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Testing with Functions as Specifications

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Abstract. Although computer systems penetrate all facets of society, the software running those systems may contain many errors. Producing high quality software appears to be difficult and very expensive. Even determining the quality of software is not easy. Testing is by far the most used way to estimate the quality of software. Testing itself is not easy and time consuming.

In order to reduce the costs and increase the quality and speed of testing, testing should be automated itself. An automatic specification based test tool generates test data, executes the associated tests, and makes a fully automatically verdict based on a formal specification. Advantages of this approach are that one specifies properties instead of instances of these properties, test data are derived automatically instead of manually, the tests performed are always up to date with the current specification, and automatic testing is fast and accurate.

We will show that functions in a functional programming language can be used very well to model properties. One branch of the automatic test system Gast handles logical properties relating function arguments and results of a single function call. The other branch of Gast handles specifications of systems with an internal state.

1 Introduction

Testing is still by far the most used method to judge the quality of software. Human testing of software is error-prone, dull, and expensive. Systems are becoming larger and more complex, and hence harder to test. Moreover, the time to market should be reduced, which limits the time for testing. Hence, many approaches to automatic software testing are proposed and used.

Most test systems execute a fixed number of human specified tests. These specified tests are specified either in code, as in JUnit [1], or by a capture and playback tool. We focus on automatic test systems that generate test cases based on a formal specification, e.g. [2]. Instead of specifying a fixed number of fixed values and the expected response, one specifies a relation between input and output that holds for all arguments. Apart from generating the test cases, the test system also executes the tests, and makes a verdict based on the test results.

Advantages of generating test cases from the specification are that a change of specification does not invalidate the test script: it is generated from the updated
specification. Increasing the number of tests in order to improve the confidence just requires the change of a parameter.

In [3–6] it is shown that a functional programming language, as used by the test tool Gast, is an excellent carrier for the formal specifications needed. Gast is able to handle two kind of specifications: logical properties about a (combination of) functions, and specifications of reactive systems by Extended State Machines, ESMs. The reactive systems are specified by a, potential infinite and nondeterministic, state transition function. Those specifications can be partial.

The quality of the test is dependent on the quality of the specification. Obviously, aspects that are not specified cannot be tested by a system that generates tests based on the specification. Experience shows that writing formal specifications is a very useful activity on its own. Most inaccuracies and misconceptions in the requirements are discovered during the construction of the specification.

Nevertheless, experience shows that a significant number of issues raised during testing is caused by inaccuracies in the specification. A better specification increases the speed of testing the product and improves the value of the test results. One can validate the specification to see if it captures the informal requirements correctly. This is a human activity that can be supported by tools. On the other hand one can also verify the consistency of the formal specification. This is usually done by inspections, or by verifying properties of the formal specification using a model checker or theorem prover. Especially for specifications that are heavily data dependent, model checkers have troubles with automatic verification.

In this paper we show that consistency properties of ESM-specifications can also be tested fully automatically using the other branch of our test tool Gast. Advantages of this lightweight and effective method to improve the quality of specifications are that it does not require the transformation of specifications, errors are reported in terms of the original model, and last-but-not-least it works also very well for models that strongly dependent on sophisticated data types. The limitation is that the test results are usually weaker than the results of a complete formal verification (if it is possible).

The testing of individual functions is discussed in section 2. The specification and testing of reactive systems in the next section. The testing of specifications in order to verify their quality, in discussed in section 4. Finally, we will discuss related work and draw conclusions.

2 Testing Functions

The relation between input and output of a single function can be conveniently specified in predicate logic. As an example we consider a function that takes a string and a character as argument and yields a sorted list of the indices for all occurrences of the given character in the string, e.g. \texttt{indices("A test", t)} should yield the list \{2, 5\}. We can specify the result of this function in at least two ways: we can give a reference implementation (perhaps very inefficient, but obvious correct), or we can state a property about the resulting list on indices.
**Specification** The declarative specification gives a property of all indices in the sequence yield by $indices$:

$$s \in \text{String}, c \in \text{Char}, i \in 0..\#s - 1 \cdot isMember(i, indices(s, c)) \Leftrightarrow s[i] = c$$

The function $isMember$ checks if the element occurs in a list, and $\#s$ is the length of the string $s$. The characters are numbered from 0 to $\#s - 1$ in $s[i]$ which indicates string subscription.

This property states that an index $i$ is part of the result of $indices(c, s)$ if and only if $s[i] = c$. The universal quantifiers over $c$ and $s$ are often omitted, as is usual in logic.

Every logical property is transformed to a function. The name of the function is used as reference to the property. The function arguments are interpreted as universal quantifiers. GAST provides a complete set of logical operators including $\forall$, $\exists$, $\land$, $\neg$, $\Rightarrow$ and $\Leftrightarrow$. The property state above is expressed in **Clean** as:

```clean
propIndices :: String Char → Property
propIndices s c = p For [0..size s-1] where p i = isMember i (indices s c) ⇐⇒ (s.[i] == c)
```

The operators `For` and `⇐⇒` in this function definition is provided by the GAST-library. In this situation it is safe to replace `⇐⇒` by the equality `==`. For implementation reasons the result of a specifying function is `Property` instead of `Bool`, if the specification contains a test operator like `⇐⇒`.

Note that this specification does not specify that the resulting list ought to be sorted, e.a. a function that yields $[5, 2]$ as result to $indices(\"A test\", \text{t})$ also obeys this property (and hence passes the test). This is not a fundamental problem, in fact it is a feature: in practise we usually work with partial specifications, rather than complete specifications. Specifying that the indices should be increasing can look like:

```clean
propIncreasing :: String Char → Bool
propIncreasing s c = increasing (indices s c)
```

In this situation it is safe to replace `Increasing True` by the equality `==`. For implementation reasons the result of a specifying function is `Property` instead of `Bool`, if the specification contains a test operator like `==`.

**Reference implementation** Using a reference implementation the function $indices$ can be specified in **Clean** as:

```clean
propIndices2 :: String Char → Bool
propIndices2 s c = indices s c == [i | i ← [0..size s-1] | s.[i] == c]
```

In this function the reference implementation is stated as the list comprehension $[i | i ← [0..size s-1] | s.[i] == c]$, this are all numbers $i$ between 0 and $size s-1$ where element $i$ of string $s$ is equal to the given character $c$.

**Invoking tests** The first property can be tested by evaluating the expression

```
test propIndices
```

Start = test 1000 propIndices
This will cause the evaluation of the function `propIndices` for at most 1000 (the standard number of tests) values. In this test the function `indices` is the Implementation Under Test, IUT, all other parts of the language are expected to work correctly.

**Partial functions** Many function used in programming are partial functions, they work correctly for a part of the input domain. For example the square root function works only for non-negative real numbers and the factorial function works only for non-negative integer values. From the outside it is not visible that these functions are partial functions, hence the test system is not able to limit the test data automatically to the part of the input type where the function is defined.

Gast provides two ways to cope partial functions. In logic properties of partial functions include usually an implication operator restricting the actual property to input values that should behave as requested, e.g. \( \forall x \in R. x \geq 0 \Rightarrow (\sqrt{x})^2 = x \). In Gast we can directly express this:

```
propSqrt :: Real -> Bool
propSqrt x = x >= 0 ==> let y = sqrt x in y*y == x
```

As an experienced programmer may expect, Gast finds counterexamples very quickly due to rounding errors. A better specification states that the difference \((\sqrt{x})^2 - x\) should be less than some small number \(\delta\):

```
propSqrt2 :: Real -> Property
propSqrt2 x = x >= 0.0 ==> let y = sqrt x in y*y - x < delta
where delta = 1E-10
```

The other way to cope with partial functions is to limit the test data explicit to allowed inputs. For our square root example this can be:

```
propSqrt3 :: Real -> Bool
propSqrt3 x = let y = sqrt x in y*y - x < delta
where delta = 1E-10
```

Start = test (propSqrt3 For [0.0, 0.123456789 .. ])

Of course limiting the test data to allowed inputs is more efficient in terms of actual tests done. For the actual testing rejecting test data (and generating them) is a waste of time.

### 2.1 The test algorithm

The IUT passes the test if the property holds for all generated arguments, i.e. it evaluates to True. The property does not hold if a counterexample is found.

For a property `prop` with one universal quantified variable, that is a function with one argument, the test algorithm is given by `testLogical`. The function takes the list of all possible test data and the number of test to be done as argument. If the number of tests to be done is 0, the property passes the test. Otherwise, the property is evaluated for the first test value \(t\). If this test succeeds,
evaluates to True, testing continues with the rest of the test values. Otherwise a counterexample is found, and the test yields fail. The actual implementation shows also the test value that is the counterexample.

\[
\text{testLogical ([}t : ts], n) = \begin{cases} 
\text{pass} & \text{if } n = 0 \\
\text{elseif } \text{prop}(t) & \text{then testLogical } (ts, n - 1) \\
\text{else fail} 
\end{cases}
\]

\[
\text{testLogical } ([], n) = \text{proof}
\]

The list of test values is provided by the operator \texttt{For}, or generated by the function \texttt{ggen} discussed below. For properties with more than one universal quantified variable the test algorithm tries every combination in a fair order: Instead of combining the first value of the first argument with all possible values for the second argument before looking at the second value for the first argument, the values are combined in an interleaved way. For a 2-argument function \( f \), the system generates two sequences of arguments, call them \([a, b, c, ..] \) and \([u, v, w, ..] \) respectively. The desired order of tests is \( f a u, f a v, f a w, f b u, f b v, f b w, .. \) rather than \( f a u, f a v, f a w, ..., f b u, f b v, f b w, .. \).

### 2.2 Implementation of the test system

The properties to be tested are functions with a variable number of arguments, the universal quantified variables. The result is either a Boolean or an element of the type \texttt{Prop} introduced above. We introduce the class \texttt{Testable} in order to create a function that eats all kinds of everything as an argument.

\[
\text{class Testable a where evaluate :: a RandomStream Admin } \rightarrow \{\text{Admin}\}
\]

The random stream is a list of pseudo random numbers used in the selection of test data. The type \texttt{Admin} is used to record information of the current test. In theory it would be sufficient to yield a Boolean result indicating if the test was successful or not. In practice we also want to record some information about the tests done. For instance, we do not only want to know that there exists a counterexample, but also the value of the universal quantified variables for this counterexample. This information is stored in the record \texttt{Admin}. The list of \texttt{admin}'s that is the result of the function \texttt{evaluate} contains one record for each test performed. An additional function is used to combine the results of the first \( N \) tests.

The instance of \texttt{evaluate} for Booleans is very easy. There is only one element in the list of results. If the Boolean is \texttt{True} the property holds (\texttt{OK}), otherwise a counterexample (\texttt{CE}) is found.

\[
\text{instance Testable Bool where}
\text{evaluate } b \text{ rs admin}
\text{ = \{[admin & res = if } b \text{ OK CE, args = reverse result.args]\}}
\]
A function \(a \rightarrow b\) as argument of \texttt{evaluate} implies that we to test a logical expression containing a universal quantified variable of type \(a\). We can test this expression if \(a\) is a valid test argument, and we can test things of type \(b\). A type \(a\) is a valid test argument if elements of this type can be transformed to strings by \texttt{genShow}[^1], and generated by \texttt{ggen}.  

\begin{verbatim}
  class TestArg a | genShow[\*], ggen[\*] a

  instance Testable (a \rightarrow b) | Testable b & TestArg a
  where
    evaluate f rs result
      \$ (rs.rs2) = split rs
      = forall f (generateAll rs) rs2 result

  For the implementation of logical operators it is a little inconvenient that the class \texttt{Testable} eats almost each function. The type \texttt{Property} is merely used to stop the class \texttt{Testable} from evaluating a function as a logical expression. In order to be able to continue the evaluation of such an expression we just have to remove the constructor \texttt{Prop}.

  :: Property = Prop (RandomStream Admin \rightarrow [Admin])

  instance Testable Property
  where evaluate (Prop p) rs result = p rs result

  The operator \texttt{For} that can be used to supply a list of test data that is to be used instead of the test data generated by \texttt{Gast} is defined as:

  (For) infixl 0 :: !(x-p) ![x] \rightarrow Property | Testable p & TestArg x
  (For) p list = Prop (forall p list)

  The logical implication operator, \(\rightarrow\), is used for argument selection. If its left-hand argument evaluates to \texttt{False}, this test case is rejected: it is neither a success nor a counterexample.

  class (\(\Rightarrow\)) infixr 1 b :: b p \rightarrow Property | Testable p

  instance \(\Rightarrow\) Bool
  where
    (\(\Rightarrow\)) c p
      | c = Prop (evaluate p)
      = Prop (Ars r = [(r & res = Rej)])

  A similar instance of \(\Rightarrow\) exists for \texttt{Property}.
\end{verbatim}

### 2.3 Generating test data

Test data are generated by the \texttt{generic}[^1] function \texttt{ggen}. \texttt{Gast} contains instances of the function \texttt{ggen} for all basic types. By deriving an instance for a user

[^1]: To avoid confusion with generic programming in object oriented languages this is also called \textit{polytypical} programming. Generic programming in the OO-spirit is called polymorphic programming in functional programming.
defined type, all instances of this type are enumerated in a pseudo random order with a very strong small to large bias. The basic idea is that generic programming provides an universal tree representation of arbitrary data types. The test data are obtained by a breadth-first traversal of the tree of all possible instances of the type.

For an individual test it is possible to deviate from the arguments by \texttt{ggen}. For instance, if we want to test the function \textit{indices} only for the strings "Hello world!" and "A test", we evaluate the expression:

\begin{verbatim}
test (propIndices For ["Hello World!","A test"])
\end{verbatim}

Using the given strings in all situations where \texttt{Gast} needs to quantify over strings is obtained by defining an instance of \texttt{ggen} for the type \texttt{String} like:

\begin{verbatim}
ggen[String] x y = ["Hello World!","A test"]
\end{verbatim}

The arguments \(x\) and \(y\) can be used to vary the order of the generated elements.

The generic function \texttt{ggen} and the operator \texttt{For} yield powerful and flexible generation of test data. The ability to combine logical operators with the concise high level computations of a functional language and the flexible automatic test data generation, makes \texttt{Gast} a very powerful tool for testing functions over complex data types.

**Generic test data generation** One of the distinguishing features of \texttt{Gast} is that it is able to generate test data in a systematic way. This guarantees that test are never repeated, which is useless in a referential transparent language like \texttt{Clean}. For finite data types it is even possible to prove properties using a test system: a properties is proven if it holds for all elements of the finite data type.

The generic function \texttt{gen} generates the lazy list of all values of a type by generating all relevant generic representations [12] of the members of that type.

\begin{verbatim}
generic gen a :: [a]
\end{verbatim}

For the type \texttt{UNIT} there is only one possibility: the constructor \texttt{UNIT}.

\begin{verbatim}
gen[UNIT] = [UNIT]
\end{verbatim}

For a \texttt{PAIR} we combine the lists of values generated by \texttt{f} and \texttt{g} in all possible ways. We use the library function \texttt{diag2} rather than a list-comprehension like \([\text{Pair} a b \mapsto a-f, b-g]\) in order to obtain the required fair order.

\begin{verbatim}
gen[PAIR] f g = map (\(\lambda(a,b)\Rightarrow\text{PAIR} a b\)) (\texttt{diag2}\ f\ g)
\end{verbatim}

For the choice in the type \texttt{EITHER} we use an additional Boolean argument to merge the elements in a nice interleaved way. The definition of the function \texttt{Merge} is somewhat tricky in order to avoid that it becomes strict in its list elements.

\begin{verbatim}
gen[\texttt{EITHER}] f g = Merge True f g
where
  Merge :: !Bool \[a] \[b] \rightarrow [\texttt{EITHER} a b]
  Merge left as bs
\end{verbatim}
\[
| \text{left} \\
| = \text{case as of} \\
| [] = \text{map RIGHT } bs \\
| a:as = [\text{LEFT } a: \text{Merge (not left) as } bs] \\
| = \text{case bs of} \\
| [] = \text{map LEFT as} \\
| b:bs = [\text{RIGHT } b: \text{Merge (not left) as } bs]
\]

In order to let this merge algorithm terminate for recursive data types we assume that the non recursive case (like \texttt{Nil} for lists, \texttt{Leaf} for trees) is listed first in the type definition. Using some insight knowledge of the generic representation of allow us to make the right initial choice in \texttt{gen(EITHER)}. In principle the generic representation contains sufficient information to find the terminating constructor dynamically, but this is more expensive and does not add any additional power.

Finally we have to provide instances of \texttt{gen} for the basic types of \texttt{Clean}. Some examples are:

\[
\begin{align*}
\text{gen[Int]} &= [0: [i \in n-[1..\text{maxint}], i-n, n]] \\
\text{gen[Bool]} &= [\text{False}, \text{True}] \\
\text{gen[Char]} &= \text{map toChar [32..126]} ++ ['\lambda\alpha\lambda\beta'] \\
\text{gen[String]} &= \text{map toString lists} \\
\text{where} \\ 
\text{lists} &= [[\text{Char}]] \\
\text{lists} &= \text{gen[]} \\
\end{align*}
\]

The actual algorithm used in \texttt{GAST} is slightly more complicated. It uses a stream of pseudo random numbers to make small perturbations to the order of elements generated. Basically the choice between \texttt{Left} and \texttt{Right} in \texttt{gen(Either)} becomes a pseudo random one instead of

\section{Testing Reactive Systems}

A reactive system has an internal state that can be changed by inputs and is preserved between the inputs. This implies that the reaction on the current input can depend on previous inputs. E.g. the system gets a number as input and the response is the number of inputs seen. The reactive systems that are discussed here can be nondeterministic. During the tests we look only at the inputs and responses of the reactive system, the internal state is not known. This is called Black Box Testing, BBT.

The reactive system tested is the Implementation Under Test, IUT. Since the state of the IUT is hidden, stating properties relating input, output and state is not feasible. To circumvent this problem we specify reactive systems by an extended state machine and require that the observed behavior of the IUT is conform to this specification.

From Finite State Machines, FSMs, we inherit the synchronous behavior of systems. Each input yields a, possible empty, sequence of outputs. After producing this sequence of outputs the system becomes quiescent; it waits for a new
input. Among other advantages this yields a convenient notion of no output: the empty sequence. We extend the FSM model in several directions:

- The state, input and output can be of any (recursive) data type. This includes also infinite data types and parameterized data types. Hence, we have a state machine rather than a finite state machine. A machine specification having parameterized data types is also known as an extended state machine.
- It is not required that the specification or implementation of the state machine is deterministic.

3.1 Extended State Machines

An Extended State Machine, ESM, as used by GAST consists of states with labelled transitions between them. A transition is of the form \( s \xrightarrow{i,o} t \), where \( s, t \) are states, \( i \) is an input which triggers the transition, and \( o \) is a, possibly empty, list of outputs. A transition \( s \xrightarrow{i,o} t \) is formalized as a tuple \((s, i, t, o)\). A relation based specification \( \delta \) is a set of these tuples: \( \delta \subseteq S \times I \times S \times [O] \). Where \( S \) is the type of states, \( I \) is the type of inputs, and \( O \) is the type of outputs. We use \([O]\) in the transitions to indicate a sequence of elements of type \( O \). It is not required that all these types are different. Specifications can be partial: not for every \( s \in S \) and \( i \in I \) there must be a tuple in \( \delta \) specifying the new state and the output. A specification is total if it is not partial. If a specification is nondeterministic there are \( s \in S \) and \( i \in I \) with more than one tuple in \( \delta \).

In practice it is usually more convenient to have a specifying function instead of a transition relation. The transition function takes the current state and input as argument and produces the set of all specified tuples of target state and output sequence. The transition function is defined by \( f(s, i) = \{ (t, o) \mid (s, i, t, o) \in \delta \} \). The type of this function is: \( \text{State} \times \text{Input} \rightarrow \mathbb{P}(\text{State} \times [\text{Output}]) \). Here we used \( \mathbb{P}(X) \) as notation for a set of elements of type \( X \). Transition \( s \xrightarrow{i,o} t \) is equivalent to \((t, o) \in \delta_f(s, i)\). A specification is partial if for some state \( s \) and input \( i \), \( \delta_f(s, i) = \emptyset \). A specification is deterministic if for all states and inputs the size of the set of targets contains at most one element: \( \# \delta_f(s, i) \leq 1 \).

A trace \( \sigma \) is a sequence of inputs and associated outputs from the given state. A trace is defined inductively: the empty trace connects a state to itself: \( s \xrightarrow{} s \). We can combine a trace \( s \xrightarrow{\sigma} t \) and a transition \( t \xrightarrow{i,o} u \), to the trace \( s \xrightarrow{\sigma i,o} u \). An input trace contains only the input elements of a trace.

We define \( s \xrightarrow{i,o} \equiv \exists t. s \xrightarrow{i,o} t \) and \( s \xrightarrow{\sigma} \equiv \exists t. s \xrightarrow{\sigma} t \). All traces from a given state are defined as: \( \text{traces}(s) \equiv \{ \sigma | s \xrightarrow{\sigma} \} \).

The inputs allowed in some state are given by \( \text{init}(s) \equiv \{ i | \exists o. s \xrightarrow{i,o} \} \). The states after applying trace \( \sigma \) in state \( s \) are given by \( s \text{ after } \sigma \equiv \{ t | s \xrightarrow{\sigma} t \} \). We overload \( \text{traces} \), \( \text{init} \), and \( \text{after} \) for sets of states instead of a single state by taking the union of the notion for the members of the set. When the transition function, \( \delta_f \), to be used is not clear from the context, we will add it as subscript.

We will often identify a machine with its transition function. However, a complete description also determines the initial state \( s_0 \).
Examples As illustration we show some state machines modelling coffee vending machines in figure 1. In section 4 we will test some properties of these specifications. The global specification of these coffee vending machines is that it can deliver coffee after insertion of coins with a value of 10 cent, and pressing the

\[ c_0 :: \text{State} \times \text{IO} \rightarrow \mathbb{P}(\text{State},\{\text{IO}\}) \]
\[ c_0(S_0, \text{Nickel}) = \{(S_5, \text{[]})\} \]
\[ c_0(S_0, \text{Dime}) = \{(S_{10}, \text{[]})\} \]
\[ c_0(S_5, \text{Nickel}) = \{(S_{10}, \text{[]})\} \]
\[ c_0(S_{10}, \text{Button}) = \{(S_0, [\text{Coffee}])\} \]
\[ c_0(s, i) = \emptyset \]

\[ c_1 :: \text{State} \times \text{IO} \rightarrow \mathbb{P}(\text{State},\{\text{IO}\}) \]
\[ c_1(S_0, \text{Nickel}) = \{(S_5, \text{[]})\} \]
\[ c_1(S_0, \text{Dime}) = \{(S_{10}, \text{[]})\} \]
\[ c_1(S_5, \text{Nickel}) = \{(S_{10}, \text{[]})\} \]
\[ c_1(S_{10}, \text{Button}) = \{(S_0, [\text{Coffee}], (S_{10}, \text{[]}))\} \]
\[ c_1(s, i) = \emptyset \]

\[ c_2 :: \text{State} \times \text{IO} \rightarrow \mathbb{P}(\text{State},\{\text{IO}\}) \]
\[ c_2(S_0, \text{Nickel}) = \{(S_5, \text{[]})\} \]
\[ c_2(S_0, \text{Dime}) = \{(S_{10}, \text{[]})\} \]
\[ c_2(S_5, \text{Nickel}) = \{(S_{10}, \text{[]})\} \]
\[ c_2(S_{10}, \text{Button}) = \{(S_0, [\text{Coffee}])\} \]
\[ c_2(s, i) = \{(s, \text{[]})\} \]

\[ c_3 :: \text{State} \times \text{IO} \rightarrow \mathbb{P}(\text{State},\{\text{IO}\}) \]
\[ c_3(S_0, \text{Nickel}) = \{(S_5, \text{[]})\} \]
\[ c_3(S_0, \text{Dime}) = \{(S_{10}, \text{[]})\} \]
\[ c_3(S_5, \text{Nickel}) = \{(S_{10}, \text{[Nickel]})\} \]
\[ c_3(S_{10}, \text{Button}) = \{(S_0, [\text{Coffee}])\} \]
\[ c_3(s, i) = \{(s, \text{[]})\} \]

\[ c_4 :: \mathbb{Z} \times \text{IO} \rightarrow \mathbb{P}([\mathbb{Z}],\{\text{IO}\}) \]
\[ c_4(n, \text{Nickel}) = \{(n + 5, \text{[]})\} \]
\[ c_4(n, \text{Dime}) = \{(n + 10, \text{[]})\} \]
\[ c_4(n, \text{Button}) = \text{if } n \geq 10 \]
\[ \text{then } \{(n - 10, [\text{Coffee}])\} \]
\[ \text{else } \{(n, \text{[]})\} \]

Fig. 1. Some coffee vending machines.
coke button. An input is either a nickel, a 5-cent coin, a dime, a 10-cent coin, or pressing the coke button. The output is either the return of a coin, or coke. For simplicity we will use the same type \( \text{IO} \) for input and output, we take care that the Coke is never an input and Button is never an output. The state of the first three machines is the algebraic data type State, it just records the amount of money inserted. The last machine uses a number as state. The types State and \( \text{IO} \) are enumeration types defined as:

\[
\text{State} = S_0 \mid S_5 \mid S_{10} \\
\text{IO} = \text{Nickel} \mid \text{Dime} \mid \text{Coffee} \mid \text{Button}
\]

We will discuss each of the machines briefly:

\( c_0 \) This is the simplest partial specification meeting the informal requirements. After inserting two nickels, or one dime, and pressing the coke button, the machine produces coke. Note that this is a partial specification, for instance the effect of the input Button in state \( S_0 \) is undefined.

\( c_1 \) This is a partial specification meeting the informal requirements. After inserting two nickels, or one dime, and pressing the coke button, the machine can produce coke. This machine is very similar to \( c_0 \), but nondeterministic. On input Button in state \( S_{10} \), it can either produce coke and go to \( S_0 \), or do nothing. This is a partial specification, for instance the effect of Button in \( S_0 \) is undefined.

\( c_2 \) The unlabelled transitions are applicable on any other input and produce the empty output. They make the specification total. All these transitions are represented by the last function alternative.

\( c_3 \) This is also a total specification. It states that coins should be returned if the value of the inserted money becomes higher than 10 cents.

\( c_4 \) This machine uses a single integer as state. It stores the total amount of money inserted and produces coke while there is enough money. There are infinitely many states. Only non-negative multiples of 5 can be reached.

Some traces of \( c_2 \) are: [], [(Nickel, [])], [(Nickel, [])], [(Nickel, [])], [(Nickel, [])], (Nickel, []), (Button, [Coffee]), and [(Dime, []), (Button, [Coffee])]. Sequences of input-output pairs that are not traces of \( c_2 \) are: [(Nickel, [])], (Dime, []), and [(Dime, [Coffee])].

### 3.2 Representation of specification functions in Gast

In order to test machines in GAST, the specifying function is expressed in the functional programming language CLEAN[7]. The resulting set of pairs is represented by a list of pairs. The CLEAN compiler will check the specification on matters like type correctness and proper use of identifiers.

As example we show the representation of \( c_1 \) in CLEAN. The enumeration types used as well as the transition function can be mapped directly to CLEAN.
:: State = S0 | S5 | S10
:: IO = Nickel | Dime | Coffee | Button

c1 :: State IO -> [(State,[IO])]
c1 S0 Nickel = [(S5,[])]
c1 S0 Dime = [(S10,[])]
c1 S5 Nickel = [(S10,[])]
c1 S10 Button = [(S0,[Coffee]),(S10,[])]
c1 s i = []

Function arguments starting with a capital are constants that must be matched to the actual arguments in order to make this alternative applicable. Lowercase arguments match any actual argument. Alternatives are tried textual order, the first one that matches is applied.

Using higher order functions, specifications can be manipulated. As a very simple example we list the function enableInput, that enables input in any state. This function takes a machine specification \( m \) as argument, and yields an input enabled version of \( m \). If no transition is specified for some state and input, it adds the transition to the same state with an empty output sequence. Since this is a polymorphic function, it will work for any specification using arbitrary types for state \( s \), input \( i \) and output \( o \).

\[
\text{enableInput} :: (s \rightarrow ([s, [o]])) \rightarrow s \rightarrow ([s, [o]])
\]

\[
\text{enableInput} \ m = \ m'
\]

\[
\text{where } m' \ s \ i = \text{case } m \ s \ i \ of
\]
\[
[] = ([s, []])
\]
\[
r = r
\]

Applying this function to \( c_0 \) yields a specification that is equivalent to \( c_2 \). Applying it to \( c_2 \), \( c_3 \), or \( c_4 \) does not change these specifications. Note that \( \text{enableInput} \ c_1 \) is not equivalent to \( c_2 \), the first specification still contains the transition \( S_{10} \xrightarrow{\text{Button}[]} S_{10} \), which is not present in \( c_2 \).

### 3.3 Implementations under test

The assumption is that also the implementation under test is an extended state machine. Since the IUT is a black box, its state is invisible. Even if the IUT is nondeterministic, it will choose exactly one transition on each input.

In contrast to the specification, the implementation should be input enabled: the result of any input in any reachable state should be specified. In terms of the transition function this is \( \forall s \in \text{State}.\forall i \in \text{Input}.\delta_f(s,i) \neq \emptyset \). The motivation for this requirement is that an IUT cannot prevent that inputs are applied. It is perfectly acceptable if some inputs in specific states brings the implementation in an error state. For our tests it is sufficient if the IUT accepts each input that is allowed by the specification. The broader input enabledness requirements prevents complicated analysis or runtime problems.

In the examples above, a coffee vending machine cannot prevent that a user presses the button or inserts a coin in any state. This implies that \( c_1 \) cannot be
a correct implementation. or instance the effect of applying the input Button, pressing the coffee button, in state \( S_0 \) is undefined. The machines \( c_2 \), \( c_3 \) and \( c_4 \) are input enabled, and hence can be used as IUT.

The implementation can be in any programming language or even in hardware, for testing it is only required that \( \text{GAST} \) can provide an input to the IUT and observe the associated output.

### 3.4 Conformance

Intuitively an IUT is conform to a specification if the observed transitions are part of the specification, or the specification does not specify anything for this state and input: \( \delta_f(s, i) = \emptyset \). Formally, conformance of the iut to the specification \( \text{spec} \) is defined as:

\[
iut \conf \text{spec} \equiv \forall \sigma \in \text{traces}_\text{spec}(s_0). \forall i \in \text{init}(s_0 \after \text{spec} \sigma) \forall o \in [O].
\]

\[
(t_0 \after iut \sigma) \xrightarrow{s_0 \after \text{spec} \sigma} (s_0 \after \text{spec} \sigma)
\]

If the specification allows input \( i \) after trace \( \sigma \), the observed output of the IUT should be allowed by the specification.

This notion of conformance is very similar to the \( ioco \) relation of [8] for Labelled Transition Systems, LTSs. In an LTS each input and output is modelled by a separate transition. In our approach an input and all induced outputs up to quiescence are modelled by a single transition with a sequence of outputs. The conformance relation for (timed) EFSMs in [9] is similar, our systems have a sequences of output. If there is no other information we use quiescence to determine the end of the sequence of outputs of the IUT. In [9] there is no notion of quiescence, and the EFSMs have only a single output.

**Examples** Since both the specification and the IUT are given as an ESM, an ESM can be used as specification and as IUT. We have seen that \( c_1 \) in figure 1 cannot be a correct implementation since it is not input enabled. The machines \( c_2 \), \( c_3 \) and \( c_4 \) are correct implementations of \( c_1 \). Although the response \([\[]\] to the input Button in \( S_{10} \) will never occur. According to the conformance relation this is not necessary. It is sufficient that the behavior for some specified input after a trace is allowed by the specification. Note that \( c_3 \) and \( c_4 \) have behavior that is not covered by the specification. This is allowed according to the conformance relation because nothing is specified for that combination of state and input.

Machine \( c_3 \) is not a correct implementation of \( c_2 \). After the inputs \([\text{Dime, Dime}]\) the machine \( c_2 \) only allows the output \([\[]\], while \( c_3 \) produces \([\text{Dime}]\). The same input trace shows that \( c_2 \) is not a correct implementation of \( c_3 \).

Although \( c_4 \) behaves correct to \( c_2 \) as specification for the input sequence \([\text{Dime, Dime}]\), it is not a correct implementation. This is shown for instance by the input sequence \([\text{Dime, Dime, Button, Button}]\). For this input \( c_4 \) produces a second cup of coffee, while \( c_2 \) only allows an empty output.

Finally, \( c_4 \) is not a correct implementation of \( c_3 \), nor is \( c_3 \) an implementation of \( c_4 \). This is shown for instance by the input sequence \([\text{Dime, Dime}]\).
Testing Conformance The testing algorithm takes a sequence of inputs as argument. The specification and implementation start in their initial state. As long as the specification specifies transitions for the current state and input, \( \text{spec}(s, i) \neq \emptyset \), the next input is applied to the IUT. If the response is conform to the specified behavior, testing continues with the next input element and the new state of the specification, otherwise an error is found. If nothing is specified for the current state and input, testing of this input sequence is terminated. The associated test result is pass. If the end of the input sequence is reached the implementation has been successfully tested with this input sequence.

The function \( \text{testConformance} \) takes the sequence of inputs, the observed trace and the number of steps to go as argument and produces a test verdict.

\[
\text{testConformance} ([i : is], \sigma, n) = \begin{cases} 
\text{if } n \neq 0 \land i \in \text{init}(s_0 \text{ after spec } \sigma) \\
\text{then let } o = \text{iut.apply}(i) \text{ in} \\
\text{if } (s_0 \text{ after spec } \sigma) \xrightarrow{i/o}, \\
\text{then } \text{testConformance} (is, \sigma; i/o, n - 1) \\
\text{else fail} \\
\text{else pass}
\end{cases}
\]

The first condition checks if there are still inputs to be tested, \( n \neq 0 \), and if the specification states something for the next input after the observed trace, \( i \in \text{init}(s_0 \text{ after spec } \sigma) \). The innermost condition verifies whether the observed transition is allowed by the specification in the current state. For a more efficient implementation we keep track of the states allowed after the current trace. For deterministic specifications there is at most one state allowed at any moment. If the transition is allowed, testing continues with the rest of the inputs. An IUT passes the test of an input sequence, if the sequence becomes empty. During one test run, \( \text{GAST} \) can test several input sequences. The IUT and the specification are reset before each new input sequence.

Test Data Generation In order to test conformance, \( \text{GAST} \) needs a collection of input sequences. \( \text{GAST} \) has several algorithms for input generation, e.g.:

- Systematic generation of sequences based on the input type by the same algorithm that is used for logical properties.
- Sequences that cover all transitions in a finite state machine. Under the assumption that the IUT has more states than the specification, this can prove the conformance of the IUT [10].
- Pseudo random walk through the transitions of a specification. This generates long test sequences that can penetrate deep in the state space. It appears to be very effective for machines with a large or infinite number of transitions
- User defined sequences for specific purposes.
Due to the lazy evaluation of CLEAN, only those inputs are generated than are actually needed by the test algorithm. This allows us to work with potentially infinite lists of inputs. This is known as on-the-fly generation of test data.

The machines given in figure 1 are so small that each of these algorithms indicated the errors very soon if the implementation is incorrect. The FSM-based algorithm can be used to prove that $c_3$ is correct implementations of $c_2$, it cannot be used for $c_4$ as specification since it has infinitely many states.

In section 4 we will use the part of GAST introduced in the next section to test properties of these ESM-specifications.

4 Quality of Specifications

Apart from the number of tests, the quality of testing is determined by the quality of the properties stated. Obviously, aspects of a system that are not specified cannot be tested. The CLEAN-compiler used by GAST checks many aspects, like proper use of identifiers and type-correctness, of the specification before it can be used. Semantical errors cannot be catched by the compiler. Incorrect specifications can cause strange test results. If the specification and the IUT contain the same error, it will pass unnoticed. In practice many issues spotted during testing are due to incorrect specifications.

In an incremental software process this is not a serious problem. The specification and the implementation are improved at the same time. Testing shows the differences in behavior of the implementation and the specification. In this way the quality of the specification and the implementation increases. This approach is only feasible when testing is fast and automatic, GAST was found to be very useful [5].

For software processes that creates the software in one go, like the waterfall-model or the V-model, incorrect specifications can seriously delay the delivery of the system. It is desirable to verify and improve the quality of specifications before they are used to test the actual implementation.

4.1 Testing Specifications

In every situation it is desirable to check properties of the specifications used. This can be done by a model checker, like FDR or SPIN, but also by testing. Formal verification by a model checker requires a transformation of the model to a suited input language, like CSP or Promela. Testing can be done with the given specifications and appears to be fast and effective. For specifications of small finite systems\(^2\), a number of properties cannot only be tested, but the property can even be proven correct or falsified by a counterexample. The specifications of reactive systems introduced in section 3 are ordinary functions in CLEAN, hence they can be tested like any function as shown in section 2. In this section we will show how, general or domain specific, properties properties of ESM specifications can be tested.

\(^2\)A system is finite if the number of states, inputs and outputs in finite.
General properties like determinism and completeness can be checked for any ESM specification. A specification is deterministic if for every state and input there is at most one transition defined:

$$\forall s \in S, i \in I \bullet \#\delta_f(s, i) \leq 1$$

To make this property applicable to any specification in GAST we parameterize it with the machine specification $m$:

$$\text{propDeterministic} :: (\text{Spec } s \triangleright o) s i \rightarrow \text{Bool}$$

$$\text{propDeterministic } m s i = \text{length}(m s i) \leq 1$$

Where $\text{Spec } s \triangleright o$ is an abbreviation for $s i \rightarrow [(s, [o])]$. Specification $c1$ introduced above can be tested by evaluating $\text{test (propDeterministic } c1)$. GAST spots the counterexample for state $S_{10}$ and input $\text{Button}$ in a split second. Due to the limited number of states and inputs GAST will prove that specifications $c2$ and $c3$ are deterministic. For $c4$ there are infinitely many states, so a proof by exhaustive testing is not possible. Testing yields $\text{pass}$. In the same spirit we can test whether a specification is total:

$$\forall s \in S, i \in I \bullet \delta_f(s, i) \neq \emptyset$$

This can also be specified directly in GAST:

$$\text{propTotal} :: (\text{Spec } s \triangleright o) s i \rightarrow \text{Bool}$$

$$\text{propTotal } m s i = \text{not (isEmpty}(m s i))$$

As we might expect, GAST find counterexamples for $c1$, proves the property for $c2$ and $c3$ and machine $c4$ passes any number of tests. These general properties can be applied to any ESM-specification and are part of the library GAST.

Note that all properties in this section are tested at a specification, and not at an implementation of that model. These tests can be done before an implementation exists.

Domain specific properties As example of a domain specific property we require that coffee machines "does not lose money": the value of a state and the input should be equal to the value of the target state and the associated output for any transition specified. In logic this property reads:

$$\forall s \in S, i \in I, (t, o) \in \delta_f(s, i) \bullet \text{value}(s) + \text{value}(i) = \text{value}(t) + \text{value}(o)$$

This can be directly transformed to GAST. First, we construct a class $\text{value}$ that yields the value of states, inputs and outputs. The value of a state is the amount of money inserted, the value of a coin is its value, the value of Coffee is 10, and the value of Button is 0. In order to test various machines easy, we make the specification to check an argument, $m$, of the property.

$$\text{propFair } m s i = p \text{ For } m s i$$

where $p (t, o) = \text{value } s + \text{value } i \equiv \text{value } t + \text{value } o$
Gast proves this property for $c_1$, and $c_3$. The property does not hold for $c_2$, one of the counterexamples found by the test system is inserting a *Dime* in state $S_5$. The property holds also for $c_4$. Since this machine has infinitely many states, the property passes the test, but a proof for all states is impossible. The states can be limited to multiples of 5 between 0 and 100 by evaluating \texttt{test(propFair m5 For \{0,5..100\})}. Now the property is proven by Gast.

This property shows also that making a specification input enabled by adding transitions to the same state without output, as done by \texttt{enableInput}, is not an harmless operation. Property \texttt{propFair} does not hold for the input enabled version of machine $c_1$, \texttt{enableInput c1}.

Finally, we can require that the value of a target state is nonnegative if the value of the source state is nonnegative: $s \xrightarrow{\text{Ins}} t \cdot \text{value}(s) \geq 0 \Rightarrow \text{value}(t) \geq 0$.

\texttt{propNonNeg m s i} = \texttt{propFor p m s i where p (t,o) = value s \geq 0 \Rightarrow value t \geq 0}

This property is proven for the states $\{0,5..100\}$ of $m5$, but testing it for all states yields counterexamples due to integer overflow. Gast proves this property for the other specifications.

### 4.2 A priority queue

As a more sophisticated example we show a priority queue that always dequeues the smallest elements first. It is only able to enqueue and dequeue elements after the input \texttt{Init}. The input \texttt{Reset} brings it back to the state \texttt{New}. This system is specified by the state chart in figure 2, or the function \texttt{QSpec} in figure 3.

Using overloading, the function \texttt{QSpec} is defined very general, it works for any type for which the operators $<$, $+$, and a zero are defined. This implies that we can put for instance integers, doubles, or characters in such a priority queue.

**Testing general properties of the specification** The quality of this specification can be investigated by testing some of its desired properties. The specification passes any number of tests for being deterministic. When testing it for being total, Gast almost immediately spots a counterexample for state $Q []$ and input \texttt{Init}. The fact that the specification is not total implies that not all behavior can be tested by Gast: according to the conformance relation, any behavior is allowed is the specification does not specify a transition for a given state and input.

**Testing specific properties of specification** For this specification we can also state and test some specific properties like for all states $s_1$ that are reached after applying the input sequence \texttt{[In c]} for any $c$ starting in any state $s$, the
\[
Q\text{Spec} :: (Q\text{state} \ a) \times (Q\text{in} \ a) \rightarrow [(Q\text{state} \ a, [Q\text{out} \ a])] \mid <, +, \text{zero} \ a
\]

\[
\begin{align*}
Q\text{Spec} (\text{New}, \text{Init}) &= [(Q \ [\ ], [\ ])] \\
Q\text{Spec} (\text{New}, \text{Size}) &= [(\text{New}, [\text{Int} \ 0])] \\
Q\text{Spec} (\text{New}, \text{Sum}) &= [(\text{New}, [\text{El} \ \text{zero}])] \\
Q\text{Spec} (\text{New}, \text{any}) &= [(\text{New}, [\ ])] \\
Q\text{Spec} (Q \ q, \text{In} \ a) &= [(Q(q \ [\ ]); [\ ])] \\
Q\text{Spec} (Q \ q; \text{Out}) &= [(Q(q); [\text{El} \ a])] \\
Q\text{Spec} (Q \ q; \text{Size}) &= [(Q(q); [\text{Int} \ \text{length} \ q])] \\
Q\text{Spec} (Q \ q; \text{Sum}) &= [(Q(q); [\text{El} \ \text{sum} \ q])] \\
Q\text{Spec} (\text{state}; \text{Reset}) &= [(\text{New}, [\ ])] \\
Q\text{Spec} (\text{state}; \text{Out}) &= [(\text{state}, [\ ])] \\
Q\text{Spec} (\text{state}; \text{any}) &= [(\text{state}, [\ ])]
\end{align*}
\]

The additional function \( \text{ins} \) inserts an element at the appropriate place in an ordered list. It can be defined as:

\[
\begin{align*}
\text{ins} \ ([\ ]; c) &= [c] \\
\text{ins} \ ([a; \ [b : x]]; c) \mid a < b &= [a; b : x] \\
&= [b; \text{ins} \ a \ x]
\end{align*}
\]

Fig. 3. The priority queue as function.

The size of the queue should be one bigger than it was. The size of the queue is determined by applying the input \( \text{Size} \).

\[
\forall s \in (Q\text{state Char}), \forall c \in \text{Char}, \forall (s_0, [\text{Int} \ n]) \in Q\text{Spec}(s, \text{Size}), \\
\forall s_1 \in (s \ \text{after}_{Q\text{Spec}} [\text{In} \ c]), \forall (s_2, [\text{Int} \ m]) \in Q\text{Spec}(s_1, \text{Size}) \cdot m = n + 1
\]

We used list comprehensions in \texttt{Clean} to mimic set notation. The operator \( \text{after} \) implements the \( \text{after} \) operation introduced in section 3.1.

\[
\begin{align*}
\text{propQsize} :: (Q\text{state Char}) \text{ Char} & \rightarrow \text{Bool} \\
\text{propQsize} \ s \ c &= \text{and} \ [\ m \leftarrow n + 1, \ (s_0, [\text{Int} \ n]) \leftarrow Q\text{Spec} \ s \ \text{Size} \\
&\text{, } s_1 \leftarrow ([s] \ \text{after}_{Q\text{Spec}} [\text{In} \ c] \\
&\text{, } (s_2, [\text{Int} \ m]) \leftarrow Q\text{Spec} \ s_1 \ \text{Size}]
\end{align*}
\]

After 6 tests, \texttt{GAST} tells us that this property does not hold for the state \texttt{New} and input ‘\texttt{d}’, in fact it does not hold for any input in state \texttt{New}.

Since the priority queue works for any type with operator \( \langle \text{and} \rangle \) and \( \text{+} \), and a \texttt{zero}. We can choose the type used in testing. If it works for one type, it will work for every type, provided that the operators are implemented correctly. Usually, a small type gives the best test results. For that reason we will use characters here, although a small special type like \( \mathbb{T} = A \mid B \mid C \) is even more effective.
In the same way we can test whether the sum of the elements increases if we insert a positive element. Even if we rule out the problems with the state \( \text{New} \), GAST finds counterexamples caused by overflow. This indicates that the specification does not handle the limitations of finite representations of elements.

\[
\forall s \in (\textit{Qstate} \ \textit{Char}), \forall c \in \textit{Char}, \forall (s_0, \textit{El} v) \in \textit{QSpec}(s, \textit{Sum}), \\
\forall s_1 \in (s \ \textit{afterQSpec} \ [\text{In} \ c]), \forall (s_2, \textit{El} w) \in \textit{QSpec}(s_1, \textit{Size}) \cdot w > v
\]

\( \text{propQ4} \) \( s \ c = c > \text{zero} \implies \text{and} \ [ \lor v \ (s0, \textit{El} v) \rightarrow \textit{QSpec} \ s \ \text{Sum} \\
, s1 \rightarrow ([s] \ \textit{afterQSpec} \ [\text{In} \ c] \\
, (s2, \textit{El} w) \rightarrow \textit{QSpec} \ s1 \ \text{Sum} \ ]
\)

Since we have access to the states of the specification, we can use its internals in our tests. For instance, we can test whether the elements in the queue are ordered such that the head of the list is smaller than or equal to any element in that list. With this test we verify the distinguishing qualification of a priority queue. This property is not enforced by the type system, but by the manipulations allowed in \( \textit{QSpec} \). We test this for every state reached by applying any input sequence in the initial state \( \text{New} \).

\[
\forall i \in (\textit{Qin} \ \textit{Char}), \forall (Q \ q) \in (\textit{New} \ \textit{afterQSpec} \ i), \forall e \in q \cdot \text{hd}(q) \leq e
\]

For GAST this can be expressed as:

\[
\text{propPriority} :: \ [\textit{Qin} \ \textit{Char}] \rightarrow \text{Bool} \\
\text{propPriority} \ i \ = \ \text{and} \ [ \ \text{hd} \ q \leq e \ \lor Q \ q \rightarrow ([\textit{New}] \ \textit{afterQSpec} \ i), \ e \rightleftarrows q ]
\]

This property passes any number of tests, GAST test 100,000 different input sequences in 40 seconds.

Usually, properties of specifications are verified with a model checker. Due to the data dependencies used in the properties it is in this case not simple to verify the shown properties with a model checker. Moreover, in order to use a model checker the given model specification has to be translated to the world of the model checker, and produces results in terms of its own model. Here the model specification in \( \textit{Clean} \) is used by GAST to test its properties. Only the desired logical property has to be stated in \( \textit{Clean} \).

The successful tests shown here does not indicate that testing of specifications has the same power as a fully fledged model checker. Due to the sophisticated logic used in state-of-the-art model checkers, they have their own significant contribution. Nevertheless, testing specifications is an elegant, powerful and lightweight alternative approach to verify properties of specifications.

**Testing implementations** In order to verify the testing quality of GAST we made a correct implementation of this queue and ten mutants containing common (programming) errors like: an ordinary queue instead of a priority queue, a stack instead of a priority queue, a queue of at most 25 elements, various errors in the function \( \text{ins} \) for duplicated elements, return to the state \( \text{New} \) when the
queue becomes empty by an Out, and an implicit Init on an input In a when the system is in the state New.

We tested with the standard generic generation of test data for a queue of characters. Gast generates, tests and evaluates about 50,000 individual inputs per second on an average PC. It found errors in all mutants. Errors were always spotted within 0.5 seconds, usually much faster. This depends on the order of inputs and hence on the seed used for the generation of pseudo random numbers.

5 Related work

Many automatic test tools are developed in order to speedup testing and make (regression) more accurate. Most of these test tools are script based and execute a predefined sequence of actions. One of the best known examples is JUNIT [1] for JAVA-programs, it has been ported to a very large number of other programming languages.

Model based tools like Gast are more powerful since they generate the test data themselves. In this way it is possible to increase the quality of the test by generating more test data, instead by manually specifying more tests. Moreover, generation test data based on the current version of the specification guarantees that the tests done are always conform the current version of the specification.

For the testing of logical properties the test tool Quickcheck [6], is clearly the closest related tool. Distinguishing futures of Gast are the systematic generation of test data (instead of programmer controlled pseudo random generation), and hence the ability to proof properties. Also the set of logical operators in Gast is richer.

For the testing of reactive systems a number of model based test systems is available. The dominant approach is based on labelled transition systems and Torx [8] can be regarded as the godfather of tools using this approach. None of these tools uses a functional programming language to express the state transition function. We have show that a fpl yields a very concise way to specify reactive systems.

Much work has been done to verify and improve the quality of specifications. Most notably is the work to prove properties of the specifications with proof tools or model checkers. In fact a number of the properties shown can be verified with Clean’s own proof system called Sparkle[13]. This would require a significant user guidance that looses its value after any tiny change of the specification.

Model checkers, like [14,15], are usually geared to verify properties about the communication between processes, they have troubles with data intensive systems like the priority queue used in this paper. Model checkers require a translation of our specifications. Moreover, these systems require user guidance, and hence specific skills of the user. Testing properties provides a valuable and effective alternative within the framework used to write the specification.

The tools BLAST [16] and MOPS [17] verify properties of C-programs. Both model checkers are FSM based. They differ in model, programming language, purpose and techniques used from our approach.
There are a few reports on specification testing in the literature, e.g. [18–21], usually based on Z, [11], VDM, or B specifications. It focuses on animation of specifications to validate the specification by humans, on the evaluation of given input-output combinations, or on the question if there are instances of the specified transitions. A number of significant consistency aspects is checked by the strong type system of the CLEAN-compiler. To the best of our knowledge, this is the first report on testing specifications fully automatically in a systematic way, by generating test values, executing the tests, and generating a test verdict.

6 Discussion

In specification based testing one states general properties instead of instances of these properties for specific arguments. Advantages of this approach are the higher level of abstraction, and the automatic generation of test data from the specification. Manual generation of test data is dull and error-prone. Moreover, the validity of generated test data has to be checked after every change of the underlaying specification.

Using functional programming languages as notation for specifications appears to be very effective. The obtained specifications are very concise, and well suited to be handled by a test system like Gast.

Having the ability to test logical properties and reactive systems united in a single tool, allows us to verify the quality of specifications by automatic testing. This is a unique property of Gast. The properties tested are consistency rules for the specification of reactive systems. The same specification is used to test implementation and properties of the specification itself. Testing consistency properties of ESMs is possible since Gast combines the ability to automatically test logic properties and reactive systems. The tested properties can be general properties of specifications as well as domain specific. Testing specifications increases the quality and confidence in those specifications, and hence the quality of tests of implementations done with these specifications. Testing these properties is a lightweight and effective alternative for model checking. It works also in data intensive situations that are often hard for model checkers. An other advantage is that no other formalisms, translations and tools are needed. The examples in this paper show that many "obvious" properties of specifications are falsified by testing.

By verifying logical properties through testing, an ESM-specification can be made consistent. Another important quality attribute of an ESM-specification is to validate that it correctly states what the user requires. This validation cannot be done by fully automatic testing, but requires human guidance. Due to the executable nature of our specifications, they are also very suited for validation by simulation. We will address this in another paper.

References

1. See www.junit.org