The following full text is a publisher's version.

For additional information about this publication click this link.
http://hdl.handle.net/2066/36637

Please be advised that this information was generated on 2018-02-10 and may be subject to change.
Transition from two-dimensional electron-hole to geminate-exciton photoluminescence in GaAs/Al_xGa_{1-x}As heterostructures under a high in-plane magnetic field

B. M. Ashkinadze and E. Cohen
Solid State Institute, Technion-Israel Institute of Technology, Haifa 32000, Israel

V. V. Rudenkov, P. C. M. Christianen, and J. C. Maan
High Field Magnet Laboratory, Institute for Molecules and Materials, Radboud University Nijmegen, Toernooiveld 7, 6525ED Nijmegen, The Netherlands

L. N. Pfeiffer
Bell Laboratories, Lucent Technologies, Murray Hill, New Jersey 07974, USA

(Received 5 March 2007; revised manuscript received 17 June 2007; published 27 August 2007)

We studied the evolution of the photoluminescence (PL) spectra in modulation-doped GaAs-based heterostructures (single quantum wells and heterostructures [quantum well (MDQW) and single heterojunction (SHJ)]) under a perpendicular applied magnetic field $B_\parallel$ which was applied parallel to the two-dimensional electron gas (2DEG) layer. Under low in-plane fields, $B_\parallel < 7$ T, the radiative recombination of the photoexcited hole with the 2DEG gives rise to a broad PL band that shifts quadratically with $B_\parallel$. This band transforms into a narrow PL line whose peak energy $E$ shifts linearly with $B_\parallel$ in the range of $10-33$ T. The slope of the linear $E(B)$ dependence was measured as $\alpha_{ex} = 0.77 \pm 0.02$ meV/T in all the studied structures. The same linear slope is also measured in the PL spectra of bulk, undoped GaAs under high $B$. We thus attribute the sharp PL line observed in the doped heterostructures to magnetoexcitons that are photogenerated outside the 2DEG layer by a geminate formation process. The slope of the magnetoexciton energy dependence on $B_\parallel$ is compared with that measured for unbound-electron-hole Langdau level transitions under a perpendicular $B_\perp$. The ratio of the measured slopes, $\alpha_{ex}/\alpha_0 = 0.8$, is found to be equal to the ratio of the reduced excitonic mass to the reduced cyclotron mass of GaAs.

DOI: 10.1103/PhysRevB.76.075344

PACS number(s): 78.55.-m, 71.35.-y

I. INTRODUCTION

The radiative recombination of a two-dimensional electron gas (2DEG) with photoexcited free holes in modulation-doped heterostructures [quantum well (MDQW) and single heterojunction (SHJ)] under a perpendicular applied magnetic field $B_\parallel$ gives rise to the photoluminescence (PL) (2De-h PL) spectra that contain valuable spectroscopic information on the 2DEG many-body interaction, particularly in the quantum Hall effect regime.1-4 The existing theoretical models for the 2De-h PL consider the recombination of the two-dimensional (2D) electron with a valence hole that is separated by a distance of $d_0$ from the 2DEG layer.5 All the dynamical processes, namely, photoexcitation, space-time evolution of the holes, as well as an exciton formation, are ignored.

The importance of dynamical processes in photoexcited heterostructures containing a 2DEG was manifested in the resonant enhancement of inelastic light scattering by the 2DEG when the photon energy is resonant with quantum-well excitons having energies higher than the Fermi energy.6 Dynamical processes also control the occupation of photoexcited states and give rise to the coexistence of several high-energy PL lines in the low-temperature magneto-PL spectra of MDQWs at electron filling factors $\nu < 1$.7 Another case is a remarkable transformation of the excitonic recombination spectrum in high-quality modulation-doped SHJs to 2De-h PL spectrum that occurs with increasing $B_\perp$ (at $\nu < 2$).8,9 This was explained by the dissociation of the excitons, generated in the thick GaAs layer, at the 2DEG interface with subsequent free hole recombination with the 2D electrons.4 Under low magnetic field applied parallel to the SHJ’s interface ($B_\perp < 1-2$ T), 2De-h PL intensity enhancement and spectral modifications were discovered and explained by a free hole spatial redistribution.7

At $B_\parallel = 0$, an electron and a hole photogenerated at the same point of space (geminate e-h) are instantly separated since they have momenta that are equal in magnitude and opposite in direction. Then, the hole can recombine with a 2D electron or bind an electron by the bimolecular exciton formation mechanism.8 An applied magnetic field strongly affects the motion of the photoexcited charge carriers and their spatial distribution at rather low $B$.5 At high $B$, the exciton binding energy significantly increases.10,11

In the present paper, we report on the effect of a high magnetic field, applied parallel to the 2DEG plane ($B_\parallel < 33$ T), on the photoexcited system dynamics which, in turn, affects the PL spectrum of modulation-doped heterostructures. In all the structures studied here, a transformation is observed from a broad 2De-h PL spectrum at low $B_\parallel < 7$ T (reported in our previous study)7 to a narrow PL line at high $B$. The peak energy of this line shifts linearly with $B$ above 10 T. The slope of the linear $E(B)$ dependence was measured as $\alpha_{ex} = 0.77 \pm 0.02$ meV/T in all the studied samples. We attribute this PL line to magnetoexcitons that are photogenerated outside the 2DEG layer by a geminate formation process.

The paper is laid out as follows. Section II details the experimental procedure followed (in Sec. III) by the experimental results. In Sec. IV, we discuss the effects of $B_\parallel$ on the
2De-h PL spectra in MDQWs and SHJs. In Sec. V, geminate-exciton formation under a high magnetic field is considered. The dependence of the magnetoexciton energy on \(B_y\) is compared with that of the lowest Landau transitions between conduction and valence subbands under \(B_z\) and is analyzed in Sec. VI.

II. EXPERIMENTAL DETAILS

Several MDQW and SHJ GaAs/AlGaAs samples were studied, all grown along the (100) direction by molecular beam epitaxy. The MDQW samples contain a single quantum well of various widths (44, 25, and 20 nm), and the SHJ samples have a thick GaAs buffer layer (width of 1 \(\mu\)m). The \(n\)-type \(\delta\)-doped layer is separated from the interface by an undoped AlGaAs layer (widths of 50–100 nm). The 2DEG density range was \(n_{2D}= (0.7-2.5) \times 10^{11} \text{ cm}^{-2}\) and the 2DEG mobility was \(\mu_x = (2-5) \times 10^6 \text{ cm}^2/\text{V s}\) at 2 K. A Ti:sapphire laser illuminated the sample, and the incident light intensity (photon energy of 1.58 eV) was kept below \(10^{-2} \text{ W/cm}^2\). A single optical fiber was used for photoexcitation and PL collection from the sample. The sample was mounted in a cryostat and was immersed in liquid \(^3\)He at temperature of \(T_L=1.2\) K. The cryostat was placed in an electromagnet producing a magnetic field that reached a maximum value of 33 T. The sample plane (the 2DEG layer) was parallel to \(B_y\), while the photoexciting laser beam and the outgoing PL were directed perpendicularly to the sample plane. The PL was measured with a spectrometer equipped with a cooled charge coupled device, and the spectral resolution was \(\sim 0.1\) meV.

III. EXPERIMENTAL RESULTS

Figure 1(a) shows a series of PL spectra measured at increasing \(B_y\) for the 44-nm-wide MDQW (\(n_{2D}=1 \times 10^{11} \text{ cm}^{-2}\)). The panel on the left hand side displays the PL spectra at the low-\(B_y\) range. At \(B_y=0\), a typical 2De-h PL spectrum of MDQWs is observed. The PL intensity reaches a maximum at the low-energy side (\(E_g\)), and it vanishes at \(E=E_g+E_F\) (\(E_F\) is the 2DEG Fermi energy). Thus, the PL bandwidth is of 3.6 meV. As \(B_y\) increases to 8 T, the spectrum transforms into an asymmetric PL band with its maximum intensity at the high-energy side showing a blue nonlinear (diamagnetic) shift.\(^7\)

For \(B_y > 9\) T (right panel of Fig. 1(a)), the PL spectrum is dominated by a narrow line (width <0.5 meV) whose peak energy dependence on \(B_y\), \(E(B_y)\), is plotted in Fig. 1(b) (open circles). It is well approximated by a linear dependence with a slope of 0.79 meV/T (dashed line). The integrated PL intensity \(J\) is also shown in Fig. 1(b) (crosses). It varies little (<25\%) in the range of 0–33 T. A similar PL behavior was observed for all the studied MDQWs; however, the \(B_y\) values at which the linear \(E(B_y)\) dependence starts are higher for the narrower (25 and 20 nm wide) MDQWs.

Figure 2 shows a similar series of the PL spectra obtained with the SHJ sample having \(n_{2D}=1.5 \times 10^{11} \text{ cm}^{-2}\). The main difference between the SHJ and MDQW spectra is clearly seen in the low field range, \(B_y < 3\) T. At \(B_y=0\), the SHJ spectrum consists of two narrow excitonic lines that originate in the 1-\(\mu\)m-thick GaAs buffer layer: the high-energy line is due to free excitons and the low-energy one to localized excitons. The very weak, broad band below the excitons is dominated by a narrow line (width <0.5 meV) whose peak energy dependence on \(B_y\) is very low (in SHJs having \(n_{2D}=1 \times 10^{11} \text{ cm}^{-2}\)), because the strong built-in electric field \(E_{kj}\) accelerates the holes away from the GaAs/AlGaAs interface where the 2DEG forms.\(^2\)

A remarkable modification of the SHJ PL spectrum upon applying a low in-plane field (\(B_y < 4\) T) is seen in left panel of Fig. 2. With increasing \(B_y\), the 2De-h PL intensity increases while the exciton PL intensity diminishes. The spectrum transforms into a strongly asymmetric band with its maximum at the high-energy PL side, and the excitonic lines are hardly seen.\(^3\) With further field increase (\(B_y > 8\) T, right panel of Fig. 2), the PL spectrum narrows and becomes sym-
FIG. 2. PL spectra of a SHJ under in-plane $B$. The low-field spectra (left panel) show a transformation from the excitonic PL to 2De-h PL occurring at $B_l < 3$ T. At higher $B_l$ (right panel), the 2De-h PL band transforms into a geminate-exciton PL line.

metric. The PL peak energy shows an $E(B_l)$ dependence that is similar to that of the MDQW. Similar PL evolution with $B_l$ was observed for several other SHJ samples that were studied here.

Since the SHJs contain a 1-$\mu$m-thick, undoped GaAs buffer layer, we found it beneficial to compare their magneto-PL spectra under $B_l$ with those of a bulk, undoped GaAs layer (10 $\mu$m-thick). Figure 3 (right panel) displays some magneto-PL spectra of this GaAs layer, observed at several $B$ values. At $B=0$, the spectrum consists of free (FE) and bound exciton PL lines, and as $B$ increases, the free exciton line dominates the spectrum. Under high fields ($B > 15$ T), it splits into two lines. The peak energy $E$ dependence on $B$ (of the free exciton line and of the center of gravity for the two split lines) is plotted in Fig. 3 (open circles). This curve is fitted with a quadratic (diamagnetic) exciton shift for $B < 7$ T, and at higher fields, it is well approximated by a linear function with a slope of 0.77 meV/T (solid line).

In Fig. 4(a), we compare representative PL spectra of two SHJs having different $n_{2D}$, measured at $B_l=6$ and 26 T, with those of the undoped GaAs sample. The SHJ spectra show similar shifts as those of the undoped GaAs sample, but the latter has impurity-bound exciton bands, which are lacking in the former. Also, the PL line of the SHJ with higher $n_{2D}$ is observed at lower energy than that of the lower density SHJ, and both are still lower than the GaAs free magnetoexciton. The $E(B)$ dependence of these three samples is compared in Fig. 4(b). In the low-$B$ range [inset of Fig. 4(b)], the $E(B)$ dependencies for the SHJs follow the diamagnetic shift of free (bound) excitons of bulk GaAs (at $B < 4$, the FE peak energies coincide for all three samples). As the excitonic PL lines in the SHJs are transformed into the 2De-h PL band, the PL peak energy in the range of 2–10 T shows a diamagnetic shift, which is weaker than that of the free exciton.

In the range of 10–33 T, the PL line positions of the studied SHJs samples move almost in parallel to that of the bulk FE line. All $E(B)$ dependencies are approximated by straight lines with a slope of 0.77±0.02 meV/T. The energy differences between the $E(B)$ line for the SHJs and the bulk GaAs sample are $\approx 1$ meV [for SHJ(a), low $n_{2D}$] and $\approx 2$ meV [for SHJ(b), high $n_{2D}$] as seen in Fig. 4(b). It is important to notice that the integrated PL intensity $J$ varies only slightly in the entire range of 0–33 T.

IV. 2De-h SPECTRAL CHANGE UNDER IN-PLANE $B_l < 10$ T

Before discussing the PL spectra that are observed under a high in-plane magnetic field in various modulation-doped heterostructures, we briefly review the physical model of a
FIG. 4. (a) The PL spectra of two SHJs having different $n_{2D}$ and an undoped, bulk GaAs sample at two $B_\parallel$ values. (b) The PL peak energy dependencies on $B$ for these samples. The inset shows the low-$B_\parallel$ range.

2DEG subjected to a built-in electric field $E_{E\parallel}^c$ and an in-plane magnetic field $B_\parallel^c$ (see Fig. 5). This crossed field configuration causes an electron drift in the $y$ direction, and it leads to a shift of the electron subband minimum to high wave vectors $k_{E\parallel}^y$ and to an increase in the in-plane electron effective mass (in the $y$ direction). We reported recently on the effect of an in-plane magnetic field on the 2De-h PL spectra of heterostructures in the range of $B_\parallel < 7$ T. The 2De-h PL spectral modifications with increasing $B_\parallel$ were then explained by invoking direct optical transitions in an indirect band gap structure that results from the shift in $k$ space of the conduction and valence subbands by $k_{E\parallel}^y = d_0/L_{E\parallel}$ [as shown schematically in Fig. 5(b)]. Here, $d_0$ is the 2De-h spatial separation and $L_{E\parallel}$ is the magnetic length. In addition, the 2DEG Fermi energy decreases due to the electron effective mass increase. For such an indirect band gap structure, the direct optical transitions giving rise to the same emitted photon energy involve the conduction- and valence-) band states of various energies (according to the momentum and energy conservation laws). This is in contrast to the optical transitions occurring in the direct band gap structure (e.g., at $B = 0$), and thus, a dramatic modification of the 2De-h spectrum is caused by applying in-plane $B_\parallel$.

2DEG subjected to a built-in electric field $E_{E\parallel}^c$ and an in-plane magnetic field $B_\parallel^c$ (see Fig. 5). This crossed field configuration causes an electron drift in the $y$ direction, and it leads to a shift of the electron subband minimum to high wave vectors $k_{E\parallel}^y$ and to an increase in the in-plane electron effective mass (in the $y$ direction). We reported recently on the effect of an in-plane magnetic field on the 2De-h PL spectra of heterostructures in the range of $B_\parallel < 7$ T. The 2De-h PL spectral modifications with increasing $B_\parallel$ were then explained by invoking direct optical transitions in an indirect band gap structure that results from the shift in $k$ space of the conduction and valence subbands by $k_{E\parallel}^y = d_0/L_{E\parallel}$ [as shown schematically in Fig. 5(b)]. Here, $d_0$ is the 2De-h spatial separation and $L_{E\parallel}$ is the magnetic length. In addition, the 2DEG Fermi energy decreases due to the electron effective mass increase. For such an indirect band gap structure, the direct optical transitions giving rise to the same emitted photon energy involve the conduction- and valence-) band states of various energies (according to the momentum and energy conservation laws). This is in contrast to the optical transitions occurring in the direct band gap structure (e.g., at $B = 0$), and thus, a dramatic modification of the 2De-h spectrum is caused by applying in-plane $B_\parallel$.

The PL spectra for the 44-nm-wide MDQW [Fig. 1(a), left panel] show spectral modifications similar to those previously studied for the 25-nm-wide MDQW. However, the PL transformations for the 44-nm-wide MDQW are observed at lower $B_\parallel$, and this is due to larger electron-hole separation since $k_{E\parallel}^y = d_0/B_\parallel$. Moreover, the 2De-h PL band in the studied sample significantly narrows from 3.6 meV ($B = 0$) to 0.9 meV at $7$ T. Such a narrowing at large $k_{E\parallel}^y$ was also obtained in the developed model.

In SHJs, the in-plane magnetic field causes spatial redistribution of the photoexcited holes, in addition to the band gap modification discussed above. Electrons and holes (e-h) are photoexcited across the whole 1-$\mu$m-wide undoped buffer GaAs layer. The photoexcited holes drift in the built-in electric field $E_{E\parallel}$ formed by the positive charged donors in the AlGaAs barrier. Assuming homogeneous e-h photogeneration in the GaAs layer with a rate $G$, a steady-state spatial distribution of free holes along the $z$ axis, $p(z)$, in the presence of the constant $E_{E\parallel}$ can be obtained from the equation

$$G - p/\tau + \mu E_{E\parallel}(dp/dz) = 0,$$

and its solution is as follows:

$$p(z) = G\tau[\exp(\mu E_{E\parallel}z) - 1].$$

Here, $\tau$ is the hole lifetime and $L_E = \mu E E_{E\parallel}$ is the drift length ($\mu$ is the hole mobility). The expected spatial distribution of the itinerant holes is schematically drawn in Fig.
of a magnetic field

In the previous discussion of the 2De-h PL modification induced by a magnetic field, it was assumed that an electron and a hole photogenerated at the same point of space (geminate e-h) are instantly separated, and then, the hole can recombine with the 2DEG. The geminate electron and hole moving in opposite directions lose their mutual memory (and thus become unbound) after a time interval of \( \theta \). This time can be estimated using the model of electron capture by an attractive center (hole).\(^{19}\) In this model, the electron is captured if it loses the energy of \( kT_e \) being in the sphere of radius \( R_T=\varepsilon/kT_L \) surrounding the hole (\( \varepsilon \) is the dielectric constant).

At \( B=0 \), the geminate e-h pair will be separated by a distance of \( R_T^e \) for \( \theta=R_T^e/V=10^{-11} \) s (taking a relative velocity of \( V=\sim 10^7 \) cm/s and \( T_L=2 \) K). This time is much shorter than the energy relaxation time due to electron-phonon scattering, \( \tau_e=\tau_m (kT_L/4m_e^2s) \sim 5 \times 10^{-10} \) s.\(^{20}\) Here, \( s \) is the sound velocity and \( \tau_m \sim 4 \times 10^{-11} \) s is the momentum relaxation time for electrons having mobility above \( 10^6 \) cm²/V s. Since \( \theta<\tau_e \), the geminate e-h pair does not directly form an exciton and is separated. Thus, the 2De-h recombination takes place before the slow-acting bimolecular exciton formation occurs.\(^{21}\)

Under a high magnetic field, the geminate-exciton formation process controls the PL of semiconductors. The importance of geminate recombination was considered in several theories,\(^{22,23}\) in connection with the observed enhancement of PL intensity\(^{24}\) and Raman light scattering efficiency\(^{24}\) under a magnetic field.

We propose that the observed PL spectral evolution under high magnetic fields (Figs. 1–4) is due to a transformation of the 2De-h PL into the PL of geminate-formed magnetoexcitons.

In the plane perpendicular to the magnetic field, the photogenerated electron and hole move on the same circular orbits and in the opposite directions (or on close cycloids in the case of \( E_x^e \) and \( B_y^e \)). Their separation in this plane occurs by a diffusion process with a coefficient \( D=\tau_m r_B^2/\tau_e \), where \( r_B \) is the cyclotron radius.\(^{25}\) The geminate electron-hole pair conserves their mutual memory during a time of \( \theta=R_T^e/D = (R_T^e/r_B^2)\tau_m \). At \( B>5 \) T, \( \theta \) is of the order of \( 10^{-11} \) s and \( \theta<\tau_e \). Thus, the geminate electron and hole lose energy and bind into an exciton before they are separated (the geminate pair moving parallel to \( B \), in general, will be separated). It is worth noting that the geminate-exciton formation mechanism is most important for polymers and semiconductors having low carrier mobility where geminate pairs are slowly separated even in the absence of \( B. \)

Thus, we attribute the narrow PL lines emerging in all MDQWs and SHJs under high \( B \) to free, geminate-formed magnetoexcitons. The weak integrated PL intensity dependence on \( B \), measured in all the studied samples [Fig. 1(b)] is also explained by the transformation of the indirect in \( k \)-space 2De-h PL to the geminate-formed free magnetoexciton PL. This underlines the importance of the dynamical processes in controlling the PL spectrum. Geminate-formed magnetoexcitons also play an important role in the interpre-
VI. FREE EXCITONS UNDER A HIGH MAGNETIC FIELD

In the range of $B_\perp=10$–33 T, all the studied GaAs-based structures exhibit a linear $E(B)$ dependence with the same slope, $\alpha_{ex}=0.077\pm0.02$ meV/T (Figs. 1–4). For the SHJ samples subjected to a perpendicular field $B_\perp$, the high-energy PL line (free exciton PL) has an $E(B)$ dependence which is similar to that of $E(B)$, while the low-energy, 2De-h PL line shows a different $E^{\perp L}(B_\perp)$ dependence.4 The latter is determined by the shift of the lowest-energy electron-hole Landau transition $E^{\perp L}$ with increasing $B_\perp$.

In MDQWs subjected to $B_\perp$, the main (lowest energy, 2De-h) PL line follows the $E^{\perp L}(B_\perp)$ dependence at low $B_\perp$ (at filling factors $\nu>2$). At higher $B_\perp$ (above $\sim10$ T), excitonlike lines (charged and neutral excitons) dominate the PL spectrum of GaAs-based MDQWs (having $n_{2D}=2\times10^{11}$ cm$^{-2}$). Their $E(B)$ can also be approximated by a nearly linear dependence that has the same slope of $0.77\pm0.02$ meV/T.2,6

Such a universal linear $E(B)$ dependence of the geminate-formed exciton PL line observed at high $B_\perp$ deserves special consideration. Its slope $\alpha_{ex}$ is likely to be an important inherent parameter which is determined by the $B$ dependence of the exciton binding energy $E_X(B)$, since $E(B)=E^{\perp L}(B)+E_X(B)$.

For an unbound electron-hole pair, the energy of the optical transitions between the lowest Landau levels of the conduction and valence subbands varies as

$$E^{\perp L}(B_\perp)=E_{go}+(1/2)\langle\hbar eL\mu_c\rangle B_\perp,$$

where $E_{go}$ is the band gap energy at $B=0$ and $\mu_c=m_e/m_h/(m_e+m_h)$ is the reduced electron-hole cyclotron effective mass. In the approximation of simple, parabolic conduction and valence bands,27 the slope of the linear $E^{\perp L}(B_\perp)$ dependence is $\alpha_{ex}=(1/2)\langle\hbar eL\mu_c\rangle=0.96$ meV/T for electron and hole cyclotron effective masses of bulk GaAs, $m_e=0.068 m_0$ and $m_h=0.52 m_0$.28 For a 20-nm QW, $\alpha_0=1.02$ meV/T (for $m_3=0.35 m_0$).29

The dotted line in Fig. 1(b) shows the $E(B)$ dependence of the lowest-electron-hole Landau level transition for the 44 nm MDQW. From this line, we get $\alpha_0=0.96$ meV/T, and thus $\mu_c=0.06 m_0$. This determines the hole cyclotron mass value of $0.02 m_0$.

The obtained $E(B)$ dependence for the geminate-formed exciton PL suggests that the magnetoexciton binding energy $\delta E_X$ depends almost linearly on $B$ in the range of 10–33 T. The $\delta E_X(B)$ dependence was analyzed in several theoretical approximations.10 For simple band structures, these theories do not predict a linear $E(B)$ [or $\delta E_X(B)$] dependence in the range of

$$\gamma=\alpha_{ex}B/\delta E_X(0)=\left[\frac{\hbar^2 e^2}{\mu_c^3}\right]B \sim 2-7,$$

which corresponds to the $B$ range of 10–33 T at $\mu_c=0.06 m_0$ and $\kappa=13$.

It is of interest to compare the results with the ones obtained by other authors and, in particular, with the calculations of the exciton binding energy $\delta E_X$. The latter is determined by the shift of the lowest-energy electron-hole Landau level transition for the exciton Bohr radius.11

VII. CONCLUSIONS

The effects of a magnetic field, applied parallel to the 2DEG layer, on the low-temperature photoluminescence spectrum of modulation-doped, GaAs-based heterostructures (single quantum wells and heterojunctions), are studied for $B_\perp$ up to 33 T. At $B_\perp<7$ T, the remarkable changes of the 2DEG free hole PL spectra are due to the $B_\perp$-induced direct-indirect band gap transformation.7,13,14

At $B_\perp>10$ T, the PL spectrum observed in all the studied modulation-doped heterostructures as well as undoped, bulk GaAs consists of a narrow PL line whose peak energy $E$ shifts linearly with $B$. We attribute this sharp PL line to magnetoexcitons that are photogenerated by a geminate formation process.

The linear $E(B)$ dependence of the geminate-formed excitons in the QWs subjects to a perpendicular field is well described by the expression

$$E_X(B)=E_{X0}+\alpha_{ex}B.$$

From the measured $\alpha_{ex}B/\delta E_X(0)$ ratio of $\sim0.8$, we get $\mu_c\sim0.04 m_0$. Remarkably, this value coincides with the reduced excitonic mass $\mu_0^{-1}=m_0^{-1}+(m_h^{-1})^{-1}$ that defines the exciton Bohr radius.11 Here, $m_h$ is the hole effective mass in spherical valence-band approximation. Thus, the simple empirical expression [Eq. (5)] describes well the PL exciton energy behavior under a high magnetic field.

At low $B$ ($\gamma<1$), the $E(B)$ dependence shown in Fig. 3 is described by the expression for the excitonic diamagnetic shift obtained by perturbation theory: $E(B)=E_{X0}+\Delta E_X=\gamma E_{X0} B^2/2\kappa^2=4.2$ meV using the $\mu_0$ value. Thus, the magnetoexciton energy dependence in the entire $B$ range is obtained by two simple, empirical expressions that use three well-known GaAs parameters, $\mu_0$, $\gamma$, and $\kappa$.

As seen from Fig. 4, the $E(B)$ dependence for the geminate-formed excitons in the SHJs shifts to lower energy with increasing the 2DEG density. This can be explained invoking a shallow well for the excitons that is formed near the interface with the 2DEG in the SHJs.32 Due to the built-in electric field gradient, the excitons photogenerated in the GaAs buffer layer drift to the higher $E_{Xj}$ region and are localized in the well. Geminate-formed excitons are likely to occupy this well, and the localization energy increases as $E_{Xj}$ becomes higher (for increased $n_{2D}$); thus, the exciton PL peak shifts to low energy.
magnetoexcitons is characterized by a universal slope of \( \alpha_{\text{ex}} = 0.77 \pm 0.02 \text{ meV/T} \). It is different from that of unbound-electron-hole Landau level transitions under a perpendicular \( B \). The ratio of these slopes (\( \alpha_{\text{ex}} / \alpha_{0} \approx 0.8 \)) is equal to the ratio of the reduced excitonic mass to the reduced cyclotron mass, \( \mu_{\text{ex}} / \mu_{c} \) of GaAs. We show that two simple, empirical expressions based on three well-known GaAs parameters \( \mu_{0} \), \( \mu_{c} \), and \( \kappa \), allow us to describe the magnetoexciton energy dependence in the entire \( B \) range.

33. Y. V. Zhilyaev, V. V. Rossin, T. V. Rossinka, and V. V. Travnikov, JETP Lett. 49, 564 (1989).
37. At 30 T, the lowest electron energy (0 Landau level) shifts by ~25 meV, and \( m_{c} \) increases by <5% due to conduction-band nonparabolicity. Such a nonparabolicity can be taken into account by a slight slope change (by 0.02 meV/T) for the studied \( B \) range.