Measurement of forward-backward multiplicity correlations in lead-lead, proton-lead, and proton-proton collisions with the ATLAS detector

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Two-particle pseudorapidity correlations are measured in $\sqrt{s_{NN}} = 2.76$ TeV Pb+Pb, $\sqrt{s_{NN}} = 5.02$ TeV $p+Pb$, and $\sqrt{s} = 13$ TeV $pp$ collisions at the Large Hadron Collider (LHC), with total integrated luminosities of approximately 7 $\mu$b$^{-1}$, 28 nb$^{-1}$, and 65 nb$^{-1}$, respectively. The correlation function $C_N(\eta_1,\eta_2)$ is measured as a function of event multiplicity using charged particles in the pseudorapidity range $|\eta| < 2.4$. The correlation function contains a significant short-range component, which is estimated and subtracted. After removal of the short-range component, the shape of the correlation function is described approximately by $1 + \langle a_1^2 \rangle^2 \eta_1 \eta_2$ in all collision systems over the full multiplicity range. The values of $\langle a_1^2 \rangle^2$ are consistent for the opposite-charge pairs and same-charge pairs, and for the three collision systems at similar multiplicity. The values of $\langle a_1^2 \rangle^2$ and the magnitude of the short-range component both follow a power-law dependence on the event multiplicity. The short-range component in $p + Pb$ collisions, after symmetrizing the proton and lead directions, is found to be smaller at a given $\eta$ than in $pp$ collisions with comparable multiplicity.

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I. INTRODUCTION

Heavy-ion collisions at Relativistic Heavy Ion Collider (RHIC) and the Large Hadron Collider (LHC) create hot, dense matter whose space-time evolution can be well described by relativistic viscous hydrodynamics [1,2]. Owing to strong dense matter whose space-time evolution can be well described (RHIC) and the Large Hadron Collider (LHC) create hot, flow coefficients referred to as harmonic flow. The measurements of harmonic coefficients in the azimuthal angle, commonly transverse plane have revealed strong harmonic modulation around the collision axis. Studies of the multiplicity correlation in the transverse plane have revealed strong harmonic modulation of the particle densities in the azimuthal angle, commonly referred to as harmonic flow. The measurements of harmonic flow coefficients $v_n$ [3–6] and their EbyE fluctuations [7–10] have placed important constraints on the properties of the medium and transverse energy density fluctuations in the initial state.

Two-particle correlations in the transverse plane have also been studied in high-multiplicity $pp$ [11–13] and $p + Pb$ [14–18] collisions, and these studies have revealed features that bear considerable similarity to those observed in heavy-ion collisions. These findings have generated many theoretical interpretations [19], and much discussion as to whether the mechanisms that result in the observed correlations are or are not fundamentally the same in the different collision systems.

This paper reports measurements of multiplicity correlations in the longitudinal direction in $pp$, $p + Pb$, and Pb+Pb collisions, which are sensitive to the early-time density fluctuations in pseudorapidity ($\eta$) [1,2]. These density fluctuations generate long-range correlations (LRC) at the early stages of the collision, well before the onset of any collective behavior, and appear as correlations of the multiplicity densities of produced particles separated in $\eta$. For example, the EbyE differences between the partonic flux in the target and the projectile may lead to a long-range asymmetry of the produced system [20–22], which manifests itself as a correlation between the multiplicity densities of final-state particles with large $\eta$ separation.

Longitudinal multiplicity correlations can also be generated during the space-time evolution in the final state as resonance decays, single-jet fragmentation, and Bose-Einstein correlations. These latter correlations are typically localized over a smaller range of $\eta$, and are commonly referred to as short-range correlations (SRC). On the other hand, dijet fragmentation may contribute to the LRC if the $\eta$ separation between the two jets is large.

Many previous studies are based on forward-backward (FB) correlations of particle multiplicity in two $\eta$ ranges symmetric around the center-of-mass of the collision systems, including $e^+e^-$ [23], $pp$ [24–27], and $A + A$ [28,29] collisions where a significant anticorrelation between forward and backward multiplicities has been identified. Recently, the study of multiplicity correlations has been generalized by decomposing the correlation function into orthogonal Legendre polynomial functions, or more generally into principal components, each representing a unique component of the measured FB correlation [21,30].

Particle production in $pp$ collisions is usually described by QCD-inspired models, such as PYTHIA [31] and EPOS [32], implemented in Monte Carlo (MC) event generators with free parameters that are tuned to describe experimental measurements. Previous studies show that these models can generally describe the $\eta$ and $p_T$ dependence of the inclusive charged-particle production [33,34], as well as the

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underlying event accompanying various hard-scattering processes [35,36]. In many such models, events with large charged-particle multiplicity are produced through multiple parton-parton interactions (MPI), which naturally serve as sources for the FB multiplicity asymmetry describe above. Therefore, a detailed measurement of pseudorapidity correlation in pp collisions also provides new constraints on the longitudinal dynamics of MPI processes in these models.

The two-particle correlation function in pseudorapidity is defined as [37,38]

\[
C(\eta_1, \eta_2) = \frac{\langle N(\eta_1)N(\eta_2) \rangle}{\langle N(\eta_1) \rangle \langle N(\eta_2) \rangle} \equiv \langle \rho(\eta_1)\rho(\eta_2) \rangle,
\]

\[
\rho(\eta) \equiv \frac{N(\eta)}{\langle N(\eta) \rangle},
\]

(1)

where \(N(\eta)\) is the multiplicity density distribution in a single event and \(\langle N(\eta) \rangle\) is the average distribution for a given event-multiplicity class. The correlation function is directly related to a single-particle quantity \(\rho(\eta)\), which characterizes the fluctuation of multiplicity in a single event relative to the average shape of the event class.

Following Refs. [21,38], \(\rho(\eta)\) in the interval \([-Y,Y]\) is written in terms of Legendre polynomials:

\[
\rho(\eta) \propto 1 + \sum_n a_n T_n(\eta), \quad T_n(\eta) \equiv \frac{2n+1}{3} Y P_n(\eta),
\]

(2)

and the scale factor in Eq. (2) is chosen such that \(T_1(\eta) = \eta\).

Using Eqs. (1) and (2), the correlation function \(C\) can be expressed in terms of the \(T_n\), which involve terms in \(\langle a_0 a_0 \rangle\), \(\langle a_0 a_n \rangle\), and \(\langle a_n a_m \rangle\), with \(n,m \geq 1\). Terms involving \(a_0\) reflect multiplicity fluctuations in the given event class, while the dynamical fluctuations between particles at different pseudorapidities in events of fixed multiplicity are captured by the terms in \(\langle a_n a_m \rangle\), \(n,m \geq 1\). It is the study of these dynamical fluctuations that is the goal of this analysis.

As discussed in more detail in Ref. [38], the terms involving \(\langle a_0 a_n \rangle\) can be removed, provided all deviations from 1 are small, by defining

\[
C_N(\eta_1, \eta_2) = \frac{C(\eta_1, \eta_2)}{C_p(\eta_1)C_p(\eta_2)},
\]

(3)

where

\[
C_p(\eta) = \int_{-Y}^{Y} C_p(\eta,\eta')d\eta',
\]

(4)

with a similar expression for \(C_p(\eta_2)\). The quantities \(C_p(\eta_1)\) and \(C_p(\eta_2)\) are referred to as the single-particle modes. The \(\langle a_0 a_0 \rangle\) term can be removed by renormalizing average value in the \(\eta_1, \eta_2\) phase space to be 1. The final result is

\[
\rho_N(\eta_1, \eta_2) = 1 + \sum_{n,m=1}^{\infty} a_{n,m} T_n(\eta_1)T_m(\eta_2) + T_n(\eta_2)T_m(\eta_1)/2,
\]

(5)

and

\[
a_{n,m} \equiv \langle a_n a_m \rangle.
\]

The two-particle Legendre coefficients can be calculated directly from the measured correlation function:

\[
a_n,m = \left(\frac{3}{2Y^3}\right)^2 \int_{-Y}^{Y} C_N(\eta_1, \eta_2)\times \frac{T_n(\eta_1)T_m(\eta_2) + T_n(\eta_2)T_m(\eta_1)}{2} d\eta_1 d\eta_2.
\]

(6)

The two-particle correlation measure, in effect, the root-mean-square (rms) values of the EbyE \(a_n\), \(a_n^{1/2}\), or the cross correlation between \(a_n\) and \(a_n^{1/2}\). The correlation functions satisfy the symmetry condition \(C(\eta_1, \eta_2) = C(\eta_2, \eta_1)\) and \(C_N(\eta_1, \eta_2) = C_N(\eta_2, \eta_1)\).

This paper presents a measurement of the two-dimensional (2-D) correlation function \(C_n(\eta_1, \eta_2)\) over the pseudorapidity range of \(|\eta| < 2.4\) in \(\sqrt{s_{NN}} = 2.76\) TeV Pb+Pb, \(\sqrt{s_{NN}} = 5.02\) TeV \(p + Pb\), and \(\sqrt{s} = 13\) TeV pp collisions, using the ATLAS detector. The analysis is performed using events for which the total number of reconstructed charged particles, \(N_{ch}\), with \(|\eta| < 2.5\) and transverse momentum \(p_T > 0.4\) GeV, is in the range \(10 \leq N_{ch} < 300\). Both the Pb+Pb and \(p + Pb\) data cover this range of \(N_{ch}\), but for pp the range extends only to approximately 160. The measured \(C_N(\eta_1, \eta_2)\) is separated into a short-range component \(\delta_{SRC}(\eta_1, \eta_2)\) and \(C_{NCH}(\eta_1, \eta_2)\), which contains the long-range component. The nature of the FB fluctuation in each collision system is studied by projections as well as Legendre coefficients \(\langle a_n a_m \rangle\) of \(C_{NCH}(\eta_1, \eta_2)\). The magnitudes of the FB fluctuations are compared for the three systems at similar event multiplicity. A comparison is also made between the pp data and QCD-inspired models.

II. ATLAS DETECTOR AND TRIGGER

The ATLAS detector [39] provides nearly full solid-angle coverage of the collision point with tracking detectors, calorimeters, and muon chambers and is well suited for measurement of two-particle correlations over a large pseudorapidity range. The measurements were performed using the inner detector (ID), minimum-bias trigger scintillators (MBTS), the forward calorimeter (FCal), and the zero-degree calorimeters (ZDC). The ID detects charged particles within \(|\eta| < 2.5\) using a combination of silicon pixel detectors, silicon microstrip detectors (SCT), and a straw-tube transition radiation tracker (TRT), all immersed in a 2-T axial magnetic field [40]. An additional pixel layer, the “insertable B layer” (IBL) [41,42] installed between run 1 and run 2 (2013–2015), is used in the 13-TeV pp measurements. The MBTS system detects charged particles over \(2.1 \leq |\eta| \leq 3.9\) using two hodoscopes of counters positioned at \(z = \pm 3.6\) m. The FCal consists of three sampling layers, longitudinal in shower depth.

\[2\text{ATLAS uses a right-handed coordinate system with its origin at the nominal interaction point (IP) in the center of the detector and the } z \text{ axis along the beam pipe. The } x \text{ axis points from the IP to the center of the LHC ring, and the } y \text{ axis points upward. Cylindrical coordinates } (r, \phi) \text{ are used in the transverse plane, } \phi \text{ being the azimuthal angle around the beam pipe. The pseudorapidity is defined in terms of the polar angle } \theta \text{ as } \eta = -\ln \tan(\theta/2).\]
and covers $3.2 < |\eta| < 4.9$. The ZDC, available in the Pb+Pb and $p + Pb$ runs, are positioned at $\pm 140$ m from the collision point, detecting neutrons and photons with $|\eta| > 8.3$.

This analysis uses approximately $7 \, \mu b^{-1}$ of Pb+Pb data, 28 nb$^{-1}$ of $p + Pb$ data, and 65 nb$^{-1}$ of $pp$ data taken by the ATLAS experiment at the LHC. The Pb+Pb data were collected in 2010 at a nucleon-nucleon center-of-mass energy $\sqrt{s_{NN}} = 2.76$ TeV. The $p + Pb$ data were collected in 2013, when the LHC was configured with a 4-TeV proton beam and a 1.57-TeV per-nucleon Pb beam that together produced collisions at $\sqrt{s_{NN}} = 5.02$ TeV. The higher energy of the proton beam results in a rapidity shift of 0.47 of the nucleon-nucleon center-of-mass frame towards the proton beam direction relative to the laboratory rest frame. The $pp$ data were collected during a low-luminosity operation of the LHC in June and August 2015 at collision energy $\sqrt{s} = 13$ TeV.

The ATLAS trigger system [43] consists of a level-1 (L1) trigger implemented using a combination of dedicated electronics and programmable logic, and a high-level trigger (HLT) implemented in processors. The HLT reconstructs charged-particle tracks and primary vertices are reconstructed in the ID using algorithms whose implementation was optimized for better performance between LHC runs 1 and 2. In order to compare directly the $p + Pb$ and $Pb+Pb$ systems using event selection based on the multiplicity of the collisions, a subset of data from peripheral $Pb+Pb$ collisions, collected during the 2010 LHC heavy-ion run with a minimum-bias trigger, was reanalyzed using the same track reconstruction algorithm as that used for $p + Pb$ collisions. For the $p + Pb$ and $Pb+Pb$ analyses, tracks are required to have a $p_T$-dependent minimum number of hits in the SCT, and the transverse ($d_0$) and longitudinal ($z_0 \sin \theta$) impact parameters of the track relative to the vertex are required to be less than 1.5 mm. A description of the 2010 Pb+Pb data and 2013 $p + Pb$ data can be found in Refs. [5] and [45], respectively.

For the 13-TeV $pp$ analysis, the track selection criteria were modified slightly to profit from the presence of the IBL in run 2. Furthermore, the requirements of $|d_0| < 1.5$ mm and $z_0 \sin \theta < 1.5$ mm are applied, where $d_0$ is the transverse impact parameter of the track relative to the average beam position. These selection criteria are the same as those in Refs. [12,33].

In this analysis, the correlation functions are constructed using tracks passing the above selection requirements and which have $p_T > 0.2$ GeV and $|\eta| < 2.4$. However, slightly different kinematic requirements, $p_T > 0.4$ GeV and $|\eta| < 2.5$, are used to count the number of reconstructed charged particles in the event, denoted by $N_{ch}^{rec}$, to be consistent with the requirements used in the HLT. Figure 1 compares the normalized $N_{ch}^{rec}$ distributions of events in the three colliding systems. The distribution decreases slowly in the $Pb+Pb$ system, but decreases much faster in the $p + Pb$ and $pp$ systems. A major goal of the analysis is to compare the correlation function from the three collisions systems at similar $N_{ch}^{rec}$ values, which can reveal whether the FB multiplicity fluctuation is controlled by the collision geometry or the overall activity of the event.

The efficiency of the track reconstruction and track selection requirements, $\epsilon(\eta, p_T)$, is evaluated using simulated $p + Pb$ or $Pb+Pb$ events produced with the HIJING event generator [46] or simulated $pp$ events from the PYTHIA 8.
The reconstruction efficiency for Pb events in the multiplicity region of interest was very small; therefore, the reconstruction efficiency for Pb events was taken from the larger p + Pb sample. The p + Pb efficiency was found to be consistent with the efficiency from the Pb + Pb MC simulation, but of much higher precision. The response of the detector to these MC events is simulated using GEANT4 [48,49] and the resulting events are reconstructed with the same algorithms that are applied to the data. The efficiencies for the three datasets are similar for events with similar multiplicity. Small differences are due to changes in the detector conditions in run 1 and changes in the reconstruction algorithm between runs 1 and 2. In the simulated events, the efficiency reduces the measured charged-particle multiplicity relative to the event generator multiplicity for primary charged particles. The reduction factors for $N_{\text{ch}}^{\text{rec}}$ and the associated efficiency uncertainties are $b = 1.29 \pm 0.05$, $1.29 \pm 0.05$, and $1.18 \pm 0.05$ for Pb + Pb, $p + Pb$, and pp collisions, respectively. The values of these reduction factors are found to be independent of multiplicity over the $N_{\text{ch}}^{\text{rec}}$ range used in this analysis, $10 \leq N_{\text{ch}}^{\text{rec}} \leq 300$. Therefore, these factors are used to multiply $N_{\text{ch}}^{\text{rec}}$ to obtain the efficiency-corrected average number of charged particles with $p_T > 0.4$ GeV and $|\eta| < 2.5$, $N_{\text{ch}} = b N_{\text{ch}}^{\text{rec}}$. The quantity $N_{\text{ch}}$ is used when presenting the multiplicity dependence of the SRC and LRC.

B. Two-particle correlations

The two-particle correlation function defined in Eq. (1) is calculated as the ratio of distributions for same-event pairs $S(\eta_1, \eta_2) \propto \langle N(\eta_1)N(\eta_2) \rangle$ and mixed-event pairs $B(\eta_1, \eta_2) \propto \langle N(\eta_1)N(\eta_2) \rangle$ [5]:

$$C(\eta_1, \eta_2) = \frac{S(\eta_1, \eta_2)}{B(\eta_1, \eta_2)}.$$  

The mixed-event pair distribution is constructed by combining tracks from one event with those from another event with similar $N_{\text{ch}}^{\text{rec}}$ (matched within two tracks) and $z_{\text{vtx}}$ (matched within 2.5 mm). The events are also required to be close to each other in time to account for possible time-dependent variation of the detector conditions. The mixed-event distribution should account properly for detector inefficiencies and nonuniformity but does not contain physical correlations. The normalization of $C(\eta_1, \eta_2)$ is chosen such that its average value in the $(\eta_1, \eta_2)$ plane is one. The correlation function satisfies the symmetry $C(\eta_1, \eta_2) = C(\eta_2, \eta_1)$ and, for a symmetric collision system, $C(\eta_1, \eta_2) = C(-\eta_1, -\eta_2)$. Therefore, for pp and Pb + Pb collisions, all pairs are entered into one quadrant of the $(\eta_1, \eta_2)$ space defined by $\eta_- \equiv \eta_1 - \eta_2 > 0$ and $\eta_+ \equiv \eta_1 + \eta_2 > 0$ and then reflected to the other quadrants. For p + Pb collisions, all pairs are entered into one half of the $(\eta_1, \eta_2)$ space defined by $\eta_1 - \eta_2 > 0$ and then reflected to the other half. To correct $S(\eta_1, \eta_2)$ and $B(\eta_1, \eta_2)$ for the individual inefficiencies of particles in the pair, the pairs are weighted by the inverse product of their tracking efficiencies $1/(\epsilon_1 \epsilon_2)$. Remaining detector distortions not accounted for by the reconstruction efficiency largely cancel in the same-event to mixed-event ratio.

In a separate analysis, the correlation functions in $p + Pb$ collisions are also symmetrized in the same way as for Pb + Pb and pp collisions such that $C(\eta_1, \eta_2) = C(-\eta_1, -\eta_2)$, and they are compared with correlation functions obtained for symmetric collision systems. This symmetrized $p + Pb$ correlation function is used only at the end of Sec. IV, in relation to Fig. 16. In all other cases, the $p + Pb$ correlation function is unsymmetrized.

C. Outline of the procedure for separating SRC and LRC

As explained in the introduction, the aim of this analysis is to measure and parametrize the long-range correlation, which requires the separation and subtraction of the short-range component. The separation of SRC and LRC is quite involved and so is briefly summarized here, with details left to the relevant later sections.

The core of the separation method is to exploit the difference between the correlations for opposite-charge and same-charge pairs, $C^+(\eta_1, \eta_2)$ and $C^{\pm}(\eta_1, \eta_2)$, respectively. The SRC component centered around $\eta_- \equiv \eta_1 - \eta_2 \sim 0$ is found to be much stronger for opposite-charge pairs, primarily due to local charge conservation, while the LRC and single-particle modes are expected to be independent of the charge combination. With this assumption, the ratio

$$R(\eta_1, \eta_2) = C^+(\eta_1, \eta_2)/C^{\pm}(\eta_1, \eta_2)$$  

is given approximately by

$$R(\eta_1, \eta_2) \approx 1 + \delta_{\text{SRC}}(\eta_1, \eta_2) - \delta_{\text{SRC}}^{\pm}(\eta_1, \eta_2).$$  

This analysis assumes further that the dependence of $\delta_{\text{SRC}}$ on $\eta_- + \eta_+$ factorizes and that the dependence...
on $\eta_+$ is independent of the charge combination $\delta_{\text{SRC}}^{\pm\pm} = f(\eta_+)g^{\pm\pm}(\eta_-)$, $\delta_{\text{SRC}}^{\pm-} = f(\eta_+)g^{\pm-}(\eta_-)$, where $g^{\pm\pm}(\eta_-)$ and $g^{\pm-}(\eta_-)$ are allowed to differ in both shape and magnitude. With these assumptions, $f(\eta_+)$ can be determined from $R$ by suitable integration over $\eta_-$, as described in Sec. III D.

To complete the determination of $\delta_{\text{SRC}}^{\pm\pm}$, the quantity $g^{\pm\pm}$ is determined and parameterized from suitable projections of $C_N^{\pm\pm}(\eta_+,\eta_-)$ in the $\eta_-$ direction, as described in Sec. III E. The use of $C_N^{\pm\pm}$ rather than $C^{\pm\pm}$ is because the former does not contain the single-particle modes. The procedure to obtain a correlation function with the SRC subtracted is also described in Sec. III E. With $\delta_{\text{SRC}}^{\pm\pm}$ determined, $\delta_{\text{SRC}}^{\pm-}$ is obtained directly from Eq. (9). The $\delta_{\text{SRC}}^{\pm\pm}$ and $\delta_{\text{SRC}}^{\pm-}$ are then averaged to obtain the SRC for all charge combinations, $\delta_{\text{SRC}}$.

**D. Probing the SRC via the same-charge and opposite-charge correlations**

Figure 2 shows separately the correlation functions for same-charge pairs and opposite-charge pairs from Pb+Pb collisions with $200 \leq N_{\text{ch}}^{\text{rec}} < 220$. The ratio of the two, $R(\eta_1,\eta_2)$ via Eq. (8), is shown in the top right panel. The correlation functions show a narrow ridgeline shape along $\eta_1 \approx \eta_2$ or $\eta_- \approx 0$, and a falloff towards the corners at $\eta_1 = -\eta_2 = \pm 2.4$. The magnitude of the ridge for the opposite-charge pairs is stronger than that for the same-charge pairs, which is characteristic of the influence from SRC from jet fragmentation or resonance decays. In regions away from the SRC, i.e., large values of $|\eta_-|$, the ratio approaches unity, suggesting that the magnitude of the LRC is independent of the charge combinations. To quantify the shape of the SRC in the ratio along $\eta_+$, $R$ is expressed in terms of $\eta_+$ and $\eta_-$, $R(\eta_+,\eta_-)$, and the following quantity is calculated:

$$f(\eta_+) = \frac{\int_{-0.4}^{0.4} R(\eta_+,\eta_-)/0.8 \, d\eta_- - 1}{\int_{-0.4}^{0.4} R(0,\eta_-)/0.8 \, d\eta_- - 1}.$$  

As shown in Fig. 2, the quantity $f(\eta_+)$ is nearly constant in Pb+Pb collisions, implying that the SRC is consistent with being independent of $\eta_+$. To quantify the shape of the SRC along the $\eta_+$ direction, $R(\eta_+\eta_-)$ is fit to a Gaussian function in slices of $\eta_-$. The width, as shown in the bottom middle panel of Fig. 2, is constant, which may suggest that the shape of the SRC in $\eta_-$ is the same for different $\eta_+$ slices.

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4The validity of the various assumptions is confirmed in the data from the extracted $\delta_{\text{SRC}}^{\pm\pm}(\eta_+,\eta_-)$ and $\delta_{\text{SRC}}^{\pm-}(\eta_+,\eta_-)$ after applying the separation procedure.
Figure 3 shows the correlation function in $p+Pb$ collisions with multiplicity similar to the $Pb+Pb$ data in Fig. 2. The correlation function shows a significant asymmetry between the proton-going side (positive $\eta_+$) and lead-going side (negative $\eta_-$). However, much of this asymmetry appears to be confined to a small $|\eta_-|$ region where the SRC dominates. The magnitude of the SRC, estimated by $f(\eta_+)$ shown in the bottom-right panel, increases by about 50% from the lead-going side (negative $\eta_-$) to the proton-going side (positive $\eta_+$), but the width of the SRC in $\eta_-$ is independent of $\eta_+$ as shown in the bottom-middle panel. In contrast, the LRC has no dependence on the charge combinations, since the value of $R$ approaches unity at large $|\eta_-|$.

Figure 4 shows the width in $\eta_-$ of the short-range component as a function of $N_{ch}$ in the three collision systems. The width is obtained as the Gaussian width of $R(\eta_+; \eta_-)$ in the $\eta_-$ direction, and then averaged over $\eta_+$ as the width is observed to be independent of $\eta_+$, as shown in Figs. 2 and 3. This width reflects the extent of the short-range correlation in $\eta$, and it is observed to decrease with increasing $N_{ch}$ in all collision systems. At the same $N_{ch}$ value, the width is smallest in $pp$ collisions and largest in $Pb+Pb$ collisions. In Fig. 5, the width of the short-range component from $pp$ data is compared with PYTHIA 8 based on the A2 tune [50] and EPOS based on the LHC tune [32]. The width is underestimated by PYTHIA 8 A2 and overestimated by EPOS LHC.

![Diagram](image-url)
E. Separation of the SRC and the LRC

As discussed in Sec. III C, the ratio of the correlation function between opposite-charge and same-charge pairs $R(\eta_{+}, \eta_{-})$ is the key to the separation of the SRC and LRC. Following Eqs. (8) and (9), this ratio can be approximated by

$$R(\eta_{+}, \eta_{-}) \approx 1 + f(\eta_{+})[g^{+}(\eta_{-}) - g^{\pm\pm}(\eta_{-})],$$

$$\delta_{\text{SRC}}^{\pm\pm} = f(\eta_{+})g^{+}(\eta_{-}),$$

$$\delta_{\text{SRC}}^{\pm\pm} = f(\eta_{+})g^{\pm\pm}(\eta_{-}),$$

(11)

where $f(\eta_{+})$ describes the shape along $\eta_{+}$ and can be calculated via Eq. (10). The functions $g^{+}$ and $g^{\pm\pm}$ describe the SRC along the $\eta_{-}$ direction for the two charge combinations, which differ in both magnitude and shape.

In order to estimate the $g^{\pm\pm}(\eta_{-})$ function for same-charged pairs, the $C_N(\eta_{+}, \eta_{-})$ distributions for same-charge pairs are projected into one-dimensional (1-D) $\eta_{-}$ distributions over a narrow slice $|\eta_{+}| < 0.4$. The distributions are denoted by $C_N(\eta_{-})$. They are shown, after a small iterative correction discussed below, in the second column of Fig. 6 for the same-charge pairs in Pb+Pb and $p + Pb$ collisions. The SRC appears as a narrow peak on top of a distribution that has an approximately quadratic shape. Therefore, a quadratic fit is applied to the data in the region of $|\eta_{-}| > 1.5$, and the difference between the data and fit in the $|\eta_{-}| < 2$ region is taken as the estimated SRC component or the $g^{\pm\pm}(\eta_{-})$ function, which is assumed to be zero for $|\eta_{-}| < 1.5$. This range $|\eta_{-}| > 1.5$ is about twice the width of the short-range peak in the $R(\eta_{+}, \eta_{-})$ distribution along the $\eta_{-}$ direction (examples are given in the bottom middle panel of Figs. 2 and 3). This width is observed to decrease from 1.0 to 0.7 as a function of $N_{ch}^{rec}$ in the $p + Pb$ collisions, and is slightly broader in Pb+Pb collisions and slightly narrower in pp collisions at the same $N_{ch}^{rec}$.

The range of the fit is varied from $|\eta_{-}| > 1.0$ to $|\eta_{-}| > 2.0$ to check the sensitivity of the SRC estimation, and the variation is included in the final systematic uncertainties. Furthermore, this study is also repeated for $C_N(\eta_{-})$ obtained in several other $\eta_{+}$ slices within $|\eta_{+}| < 1.2$, and consistent results are obtained. Once the distribution $g^{\pm\pm}(\eta_{-})$ for same-charge pairs is obtained from the fit, it is multiplied by the $f(\eta_{+})$ function calculated from $R(\eta_{1}, \eta_{2})$ using Eq. (10), to obtain the...
\[ \delta_{\text{SRC}}(\eta_1, \eta_2) \] from Eq. (11) in the full phase space. Subtracting this distribution from the \( C_N(\eta_1, \eta_2) \) distribution, one obtains the initial estimate of the correlation function containing mostly the LRC component.

The LRC obtained via this procedure is still affected by a small bias from the SRC via the normalization procedure of Eq. (3). This bias appears because the \( \delta_{\text{SRC}}(\eta_1, \eta_2) \) contribution is removed from the numerator but is still included in the denominator via \( C_p(\eta_1) \). This contribution is not uniform in \( \eta \): If the first particle is near midrapidity \( \eta_1 \approx 0 \) then all pairs in \( \delta_{\text{SRC}}(\eta_1, \eta_2) \) contribute to \( C_p(\eta_1) \), whereas if the first particle is near the edge of the acceptance \( \eta_1 \approx \pm Y \) then only half of the pairs in \( \delta_{\text{SRC}}(\eta_1, \eta_2) \) contribute to \( C_p(\eta_1) \). The acceptance bias in \( C_p \) is removed via a simple iterative procedure: First, the \( \delta_{\text{SRC}} \) contribution determined from the above procedure is used to eliminate the SRC contribution to the single-particle mode:

\[
\begin{align*}
C^\text{sub}_{p}(\eta_1) &= \frac{\int^Y |C(\eta_1, \eta_2) - \delta_{\text{SRC}}(\eta_1, \eta_2)| d\eta_2}{2Y},
\end{align*}
\]  

with a similar expression for \( C^\text{sub}_{p}(\eta_2) \). The \( C^\text{sub}_{p}(\eta_1) \), \( C^\text{sub}_{p}(\eta_2) \) are then used to redefine the \( C_N \) function:

\[
C'_N(\eta_1, \eta_2) = \frac{C(\eta_1, \eta_2)}{C^\text{sub}_{p}(\eta_1)C^\text{sub}_{p}(\eta_2)}.  
\]  

This distribution, which is very close to the distribution before correction, is shown in the second column of Fig. 6 for projection over a narrow slice \( |\eta - 1| < 0.4 \). The estimation of \( \delta_{\text{SRC}}(\eta_1, \eta_2) \) is repeated using the previously described procedure for the \( C'_N(\eta_1, \eta_2) \) and the extracted distribution is shown in the third column of Fig. 6. Subtracting this distribution from \( C'_N(\eta_1, \eta_2) \), one obtains the correlation function containing only the LRC component. The resulting correlation function, denoted \( C^\text{sub}_{N}(\eta_1, \eta_2) \), is shown in the last column of Fig. 6.

The results presented in this paper are obtained using the iterative procedure discussed above. In most cases, the results obtained from the iterative procedure are consistent with the one obtained without iteration. In \( p + \text{Pb} \) and \( \text{Pb}+\text{Pb} \) collisions, where the SRC component is small, the difference between the two methods is found to be less than 2\%. In \( pp \) collisions with \( N_{\text{ch}}^{\text{rec}} > 100 \), the difference between the two methods reaches 4\% where the SRC is large and therefore the bias correction is more important.

In principle, the same analysis procedure can be applied to opposite-charge and all-charge pairs. However, due to the much larger SRC, the extracted LRC for opposite-charge pairs has larger uncertainties. Instead, the SRC for opposite-charge pairs is obtained directly by rearranging the terms in Eq. (9) as

\[
\delta_{\text{SRC}}(\eta_1, \eta_2) = R(\eta_1, \eta_2) - 1 + \delta_{\text{SRC}}(\eta_1, \eta_2).  
\]  

The SRC for all-charge pairs is calculated as the average of \( \delta_{\text{SRC}}^+ \) and \( \delta_{\text{SRC}}^- \) weighted by the number of same-charge and opposite-charge pairs. The LRC is then obtained by subtracting the SRC from the modified \( C_N(\eta_1, \eta_2) \) using the same procedure as that for the same-charge pairs.

For \( pp \) collisions, the pseudorapidity correlations are also compared with the PYTHIA 8 A2 and EPOS LHC event generators mentioned above. The analysis procedure used on the data is repeated for the two models in order to extract the SRC and LRC components. The correlation is carried out on the generated, as opposed to the reconstructed, charged particles.

\section*{F. Quantifying the magnitude of the forward-backward multiplicity fluctuations}

In the azimuthal correlation analysis, the azimuthal structure of the correlation function is characterized by harmonic coefficients \( v_n \) obtained via a Fourier decomposition \cite{5,51}. A similar approach can be applied for pseudorapidity correlations \cite{21,38}. Following Eq. (5), the correlation functions are expanded into Legendre polynomial functions, and the two-particle Legendre coefficients \( \langle a_n a_m \rangle \) are calculated directly from the correlation function according to Eq. (6). The two-particle correlation method measures, in effect, the rms values of the EbyE \( a_n \), and the final results for the coefficients are presented in terms of \( \sqrt{\langle a_n a_m \rangle} \). As a consequence of the condition for a symmetric collision system, the odd and even coefficients should be uncorrelated in \( pp \) and \( \text{Pb}+\text{Pb} \) collisions:

\[
a_{n.n+1} = \langle a_n a_{n+1} \rangle = 0.  
\]  

However, even in \( pp \) or \( \text{Pb}+\text{Pb} \) collisions, the correlation function after SRC removal, \( C^\text{sub}_{N}(\eta_1, \eta_2) \), is observed to be nearly symmetric between \( \eta \) and \(-\eta \) (right column of Fig. 6), and hence the \( \langle a_n a_{n+1} \rangle \) values are very small and considered to be negligible in this paper.

The shape of the first two Legendre bases in 2-D are shown in Fig. 7. The first basis function has the shape of \( \eta_1 \times \eta_2 \) and is directly sensitive to the FB asymmetry of the EbyE fluctuation. The second basis function has a quadratic shape in the \( \eta_1 \) and \( \eta_2 \) directions and is sensitive to the EbyE fluctuation in the width of the \( N(\eta) \) distribution. It is shown in Sec. IV that the data require only the first term, in which case the shape of the correlation function can be approximated by

\[
C^\text{sub}_{N}(\eta_1, \eta_2) \approx 1 + \langle a^2_1 \rangle \eta_1 \eta_2 = 1 + \frac{\langle a^2_1 \rangle}{4} \left( \eta_1^2 - \eta_2^2 \right).  
\]  

Therefore, a quadratic shape is expected along the two diagonal directions \( \eta_+ \) and \( \eta_- \) of the correlation function, and the \( \langle a^2_1 \rangle^{1/2} \)
The methods to estimate uncertainties in the resulting \((a_1^2)^{1/2}\) values. These uncertainties are not always the same for \(C_N\) and \(C_{\text{sub}}\) because \(C_{\text{sub}}\) is not sensitive to the variation in the short-range region, \(\eta_- \approx 0\). In the following, the uncertainty from each source is discussed.

The main source of uncertainty for \(C_{\text{sub}}(\eta_1,\eta_2)\) arises from the procedure to separate the SRC and the LRC. Since the estimated SRC component for the opposite-charge pairs is more than a factor of two larger than that for the same-charge pairs (e.g., Figs. 2 and 3), the difference between \(C_{\text{sub}}(\eta_-)\) and \(C_{\text{sub},\pm\pm}\) is a conservative check of the robustness of the subtraction procedure. This difference is typically small for events with large \(N_{\text{ch}}\) and it is found to be within 0.2–2.2\% of the correlation signal and 1–6\% for \((a_1^2)^{1/2}\) in the three collision systems. The stability of LRC is also checked by varying the fit range and varying the \(\eta_-\) slice used to obtain the \(\delta_{\text{SRC}}(\eta_-)\) distribution for same-charge pairs. This uncertainty amounts to 1–2\% in the correlation signal and 1–5\% for \((a_1^2)^{1/2}\) in Pb+Pb collisions, and is larger in \(p + \text{Pb}\) and \(pp\) collisions due to a stronger SRC for events with the same \(N_{\text{ch}}\).

Uncertainties due to the event mixing are evaluated by varying the criteria for matching events in \(N_{\text{ch}}\). The \(d_n, m\) values are calculated for each case. The uncertainty from variation of the matching range in \(z_{\text{vtx}}\) is less than 0.5\% of the correlation signal for both \(C_N\) and \(C_{\text{sub}}\). The bin size in \(N_{\text{ch}}\) for event matching is varied such that the number of events in each bin varies by a factor of three. Most of the changes appear as modulations of the projections of the correlation function in \(\eta_1\) or \(\eta_2\) as defined in Eq. (4), and the renormalized correlation functions \(C_N(\eta_1,\eta_2)\) and \(C_{\text{sub}}(\eta_1,\eta_2)\) are very stable. The difference between different variations amounts to at most 2\% of the correlation signal or \((a_1^2)^{1/2}\). The analysis is also repeated separately for events with \(|z_{\text{vtx}}| < 50 \text{ mm}\) and \(50 < |z_{\text{vtx}}| < 100 \text{ mm}\). Good agreement is seen between the two. To evaluate the stability of the correlation function, the entire dataset is divided into several groups of runs, and the correlation functions and \(d_n\) coefficients are calculated for each group. The results are found to be consistent within 2\% for \((a_1^2)^{1/2}\).

The 13-TeV \(pp\) results are obtained from the June 2015 and August 2015 datasets with different \(\mu\) values. The influence of the residual pileup is evaluated by comparing the results obtained separately from these two running periods, and no systematic difference is observed between the results.

The shape of the correlation function is not very sensitive to the uncertainty in the tracking efficiency correction, since this correction is applied in both the numerator and denominator. On the other hand, both the correlation signal and reconstruction efficiency are observed to increase with \(p_T\), and hence the correlation signal and associated \((d_{n,m})\) coefficients are expected to be smaller when corrected for reconstruction efficiency. Indeed, a 1–2\% decrease in \((a_1^2)^{1/2}\) is observed after applying this correction. This change is conservatively included in the systematic uncertainty.

The correlation function \(C_N(\eta_1,\eta_2)\) has some small localized structures that are not compatible with statistical fluctuations. These structures are due to residual detector effects in the pair acceptance that are not removed by the event-mixing procedure, which can be important for extraction of the higher-order coefficients. Indeed, the Legendre coefficients for
TABLE I. Summary of average systematic uncertainties for the correlation function $C_{N}^{ab}(\eta_{1},\eta_{2})$ with $p_{T} > 0.2$ GeV. The uncertainty is calculated as the variation relative to the correlation signal of $C_{N}^{ab}(\eta_{1},\eta_{2})$, averaged over the entire $\eta_{1}$ and $\eta_{2}$ space. The range in the table covers the variation of this uncertainty for different $N_{ch}^{rec}$ classes.

<table>
<thead>
<tr>
<th>Collision system</th>
<th>Pb+Pb</th>
<th>$p + Pb$</th>
<th>$pp$</th>
</tr>
</thead>
<tbody>
<tr>
<td>Charge dependence [%]</td>
<td>0.2–1.6</td>
<td>0.2–1.9</td>
<td>0.7–2.2</td>
</tr>
<tr>
<td>SRC LRC separation [%]</td>
<td>1.0–2.2</td>
<td>1.2–5.7</td>
<td>1.1–3.9</td>
</tr>
<tr>
<td>Event-mixing [%]</td>
<td>0.7–1.0</td>
<td>0.4–2.5</td>
<td>0.2–1.8</td>
</tr>
<tr>
<td>$z_{\text{st}}$ variation [%]</td>
<td>0.4–0.7</td>
<td>0.3–1.8</td>
<td>0.2–2.0</td>
</tr>
<tr>
<td>Run-by-run stability [%]</td>
<td>0.4–0.8</td>
<td>0.3–1.7</td>
<td>0.2–1.6</td>
</tr>
<tr>
<td>Track selection &amp; efficiency [%]</td>
<td>0.7–1.4</td>
<td>0.2–0.3</td>
<td>0.3–0.6</td>
</tr>
<tr>
<td>MC consistency [%]</td>
<td>0.4–2.2</td>
<td>0.6–2.9</td>
<td>0.6–2.9</td>
</tr>
<tr>
<td>Total [%]</td>
<td>1.6–3.6</td>
<td>1.6–7.2</td>
<td>2.0–5.9</td>
</tr>
</tbody>
</table>

$n \geq 8$ show significant nonstatistical fluctuations around zero. Therefore, the spread of $(a_{1}^{2})^{1/2}$ for $n \geq 10$ and $\sqrt{|(a_{0}a_{0}+a_{2})|}$ for $n \geq 8$ are quoted as uncertainties for the Legendre coefficients. These uncertainties are less than 0.5 $\times 10^{-5}$ for $(a_{0}a_{m})$ calculated from $C_{N}^{ab}(\eta_{1},\eta_{2})$ in all collision systems, and are larger for those calculated from $C_{N}(\eta_{1},\eta_{2})$. The corresponding relative uncertainty for $(a_{1}^{2})$ is negligible.

The HIJING and PYTHIA 8 events used for evaluating the reconstruction efficiency have a significant correlation signal and sizable $a_{0,m}$ coefficients for $C_{N}$. The correlation functions obtained using the reconstructed tracks are compared with those obtained using the generated charged particles. The ratio of the two is then used to vary the measured $C_{N}(\eta_{1},\eta_{2})$, the procedure for removal of the SRC is repeated, and the variations of $C_{N}^{ab}$ and $a_{0,m}$ are calculated. The differences in the correlation function reflect mainly the uncertainty in the efficiency correction, but also the influence of secondary decays and fake tracks. These differences are found to be mostly concentrated in a region around $\eta_{-} \approx 0$; hence, they affect mostly the estimation of the SRC component and have very little impact on $C_{N}$ and associated $a_{0,m}$. The differences in Legendre coefficients are found to be up to 5% for $a_{0}$ calculated from $C_{N}$ and are 0.2–3.5% for $(a_{1}^{2})^{1/2}$ calculated from $C_{N}^{ab}$.

The systematic uncertainties from the different sources described above are added in quadrature to give the total systematic uncertainties for the correlation functions and $(a_{1}^{2})^{1/2}$ values for both $C_{N}$ and $C_{N}^{ab}$. The systematic uncertainties associated with $C_{N}^{ab}(\eta_{1},\eta_{2})$ and $(a_{1}^{2})^{1/2}$ are given in Tables I and II, respectively. Since there are four methods for extracting $(a_{1}^{2})^{1/2}$, they are given separately in Table II. The systematic uncertainty quoted for each source in both tables covers the maximum uncertainty in the specified collision system.

TABLE II. Summary of systematic uncertainties for $(a_{1}^{2})^{1/2}$ with $p_{T} > 0.2$ GeV, calculated with four different methods: Legendre expansion of $C_{N}^{ab}(\eta_{1},\eta_{2})$, quadratic fit of the $\eta_{-}$ dependence of $C_{N}^{ab}(\eta_{1},\eta_{2})$ for $|\eta_{+}| < 0.1$, quadratic fit of the $\eta_{+}$ dependence of $C_{N}^{ab}(\eta_{1},\eta_{2})$ for $0.9 < |\eta_{-}| < 1.1$, and linear fit of the $\eta$ dependence of $r_{N}^{ab}(\eta_{N},\eta_{\text{rel}})$ for $2.2 < |\eta_{\text{rel}}| < 2.4$.

| Collision system          | Quadratic fit to $C_{N}^{ab}(\eta_{-})_{|\eta_{+}|<0.1}$ | Quadratic fit to $C_{N}^{ab}(\eta_{+})_{|0.9<|\eta_{-}|<1.1}$ | Linear fit to $r_{N}^{ab}(\eta)_{2.2<|\eta_{\text{rel}}|<2.4}$ | Global Legendre expansion of $C_{N}^{ab}$ |
|---------------------------|----------------------------------------------------------|-----------------------------------------------------------|----------------------------------------------------------|-------------------------------------------|
| Pb+Pb                     | $0.1–2.7$                                               | $0.4–2.5$                                               | $1.1–3.4$                                               | $0.2–5.5$                                               | $0.5–7.0$                                               | $1.2–7.3$                                               |
| $p + Pb$                  | $1.2–6.7$                                               | $1.4–5.3$                                               | $1.0–2.9$                                               | $0.8–3.1$                                               | $1.8–3.5$                                               | $0.3–3.4$                                               |
| $pp$                      | $0.2–3.2$                                               | $0.2–4.2$                                               | $0.2–1.4$                                               | $0.3–2.4$                                               | $0.2–3.7$                                               | $0.2–3.7$                                               |
| Charge dependence [%]     | $0.3–1.9$                                               | $0.2–3.0$                                               | $1.0–1.9$                                               | $0.7–4.7$                                               | $0.7–1.0$                                               | $0.8–1.4$                                               |
| SRC LRC separation [%]    | $0.1–2.1$                                               | $0.4–4.9$                                               | $1.8–7.2$                                               | $0.8–5.1$                                               | $0.2–5.8$                                               | $0.4–8.1$                                               |
| Event mixing [%]          | $0.6–4.4$                                               | $3.1–9.7$                                               | $2.2–5.6$                                               | $1.9–6.2$                                               | $2.8–10.0$                                              | $2.8–10.0$                                              |
| $z_{\text{st}}$ variation [%] | $0.3–3.4$                               | $0.4–3.5$                                               | $0.9–4.3$                                               | $0.3–4.5$                                               | $0.4–5.2$                                               | $1.5–6.3$                                               |
| Run-by-run stability [%]  | $1.3–2.4$                                               | $1.2–4.2$                                               | $1.4–2.7$                                               | $1.2–4.5$                                               | $2.2–8.8$                                               | $2.5–5.9$                                               |
| Track selection & efficiency [%] | $0.2–1.6$                                           | $0.2–2.6$                                               | $0.2–2.7$                                               | $0.2–1.7$                                               | $0.2–1.6$                                               | $0.2–2.5$                                               |
| MC consistency [%]        | $0.6–2.2$                                               | $0.3–1.0$                                               | $1.0–1.5$                                               | $0.5–1.4$                                               | $0.5–1.0$                                               | $1.1–2.1$                                               |
| Total [%]                 | $2.4–4.9$                                               | $1.8–5.3$                                               | $2.4–4.5$                                               | $2.3–5.0$                                               | $2.5–9.1$                                               | $3.4–8.2$                                               |

IV. RESULTS

The top row of Fig. 8 shows the correlation functions $C_{N}(\eta_{1},\eta_{2})$ in the three collision systems for events with similar multiplicity $100 \leq N_{ch}^{rec} < 120$. The corresponding estimated SRC component $\delta_{SRC}(\eta_{1},\eta_{2})$ and long-range component $C_{N}^{ab}(\eta_{1},\eta_{2})$ are shown in the middle and bottom rows, respectively. The magnitude of the SRC in $p + Pb$ is observed to be larger in the proton-going direction than in the lead-going direction, reflecting the fact that the particle multiplicity is smaller in the proton-going direction. However, this forward-backward asymmetry in $p + Pb$ collisions is mainly associated

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with the SRC component, and the $C_N^{\text{sub}}(\eta_1, \eta_2)$ distribution shows very little asymmetry. The $C_N(\eta_1, \eta_2)$ distributions show significant differences between the three systems, which is mainly due to their differences in $\delta_{\text{SRC}}(\eta_1, \eta_2)$. In fact, the estimated long-range component $C_N^{\text{sub}}(\eta_1, \eta_2)$ shows similar shape and similar overall magnitude for the three systems.

To characterize the shape of the correlation functions, the Legendre coefficients $\langle a_n d_m \rangle$ for the distributions $C_N$ and $C_N^{\text{sub}}$ shown in Fig. 8 are calculated via Eq. (6) and plotted in Fig. 9. The $\langle a_n d_m \rangle$ values are shown for the first six diagonal terms $\langle a_n^2 \rangle$ and the first five mixed terms $\langle a_n a_{n+2} \rangle$, and they are also compared with coefficients calculated for opposite-charge pairs and same-charge pairs for the same event class. The magnitudes of the $\langle a_n d_m \rangle$ coefficients calculated for $C_N$ differ significantly for the different charge combinations, and they also increase as the size of the collision system decreases, i.e., $|\langle a_n d_m \rangle|_{p+p} > |\langle a_n d_m \rangle|_{p+Pb} > |\langle a_n d_m \rangle|_{Pb+Pb}$. This is consistent with a large contribution from SRC to all $\langle a_n d_m \rangle$ coefficients obtained from $C_N$. After removal of the SRC, the $\langle a_2^2 \rangle$ coefficient is quite consistent between different charge combinations and different collision systems. All higher-order coefficients are much smaller, and they are very close to zero within the systematic uncertainties. Therefore, the rest of the paper focuses on the $\langle a_2^2 \rangle$ results.

To quantify further the shape of the LRC in $C_N^{\text{sub}}(\eta_1, \eta_2)$, the $\langle a_2^2 \rangle$ coefficients are also calculated by fitting the 1-D distributions from the three projection methods as outlined in Sec. III F: (1) quadratic fit of $C_N^{\text{sub}}(\eta_+)$ in a narrow range of $\eta_+$, (2) quadratic fit of $C_N^{\text{sub}}(\eta_+)$, and (3) linear fit of $r_N^{\text{sub}}(\eta_2)$ in a narrow range of $\eta_2$. The results for Pb+Pb collisions with $100 \leq N_{\text{ch}}^{\text{rec}} < 120$ are shown in the first row of Fig. 10 for several selected projections and associated fits. The extracted $\langle a_2^2 \rangle$ values are shown in the bottom row as a function of the range of the projections. They are compared with the $\langle a_2^2 \rangle$ values obtained directly via the Legendre expansion of the entire $C_N^{\text{sub}}$ distribution, shown by the horizontal solid line. The $\langle a_2^2 \rangle$ values from all four methods are very similar. Figures 11 and 12 show the same observables...
in \( p + Pb \) collisions and \( pp \) collisions, respectively. Results are quite similar to those in \( Pb + Pb \) collisions, albeit with larger systematic uncertainties arising from the subtraction of a larger short-range component. For \( p + Pb \) (Fig. 11), the small FB asymmetry in the \( C^\text{sub}_N \) distribution along the \( \eta_+ \) direction is responsible for the difference in \( \langle a^2_1 \rangle^{1/2} \) between \( \eta_+ \) and \( -\eta_+ \) in the bottom left panel and between \( \eta_{\text{ref}} \) and \( -\eta_{\text{ref}} \) in the bottom right panel, but they still agree within their respective systematic uncertainties.

Figure 13 shows a comparison of the \( \langle a^2_1 \rangle^{1/2} \) values extracted by the four methods as a function of \( N_{\text{ch}} \) in the three collision systems. Good agreement between the different methods is observed.

On the other hand, the SRC is expected to have strong dependence on the charge combinations and collision systems, as shown by Figs. 8 and 9. The magnitude of the SRC is quantified by \( \delta_{\text{SRC}}(\eta_1, \eta_2) \) averaged over the two-particle pseudorapidity phase space:

\[
\Delta_{\text{SRC}} = \frac{\int_{-1}^{1} \delta_{\text{SRC}}(\eta_1, \eta_2) d\eta_1 d\eta_2}{4Y^2}. \quad (19)
\]

The corresponding contribution of the SRC at the single-particle level is \( \sqrt{\Delta_{\text{SRC}}} \), which can be directly compared with the strength of the LRC characterized by \( \langle a^2_1 \rangle^{1/2} \). Figure 14 shows the values of \( \sqrt{\Delta_{\text{SRC}}} \) as a function of \( N_{\text{ch}} \) for different charge combinations in the three collision systems. The strength of the SRC always decreases with \( N_{\text{ch}} \), and it is larger for smaller collision systems and opposite-charge pairs.

Figure 15 compares the strength of the SRC in terms of \( \sqrt{\Delta_{\text{SRC}}} \) and the LRC in terms of \( \langle a^2_1 \rangle^{1/2} \) for the three collision systems. The values of \( \sqrt{\Delta_{\text{SRC}}} \) are observed to differ significantly while the values of \( \langle a^2_1 \rangle^{1/2} \) agree within \( \pm 10\% \) between the three collision systems.

The strength of the SRC and LRC can be related to the number of clusters \( n \) contributing to the final multiplicity \( N_{\text{ch}} \), where \( n \) is the sum of clusters from the projectile and target nucleon or nucleus, \( n = n_F + n_B \). The LRC is expected to be related to the asymmetry between \( n_F \) and \( n_B \):

\[
A_n = \frac{n_F - n_B}{n_F + n_B} \langle a^2_1 \rangle \propto \langle A^2_n \rangle. \quad (20)
\]

The clusters could include the participating nucleons, sub-nucleonic degrees of freedom such as the fragmentation of scattered partons, or resonance decays. In an independent cluster model [37], each cluster emits the same number of pairs and the number of clusters follows Poisson fluctuations. In this picture, both the SRC in terms of \( \Delta_{\text{SRC}} \) and LRC in terms of \( \langle a^2_1 \rangle \) should scale approximately as the inverse of the number
FIG. 10. The distributions $C_{\text{sub}}^{\eta_+}(\eta_+)$ (top left panel), $C_{\text{sub}}^{\eta_-}(\eta_-)$ (top middle panel), and $r_{\text{sub}}^N(\eta)$ (top right panel) obtained from $C_{\text{sub}}^{\eta_1,\eta_2}$ in three ranges of $\eta_+, \eta_-$, and $\eta_{\text{ref}}$, respectively, from Pb+Pb collisions with $100 \leq N_{\text{ch}}^{\text{rec}} < 120$. The solid lines indicate fits to either a quadratic function (top left two panels) or a linear function (top right panel). The $\langle a_1^2 \rangle^{1/2}$ values from the fits are shown in the corresponding lower panels as a function of the $\eta_+, \eta_-$, and $\eta_{\text{ref}}$, respectively. The error bars and shaded bands represent the statistical and systematic uncertainties, respectively. The solid horizontal line and hashed band indicate the value and uncertainty of $\langle a_1^2 \rangle^{1/2}$ obtained from a Legendre expansion of the $C_N^{\eta_1,\eta_2}$.

FIG. 11. The distributions $C_{\text{sub}}^{\eta_+}(\eta_+)$ (top left panel), $C_{\text{sub}}^{\eta_-}(\eta_-)$ (top middle panel), and $r_{\text{sub}}^N(\eta)$ (top right panel) obtained from $C_{\text{sub}}^{\eta_1,\eta_2}$ in three ranges of $\eta_+, \eta_-$, and $\eta_{\text{ref}}$, respectively, from p+Pb collisions with $100 \leq N_{\text{ch}}^{\text{rec}} < 120$. The solid lines indicate fits to either a quadratic function (top left two panels) or a linear function (top right panel). The $\langle a_1^2 \rangle^{1/2}$ values from the fits are shown in the corresponding lower panels as a function of the $\eta_+, \eta_-$, and $\eta_{\text{ref}}$, respectively. The error bars and shaded bands represent the statistical and systematic uncertainties, respectively. The solid horizontal line and hashed band indicate the value and uncertainty of $\langle a_1^2 \rangle^{1/2}$ obtained from a Legendre expansion of the $C_N^{\eta_1,\eta_2}$. 
of clusters, and hence, assuming \( n \) and \( N_{\text{ch}} \) are proportional, the \( \sqrt{\Delta\text{SRC}} \) and \( (a_1^2)^{1/2} \) values in Fig. 15 are expected to follow a simple power-law function in \( N_{\text{ch}} \):

\[
\sqrt{\Delta\text{SRC}} \sim (a_1^2)^{1/2} \sim \frac{1}{n^\alpha} \sim \frac{1}{N_{\text{ch}}^\alpha}, \quad \alpha \approx 0.5. \tag{21}
\]

A power index that is less than one half, \( \alpha < 0.5 \), would suggest that \( n \) grows more slowly than \( N_{\text{ch}}^{1/2} \), and vice versa.

To test this idea, the \( \sqrt{\Delta\text{SRC}} \) and \( (a_1^2)^{1/2} \) data in Fig. 15 are fit to a power-law function: \( c/N_{\text{ch}}^\alpha \). The function describes the \( N_{\text{ch}} \) dependence in all three collision systems, with a reduced \( \chi^2 \) values ranging between 0.2 and 0.9. The extracted power index values are summarized in Table III. The values of \( \alpha \) for the SRC are found to be smaller for smaller collision systems, they are close to 0.5 in the Pb+Pb collisions and are significantly smaller than 0.5 in the \( pp \) collisions. In contrast, the values of \( \alpha \) for \( (a_1^2)^{1/2} \) agree within uncertainties between the three systems and are slightly below 0.5.

One striking feature of the correlation function in \( p + Pb \) collisions, for example in Fig. 8, is a large FB asymmetry of the

![Graphs showing the distribution of clusters in various collision systems.](image)

FIG. 12. The distributions \( C^\text{ub}(\eta_a) \) (top left panel), \( C_N^\text{ub}(\eta_a) \) (top middle panel), and \( r_{\text{ub}}^N(\eta_a) \) (top right panel) obtained from \( C^\text{ub}(\eta_1,\eta_2) \) in three ranges of \( \eta_a, \eta_0 \), and \( \eta_{\text{rel}} \), respectively, from \( pp \) collisions with \( 100 < N_{\text{ch}}^{1/2} < 120 \). The solid lines indicate fits to either a quadratic function (top left two panels) or a linear function (top right panel). The \( (a_1^2)^{1/2} \) values from the fits are shown in the corresponding lower panels as functions of the \( \eta_a, \eta_0 \), and \( \eta_{\text{rel}} \), respectively. The error bars and shaded bands represent the statistical and systematic uncertainties, respectively. The solid horizontal line and hashed band indicate the value and uncertainty of \( (a_1^2)^{1/2} \) obtained from a Legendre expansion of the \( C^\text{ub}(\eta_1,\eta_2) \).

![Graphs showing the dependence of \( C^\text{ub}(\eta_a) \) on \( N_{\text{ch}} \).](image)

FIG. 13. The \( (a_1^2)^{1/2} \) as a function of \( N_{\text{ch}} \) from four different methods, fit \( C^\text{ub}(\eta_a) \) (solid circles), fit \( C_N^\text{ub}(\eta_a) \) (open circles), fit \( r_{\text{ub}}^N(\eta_a) \) (open squares), and Legendre expansion of \( C_N^\text{ub}(\eta_1,\eta_2) \) (open diamonds), in Pb+Pb (left panel), \( p + Pb \) (middle panel), and \( pp \) (right panel) collisions. The error bars and shaded bands represent the statistical and systematic uncertainties, respectively.
SRC, $\delta_{\text{SRC}}(\eta_1, \eta_2)$ along the $\eta_+$ direction. Even in $pp$ collisions, the $\delta_{\text{SRC}}$ distribution is not uniform, but instead shows a quadratic increase towards large $|\eta_+|$ values. According to the discussion in Sec. III B, the shape of the $\delta_{\text{SRC}}$ distribution in $\eta_+$ is described by the $f(\eta_+)$ defined in Eq. (10). Examples of the $f(\eta_+)$ are shown in Fig. 16 for $p + Pb$, symmetrized-$p + Pb$, $pp$, and $Pb+Pb$ collisions with $100 \leq N_{\text{ch}}^p \leq 120$. As described in Sec. III B, symmetrized-$p + Pb$ results are obtained by averaging the proton-going and lead-going directions such that $C(\eta_1, \eta_2) = C(-\eta_1, -\eta_2)$.

The independent cluster picture discussed above offers a simple interpretation of the shape of $f(\eta_+)$. Assuming the population of clusters is a function of $\eta$, $n_c(\eta)$, and on average each cluster produces $m$ charged particles according to a Poisson distribution, then the number of the SRC pairs scales as $n_c(m(m-1)) = n_c \langle m \rangle^2$ and the number of the combinatorial pairs scales as $(n_c \langle m \rangle^2)$. Therefore the strength of the SRC at given $\eta$ is expected to scale as

$$\delta_{\text{SRC}}(\eta, \eta) \propto \frac{n_c(m(m-1))}{(n_c \langle m \rangle^2)^2} = \frac{1}{n_c} \propto \frac{1}{dN_{\text{ch}}/d\eta}, \quad (22)$$

where $n_c(\eta)$ is assumed to be proportional to the local charge-particle multiplicity density $dN_{\text{ch}}/d\eta$. Hence, the fact that $f(\eta_+)$ is larger in the proton-going direction than in the Pb-going direction in $p + Pb$ collisions simply reflects the asymmetric shape of the $dN_{\text{ch}}/d\eta$ distribution in each event [52]. The quadratic shape of $f(\eta_+)$ for $pp$ and symmetrized-$p + Pb$ system therefore reflects a large, intrinsic FB asymmetry of $dN_{\text{ch}}/d\eta$ on an event-by-event level. The FB asymmetry in $pp$ collisions is slightly larger than $p + Pb$ collisions at comparable $N_{\text{ch}}$, but is significantly less in Pb+Pb collisions. This observation suggests that the FB asymmetry for particle production in $pp$ collisions could be as large as that in $p + Pb$ collisions at comparable event activity, whereas the FB asymmetry for particle production is smaller in Pb+Pb collisions.

V. COMPARISON TO MODELS

QCD-inspired models such as PYTHIA and EPOS are often used to describe the particle production in $pp$ collisions. ATLAS has previously compared the predictions of the PYTHIA8 A2 and EPOS LHC tunes with various single-particle distributions, such as the $p_T$, $\eta$ and the...
event-by-event $N_{\text{ch}}$ distributions, fully unfolded for detector effects [33,34]. Reasonable agreement has been observed for these single-particle observables. In order to perform a data model comparison, the multiplicity correlation procedure used on the data is repeated for the two models to extract the SRC and LRC components. The extracted LRC in these models is then decomposed into Legendre coefficients of different order. The coefficients are found to be dominated by $a_1^2$, consistent with the observation that the shape of the LRC are similar to those in the $pp$ data in Fig. 8. However, the values of $a_1^2$ predicted by the models are found to be much smaller than the $pp$ data at the same $N_{\text{ch}}$.

For a more direct comparison, Fig. 17 shows the $N_{\text{ch}}$ dependence of SRC and LRC from the data and the two models in $pp$ collisions. The systematic uncertainties on the model predictions are dominated by the uncertainty in separating the SRC and LRC, as discussed in Sec. III G. However, at large $N_{\text{ch}}$, they are also limited by the available MC statistics. There is some indication that the values of $\sqrt{A_{\text{SRC}}}$ from data are larger than the EPOS predictions and smaller than those from PYTHIA 8. Furthermore, the values from PYTHIA 8 increase for $N_{\text{ch}} > 120$, a trend not supported by the data. On the other hand, both models underestimate significantly the values of $a_1^2$, suggesting that the FB multiplicity fluctuations in both models are significantly weaker than in the $pp$ data. Therefore, these two models, which were tuned to describe many single-particle observables, fail to describe the longitudinal correlations between the produced charged particles.

VI. SUMMARY

Two-particle pseudorapidity correlations are measured with the ATLAS detector in $\sqrt{s_{\text{NN}}} = 2.76$ TeV $\text{Pb+Pb}$, $\sqrt{s_{\text{NN}}} = 5.02$ TeV $p + \text{Pb}$, and $\sqrt{s} = 13$ TeV $pp$ collisions at the LHC, with total integrated luminosities of approximately 7 $\mu b^{-1}$, 28 nb$^{-1}$, and 65 nb$^{-1}$, respectively. The correlation function $C_N(\eta_1, \eta_2)$ is measured using charged particles in the pseudorapidity range $|\eta| < 2.4$ with transverse momentum $p_T > 0.2$ GeV, and it is measured as a function of event multiplicity $N_{\text{ch}}$ defined by the total number of charged particles with $|\eta| < 2.5$ and $p_T > 0.4$ GeV. The correlation function shows an enhancement along the $\eta_1 \approx \eta_2$ direction and suppression at $\eta_1 \approx -\eta_2 \sim \pm 2.4$, consistent with the expectation from an event-by-event forward-backward asymmetry in the multiplicity fluctuation (the long-range correlations or LRC). However, the correlation function also has a large narrow ridge along the $\eta_1 \approx \eta_2$ direction associated with short-range correlations (SRC). The magnitudes of the SRC in $p + \text{Pb}$ is found to be larger in the proton-going direction than the lead-going direction, reflecting the fact that the particle multiplicity is smaller in the proton-going direction. This is consistent with the observation that the SRC strength increases for smaller $N_{\text{ch}}$. The SRC is observed to be much stronger for opposite-charge pairs than for the same-charge pairs, while the LRC is found to be similar for the two charge combinations. Based on this, a data-driven subtraction method was developed to separate the SRC and the LRC. The magnitudes of the SRC and the LRC are then compared for the three collision systems at similar values of $N_{\text{ch}}$.

After subtracting out the SRC $\delta_{\text{SRC}}(\eta_1, \eta_2)$, the correlation function $C_N^{\text{sub}}(\eta_1, \eta_2)$ is decomposed into a sum of products of Legendre polynomials that describe the different shape components, and the coefficients $(a_n a_m)$ are calculated. Significant values are observed for $(a_1^2)$ in all $N_{\text{ch}}$ ranges and higher-order coefficients are consistent with zero, and suggesting that $C_N^{\text{sub}}$ has an approximate functional form $C_N^{\text{sub}} \approx 1 + (a_1^2) \eta_1 \eta_2$. The quantity $(a_1^2)$ is also estimated by parametrization of the shape of the correlation function in narrow ranges of $\eta_1 = \eta_1 - \eta_2$ and $\eta_2 = \eta_1 + \eta_2$, or from a ratio $C_N^{\text{sub}}(\eta_1, \eta_2)/C_N^{\text{sub}}(-\eta_1, \eta_2)$, and consistent results are obtained. The magnitude of the SRC and $(a_1^2)$ are compared for the three collision systems as a function of $N_{\text{ch}}$. Large differences are observed for the SRC, but the values of $(a_1^2)$ agree within $\pm 10\%$ at the same $N_{\text{ch}}$. The $N_{\text{ch}}$ dependences of both the SRC and $(a_1^2)$ follow an

<table>
<thead>
<tr>
<th>$\text{Pb+Pb}$</th>
<th>$p + \text{Pb}$</th>
<th>$pp$</th>
</tr>
</thead>
<tbody>
<tr>
<td>$\alpha$ for $\sqrt{A_{\text{SRC}}}$</td>
<td>$0.505 \pm 0.011$</td>
<td>$0.450 \pm 0.010$</td>
</tr>
<tr>
<td>$\alpha$ for $(a_1^2)$</td>
<td>$0.454 \pm 0.011$</td>
<td>$0.433 \pm 0.014$</td>
</tr>
</tbody>
</table>

FIG. 16. The shape of the SRC in $\eta_1$ represented by $f(\eta_1)$ calculated via Eq. (10) for $p + \text{Pb}$, symmetrized-$p + \text{Pb}$, $pp$, and $\text{Pb+Pb}$ collisions with $100 \leq N_{\text{ch}}^{\text{rec}} < 120$. The solid lines represent a fit to a quadratic function.
approximate power-law shape. The power index for $\langle a_2^2 \rangle^{1/2}$ is approximately the same for the three collision systems. In contrast, the power-law index for the SRC is smaller for smaller collision systems. The SRC distribution shows strong dependence on $\eta_+$ in $p + \text{Pb}$ and $pp$, but much weaker dependence in $\text{Pb} + \text{Pb}$ collisions. The $\delta_{\text{SC}}(\eta_+)$ distribution, after symmetrizing the proton and lead directions, is found to be similar to the SRC in $pp$ collisions with comparable $N_\text{ch}$, suggesting that the event-by-event FB asymmetry for particle production is similar in $pp$ and $p + \text{Pb}$ collisions with comparable event activity. The PYTHIA 8 A2 and EPOS LHC models, which were tuned to describe many single-particle observables in $pp$ collisions, fail to describe the SRC and the LRC observed in the $pp$ data.

FIG. 17. The $\sqrt{\Delta_{\text{SRC}}}$ (left panel) and $\langle a_2^2 \rangle^{1/2}$ (right panel) as a function of $N_\text{ch}$ in $pp$ collisions at $\sqrt{s} = 13$ TeV, compared between data and PYTHIA 8 A2 and EPOS LHC. The shaded bands represent the total uncertainties.

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