical localization length exponent and $p$ the scattering exponent. The same power-law...
dependence holds for the temperature dependence of the full width at half-maximum (FWHM) of the $R_{xx}$ dependence holds for the temperature dependence of the full

From the slope of the linear fits, $\gamma$ for this transition as the minima quickly rise above zero).

From this we are able to access a wide temperature range in which we still observe a quantized Hall interaction, which we expect to be present above 10 K and $\nu = 0 \rightarrow 1$, in good agreement with the value $\nu = 0.45 \pm 0.04$ determined from the noninverted sample with $d_{QW} = 5.9 \text{ nm}$, in excellent agreement with the universal scaling theory. An interesting subject for further theoretical and experimental studies is whether the high-temperature limit of the QHE is influenced by a difference in localization strength and can be related to sample disorder or mobility $\mu$.

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\[ \kappa \propto -\frac{1}{2} \]
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