Measurements of long-range azimuthal anisotropies and associated Fourier coefficients for \( pp \) collisions at \( \sqrt{s} = 5.02 \) and 13 TeV and \( p + \text{Pb} \) collisions at \( \sqrt{s_{\text{NN}}} = 5.02 \) TeV with the ATLAS detector

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(Received 26 September 2016; revised manuscript received 13 June 2017; published 22 August 2017)

ATLAS measurements of two-particle correlations are presented for \( \sqrt{s} = 5.02 \) and 13 TeV \( pp \) collisions and for \( \sqrt{s_{\text{NN}}} = 5.02 \) TeV \( p + \text{Pb} \) collisions at the LHC. The correlation functions are measured as a function of relative azimuthal angle \( \Delta \phi \), and pseudorapidity separation \( \Delta \eta \), using charged particles detected within the pseudorapidity interval \( |\eta| < 2.5 \). Azimuthal modulation in the long-range component of the correlation function, with \( |\Delta \eta| > 2 \), is studied using a template fitting procedure to remove a “back-to-back” contribution to the correlation function that primarily arises from hard-scattering processes. In addition to the elliptic, \( \cos(2\Delta \phi) \), modulation observed in a previous measurement, the \( pp \) correlation functions exhibit significant \( \cos(3\Delta \phi) \) and \( \cos(4\Delta \phi) \) modulation. The Fourier coefficients \( v_n \), associated with the \( \cos(n\Delta \phi) \) modulation of the correlation functions for \( n = 2–4 \) are measured as a function of charged-particle multiplicity and charged-particle transverse momentum. The Fourier coefficients are observed to be compatible with \( \cos(n\phi) \) modulation of per-event single-particle azimuthal angle distributions. The single-particle Fourier coefficients \( v_n \) are measured as a function of charged-particle multiplicity, and charged-particle transverse momentum for \( n = 2–4 \). The integrated luminosities used in this analysis are, 64 nb\(^{-1}\) for the \( \sqrt{s} = 13 \) TeV \( pp \) data, 170 nb\(^{-1}\) for the \( \sqrt{s} = 5.02 \) TeV \( pp \) data, and 28 nb\(^{-1}\) for the \( \sqrt{s_{\text{NN}}} = 5.02 \) TeV \( p + \text{Pb} \) data.

DOI: 10.1103/PhysRevC.96.024908

I. INTRODUCTION

Observations of azimuthal anisotropies in the angular distributions of particles produced in proton-lead (\( p + \text{Pb} \)) collisions at the LHC [1–5] and in deuteron-gold (\( d + \text{Au} \)) [6–8] and \( ^3\text{He} + \text{Au} \) [9] collisions at RHIC have garnered much interest due to the remarkable similarities between the phenomena observed in those colliding systems and the effects of collective expansion seen in the \( \text{Pb} + \text{Pb} \) and \( \text{Au} + \text{Au} \) collisions [3,10–13].\(^1\) The most intriguing feature of the azimuthal anisotropies is the “ridge”: an enhancement in the production of particles with small azimuthal angle (\( \phi \)) separation which extends over a large range of pseudorapidity (\( \eta \)) separation [1,2,14,15]. In \( \text{Pb} + \text{Pb} \) [3,10–13] and \( p + \text{Pb} \) [1–3] collisions, the ridge is understood to result from sinusoidal modulation of the single-particle azimuthal angle distributions, and the characteristics of the modulation, for example the \( p_T \) dependence [16], are remarkably similar in the two systems [4].

While the modulation of the azimuthal angle distributions in \( \text{Pb} + \text{Pb} \) collisions is understood to result from the geometry of the initial state and the imprinting of that geometry on the angular distributions of the particles by the collective expansion (see, e.g., [17–19] and references therein), there is, as yet, no consensus that the modulation observed in \( p + \text{Pb} \) collisions results from the same mechanism. Indeed, an alternative explanation for the modulation using perturbative QCD and assuming saturated parton distributions in the lead nucleus is capable of reproducing many features of the \( p + \text{Pb} \) data [20–29]. Nonetheless, because of the many similarities between the \( p + \text{Pb} \) and \( \text{Pb} + \text{Pb} \) observations, extensive theoretical and experimental effort has been devoted to address the question of whether the strong-coupling physics understood to be responsible for the collective dynamics in \( A + A \) may persist in smaller systems [30–40].

A recent study by the ATLAS Collaboration of two-particle angular correlations in proton–proton (\( pp \)) collisions at center-of-mass energies of \( \sqrt{s} = 13 \) and 2.76 TeV obtained results that are consistent with the presence of an elliptic or \( \cos(2\phi) \) modulation of the per-event single particle azimuthal angle distributions [41]. This result suggests that the ridge previously observed in \( \sqrt{s} = 7 \) TeV \( pp \) collisions [14] results from modulation of the single-particle azimuthal angle distributions similar to that seen in \( \text{Pb} + \text{Pb} \) and \( p + \text{Pb} \) collisions. Indeed, the \( p_T \) dependence of the modulation was similar to that observed in the other systems. Unexpectedly, the amplitude of the modulation relative to the average differential particle yield \( \langle dN/d\phi \rangle \), was observed to be constant, within uncertainties, as a function of the charged particle multiplicity of the \( pp \) events and to be consistent between the two energies, suggesting that the modulation is an intrinsic feature of high-energy \( pp \) collisions. These results provide further urgency to address the question of whether strong coupling and collective dynamics play a significant role in small systems, including the smallest systems accessible at collider energies—\( pp \) collisions. Since the elliptic modulation observed in the \( pp \) data is qualitatively

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similar to that seen in $p + \text{Pb}$ collisions, a direct, quantitative comparison of $pp$ and $p + \text{Pb}$ measurements is necessary for evaluating whether the phenomena are related.

The modulation of the single-particle azimuthal angle distributions in $A + A$, $p/d + A$, and, most recently, $pp$ collisions is usually characterized using a set of Fourier coefficients $v_n$, that describe the relative amplitudes of the sinusoidal components of the single-particle distributions. More explicitly, the azimuthal angle distributions of the particles are parameterized according to

$$
\frac{dN}{d\phi} = \frac{dN}{d\phi} \left[ 1 + \sum_n 2v_n \cos[n(\phi - \Psi_n)] \right],
$$

where the average in the equation indicates an average over azimuthal angle. Here, $\Psi_n$ represents one of the $n$ angles at which the $n$-th-order harmonic is maximum; it is frequently referred to as the event-plane angle for the $n$th harmonic. In $\text{Pb} + \text{Pb}$ collisions, $n = 2$ modulation is understood to primarily result from an elliptic anisotropy of the initial state for collisions with nonzero impact parameter; that anisotropy is subsequently imprinted onto the angular distributions of the produced particles by the collective evolution of the medium, producing an elliptic modulation of the produced particle azimuthal angle distributions in each event [17,42,43]. The higher ($n > 2$) harmonics are understood to result from position-dependent fluctuations in the initial-state energy density which produce higher-order spatial eccentricities that extend over a wide range of $\Delta \eta$. The jet peak can be avoided by studying the long-range part of the correlation function, which is typically chosen to be $|\Delta \eta| > 2$. Because the jet contribution to the two-particle correlation function is not localized in $\Delta \eta$, that contribution has to be subtracted from the measured correlation function, typically using the correlation function measured in low-multiplicity (“peripheral”) events. Different peripheral subtraction methods have been applied for the $p + \text{Pb}$ measurements in the literature [2,4]; all of them relied on the “zero yield at minimum” (ZYAM) hypothesis to subtract an assumed flat combinatoric component from the peripheral reference correlation function. These methods were found to be inadequate for $pp$ collisions, where the amplitude of the dijet enhancement at $\Delta \phi = \pi$ is much larger than the (absolute) amplitude of the sinusoidal modulation. For the measurements in Ref. [41], a template fitting method, described below, was developed which is better suited for extracting a small sinusoidal modulation from the data. Application of the template fitting method to the $pp$ data provided an excellent description of the measured correlation functions. It also indicated substantial bias resulting from the application of the ZYAM-subtraction procedure to the peripheral reference correlation function due to the nonzero $v_{2,2}$ in low-multiplicity events. As a result, the measurements presented in Ref. [41] were obtained without using ZYAM subtraction. However, the previously published $p + \text{Pb}$ data [4] may be susceptible to an unknown bias due to the use of the ZYAM method. Thus, a reanalysis of the $p + \text{Pb}$ data is both warranted and helpful in making comparisons between $pp$ and $p + \text{Pb}$ data.

To address the points raised above, this paper extends previous measurements of two-particle correlations in $pp$ collisions at $\sqrt{s} = 13$ TeV using additional data acquired by ATLAS subsequent to the measurements in Ref. [41] and provides new measurements of such correlations in $pp$ collisions at $\sqrt{s} = 5.02$ TeV. It also presents a reanalysis of two-particle correlations in $5.02$ TeV $p + \text{Pb}$ collisions and presents a direct comparison between the $pp$ and $p + \text{Pb}$ data at the same per-nucleon center-of-mass energy as well as a comparison between the $pp$ data at the two energies. Two-particle Fourier coefficients $v_{n,n}$ are measured, where statistical precision allows, for $n = 2, 3,$ and 4 as a function of charged-particle multiplicity and transverse energy. Measurements are performed for different $p_T$ and $p_T^\text{V}$ intervals and the factorization of the resulting $v_{n,n}$ values is tested.

This paper is organized as follows. Section II gives a brief overview of the ATLAS detector subsystems and triggers used in this analysis. Section III describes the data sets and the offline selection criteria used to select events and reconstruct charged-particle tracks. The variables used to characterize the “event activity” of the $pp$ and $p + \text{Pb}$ collisions are also described. Section IV gives details of the two-particle correlation method. Section V describes the template fitting of the two-particle correlations, which was originally developed

In addition to the sinusoidal modulation, the two-particle correlation functions include contributions from hard-scattering processes that produce a jet peak centered at $\Delta \phi = \Delta \eta = 0$ and a dijet enhancement at $\Delta \phi = \pi$ that extends over a wide range of $\Delta \eta$. The jet peak can be avoided by studying the long-range part of the correlation function, which is typically chosen to be $|\Delta \eta| > 2$. Because the dijet contribution to the two-particle correlation function is not localized in $\Delta \eta$, that contribution has to be subtracted from the measured correlation function, typically using the correlation function measured in low-multiplicity (“peripheral”) events. Different peripheral subtraction methods have been applied for the $p + \text{Pb}$ measurements in the literature [2,4]; all of them relied on the “zero yield at minimum” (ZYAM) hypothesis to subtract an assumed flat combinatoric component from the peripheral reference correlation function. These methods were found to be inadequate for $pp$ collisions, where the amplitude of the dijet enhancement at $\Delta \phi = \pi$ is much larger than the (absolute) amplitude of the sinusoidal modulation. For the measurements in Ref. [41], a template fitting method, described below, was developed which is better suited for extracting a small sinusoidal modulation from the data. Application of the template fitting method to the $pp$ data provided an excellent description of the measured correlation functions. It also indicated substantial bias resulting from the application of the ZYAM-subtraction procedure to the peripheral reference correlation function due to the nonzero $v_{2,2}$ in low-multiplicity events. As a result, the measurements presented in Ref. [41] were obtained without using ZYAM subtraction. However, the previously published $p + \text{Pb}$ data [4] may be susceptible to an unknown bias due to the use of the ZYAM method. Thus, a reanalysis of the $p + \text{Pb}$ data is both warranted and helpful in making comparisons between $pp$ and $p + \text{Pb}$ data.

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and evaluating whether $v_n(p_T^V)$ depends on the choice of $p_T^V$.

The $vn,n$ coefficients can be measured using two-particle angular correlation functions, which, when evaluated as a function of $\Delta \phi = \phi^a - \phi^b$, where $a$ and $b$ represent the two particles used to construct the correlation function, have an expansion similar to that in Eq. (1):

$$
\frac{dN_{\text{pair}}}{d\Delta \phi} = \left[ 1 + \sum_n 2v_{n,n} \cos(n(\Delta \phi)) \right].
$$

If the modulation of the two-particle correlation function arises solely from the modulation of the single-particle distributions, then $v_{n,n} = v_n^2$. Often, the two-particle correlations are measured using different transverse momentum ($p_T$) ranges for particles $a$ and $b$. Since the modulation is observed to vary with $p_T$, then

$$
v_{n,n}(p_T^a, p_T^b) = v_n(p_T^a) v_n(p_T^b)
$$

if the modulation of the correlation function results solely from single-particle modulation.\footnote{See Refs. [52,53] for analyses of the breakdown of factorization.} This “factorization” hypothesis can be tested experimentally by measuring $v_{n,n}(p_T^a, p_T^b)$ for different ranges of $p_T^a$ and estimating $v_n(p_T^a)$ using

$$
v_n(p_T^a) = \frac{v_{n,n}(p_T^a, p_T^b)}{v_{n,n}(p_T^b, p_T^b)} \sqrt{v_{n,n}(p_T^b, p_T^b)}\text{.}
$$

\footnote{See Refs. [52,53] for analyses of the breakdown of factorization.}
TABLE I. The list of L1 and $N^{\text{HLT}}_{\text{trk}}$ requirements for the $pp$ and $p + \text{Pb}$ HMT triggers used in this analysis. For the $pp$ HMT triggers, the L1 requirement is on the $E_T$ over the entire ATLAS calorimetry ($E_T^{\text{L1}}$) or hits in the MBTS. For the $p + \text{Pb}$ HMT triggers, the L1 requirement is on the $E_T$ restricted to the FCal ($E_T^{\text{L1,FCal}}$).

<table>
<thead>
<tr>
<th>$pp$ 13 TeV</th>
<th>$pp$ 5.02 TeV</th>
<th>$p + \text{Pb}$</th>
</tr>
</thead>
<tbody>
<tr>
<td>L1</td>
<td>L1</td>
<td>L1</td>
</tr>
<tr>
<td>MBTS</td>
<td>$E_T^{\text{L1}} &gt; 10$ GeV</td>
<td>$N_{\text{trk}}^{\text{L1}} &gt; 60$</td>
</tr>
<tr>
<td>$E_T^{\text{L1}} &gt; 10$ GeV</td>
<td>$N_{\text{trk}}^{\text{L1}} &gt; 90$</td>
<td>$E_T^{\text{L1,FCal}} &gt; 10$ GeV</td>
</tr>
<tr>
<td>$E_T^{\text{L1}} &gt; 20$ GeV</td>
<td>$N_{\text{trk}}^{\text{L1}} &gt; 90$</td>
<td>$E_T^{\text{L1,FCal}} &gt; 50$ GeV</td>
</tr>
</tbody>
</table>

3ATLAS uses a right-handed coordinate system with its origin at the nominal interaction point (IP) in the center of the detector and the $z$ axis along the beam pipe. The $x$ axis points from the IP to the center of the LHC ring, and the $y$ axis points upward. Cylindrical coordinates $(r, \phi)$ are used in the transverse plane, $\phi$ being the azimuthal angle around the $z$ axis. The pseudorapidity is defined in terms of the polar angle $\theta$ as $\eta = -\ln \tan(\theta/2)$.

in Ref. [41]. The template fits are used to extract the Fourier harmonics $v_{n,n}$ [Eq. (2)] of the long-range correlation, and the factorization of the $v_{n,n}$ into single-particle harmonics $v_n$ [Eq. (3)] is studied. The stability of the $v_{n,n}$ as a function of the pseudorapidity separation between the charged-particle pairs is also checked. Section VI describes the systematic uncertainties associated with the measured $v_{n,n}$. Section VII presents the main results of the analysis, which are the $p_T$ and event-activity dependence of the single-particle harmonics, $v_n$. Detailed comparisons of the $v_n$ between the three data sets, 13 TeV $pp$, 5.02 TeV $pp$, and 5.02 TeV $p + \text{Pb}$, are also shown. Section VIII gives a summary of the main results and observations.

II. EXPERIMENT

A. ATLAS detector

The measurements presented in this paper were performed using the ATLAS [54] inner detector (ID), minimum-bias trigger scintillators (MBTS), calorimeter, zero-degree calorimeters (ZDC), and the trigger and data acquisition systems. The ID detects particles within the pseudorapidity range $3|\eta| < 2.5$ using a combination of silicon pixel detectors including the “insertable B-layer” (IBL) [55,56] that was installed between run 1 (2009–2013) and run 2, silicon microstrip detectors (SCTs), and a straw-tube transition radiation tracker (TRT), all immersed in a 2 T axial magnetic field [57]. The MBTS system detects charged particles over the entire ATLAS detector, positioned at $|\eta| < 1.6$ and $|\phi| < 0.8$. The MBTS system consists of a liquid argon (LAr) electromagnetic (EM) calorimeter covering $|\eta| < 3.2$, a steel–scintillator sampling hadronic calorimeter covering $|\eta| < 1.7$, a LAr hadronic calorimeter covering $1.5 < |\eta| < 3.2$, and two LAr electromagnetic and hadronic forward calorimeters (FCal) covering $3.2 < |\eta| < 4.9$. The ZDCs, situated $\pm 140 \text{ m}$ from the nominal IP, detect neutral particles, mostly neutrons and photons, with $|\eta| > 8.3$. The ZDCs use tungsten plates as absorbers, and quartz rods sandwiched between the tungsten plates as the active medium.

B. Trigger

The ATLAS trigger system [58] consists of a level-1 (L1) trigger implemented using a combination of dedicated electronics and programmable logic, and a software-based high-level trigger (HLT). Due to the large interaction rates, only a small fraction of minimum-bias events could be recorded for all three data sets. The configuration of the minimum-bias (MB) triggers varied between the different data sets. Minimum-bias $p + \text{Pb}$ events were selected by requiring a hit in at least one MBTS counter on each side (MBTS_1) or a signal in the ZDC on the Pb-fragmentation side with the trigger threshold set just below the peak corresponding to a single neutron. In the 13 TeV $pp$ data, MB events were selected by a L1 trigger that requires a signal in at least one MBTS counter (MBTS_1). In the 5.02 TeV $pp$ data, MB events were selected using the logical OR of the MBTS_1, MBTS_1, and a third trigger that required at least one reconstructed track at the HLT. In order to increase the number of events having high charged-particle multiplicity, several high-multiplicity (HMT) triggers were implemented. These apply a L1 requirement on either the transverse energy ($E_T$) in the calorimeters or on the number of hits in the MBTS, and an HLT requirement on the multiplicity of HLT-reconstructed charged-particle tracks. That multiplicity, $N_{\text{trk}}^{\text{L1}}$, is evaluated for tracks having $p_T > 0.4$ GeV that are associated with the reconstructed vertex with the highest multiplicity in the event. This last requirement suppresses the selection of events with multiple collisions (pileup), as long as the collision vertices are not so close as to be indistinguishable. The HMT trigger configurations used in this analysis are summarized in Table I.

III. DATA SETS

The $\sqrt{s} = 13$ and 5.02 TeV $pp$ data were collected during run 2 of the LHC. The 13 TeV $pp$ data were recorded over
two periods: a set of low-luminosity runs in June 2015 (used in Ref. [41]) for which the number of collisions per bunch crossing, $\mu$, varied between 0.002 and 0.04, and a set of intermediate-luminosity runs in August 2015 where $\mu$ varied between 0.05 and 0.6. The 5.02 TeV $pp$ data were recorded during November 2015 in a set of intermediate-luminosity runs with $\mu$ of $\sim$1.5. The $p + Pb$ data were recorded in run 1 during $p + Pb$ operation of the LHC in January 2013. During that period, the LHC was configured with a 4 TeV proton beam and a 1.57 TeV per-nucleon Pb beam that together produced collisions at $\sqrt{s_{NN}} =$ 5.02 TeV. The higher energy of the proton beam produces a net rapidity shift of the nucleon-nucleon center-of-mass frame by 0.47 units in the proton-going direction, relative to the ATLAS reference frame. The $p + Pb$ data were collected in two periods between which the directions of the proton and lead beams were reversed. The integrated luminosities for the three datasets are as follows: 75 nb$^{-1}$ for the $\sqrt{s} =$ 13 TeV $pp$ data, 26 pb$^{-1}$ for the $\sqrt{s} =$ 5.02 TeV $pp$ data, and 28 nb$^{-1}$ for the $\sqrt{s_{NN}} =$ 5.02 TeV $p + Pb$ data. However, due to the large interaction rates, the full luminosities could not be sampled by the various HMT triggers listed in Table I. In the $\sqrt{s} =$ 13 TeV and $\sqrt{s} =$ 5.02 TeV $pp$ data, the luminosity sampled by the HMT trigger with the highest $E^{\text{clus}}_T$ and $N_{\text{track}}^\text{HLT}$ thresholds were 64 nb$^{-1}$ and 170 nb$^{-1}$, respectively. In the $\sqrt{s_{NN}} =$ 5.02 TeV $p + Pb$ data, the $N_{\text{track}}^\text{HLT} \geq 225$ trigger sampled the entire 28 nb$^{-1}$ luminosity.

### A. Event and track selection

In the offline analysis, additional requirements are imposed on the events selected by the MB and HMT triggers. The events are required to have a reconstructed vertex with the $z$ position of the vertex restricted to ±150 mm. In the $p + Pb$ data, noncollision backgrounds are suppressed by requiring at least one hit in a MBTS counter on each side of the interaction point, and the time difference measured between the two sides of the MBTS to be less than 10 ns. In the 2013 $p + Pb$ run, the luminosity conditions provided by the LHC resulted in an average probability of 3% for pileup events. The pileup events are suppressed by rejecting events containing more than one good reconstructed vertex. The remaining pileup events are further suppressed using the number of detected neutrons, $N_n$, measured in the ZDC on the Pb-fragmentation side. The distribution of $N_n$ in events with pileup is broader than that for the events without pileup. Hence, rejecting events at the high tail end of the ZDC signal distribution further suppresses the pileup, while retaining more than 98% of the events without pileup. In the $pp$ data, pileup is suppressed by only using tracks associated with the vertex having the largest $\sum p_T^2$, where the sum is over all tracks associated with the vertex. Systematic uncertainties in the measured $v_n$ associated with the residual pileup are estimated in Sec. VI.

In the $p + Pb$ analysis, charged-particle tracks are reconstructed in the ID using an algorithm optimized for $pp$ minimum-bias measurements [59]. The tracks are required to have $p_T > 0.4$ GeV and $|\eta| < 2.5$, at least one pixel hit, with the additional requirement of a hit in the first pixel layer when one is expected, and at least six SCT hits. In addition, the transverse ($d_0$) and longitudinal [$z_0 \sin(\theta)$] impact parameters of the track relative to the vertex are required to be less than 1.5 mm. They are also required to satisfy $|d_0|/\sigma_{d_0} < 3$ and $|z_0 \sin(\theta)|/\sigma_{z_0 \sin(\theta)} < 3$, where $\sigma_{d_0}$ and $\sigma_{z_0 \sin(\theta)}$ are uncertainties in $d_0$ and $z_0 \sin(\theta)$, respectively.

In the $pp$ analysis, charged-particle tracks and primary vertices are reconstructed in the ID using an algorithm similar to that used in run 1, but substantially modified to improve performance [60,61]. The reconstructed tracks are required to satisfy the following selection criteria: $p_T > 0.4$ GeV and $|\eta| < 2.5$; at least one pixel hit, with the additional requirement of a hit in the IBL if one is expected (if a hit is not expected in the IBL, a hit in the next pixel layer is required if such a hit is expected); a minimum of six hits in the SCTs; $|d_0| < 1.5$ mm and $|z_0 \sin(\theta)| < 1.5$ mm. Finally, in order to remove tracks with mismeasured $p_T$ due to interactions with the material or other effects, the track-fit $\chi^2$ probability is required to be larger than 0.01 for tracks having $p_T > 10$ GeV.

The efficiencies $\epsilon(p_T, \eta)$ of track reconstruction for the above track selection cuts are obtained using Monte Carlo (MC) generated events that are passed through a GEANT4 [62] simulation [63] of the ATLAS detector response and reconstructed using the algorithms applied to the data. For determining the $p + Pb$ efficiencies, the events are generated with version 1.38b of the HIJING event generator [64] with a center-of-mass boost matching the beam conditions. For determining the $pp$ efficiencies, nondiffractive 13 TeV $pp$ events obtained from the PYTHIA8 [65] event generator (with the A2 set of tuned parameters [66] and the MSTW2008LO PDFs [67]) are used. Both the $pp$ and $p + Pb$ efficiencies increase by $\sim$3% from 0.4 to 0.6 GeV and vary only weakly with $p_T$ for $p_T > 0.6$ GeV. In the $p + Pb$ case, the efficiency at $p_T \sim 0.6$ GeV ranges from 81% at $\eta = 0$ to 73% at $|\eta| = 1.5$ and 65% at $|\eta| > 2.0$. The efficiency is also found to vary by less than 2% over the multiplicity range used in the analysis. In the $pp$ case, the efficiency at $p_T \sim 0.6$ GeV ranges from 87% at $\eta = 0$ to 76% at $|\eta| = 1.5$ and 69% for $|\eta| > 2.0$.

### B. Event-activity classes

As in previous ATLAS analyses of long-range correlations in $p + Pb$ [2,4] and $pp$ [41] collisions, the event activity is quantified by $N_{\text{ch}}^{\text{rec}}$: the total number of reconstructed charged-particle tracks with $p_T > 0.4$ GeV, passing the track selections discussed in Sec. III A. From the simulated events (Sec. III A), it is determined that the tracking efficiency reduces the measured $N_{\text{ch}}^{\text{rec}}$ relative to the event generator multiplicity for $p_T > 0.4$ GeV primary charged particles by

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4 A hit is expected if the extrapolated track crosses an active region of a pixel module that has not been disabled.

5 In the $pp$ analysis the transverse impact parameter $d_0$ is calculated with respect to the average beam position, and not with respect to the vertex.

6 For the $p + Pb$ simulation, the event generator multiplicity includes charged particles that originate directly from the collision or result from decays of particles with $ct < 10$ mm. The definition for
approximately multiplicity-independent factors. The reduction factors and their uncertainties are 1.29 ± 0.05 and 1.18 ± 0.05 for the \( p + Pb \) and \( pp \) collisions, respectively.

For \( p + Pb \) collisions there is a direct correlation between \( N_{\text{ch}}^{\text{rec}} \) and the number of participating nucleons in the Pb nucleus: events with larger \( N_{\text{ch}}^{\text{rec}} \) values have, on average, a larger number of participating nucleons in the Pb nucleus and a smaller impact parameter. In this case, the concept of centrality used in \( A + A \) collisions is applicable, and in this paper the terms “central” and “peripheral” are referred to as events with large and small \( N_{\text{ch}}^{\text{rec}} \), respectively. For \( pp \) collisions there may not be a correlation between \( N_{\text{ch}}^{\text{rec}} \) and impact parameter. However, for convenience, the \( pp \) events with large and small \( N_{\text{ch}}^{\text{rec}} \) are also termed as “central” and “peripheral”, respectively.

Figure 1 shows the \( N_{\text{ch}}^{\text{rec}} \) distributions for the three data sets used in this paper. The discontinuities in the distributions result from the different HMT triggers, for which an offline requirement of \( N_{\text{ch}}^{\text{rec}} > N_{\text{ch}}^{\text{HLT}} \) is applied. This requirement ensures that the HMT triggered events are used only where the HLT trigger is almost fully efficient.

The \( pp \) event activity can also be quantified using the total transverse energy deposited in the FCal \( (E_T^{\text{FCal}}) \). This quantity has been used to determine the centrality in all ATLAS heavy-ion analyses. Using the \( E_T^{\text{FCal}} \) to characterize the event activity has the advantage that independent sets of particles are used to determine the event activity and to measure the long-range correlations. Similarly in the \( p + Pb \) case, the event activity can be characterized by the sum of transverse energy measured on the Pb-fragmentation side of the FCal \( (E_T^{\text{FCal, Pb}}) \). Results presented in this paper use both \( N_{\text{ch}}^{\text{rec}} \) and the \( E_T^{\text{FCal}} \) (or \( E_T^{\text{FCal, Pb}} \)) to quantify the event activity.

**IV. TWO-PARTICLE CORRELATION ANALYSIS**

The study of two-particle correlations in this paper follows previous ATLAS measurements in \( Pb + Pb [13,69,70] \), \( p + Pb [2,4] \), and \( pp [41] \) collisions. For a given event class, the two-particle correlations are measured as a function of the relative azimuthal angle \( \Delta \phi \equiv \phi^a - \phi^b \) and pseudorapidity \( \Delta \eta \equiv \eta^a - \eta^b \) separation. The labels \( a \) and \( b \) denote the two particles in the pair, which may be selected from different \( p_T \) intervals. The particles \( a \) and \( b \) are conventionally referred to as the “trigger” and “associated” particles, respectively. The correlation function is defined as

\[
C(\Delta \eta, \Delta \phi) = \frac{S(\Delta \eta, \Delta \phi)}{B(\Delta \eta, \Delta \phi)}.
\]

where \( S \) and \( B \) represent pair distributions constructed from the same event and from “mixed events” [71], respectively. The same-event distribution \( S \) is constructed using all particle pairs that can be formed in each event from tracks that have passed the selections described in Sec. III A. The \( S \) distribution contains both the physical correlations between particle pairs and correlations arising from detector acceptance effects. The mixed-event distribution \( B(\Delta \eta, \Delta \phi) \) is similarly constructed by choosing the two particles in the pair from different events. The \( B \) distribution does not contain physical correlations, but has detector acceptance effects similar to those in \( S \). In taking the ratio, \( S/B \) in Eq. (5), the detector acceptance effects largely cancel, and the resulting \( C(\Delta \eta, \Delta \phi) \) contains physical correlations only. The pair of events used in the mixing are required to have similar \( N_{\text{ch}}^{\text{rec}} \) \( |\Delta N_{\text{ch}}^{\text{rec}}| < 10 \) and similar \( z_{\text{vtx}} \) \( |z_{\text{vtx}}| < 10 \text{ mm} \), so that acceptance effects in \( S(\Delta \eta, \Delta \phi) \) are properly reflected in, and compensated by, corresponding variations in \( B(\Delta \eta, \Delta \phi) \). To correct \( S(\Delta \eta, \Delta \phi) \) and \( B(\Delta \eta, \Delta \phi) \) for the individual \( \phi \)-averaged inefficiencies of particles \( a \) and \( b \), the pairs are weighted by the inverse product of their tracking efficiencies \( 1/(\epsilon_a \epsilon_b) \). Statistical uncertainties are calculated for \( C(\Delta \eta, \Delta \phi) \) using standard error-propagation procedures assuming no correlation between \( S \) and \( B \), and with the statistical variance of \( S \) and \( B \) in each \( \Delta \eta \) and \( \Delta \phi \) bin taken to be \( \sum 1/(\epsilon_a \epsilon_b)^2 \) where the sum runs over all of the pairs included in the bin. Typically, the two-particle correlations are used only to study the shape of the correlations in \( \Delta \phi \), and are conveniently normalized. In this paper, the normalization of \( C(\Delta \eta, \Delta \phi) \) is chosen such that the \( \Delta \phi \)-averaged value of \( C(\Delta \eta, \Delta \phi) \) is unity for \( |\Delta \eta| > 2 \).

Examples of correlation functions are shown in Fig. 2 for \( 0.5 < p_T^b < 5 \text{ GeV} \) and for two different \( N_{\text{ch}}^{\text{rec}} \) ranges for each

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[68]
FIG. 2. Two-particle correlation functions $C(\Delta \eta, \Delta \phi)$ in 13 TeV $pp$ collisions (top panels), 5.02 TeV $pp$ collisions (middle panels), and in 5.02 TeV $p + Pb$ collisions (bottom panels). The left panels correspond to a lower-multiplicity range of $0 \leq N_{ch}^{rec} < 20$. The right panels correspond to higher multiplicity ranges of $N_{ch}^{rec} \geq 120$ for 13 TeV $pp$, $90 \leq N_{ch}^{rec} < 100$ for the 5.02 TeV $pp$, and $N_{ch}^{rec} \geq 220$ for the 5.02 TeV $p + Pb$. The plots are for charged particles having $0.5 < p_T < 5$ GeV. The distributions have been truncated to suppress the peak at $\Delta \eta = \Delta \phi = 0$ and are plotted over $|\Delta \eta| < 4.6$ ($|\Delta \eta| < 4.0$ for middle row) to avoid statistical fluctuations at larger $|\Delta \eta|$. For the middle-right panel, the peak at $\Delta \phi = \pi$ has also been truncated.

The plots show results for $0 \leq N_{ch}^{rec} < 20$ while the right panels show representative high-multiplicity ranges of $N_{ch}^{rec} \geq 120$ for the 13 TeV $pp$ data, $90 \leq N_{ch}^{rec} < 100$ for the 5.02 TeV $pp$ data, and $N_{ch}^{rec} \geq 220$ for the 5.02 TeV $p + Pb$ data. The correlation functions are plotted over the range $-\pi/2 < \Delta \phi < 3\pi/2$; the periodicity of the measurement requires that $C(\Delta \eta, 3\pi/2) = C(\Delta \eta, -\pi/2)$. The low-multiplicity correlation functions exhibit features that are understood to result primarily from hard-scattering processes: a peak centered at $\Delta \eta = \Delta \phi = 0$ that arises primarily from jets and an enhancement centered at $\Delta \phi = \pi$ and extending over the full $\Delta \eta$ range which results from dijets. These features also dominate the high-multiplicity correlation functions.

Additionally, in the high-multiplicity correlation functions, each of the three systems exhibit a ridge—an enhancement centered at $\Delta \phi = 0$ that extends over the entire measured $\Delta \eta$ range.
One-dimensional correlation functions $C(\Delta \phi)$ are obtained by integrating the numerator and denominator of Eq. (5) over $2 < |\Delta \eta| < 5$ prior to taking the ratio

$$C(\Delta \phi) = \frac{\int_{-\pi/2}^{\pi/2} B(\Delta \phi) d \Delta \phi}{\int_{-\pi/2}^{\pi/2} A(\Delta \phi) d \Delta \phi},$$

(6)

This $|\Delta \eta|$ range is chosen to focus on the long-range features of the correlation functions. From the one-dimensional correlation functions, “per-trigger-particle yields,” $Y(\Delta \phi)$ are calculated [2,4,71]:

$$Y(\Delta \phi) = \left( \frac{\int_{-\pi/2}^{\pi/2} B(\Delta \phi) d \Delta \phi}{\int_{-\pi/2}^{\pi/2} A(\Delta \phi) d \Delta \phi} \right) C(\Delta \phi),$$

(7)

where $A$ denotes the total number of trigger particles, corrected to account for the tracking efficiency. The $Y(\Delta \phi)$ distribution is identical in shape to $C(\Delta \phi)$, but has a physically relevant normalization: it represents the average number of associated particles per trigger particle in a given $\Delta \phi$ interval. This allows operations, such as subtraction of the $Y(\Delta \phi)$ distribution in one event-activity class from the $Y(\Delta \phi)$ distribution in another, which have been used in studying the $p + Pb$ ridge [2,4].

V. TEMPLATE FITTING

In order to separate the ridge from other sources of angular correlation, such as dijets, the ATLAS Collaboration developed a template fitting procedure described in Ref. [41]. In this procedure, the measured $Y(\Delta \phi)$ distributions are assumed to result from a superposition of a “peripheral” $Y(\Delta \phi)$ distribution, $Y_{\text{periph}}(\Delta \phi)$, scaled up by a multiplicative factor and a constant modulated by $\cos(n \Delta \phi)$ for $n \geq 2$. The resulting template fit function,

$$Y_{\text{temp}}(\Delta \phi) = Y_{\text{ridge}}(\Delta \phi) + F Y_{\text{periph}}(\Delta \phi),$$

(8)

where

$$Y_{\text{ridge}}(\Delta \phi) = G \left( 1 + \sum_{n=2}^{\infty} 2v_{n,n} \cos(n \Delta \phi) \right),$$

(9)

has free parameters $F$ and $v_{n,n}$. A $v_{1,1}$ term is not included in $Y_{\text{ridge}}(\Delta \phi)$ [Eq. (9)] as the presence of a $v_{1,1}$ component in the measured $Y(\Delta \phi)$ is accounted for by the $F Y_{\text{periph}}(\Delta \phi)$ term. The parameter $F$ is the multiplicative factor by which the $Y_{\text{periph}}(\Delta \phi)$ is scaled. The coefficient $G$, which represents the magnitude of the combinatoric component of $Y_{\text{ridge}}(\Delta \phi)$, is fixed by requiring that the integral of $Y_{\text{ridge}}(\Delta \phi)$ be equal to the integral of the measured $Y(\Delta \phi)$, $\int_{-\pi/2}^{\pi/2} A(\Delta \phi) d \Delta \phi = \int_{-\pi/2}^{\pi/2} B(\Delta \phi) Y(\Delta \phi) d \Delta \phi$. In this paper, when studying the $N_{\text{ch}}^{\text{rec}}$ dependence of the long-range correlation, the $0 < N_{\text{ch}}^{\text{rec}} < 20$ multiplicity interval is used to produce $Y_{\text{periph}}(\Delta \phi)$. When studying the $E_T^{\text{Cal,Pb}} (E_T^{\text{Cal,Pb}} < 40 \text{ GeV})$, the $E_T^{\text{Cal,Pb}} < 10 \text{ GeV} (E_T^{\text{Cal,Pb}} < 10 \text{ GeV})$ interval is used to produce $Y_{\text{periph}}(\Delta \phi)$.

The template fitting procedure is similar to the peripheral subtraction procedure used in previous ATLAS $p + Pb$ ridge analyses [4]. In those analyses, the scale factor for the peripheral reference, analogous to $F$ in Eq. (8), was determined by matching the near-side jet peaks between the peripheral and central samples. A more important difference, however, lies in the treatment of the peripheral bin. In the earlier analyses, a ZYAM procedure was performed on the peripheral reference, and only the modulated part of $Y_{\text{periph}}(\Delta \phi)$, $Y_{\text{periph}}(\Delta \phi) - Y_{\text{periph}}(0)$, was used in the peripheral subtraction. The ZYAM procedure makes several assumptions, the most relevant of which for the present analysis is that there is no long-range correlation in the peripheral bin. As pointed out in Ref. [41], neglecting the nonzero modulation present in $Y_{\text{periph}}(\Delta \phi)$ significantly biases the measured $v_{n,n}$ values. Results from an alternative version of the template fitting, where a ZYAM procedure is performed on the peripheral reference, by using $Y_{\text{periph}}(\Delta \phi) - Y_{\text{periph}}(0)$ in place of $Y_{\text{periph}}(\Delta \phi)$ in Eq. (8), are also presented in this paper. This ZYAM-based template fit is similar to the $p + Pb$ peripheral subtraction procedure. These results are included mainly to compare with previous measurements and to demonstrate the improvements obtained using the present method.

In Ref. [41] the template fitting procedure only included the second-order harmonic $v_{2,2}$, but was able to reproduce the $N_{\text{ch}}^{\text{rec}}$-dependent evolution of $Y(\Delta \phi)$ on both the near and away sides. The left panel of Fig. 3 shows such a template fit, in the 13 TeV $pp$ data, that only includes $v_{2,2}$. The right panel shows the difference between the $Y(\Delta \phi)$ and the $Y_{\text{temp}}(\Delta \phi)$ distributions demonstrating the presence of small (compared to $v_{2,2}$), but significant residual $v_{3,3}$ and $v_{4,4}$ components. While it is possible that $\cos 3\Delta \phi$ and $\cos 4\Delta \phi$ contributions could arise in the template fitting method due to small multiplicity-dependent changes in the shape of the dijet component of the correlation function, such effects would not produce the excess at $\Delta \phi \sim 0$ observed in the right-hand panel in Fig. 3. That excess and the fact that its magnitude is compatible with the remainder of the distribution indicates that there is real $\cos 3\Delta \phi$ and $\cos 4\Delta \phi$ modulation in the two-particle correlation functions. Thus this paper extends the $v_{2,2}$ results in Ref. [41] by including $v_{3,3}$ and $v_{4,4}$ as well. A study of these higher-order harmonics, including their $N_{\text{ch}}^{\text{rec}}$ and $p_T$ dependence and factorization [Eq. (4)], can help in better understanding the origin of the long-range correlations.

Figure 4 shows template fits to the 13 TeV (left panels) and 5.02 TeV $pp$ data (right panels), for $0.5 < p_T^{\text{ch}} < 5$ GeV. From top to bottom, each panel represents a different $N_{\text{ch}}^{\text{rec}}$ range. The template fits [Eq. (9)] include harmonics 2–4. Visually, a ridge, i.e., a peak on the near side, cannot be seen in the top two rows, which correspond to low and intermediate $N_{\text{ch}}^{\text{rec}}$ intervals, respectively. However, the template fits indicate the presence of a large modulated component of $Y_{\text{ridge}}(\Delta \phi)$ even in these $N_{\text{ch}}^{\text{rec}}$ intervals. Several prior $pp$ ridge measurements rely on the ZYAM method [71,72] to extract yields on the near side [14,15]. In these analyses, the yield of excess pairs in the ridge above the minimum of the $Y(\Delta \phi)$ distribution is considered to be the strength of the ridge. Figure 4 shows that such a procedure would give zero yields in low- and intermediate-multiplicity collisions where the minimum of $Y(\Delta \phi)$ occurs at

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7The minimum of $Y_{\text{periph}}(\Delta \phi)$ is at $\Delta \phi = 0$ and is thus equal to $Y_{\text{periph}}(0)$, which the ZYAM procedure subtracts out.
$\Delta \phi \sim 0$. In high-multiplicity events the ZYAM-based yields, while nonzero, are still underestimated.

Figure 5 shows the template fits to the $p + Pb$ data in a format similar to Fig. 6. The template fits describe the data well across the entire $N_{\text{ch}}^\text{rec}$ range used in this paper. Previous $p + Pb$ ridge analyses used a peripheral subtraction procedure to remove the jet component from $Y(\Delta \phi)$ [1–5]. That procedure is similar to the ZYAM-based template fitting procedure, in that it assumes absence of any long-range correlations in the peripheral events. In the following sections, comparisons between the $v_{n,n}$ obtained from these two methods are shown.

A. Fourier coefficients

Figure 6 shows the $v_{n,n}$ obtained from the template fits in the 13 TeV $pp$ data, as a function of $N_{\text{ch}}$ and $E_T^{\text{FCal}}$. The $v_{n,n}$ from the ZYAM-based template fits as well as the coefficients obtained from a direct Fourier transform of $Y(\Delta \phi)$,

$$v_{n,n} = \frac{\int Y(\Delta \phi) \cos(n \Delta \phi) d \Delta \phi}{\int Y(\Delta \phi) d \Delta \phi}$$

are also shown for comparison. While the template $v_{n,n}$ are the most physically meaningful quantities, the Fourier $v_{n,n}$ are also included to demonstrate how the template fitting removes the hard contribution. Similarly, the ZYAM-based Fourier $v_{n,n}$ are also included, as the ZYAM-based fitting is similar to the peripheral subtraction procedure used in prior $p + Pb$ analyses [2,4], and comparing with the ZYAM-based results illustrates the improvement brought about in the template fitting procedure.

The $v_{2,2}$ values are nearly independent of $N_{\text{ch}}$ throughout the measured range. As concluded in Ref. [41], this implies that the long-range correlation is not unique to high-multiplicity events, but is in fact present even at very low multiplicities. In the $E_T^{\text{FCal}}$ dependence, however, $v_{2,2}$ shows a systematic decrease at low $E_T^{\text{FCal}}$. Further, the asymptotic value of the template $v_{2,2}$ at large $N_{\text{ch}}$ is also observed to be $\sim 10\%$ larger than the asymptotic value at large $E_T^{\text{FCal}}$. This might indicate that the $v_{2,2}$ at a given rapidity is more correlated with the local multiplicity than the global multiplicity.

The removal of the hard-process contribution to $v_{2,2}$ in the template fitting can be seen by comparing to the Fourier-$v_{2,2}$ values. The Fourier-$v_{2,2}$ values are always larger than the template $v_{2,2}$ and show a systematic increase at small $N_{\text{ch}}$ ($E_T^{\text{FCal}}$). This indicates the presence of a relatively large contribution from back-to-back dijets over this range. Asymptotically, at large $N_{\text{ch}}$ the Fourier-$v_{2,2}$ values become stable, but show a small decreasing trend in the $E_T^{\text{FCal}}$ dependence. The ZYAM-based $v_{2,2}$ values are smaller than the template-$v_{2,2}$ values for all $N_{\text{ch}}$ ($E_T^{\text{FCal}}$), and by construction systematically decrease to zero for the lower $N_{\text{ch}}$ ($E_T^{\text{FCal}}$) intervals. However, at larger $N_{\text{ch}}$ ($E_T^{\text{FCal}}$) they also show only a weak dependence on $N_{\text{ch}}$ ($E_T^{\text{FCal}}$). Asymptotically, at large $N_{\text{ch}}$, the $v_{2,2}$ values from the Fourier transform and the default template fits match to within $\sim 10\%$ (relative). In general, the $v_{2,2}$ values from all three methods agree within $\pm 15\%$ at large $N_{\text{ch}}$ or $E_T^{\text{FCal}}$. This implies that at very high multiplicities, $N_{\text{ch}} \sim 120$, the ridge signal is sufficiently strong that the assumptions made in removing the hard contributions to $Y(\Delta \phi)$ do not make a large difference. However, for the highest $p_T$ values used in this analysis, $p_T > 7$ GeV, it is observed that the width of the dijet peak in the $pp$ correlation functions broadens with increasing multiplicity. This change is opposite to that seen at lower $p_T$ where $v_{2,2}$ causes the dijet peak to become narrower.

As a result, the measured $v_{2,2}$ values become negative. This bias from the multiplicity dependence of the hard-scattering contribution likely affects the correlation functions at lower $p_T$ values and its potential impact is discussed below.

The $v_{2,2}$ component is dominant, with a magnitude approximately 30 times larger than $v_{3,3}$ and $v_{4,4}$, which are comparable to each other. This is in stark contrast to Pb + Pb collisions where in the most central events, where the average geometry has less influence, the $v_{n,n}$ have comparable magnitudes [13]. The Fourier $v_{3,3}$ shows considerable $N_{\text{ch}}$ ($E_T^{\text{FCal}}$) dependence and is negative almost everywhere. However, the $v_{3,3}$ values from the template fits are mostly positive. As the factorization
FIG. 4. Template fits to the per-trigger particle yields $Y(\Delta\phi)$, in 13 TeV (left panels) and in 5.02 TeV (right panels) $pp$ collisions for charged-particle pairs with $0.5 < p_T^{ab} < 5$ GeV and $2 < |\Delta\eta| < 5$. The template fitting includes second-order, third-order, and fourth-order harmonics. From top to bottom, each panel represents a different $N_{\text{rec}}^{\text{ch}}$ range. The solid points indicate the measured $Y(\Delta\phi)$, the open points and curves show different components of the template (see legend) that are shifted along the $y$ axis by $G$ or by $FY^{\text{template}}(0)$, where necessary, for presentation.

of the $v_{n,n}$ requires that the $v_{n,n}$ be positive [Eq. (3)], the negative Fourier $v_{3,3}$ clearly does not arise from single-particle modulation. However, because the template $v_{3,3}$ is positive, its origin from single-particle modulation cannot be ruled out. Within statistical uncertainties, the $v_{4,4}$ values from all three methods are positive throughout the measured $N_{\text{rec}}^{\text{ch}}$ range. Within statistical uncertainties, the $v_{4,4}$ values are consistent with no $N_{\text{rec}}^{\text{ch}}$ or $E_{\text{FCal}}^{\text{Pb}}$ dependence.

Figure 7 shows the $v_{n,n}$ values from the 5.02 TeV $pp$ data as a function of $N_{\text{rec}}^{\text{ch}}$ for a higher $p_T^{ab}$ bin of 1–5 GeV. The same trends seen in the 13 TeV data (Fig. 6) are observed here, and the conclusions are identical to those made in the 13 TeV case.

Figure 8 shows the $v_{n,n}$ for the $p + \text{Pb}$ data. The results are plotted both as a function of $N_{\text{rec}}^{\text{ch}}$ (left panels) and $E_{\text{FCal}}^{\text{Pb}}$ (right panels). The $v_{2,2}$ values obtained from the template fits show a systematic increase with $N_{\text{rec}}^{\text{ch}}$ over $N_{\text{rec}}^{\text{ch}} \lesssim 150$, unlike the $pp$ case where $v_{2,2}$ is nearly independent of $N_{\text{rec}}^{\text{ch}}$. This increase is much larger compared to the systematic uncertainties in the $v_{2,2}$ values (discussed later in Sec. VI). This is possibly indicative of a systematic change in the average
collision geometry which is present in $p + \text{Pb}$ but not in $pp$ collisions. A similar increase of the $v_{2,2}$ values is also observed in the $E_{\text{T}}^{\text{FCal,Pb}}$ dependence. The higher-order harmonics $v_{3,3}$ and $v_{4,4}$ show a stronger relative increase with increasing $N_{\text{ch}}^{\text{rec}}$ and $E_{\text{T}}^{\text{FCal,Pb}}$. This also implies that the assumption made in the template fitting, regarding the independence or weak dependence of the $v_{n,n}$ on $N_{\text{ch}}^{\text{rec}}$, is not strictly correct for $v_{3,3}$ and $v_{4,4}$.

Figure 8 also compares the Fourier and ZYAM-based template-$v_{n,n}$ values. The $v_{n,n}$ from the peripheral subtraction procedure used in a previous ATLAS $p + \text{Pb}$ long-range correlation analysis \[4\] are also shown. The peripheral-subtracted $v_{n,n}$ values are nearly identical to the values obtained from the ZYAM-based template fits. This is expected, as the treatment of the peripheral bin is identical in both cases: both use the ZYAM-subtracted $Y^{\text{periph}}(\Delta \phi)$ as the peripheral reference. What differs procedurally between the two methods is determination of the scale factor by which $Y^{\text{periph}}(\Delta \phi)$ is scaled up when subtracting it from $Y(\Delta \phi)$. In the peripheral subtraction case, this scale factor, analogous to the parameter $F$ in Eq. \[8\], is determined by matching the near-side jet peaks over the region $|\Delta \eta| < 1$ and $|\Delta \phi| < 1$. In the template-fitting...
case, the parameter $F$ is determined by the jet contribution to the away-side peak. The similarity of the $v_{n,2}$ values from the two procedures implies that whether the matching is done in the near-side jet peak or over the away-side peak, identical values of the scale factor are obtained. The Fourier-$v_{n,2}$ and template-$v_{n,2}$ values are surprisingly similar except at very low $N_{\text{rec}}$ or $E_T^{\text{FCal},\text{Pb}}$. This is unlike the $pp$ case (Figs. 6 and 7), where the values differed by $\sim 15\%$ (relative) at large $N_{\text{rec}}$.

This similarity does not hold for $v_{n,3}$ where the values from the template fit are systematically larger than the values obtained from Fourier decomposition. For all harmonics, the relative difference in the $v_{n,n}$ decreases with increasing event activity. Like in the $pp$ case (Fig. 6), this implies that at large enough event activity, the $v_{n,n}$ are less sensitive to the assumptions made in removing the hard contributions.

B. Test of factorization in template fits

If the $v_{n,n}$ obtained from the template fits are the result of single-particle modulations, then the $v_{n,n}$ should factorize as in Eq. (3), and the $v_{n}(p_T^a)$ obtained by correlating trigger particles at a given $p_T^b$ with associated particles in several different intervals of $p_T^b$ [Eq. (4)] should be independent of the choice of the $p_T^b$ interval. Figure 9 demonstrates the factorization of the $v_{2,2}$ in the 13 TeV $pp$ data, as a function of $N_{\text{rec}}$. The left panel shows the $v_{2,2}$ values for $0.5 < p_T^a < 5$ GeV and for four different choices of the associated particle $p_T^b$: 0.5–5, 0.5–1, 1–2, and 2–3 GeV. The right panel shows the corresponding $v_{2}(p_T^a)$ obtained using Eq. (4). While the $v_{2,2}(p_T^a, p_T^b)$ values vary by a factor of $\sim 2$ between the different choices of the $p_T^b$ interval, the corresponding $v_{2}(p_T^a)$ values agree quite well. Similar plots for the $p + \text{Pb}$ data are shown in Fig. 10.

FIG. 6. The $v_{n,n}$ obtained from the template fitting procedure in the 13 TeV $pp$ data, as a function of $N_{\text{rec}}$ (left panels), and as a function of $E_T^{\text{FCal}}$ (right panels). The top, middle, and bottom panels correspond to $v_{2,2}$, $v_{3,3}$, and $v_{4,4}$, respectively. The results are for $0.5 < p_T^a < 5$ GeV. The error bars indicate statistical uncertainties. The $v_{n,n}$ obtained from a direct Fourier transform of $Y(\Delta \phi)$ and from the ZYAM-based template fits are also shown for comparison.
due to higher statistical precision in the data, the factorization is tested for both $v_{2,2}$ and $v_{3,3}$. The variation of $v_{3,3}$ between the four $p_T^b$ intervals is a factor of $\sim 2$ while the variation of $v_{3,3}(p_T^a, p_T^b)$ is more than a factor of 3. However, the corresponding $v_n(p_T^a)$ values are in good agreement with each other, with the only exception being the $v_{2,2}$ values for $2 < p_T^b < 3$ GeV where some deviation from this behavior is seen for $N_{ch}^b \lesssim 50$.

Figure 11 studies the $p_T^b$ dependence of the factorization in the 13 TeV $pp$ data for $v_{2,2}$ (top panels) and $v_{3,3}$ (bottom panels). The results are shown for the $N_{ch}^b \geq 90$ multiplicity range. The left panels show the $v_{n,a}$ as a function of $p_T^b$ for four different choices of the associated particle $p_T^a$: $0.5–5$, $0.5–1$, $1–2$, and $2–3$ GeV. The right panels show the corresponding $v_n(p_T^a)$ obtained using Eq. (4). In the $v_{2,2}$ case, factorization holds reasonably well for $p_T^a \lesssim 3$ GeV, and becomes worse at higher $p_T^a$. This breakdown at higher $p_T^a$ is likely caused by the above-discussed multiplicity-dependent distortions of the dijet component of the correlation function which are not accounted for in the template fitting procedure. For $v_{3,3}$, the factorization holds reasonably well for $p_T^a \lesssim 3$ GeV. The $0.5 < p_T^b < 1$ GeV case shows a larger deviation in the factorization, but has much larger associated statistical uncertainties. Similar plots for the $p + Pb$ case are shown in Fig. 12. Here the factorization holds for $v_{2,2}$, $v_{3,3}$, and $v_{4,4}$ up to $p_T^b \sim 5$ GeV.

### C. Dependence of $v_{n,a}$ on $\Delta \eta$ gap

A systematic study of the $\Delta \eta$ dependence of the $v_{n,a}$ can also help in determining the origin of the long-range correlation. If it arises from mechanisms that only correlate a few particles in an event, such as jets, then a strong dependence of the correlation on the $\Delta \eta$ gap between particle pairs is expected. Figure 13 shows the measured $v_{n,a}$ (left panels) and $v_n = \sqrt{v_{n,a}}$ (right panels), as a function of $|\Delta \eta|$ for $|\Delta \eta| > 1$ in the 13 TeV $pp$ data. Also shown for comparison are the Fourier and ZYAM-based template $v_{n,a}$. The template $v_{2,2}$ (top left panel) and $v_{2}$ (top right panel) are quite stable, especially for $|\Delta \eta| > 1.5$, where the influence of the near-side jet is diminished. In contrast, the Fourier $v_{2,2}$ show a strong $|\Delta \eta|$ dependence. The $\Delta \eta$ dependence is largest at small $|\Delta \eta|$ because of the presence of the sharply peaked near-side jet, but is considerable even for $|\Delta \eta| > 2$. Similarly, the Fourier-$v_{3,3}$ shows large $|\Delta \eta|$ dependence, going from positive values at $|\Delta \eta| \sim 1$ to negative values at large $|\Delta \eta|$, while the template $v_{3,3}$ change only weakly in comparison. The Fourier $v_{3,3}$ is often negative, ruling out the possibility of it being generated by single-particle anisotropies, which require that $v_{n,a} = v_n^a$ be positive. For points where $v_{3,3}$ is negative, $v_3$ is not defined and hence not plotted. The template $v_{3,3}$ is, however, positive and, therefore, consistent with a single-particle anisotropy as its origin, except for the highest $|\Delta \eta|$ interval where it is consistent with zero. The $v_{4,4}$ values, like the $v_{2,2}$ and $v_{3,3}$...
values, vary only weakly with $|\Delta \eta|$. These observations further support the conclusion that the template $v_{n,n}$ are coefficients of genuine long-range correlations.

VI. SYSTEMATIC UNCERTAINITIES AND CROSS CHECKS

The systematic uncertainties in this analysis arise from choosing the peripheral bin used in the template fits, pileup, tracking efficiency, pair acceptance, and Monte Carlo consistency. Each source is discussed separately below.

Peripheral interval. As explained in Sec. V, the template fitting procedure makes two assumptions. First it assumes that the contributions to $Y(\Delta \phi)$ from hard processes have identical shape across all event activity ranges, and only change in overall scale. Second, it assumes that the $v_{n,n}$ are only weakly dependent on the event activity. The assumptions are self-consistent for the $N_{\text{rec}}$ dependence of the $v_{n,n}$ in the 5.02 and 13 TeV $pp$ data (Figs. 6 and 7), where the measured template-$v_{n,n}$ values do turn out to be nearly independent of $N_{\text{rec}}$. However, for the $E_{T}^{\text{FCal},Pb}$ dependence in the $pp$ data, and for both the $N_{\text{rec}}$ and $E_{T}^{\text{FCal},Pb}$ dependence in the $p + Pb$ data, a systematic increase of the template $v_{2,2}$ with event activity is seen at small event activity. This indicates the breakdown of one of the above two assumptions. To test the sensitivity of the measured $v_{n,n}$ to any residual changes in the width of the away-side jet peak and to the $v_{n,n}$ present in the peripheral reference, the analysis is repeated using $0 \leq N_{\text{rec}} < 10$ and $10 \leq N_{\text{rec}} < 20$ intervals to form $Y_{\text{periph}}(\Delta \phi)$. The variations in the $v_{n,n}$ for the different chosen peripheral intervals are taken to be a systematic uncertainty. For a given dataset,
RecchN0 50 100
T,paT(p2,2v
0.002
0.004
0.006
0.008
0.005
0.01
0.015
<5 GeV
T0.5<p
T0.5<p
T1<p
T2<p
ATLAS
-1=13 TeV, 64 nb
\( \Delta \eta < | \eta | < 5 \cos u \)

FIG. 9. The left panel shows \( v_{2,2} \) as a function of \( N_{ch}^{rec} \) in the 13 TeV pp data, for \( 0.5 < p_T < 5 \text{ GeV} \) and for different choices of the \( p_T^b \) interval. The right panel shows the corresponding \( v_2 \) values obtained using Eq. (4). The error bars indicate statistical uncertainties only.

\[ \text{this uncertainty is strongly correlated across all multiplicity intervals. Choosing a peripheral interval with larger mean multiplicity typically decreases the measured } v_{2,p}. \]

The sensitivity of the template \( v_2 \) to which peripheral interval is chosen is demonstrated in the left panels of Fig. 14, where \( v_2 \) is shown for three different peripheral \( N_{ch}^{rec} \) interval choices: \( 0 \leq N_{ch}^{periph} < 5 \), \( 0 \leq N_{ch}^{periph} < 10 \), and \( 0 \leq N_{ch}^{periph} < 20 \). In both the 13 and 5.02 TeV pp data, except at very low \( N_{ch}^{rec} \), the \( v_2 \) values are nearly independent of the chosen peripheral reference. In the 13 TeV pp case, the variation is \( \sim 6\% \) at \( N_{ch}^{rec} \sim 30 \) and decreases to \( \sim 1\% \) for \( N_{ch}^{rec} \geq 60 \). Even in the \( p + Pb \) case, where the measured template \( v_{2,2} \) exhibits some dependence on \( N_{ch}^{rec} \), the dependence of the template \( v_2 \) on the choice of peripheral bin is quite small: \( \sim 6\% \) at \( N_{ch}^{rec} \sim 30 \) and decreases to \( \sim 2\% \) for \( N_{ch}^{rec} \sim 60 \). Also shown for comparison are the corresponding \( v_2 \) values obtained from the ZYAM-based template fitting method (right panels of Fig. 14). These exhibit considerable dependence on the peripheral reference. For the 13 TeV pp case, the variation in the ZYAM-based \( v_2 \) is \( \sim 40\% \) at \( N_{ch}^{rec} \sim 30 \), and decreases to \( \sim 12\% \) at \( N_{ch}^{rec} \sim 60 \) and asymptotically at large \( N_{ch}^{rec} \) is \( \sim 7\% \). For the \( p + Pb \) case, the variation is even larger: \( \sim 35\% \) at \( N_{ch}^{rec} \sim 30 \) and \( \sim 14\% \) for \( N_{ch}^{rec} \sim 60 \). These results show that the template \( v_2 \) is quite stable as the peripheral interval is

\[ \text{FIG. 10. The left panels show } v_{2,2} \text{ (top) and } v_{3,3} \text{ (bottom) as a function of } N_{ch}^{rec} \text{ in the 5.02 TeV } p + Pb \text{ data, for } 0.5 < p_T^b < 5 \text{ GeV and for different choices of the } p_T^b \text{ interval. The right panels shows the corresponding } v_2 \text{ (top) and } v_3 \text{ (bottom) values obtained using Eq. (4). The error bars indicate statistical uncertainties only.} \]
The influence of the residual pileup is evaluated by relaxing the pileup rejection criteria and then calculating the change in the yield. In the ATLAS data, for events containing multiple vertices, only $v_{n,n}$ measurements are mostly insensitive to the tracking efficiency, the $v_{n,n}$ measurement, and supporting the flat-$v_{n,n}$ assumption made in the new method.

Pileup. Pileup events, when included in the two-particle correlation measurement, dilute the $v_{n,n}$ signal since they produce pairs where the trigger and associated particle are from different collisions and thus have no physical correlations. The maximal fractional dilution in the $v_{n,n}$ is equal to the pileup rate. In the $p + Pb$ data, nearly all of the events containing pileup are removed by the procedure described in Sec. III. The influence of the residual pileup is evaluated by relaxing the pileup rejection criteria and then calculating the change in the $Y(\Delta \phi)$ and $v_{n,n}$ values. The differences are taken as an estimate of the uncertainty for the $v_{n,n}$, and are found to be negligible in low event activity classes, and increase to 4% for events with $N_{\text{ch}}^\text{rec} \sim 300$.

In the $pp$ data, for events containing multiple vertices, only tracks associated with the vertex having the largest $\sum p_T^2$, where the sum is over all tracks associated with the vertex, are used in the analysis. Events with multiple unresolved vertices affect the results by increasing the combinatoric pedestal in $Y(\Delta \phi)$. The fraction of events with merged vertices is estimated and taken as the relative uncertainty associated with pileup in the $pp$ analysis. The merged-vertex rate in the $13 \text{ TeV} \ pp$ data is 0–3% over the 0–150 $N_{\text{ch}}^\text{rec}$ range. In the 5.02 TeV $pp$ data, it is 0–4% over the 0–120 $N_{\text{ch}}^\text{rec}$ range.

Track reconstruction efficiency. In evaluating $Y(\Delta \phi)$, each particle is weighed by $1/\epsilon(p_T, \eta)$ to account for the tracking efficiency. The systematic uncertainties in the efficiency $\epsilon(p_T, \eta)$ thus need to be propagated into $Y(\Delta \phi)$ and the final $v_{n,n}$ measurements. Unlike $Y(\Delta \phi)$, which is strongly affected by the efficiency, the $v_{n,n}$ are mostly insensitive to the tracking efficiency. This is because the $v_{n,n}$ measure the relative variation of the yields in $\Delta \phi$; an overall increase or decrease in the efficiency changes the yields but does not affect the $v_{n,n}$. However, as the tracking efficiency and its uncertainties have $p_T$ and $\eta$ dependence, there is some residual effect on the $v_{n,n}$. The corresponding uncertainty in the $v_{n,n}$ is estimated by repeating the analysis while varying the efficiency to its uncertainties.

Pair acceptance. As described in Sec. IV, this analysis uses the mixed-event distributions $B(\Delta \eta, \Delta \phi)$ and $B(\Delta \phi)$ to estimate and correct for the pair acceptance of the detector.
The mixed-event distributions are in general quite flat in $\Delta \phi$. The Fourier coefficients of the mixed-event distributions $v_{n,n}^{\text{det}}$, which quantify the magnitude of the corrections, are $\sim 10^{-4}$ in the $p + \text{Pb}$ data, and $\sim 2 \times 10^{-5}$ in the $pp$ data. In the $p + \text{Pb}$ analysis, potential systematic uncertainties in the $v_{n,n}^{\text{det}}$ due to residual pair-acceptance effects not corrected by the mixed events are evaluated following Ref. [13]. This uncertainty is found to be smaller than $\sim 10^{-5}$. In the $pp$ analysis, since the mixed-event corrections are themselves quite small, the entire correction is conservatively taken as the systematic uncertainty.

MC closure. The analysis procedure is validated by measuring the $v_{n,n}^{\text{det}}$ of reconstructed particles in fully simulated PYTHIA8 and HIJING events and comparing them to those obtained using the generated particles. The difference between the generated and reconstructed $v_{n,n}^{\text{det}}$ varies between $10^{-5}$ and $10^{-4}$ (absolute) in the $pp$ case and between 2% and 8% (relative) in the $p + \text{Pb}$ case, for the different harmonics. This difference is an estimate of possible systematic effects that are not accounted for in the measurement, such as a mismatch between the true and reconstructed momentum for charged particles, and is included as a systematic uncertainty.

As a cross-check, the dependence of the long-range correlations on the relative charge of the two particles used in the correlation is studied. If the long-range correlations arise from phenomena that correlate only a few particles in an event, such as jets or decays, then a dependence of the correlation on the relative sign of the particles making

FIG. 12. The left panels show the $v_{n,n}$ as a function of $p_T$ in the 5.02 TeV $p + \text{Pb}$ data, for $N_{\text{ch}}^{\text{rec}} \geq 140$ and for different choices of the $p_T$ interval. From top to bottom, the three rows correspond to $n = 2, 3,$ and 4. The right panels shows the corresponding $v_{n}$ values obtained using Eq. (4). The error bars indicate statistical uncertainties only. The $p_T$ intervals plotted are 0.4–0.5, 0.5–1, 1–2, 2–3, and 3–5 GeV. In some cases, the data points have been slightly shifted along the $x$ axis, for clarity.
The $|\Delta\eta|$ dependence of the $v_{n,n}$ (left panels) and $v_n$ (right panels) in the 13 TeV $pp$ data. From top to bottom the rows correspond to $n = 2, 3, \text{and } 4$, respectively. The ZYAM-template and Fourier-$v_{n,n}$ values are also shown for comparison. Only the range $|\Delta\eta| > 1$ is shown to suppress the large Fourier $v_{n,n}$ at $|\Delta\eta| \sim 0$ that arise due to the near-side jet peak. Plots are for the $N_{\text{rec,ch}} \geq 90$ multiplicity range and for $0.5 < p_T^{a,b} < 5$ GeV. The error bars indicate statistical uncertainties only. For points where $v_3$ is negative, $v_3$ is not defined and hence not plotted.

FIG. 13. The $|\Delta\eta|$ dependence of the $v_{n,n}$ (left panels) and $v_n$ (right panels) in the 13 TeV $pp$ data. From top to bottom the rows correspond to $n = 2, 3, \text{and } 4$, respectively. The ZYAM-template and Fourier-$v_{n,n}$ values are also shown for comparison. Only the range $|\Delta\eta| > 1$ is shown to suppress the large Fourier $v_{n,n}$ at $|\Delta\eta| \sim 0$ that arise due to the near-side jet peak. Plots are for the $N_{\text{rec,ch}} \geq 90$ multiplicity range and for $0.5 < p_T^{a,b} < 5$ GeV. The error bars indicate statistical uncertainties only. For points where $v_3$ is negative, $v_3$ is not defined and hence not plotted.

up the pair is expected. Figure 15 shows the measured $v_2$ from the template fits for both the same-charge and opposite-charge pairs. No systematic difference between the two is observed.

Tables II and III list the systematic uncertainties in the $v_{n,n}$ for the 13 TeV and 5.02 TeV $pp$ data, respectively. Most uncertainties are listed as relative uncertainties (in percentages of the $v_{n,n}$), while some are listed as absolute uncertainties. Uncertainties for the $p + \text{Pb}$ data are listed in Table IV. The corresponding uncertainties in the $v_n$ are obtained by propagating the uncertainties in the $v_{n,n}$ when using Eq. (3) to obtain the $v_n$. In some cases the systematic uncertainties in the $v_{n,n}$ are larger than 100%. In these cases the corresponding uncertainties in the $v_n$ cannot be calculated, as the $v_n$ are only defined for $v_{n,n} > 0$. Such cases are excluded from the $v_n$ results presented in Sec. VII below.

VII. RESULTS

Figure 16 provides a summary of the main results of this paper in the inclusive $p_T$ interval $0.5 < p_T < 5$ GeV. It compares the $v_n$ obtained from the 5.02 TeV, 13 TeV $pp$, and 5.02 TeV $p + \text{Pb}$ template fits. The left panels show $v_2$, $v_3$, and $v_4$ as a function of $N_{\text{ch}}^{\text{rec}}$ while the right panels show the results as a function of $p_T^a$ for the $N_{\text{ch}}^{\text{rec}} \geq 60$ multiplicity range. The measured $v_3$ and $v_4$ in the 5.02 TeV $pp$ data for $0.5 < p_T^{a,b} < 5$ GeV have large systematic uncertainties associated with the choice of peripheral reference and are not
FIG. 14. Dependence of $v_2$ on the peripheral bin chosen for the default (left panels) and ZYAM-based (right panels) template fitting methods. The top panels correspond to 13 TeV $pp$ collisions, middle panels correspond to 5.02 TeV $pp$ collisions, and the lower panels correspond to 5.02 TeV $p+Pb$ collisions. The results are plotted as a function of $N_{ch}^{rec}$ and for $0.5<p_T^{a,b}<5$ GeV. The error bars indicate statistical uncertainties.

shown in Fig. 16. They are shown in Fig. 18 for a different $p_T$ interval of $1<p_T^{a,b}<5$ GeV. Figure 16 shows that the $p+Pb$ $v_2$ increases with increasing $N_{ch}^{rec}$ as previously observed [4] while the $pp$ $v_2$ is $N_{ch}^{rec}$-independent within uncertainties. The $p+Pb$ $v_3$ is significantly larger than the $pp$ $v_3$ and also shows a systematic increase with $N_{ch}^{rec}$, while the $pp$ $v_3$ is consistent with being $N_{ch}^{rec}$-independent. The $pp$ and $p+Pb$ $v_4$ are consistent within large uncertainties, and the $p+Pb$ $v_4$ increases weakly with increasing $N_{ch}^{rec}$.

The difference between the $pp$ and $p+Pb$ results for the $N_{ch}^{rec}$ dependence of the $v_n$ is expected. Studies of the centrality dependence of the multiplicity distributions in $p+Pb$ collisions show a strong correlation between the multiplicity and the number of participants, or equivalently, the number of scatterings of the proton in the nucleus [73]. Regardless of the interpretation of the results, a dependence of the $v_n$ on the geometry of the $p+Pb$ collisions is expected [74]. In contrast, the relationship between multiplicity and
geometry in $pp$ collisions is poorly understood and necessarily different as there are, by definition, only two colliding nucleons. However, an early study of this problem accounting for perturbative evolution did predict a weak dependence of $v_2$ on multiplicity, as observed in this measurement [75]. A more recent study that models the proton substructure and fluctuations in the multiplicity of the final particles showed that the eccentricities $\epsilon_2$ and $\epsilon_3$ of the initial entropy-density distributions in $pp$ collisions have no correlation with the final particle multiplicity [76]. If the $v_n$ in $pp$ collisions are directly related to the $\epsilon_n$, then the calculations in Ref. [76] are consistent with the trends observed in the measured $v_n$.

The $pp$ and $p + Pb v_2(p_T)$ shown in Fig. 16 display similar trends with both increasing with $p_T$ at low $p_T$, reaching a maximum near 3 GeV and decreasing at higher $p_T$. The $v_2(p_T)$ values for the 5.02 and 13 TeV $pp$ data agree within uncertainties. The $p_T$ dependence of the $v_3$ and $v_4$ values is similar to that of $v_2$ at low $p_T$, where the $p + Pb$ results increase more rapidly with increasing $p_T$. However, unlike for $v_2$, the values of $v_3$ and $v_4$ are similar at high $p_T$ for the $pp$ and $p + Pb$ data. A direct test of the similarity of the $p_T$ dependence of the Fourier coefficients in $pp$ and $p + Pb$ collisions is provided in Fig. 17 for $n = 2$. The $pp$ $v_2$ values have been multiplied by 1.51, the ratio ($p + Pb$ to $pp$) of the maximum $v_2$ in the top right panel in Fig. 16. The resulting $v_2(p_T^a)$ values for (scaled) $pp$ and $p + Pb$ agree well for $p_T^a$ up to 5 GeV. At higher $p_T^a$ the $pp$ $v_2$ decreases more rapidly due to the above-described multiplicity-dependent change in the shape of the dijet peak in the two-particle correlation function at high $p_T$. After the scaling, the $pp$ $v_2(p_T^a)$ are slightly higher than the $p + Pb$ at low $p_T^a$, but the similarity of the shapes of the $p_T$ dependence is, nonetheless, striking.

A separate evaluation of the $N_{ch}^{rec}$ dependence of the $v_2$, $v_3$, and $v_4$ values is shown in Fig. 18 for the $1 < p_T^{a,b} < 5$ GeV interval, where the 5.02 TeV $pp$ measurements yield meaningful $v_2$ and $v_3$ results. The figure shows agreement between the 5.02 and 13 TeV $pp$ data for all three Fourier coefficients. It also shows that the $p + Pb v_2$, $v_3$, and $v_4$ rise

![Graph showing comparison of $v_2$ for same-charge and opposite-charge pairs in the 13 TeV $pp$ data.]

**FIG. 15.** Left panel: comparison of the $v_2$ for same-charge and opposite-charge pairs in the 13 TeV $pp$ data. Also shown are the $v_2$ values for the two types of pairs combined. Right panel: ratio of the same-charge to the opposite-charge $v_2$. The results are for $0.5 < p_T^{a,b} < 5$ GeV. For clarity, the data points for the same-charge and opposite-charge $v_n$ are slightly shifted along the $x$ axis. The error bars indicate statistical uncertainties.

**TABLE II.** Systematic uncertainties for the $v_{n,a}$ obtained from the template analysis in the 13 TeV $pp$ data. Where ranges are provided for both multiplicity and the uncertainty, the uncertainty varies from the first value to the second value as the multiplicity varies from the lower to upper limits of the range. Where no multiplicity range is provided the uncertainty is multiplicity independent.

<table>
<thead>
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<th>Source</th>
<th>$N_{ch}^{rec}$ range</th>
<th>$v_2,2$ syst. unc.</th>
<th>$v_3,3$ syst. unc.</th>
<th>$v_4,4$ syst. unc.</th>
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<td>7</td>
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<td>20–50</td>
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<td>2</td>
<td>&gt;100</td>
<td>&gt;100</td>
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<tr>
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<td>6–2</td>
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<td>2</td>
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<td>&gt;100</td>
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<tr>
<td>Pileup (%)</td>
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<td>0–150</td>
<td>0–150</td>
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<td>Tracking efficiency (%)</td>
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<td>Pair acceptance (absolute)</td>
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<td>$2 \times 10^{-5}$</td>
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<tr>
<td>MC closure (absolute)</td>
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<td></td>
<td>$2 \times 10^{-5}$</td>
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TABLE III. Systematic uncertainties for the $v_{n,n}$ obtained from the template analysis in the 5.02 TeV $pp$ data. Where ranges are provided for both multiplicity and the uncertainty, the uncertainty varies from the first value to the second value as the multiplicity varies from the lower to upper limits of the range. Where no multiplicity range is provided the uncertainty is multiplicity independent.

<table>
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<td>$N_{\text{ch}}^\text{rec}$</td>
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monotonically with increasing $N_{\text{ch}}^\text{rec}$ while the $pp$ results are generally $N_{\text{ch}}^\text{rec}$ independent. One possible exception to this statement is that the 13 TeV data indicate a small (~15%) decrease in $v_2$ in the two lowest $N_{\text{ch}}^\text{rec}$ intervals. The $pp$ and $p + Pb$ $v_3$ and $v_4$ agree at low $N_{\text{ch}}^\text{rec}$ while $v_2$ still differs significantly, although by a smaller amount than at larger $N_{\text{ch}}^\text{rec}$. This behavior is different from that observed in the inclusive $p_T$ interval, which may, in turn, reflect the convergence of the $v_2(p_T)$ between the $pp$ and $p + Pb$ data shown in the top right panel of Fig. 16.

Measurements [70,77] and theoretical analyses [78–82] of the correlations between the Fourier coefficients and event-plane angles of different flow harmonics in $Pb + Pb$ collisions have indicated significant “nonlinearity” resulting from collective expansion such that the response of the medium to an initial elliptic eccentricity can contribute to $\cos(4\phi)$ modulation of the produced particles. In $Pb + Pb$ collisions, the nonlinear contribution to $v_4$ is found to dominate over the geometric contribution except for the most central collisions where the initial-state fluctuations have the greatest impact. The nonlinear contribution to $v_4$ is expected to be proportional to $v_2^2$ so a comparison of the measured $v_4$ to $v_2^2$ in $pp$ and $p + Pb$ collisions may be of interest. The results are presented in Fig. 19, which shows $v_4/v_2$ versus $N_{\text{ch}}^\text{rec}$ for the 13 TeV $pp$ and the $p + Pb$ data. In the ratio, the correlated systematic uncertainties between the measured $v_4$ and $v_2^2$ cancel. The ratio is observed to be constant as a function of $N_{\text{ch}}^\text{rec}$ for both data sets even though the $p + Pb$ $v_2$ and $v_4$ increase with $N_{\text{ch}}^\text{rec}$. The $v_4/v_2^2$ ratio is observed to be 50% larger in the $pp$ data than in the $p + Pb$ data. Naively, this would indicate a larger nonlinear contribution to $v_4$ in $pp$ collisions compared to $p + Pb$ collisions.

TABLE IV. Systematic uncertainties for the $v_{n,n}$ obtained from the template analysis in the 5.02 TeV $p + Pb$ data. Where ranges are provided for both multiplicity and the uncertainty, the uncertainty varies from the first value to the second value as the multiplicity varies from the lower to upper limits of the range. Where no multiplicity range is provided the uncertainty is multiplicity independent.

<table>
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<th>Source</th>
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VIII. CONCLUSION

In summary, this paper presents results of two-charged-particle correlation measurements made by ATLAS in $\sqrt{s} = 13$ and 5.02 TeV $pp$ collisions and in 5.02 TeV $p + Pb$ collisions at the LHC. This measurement uses integrated luminosities of 64 nb$^{-1}$ for the $\sqrt{s} = 13$ TeV $pp$ data, 170 nb$^{-1}$ for the $\sqrt{s} = 5.02$ TeV $pp$ data, and 28 nb$^{-1}$ for the $\sqrt{s_{NN}} = 5.02$ TeV $p + Pb$ data. The 13 TeV measurements represent an extension of results presented in Ref. [41] using a larger data sample. The $p + Pb$ results are obtained from a
FIG. 16. Left panels: comparison of the $v_n$ obtained from the template fitting procedure in the 13 TeV $pp$, 5.02 TeV $pp$, and 5.02 TeV $p + \text{Pb}$ data, as a function of $N_{\text{ch}}^{\text{rec}}$. The results are for $0.5 < p_T < 5$ GeV. Right panels: the $p_T$ dependence of the $v_n$ for the $N_{\text{ch}}^{\text{rec}} \geq 60$ multiplicity range. From top to bottom the rows correspond to $n = 2$, 3, and 4, respectively. The error bars and shaded bands indicate statistical and systematic uncertainties, respectively.

reanalysis of run 1 data presented in Ref. [4] using a template fitting procedure developed for $pp$ collisions and applied in Ref. [41]. The correlation functions are measured for different intervals of measured charged-particle multiplicity and FCal transverse energy and for different intervals of charged-particle transverse momentum; many of the results are presented for an “inclusive” $p_T$ interval $0.5 < p_T < 5$ GeV.

One-dimensional distributions of per-trigger-particle yields as a function of azimuthal angle separation, $Y(\Delta \phi)$, are obtained from the long-range ($\mid \Delta \eta \mid > 2$) component of the correlation functions. A template fitting procedure is applied to the $Y(\Delta \phi)$ distributions to remove the contributions from hard-scattering processes and to measure the relative amplitudes $v_{n,n}$ of the sinusoidal modulation of the soft underlying event. Results for $v_{2,2}$, $v_{3,3}$, and $v_{4,4}$ are obtained for all three colliding systems. An analysis of the factorizability of the $v_{n,n}$ shows good factorization for most of the measured $N_{\text{ch}}^{\text{rec}}$ and $p_T$ intervals although factorization is observed to break
down for the most extreme combinations of $p_T^a$ and $p_T^b$ in the lowest and highest multiplicity or transverse energy intervals. Since the $v_{n,n}$ results are observed to be consistent with the presence of single-particle modulation of the per-event $dN/d\phi$ distributions, single-particle $v_n$ values are extracted and plotted versus $N_{\text{ch}}^\text{rec}$ and $p_T$.

FIG. 17. Comparison of the shapes of the $v_2(p_T)$ in the 13 TeV $pp$ and 5.02 TeV $p + Pb$ data. The $pp$ $v_2$ has been scaled by a factor of 1.51 along the $y$ axis in order to match the maximum of the $v_2$ in the two data sets. The results are for $0.5 < p_T^a, b < 5$ GeV and $N_{\text{ch}}^\text{rec} \geq 60$. The error bars indicate statistical uncertainties.

FIG. 18. Comparison of the $v_n$ obtained from the template fitting procedure in the 13 TeV $pp$, 5.02 TeV $pp$, and 5.02 TeV $p + Pb$ data, as a function of $N_{\text{ch}}^\text{rec}$. The results are for $1 < p_T^b < 5$ GeV. The three panels correspond to $n = 2, 3,$ and $4$. The error bars and shaded bands indicate statistical and systematic uncertainties, respectively.

FIG. 19. Ratio of $v_2$ to $v_4^2$ as a function of $N_{\text{ch}}^\text{rec}$ in the 13 TeV $pp$ and 5.02 TeV $p + Pb$ data. The results are for $0.5 < p_T^b < 5$ GeV. The error bars and shaded bands indicate statistical and systematic uncertainties, respectively.
Comparisons of the $v_2$, $v_3$, and $v_4$ values between 13 and 5.02 TeV $pp$ collisions show no significant variation in these quantities with center-of-mass energy. As observed in Ref. [41], the $v_2$ values obtained in $pp$ collisions at both energies are observed to be independent of $N_{\text{ch}}^{\text{rec}}$ within uncertainties for the inclusive $p_T$ interval. However, for the $1 < p_T < 5$ GeV interval a $\sim 15\%$ decrease in $v_2$ is seen in the lowest $N_{\text{ch}}^{\text{rec}}$ intervals. The $p + \text{Pb}$ $v_2$ values are larger than the $pp$ $v_2$ values for all multiplicities and are observed to increase slowly with $N_{\text{ch}}^{\text{rec}}$. However, the $p + \text{Pb}$ trend appears to converge with the $pp$ values for the lowest multiplicities, at least in the inclusive $p_T$ interval. For the $1 < p_T < 5$ GeV interval, the $v_2(p_T)$ trends do not show the same convergence between $pp$ and $p + \text{Pb}$ results. Similar to the results for $v_2$, the $pp$ $v_3$ and $v_4$ values are consistent with being independent of $N_{\text{ch}}^{\text{rec}}$ within uncertainties and the $p + \text{Pb}$ values are observed to increase with $N_{\text{ch}}^{\text{rec}}$. The $pp$ and $p + \text{Pb}$ $v_3$ and $v_4$ values are consistent within uncertainties in the lowest measured $N_{\text{ch}}^{\text{rec}}$ intervals.

The $p_T$ dependence of the $pp$ and $p + \text{Pb}$ $v_2$ values is similar: both rise approximately linearly with $p_T$ and reach a maximum near 3 GeV. The maximum $p + \text{Pb}$ $v_2$ value is approximately 50% larger than the maximum $v_2$ values for the 13 and 5.02 TeV $pp$ data, which are consistent within uncertainties. The $p + \text{Pb}$ $v_3$ and $v_4$ values also increase more rapidly with increasing $p_T$ than the corresponding $pp$ values for $p_T < 2$ GeV, but the $p + \text{Pb}$ $v_3$ values saturate above 3 GeV while the measured 13 TeV $pp$ $v_3$ values continue to increase with increasing $p_T$ over the full range of the measurement. A test of the similarity of the $p_T$ dependence of the $pp$ and $p + \text{Pb}$ $v_2$ values rescaling $pp$ $v_2$ values shows that the $pp$ and $p + \text{Pb}$ $v_2(p_T)$ distributions are remarkably similar in shape for $p_T < 5$ GeV.

An evaluation of the $v_2/v_2^0$ ratio in the inclusive $p_T$ interval shows results that are $N_{\text{ch}}^{\text{rec}}$ independent for both the 13 TeV $pp$ data and the $p + \text{Pb}$ data. This ratio is observed to be 50% larger for the $pp$ data than for the $p + \text{Pb}$ data.

The similarities between the $pp$ and $p + \text{Pb}$ results presented here suggest a common physical origin for the azimuthal anisotropies. The difference in the observed multiplicity dependence of the Fourier coefficients likely arises from the different geometry of the $pp$ and $p + \text{Pb}$ collisions.


024908-28
96, 024908 (2017)