I. INTRODUCTION

Vector-boson scattering (VBS) processes provide a unique method to examine the mechanism of electroweak symmetry breaking and to search for physics beyond the Standard Model (SM) [1–3]. In the SM, the Higgs boson prevents the longitudinal scattering amplitude of the $V V \to V V$ ($V=W$ or $Z$) process from continuously increasing as a function of the center-of-mass energy of the diboson system, which would violate unitarity at energies above approximately 1 TeV [4–6]. In many new physics scenarios [7,8], the Higgs boson has non-SM $HVV$ couplings below current experimental sensitivity and additional resonances are introduced to restore unitarity in the high-energy regime. The energy dependence of the VBS production cross-section above the Higgs boson mass scale can be used to test whether the Higgs boson discovered at the Large Hadron Collider (LHC) [9,10] unitarizes the scattering amplitude fully or only partially [2].

The VBS topology consists of a proton–proton collision with two initial quarks that each radiate an electroweak boson. The two bosons subsequently scatter and then decay. The two outgoing quarks are often close to the beam direction. Multiple processes can produce the same final state of two bosons ($V$) and two jets ($j$) from the fragmentation of the two outgoing quarks ($VVjj$). The production of $VVjj$ at tree level is composed of electroweak production involving only electroweak-interaction vertices (denoted by “$VVjj$-EW”), and strong production involving at least one strong-interaction vertex (denoted by “$VVjj$-QCD”). The electroweak production is further categorized into two components. The first component is the EW VBS production with actual scattering of the two electroweak bosons. The scattering occurs via triple or quartic gauge vertices, the $s$- and $t$-channel exchange of a Higgs boson, or a $W/Z$ boson (throughout this paper, the notation “$Z$ boson” means “$Z/\gamma'$ boson”, unless specified otherwise). The second component is the EW non-VBS production with electroweak vertices only, where the two bosons do not scatter. The EW non-VBS component cannot be separated from the EW VBS component in a gauge invariant way [1]. It is therefore included in the signal generation and cannot be distinguished from the EW VBS. Representative Feynman diagrams at tree level are shown in Fig. 1 for EW VBS production, in Fig. 2 for EW non-VBS production, and in Fig. 3 for $VVjj$-QCD production. Triboson production with one of the bosons decaying hadronically also yields the same $VVjj$ final state. The resonant decay of a boson into two quarks can be suppressed by applying a requirement on the invariant mass of the two quarks. As a consequence, triboson processes are suppressed in the EW VBS signal region.

The scattering of two massive vector bosons can lead to $W^\pm W^\pm jj$, $W^+ W^- jj$, $W^\pm Zjj$ or $ZZjj$ diboson states. The $W^\pm W^\pm jj$ electroweak production does not involve diagrams with the $s$-channel exchange of a Higgs boson or a vector boson, and the contributions from strong production are greatly suppressed due to the lack of Feynman diagrams with two gluons or one quark and one gluon in the initial state [11]. The $W^\pm W^\pm jj$ channel is found to have the largest cross-section ratio of electroweak to strong production [12]. Leptonic decays of the $W$ bosons ($W \to \ell \nu$) are used, which allow the identification of the electric
charges of the two \( W \) bosons. The presence of two leptons with the same electric charge in the final state significantly reduces SM backgrounds. For these reasons, \( W^+W^-jj \) production is one of the best channels for VBS studies at the LHC [13].

Due to the non-Abelian nature of the SM electroweak theory, gauge bosons interact with each other. Besides the triple \( WWZ \) and \( WW\gamma \) gauge boson vertices, the SM also predicts the existence of quartic \( WWWW \), \( WW\gamma\gamma \), \( WWZZ \), and \( WWZ\gamma \) vertices. Possible physics beyond the SM can affect these vertices and introduce anomalous triple gauge couplings (aTGCs) or anomalous quartic gauge couplings (aQGCs). An effective field theory (EFT) framework [14–17] provides a generic platform for introducing the effect of new physics by adding additional terms in the SM chiral Lagrangian. The lowest-order terms contributing to aQGCs are the dimension-four operators \( L_4 \) and \( L_5 \):

\[
\alpha_4 L_4 = \alpha_4 \text{tr}(V_\mu V_\nu) \quad \text{and} \quad \alpha_5 L_5 = \alpha_5 \text{tr}(V_\mu V_\mu),
\]

(1)

where \( \alpha_4 \) and \( \alpha_5 \) are dimensionless anomalous coupling parameters and \( V_\mu = \Sigma(D_\mu \Sigma)^\dagger \) with \( D_\mu \) being the covariant derivative operator. The field \( \Sigma \) is a \( 2 \times 2 \) matrix, which transforms as \( \Sigma \rightarrow U\Sigma V^\dagger \) under local SU(2)_L transformations \( U \) and U(1)_Y transformations \( V \).

The EFT approach is applicable to many models of physics beyond the SM including, but not limited to, two- or multi-Higgs-doublet models, extended scalar sectors, technicolor models, models of complete or partial compositeness, Little Higgs models, Twin Higgs models, etc. For example, certain heavy resonances would manifest as nonzero values of the \( \alpha_5 \) coupling parameter among others, but not influence \( \alpha_4 \) [18]. While other models of physics beyond the SM such as a Higgs triplet, \( W'/Z' \), or Kaluza–Klein graviton would...
manifest as nonzero parameter points in the \((\alpha_4, \alpha_5)\) plane [19].

Searches for processes containing QGCs have been performed by previous experiments, for example, \(e^+e^- \to WW\gamma, \nu\nu\gamma\) [20–23] by the LEP experiments, \(p\bar{p} \to pW^+W^-\bar{p} \to pe^+\nu e^-\bar{\nu} \bar{p}\) by the D0 experiment [24], \(pp \to W\gamma \to \ell\nu\gamma\gamma\) [25] and \(pp \to pW^+W^- p \to pe^+\nu\mu^+\nu\bar{p}\) [26] by the CMS experiment, \(p(\gamma\gamma) \to pW^+W^- p \to pe^+\nu\mu^+\nu\bar{p}\) [27] and \(pp \to pW\gamma p \to p\ell\nu\gamma\gamma\) [28] by the ATLAS experiment. None of these processes have been observed above 5 sigma significance, which is expected due to their low SM cross sections and large backgrounds. These results are used to set limits on corresponding aQGCs with at least one photon involved.

Experimental investigation of QGCs with four massive vector bosons has only been attempted at the LHC. Using 20.3 fb\(^{-1}\) of data collected at \(\sqrt{s} = 8\) TeV, evidence of \(W^+W^-\) decaying to \(\ell^+\ell^-\nu\bar{\nu}\) in association with two jets was recently presented [29] by the ATLAS Collaboration. Similar results were obtained by the CMS Collaboration [30] in the same final state. ATLAS has published a search for WZ production in association with two jets [31], WW/WZ production in association with a high-mass dijet system [32], and WWW production [33]. This paper completes and extends the results presented in the form of a letter in Ref. [29]. An updated Monte Carlo simulation for the signal is used, and a new signal region more sensitive to aQGCs is developed and more stringent limits on \(\alpha_4\) and \(\alpha_5\) are derived.

II. THE ATLAS DETECTOR

The ATLAS detector [34] is a multipurpose particle detector designed to measure a wide range of physics processes from \(pp\) collisions at the TeV scale. It consists of an inner tracking detector (ID), calorimeters, a muon spectrometer (MS), and solenoidal and toroidal magnets in a cylindrical geometry with forward-backward symmetry.\(^2\)

The ID consists of three subdetectors. The pixel detector and semiconductor tracker (SCT) are composed of silicon pixel and microstrip detectors and extend to \(|\eta| = 2.5\). In this region, the pixel detector has 3 cylindrical layers and the SCT has 4 layers. The transition radiation tracker (TRT) is built of gas-filled straw-tube detectors and extends to \(|\eta| = 2.0\). The ID is surrounded by a thin superconducting solenoid magnet that creates a 2 T axial magnetic field for charged-particle momentum measurements.

The calorimeter system consists of electromagnetic (EM) and hadronic calorimeters. A high-granularity sampling calorimeter with lead absorber layers and liquid argon (LAr) measures the energy and position of electromagnetic showers in the pseudorapidity region of \(|\eta| < 3.2\). Hadronic showers are measured by steel and scintillator tile calorimeters for \(|\eta| < 1.7\) and copper/LAr calorimeters for \(1.5 < |\eta| < 3.2\). The forward calorimeter extends the coverage, spanning \(3.1 < |\eta| < 4.9\) with additional copper/LAr and tungsten/LAr calorimeters.

The MS covers the pseudorapidity range of \(|\eta| < 2.7\) and is instrumented with separate trigger and precision tracking chambers. A precision measurement of the track coordinates in the bending direction of the toroidal magnetic field is provided by drift tubes up to \(|\eta| = 2.0\). At larger pseudorapidities, cathode strip chambers with higher granularity are used in the innermost station covering \(2.0 < |\eta| < 2.7\). The muon trigger system consists of resistive plate chambers in the barrel (\(|\eta| < 1.05\)) and thin gap chambers in the endcap regions (\(1.05 < |\eta| < 2.4\)).

A three-level trigger system is used to record the events used in this analysis. The level-1 trigger is implemented in hardware and reduces the event rate to about 75 kHz. This is followed by two software-based trigger levels that together reduced the event rate to about 600 Hz during the 2012 data-taking period.

III. EVENT SELECTION

Candidate events are collected by single-lepton triggers with thresholds of \(p_T = 36\) GeV (muons) or \(p_T = 60\) GeV (electrons) or single-isolated-lepton triggers with a lower threshold of \(p_T = 24\) GeV. The events must also occur during stable beam conditions and with the relevant detector systems functional. The resulting total integrated luminosity is 20.3 fb\(^{-1}\) with an uncertainty of 2.8% [35].

Tracks used in this analysis are reconstructed using an “inside-out” algorithm starting with seeds made from hits in the pixel detector and the first layer of the SCT and attempting to extend these into the remaining silicon layers and finally into the TRT [36]. Proton–proton interaction vertices are reconstructed by extrapolating the \(z\)-position of tracks at the beamline, grouping two or more tracks into vertex candidates, and then reconstructing the vertex position and its corresponding error matrix. Tracks incompatible with the vertex by more than seven standard deviations are used to look for additional vertices. The vertex with the largest sum of squared transverse momenta of associated tracks \((\sum p_T^2)\) is taken to be the primary...
vertex. The primary vertex is required to have at least three associated tracks with $p_T > 0.4$ GeV.

Three types of lepton identification criteria are defined for signal selection and background rejection, which are non-exclusive: a tight lepton criterion used to select the final two same-electric-charge leptons, a veto lepton used to reject events with an additional lepton present in $W^\pm Z$ or $ZZ$ events, and a loose lepton category used to estimate the background contribution from events with nonprompt leptons from in-flight hadron decays or with jets misidentified as leptons.

Electrons are reconstructed from a combination of track information in the ID and cluster information in the electromagnetic calorimeter. Tight electrons must satisfy identification criteria similar to the tight definition used in Refs. [37–39], which includes requirements on the electron track, the shape of the shower in the EM calorimeter, and the ratio of energies deposited in the EM and hadronic calorimeters. Additionally, the track hit information is used to identify and remove electrons arising from photon conversions. Electron candidates must have $p_T > 25$ GeV and $|\eta| < 2.47$. Electrons within the transition region $(1.37 < |\eta| < 1.52)$ between the EM barrel and endcap calorimeters are excluded. The transverse ($d_0$) and longitudinal ($z_0$) impact parameters must satisfy $|d_0/\sigma_{d_0}| < 3$ and $|z_0 \times \sin \theta| < 0.5$ mm, where $\sigma_{d_0}$ is the uncertainty in the measurement of $d_0$. Finally, calorimeter and tracking isolation selections are applied as follows: the sum of the transverse energies of all calorimeter clusters ($E_T^{\text{clus}}$) and the sum of the transverse momenta of tracks ($p_T^{\text{clus}}$) within a cone of size $\Delta R = 0.3$, are required to be less than 14% and 6% of the electron’s transverse energy, respectively. The energy from the electron itself is excluded in the calculations of $E_T^{\text{clus}}$ and $p_T^{\text{clus}}$.

Veto and loose electrons are only required to pass a loose identification selection defined in Ref. [37]. The $p_T$ threshold is lowered to 7 GeV, and the tracking isolation requirement is removed for veto electrons. For loose electrons, the impact parameter requirements are loosened to $|d_0/\sigma_{d_0}| < 10$ and $|z_0 \times \sin \theta| < 5$ mm, and the calorimeter and tracking isolation criteria are $0.14 < E_T^{\text{clus}}/p_T < 2$ and $0.06 < p_T^{\text{clus}}/p_T < 2$.

Muons are reconstructed from tracks in the ID and MS and fall into one of three categories: combined, standalone, and tagged [40]. Combined muons contain matching tracks in the ID and MS. Stand-alone muons consist only of a track in the MS, while tagged muons have an ID track that is matched to a track segment in the MS. In this analysis, tight muons are required to be reconstructed as combined muons with the same electric charge measured in the ID and MS. They must have $p_T > 25$ GeV and $|\eta| < 2.5$. The ID tracks associated with these muons must pass a number of quality requirements. The number of hits or dead sensors crossed in the pixel detector must be at least one, and in the SCT this number must be at least five. For muons with $0.1 < |\eta| < 1.9$, the track must have at least six hits in the TRT, and the fraction of these that are outliers must not exceed 90%. Tight muons have the same impact parameter requirements as tight electrons and have calorimeter and tracking isolation requirements defined by $E_T^{\text{clus}}/p_T < 0.07$ and $p_T^{\text{clus}}/p_T < 0.07$ where a cone of size $\Delta R = 0.3$ is used.

The selection of veto muons includes stand-alone and tagged muons. The $p_T$ threshold is lowered to 6 GeV, the calorimeter isolation requirement is dropped, and the track isolation selection is loosened to be less than 15% of the muon $p_T$. Loose muons must be combined muons, but just as for loose electrons, the impact parameter requirements are loosened to $|d_0/\sigma_{d_0}| < 10$ and $|z_0 \times \sin \theta| < 5$ mm, and the calorimeter and tracking isolation criteria are $0.07 < p_T^{\text{clus}}/p_T < 2$ and $0.07 < p_T^{\text{clus}}/p_T < 2$.

To improve agreement between data and simulation, lepton selection efficiencies are measured in both data and simulation, and correction factors are applied to the simulation to account for differences with respect to data [39,40]. Furthermore, the simulation is tuned to reproduce the calorimeter energy and the muon momentum scales and resolutions observed in data. The simulation also includes modeling of additional $p\bar{p}$ interactions in the same and neighboring bunch crossings.

Jets are reconstructed from topological clusters in the calorimeter using the anti-$k_T$ algorithm [41] with a radius parameter of 0.4 [42]. Jets are required to have $p_T > 30$ GeV and $|\eta| < 4.5$. In order to reduce the probability of selecting a jet from a pileup interaction, jets with $|\eta| < 2.4$ and $p_T < 50$ GeV are required to have a jet vertex fraction greater than 50%. The jet vertex fraction is defined as the ratio of the sum of the $p_T$ of all tracks associated with both the jet and the primary vertex to the sum of the $p_T$ of all tracks in the jet [43]. Jets stemming from the fragmentation of a charm or bottom quark are identified with a neural network discriminator using input variables related to the impact parameter significance of tracks in the jet and secondary vertices reconstructed from these tracks [44]. The jet is classified as a $b$-jet if the output of this neural network discriminator exceeds a working point chosen to have a 70% efficiency for identifying jets from top quarks containing $b$-hadrons.

The measurement of the two-dimensional missing transverse momentum vector $\vec{E}_T^{\text{miss}}$ and its magnitude $E_T^{\text{miss}}$ [45] is based on the measurement of all topological clusters in the calorimeter, and muon tracks reconstructed by the ID and MS. The energies of clusters in the calorimeter are calibrated according to their association with a reconstructed object.

In order to deal with the case where a single particle is reconstructed as more than one object, an overlap removal procedure is followed. If the event contains a tight electron and a jet with $\Delta R(e, j) < 0.3$, the jet is removed since it is likely that it corresponds to the electron energy deposits picked up by the jet reconstruction algorithm. If the same is true for a jet and a tight muon, the event is rejected since the muon likely originates from the decay of a hadron within the jet. When estimating the background from nonprompt leptons, jets are also removed if they fall within $\Delta R = 0.3$. 
of a loose lepton. For electrons and muons separated by \( \Delta R < 0.1 \), the electron is removed since it is likely that it originates from a photon radiated from the muon.

Signal candidate events are selected by requiring two tight leptons with the same electric charge and an invariant mass \( m_{\ell\ell} \) greater than 20 GeV. Three final states are considered based on the lepton flavor, namely \( e^+e^-, e^+\mu^- \), and \( \mu^+\mu^- \). To reduce background contributions from the \( W^+Z \) and ZZ processes, events with a third lepton of the veto type are rejected. An additional requirement is made in the \( e^\pm e^\pm \) final state that the invariant mass of the two electrons differs from the combined world average of the Z pole mass \([46]\) by at least 10 GeV. This selection criterion reduces the background from the \( W^+Z \) and ZZ processes, events with a third lepton of the veto type are rejected. An additional requirement is made in the \( e^\pm e^\pm \) final state that the invariant mass of the two electrons differs from the combined world average of the Z pole mass \([46]\) by at least 10 GeV. This selection criterion reduces the background from the \( Z(\rightarrow e^+e^-) + \) jets process where one electron’s charge is misidentified. Since two neutrinos are produced from the decays of the two W bosons, \( E_T^{\text{miss}} \) is required to be greater than 40 GeV. Events are required to have at least two jets. In order to reduce the background from top-quark pair and single top-quark production, the event is rejected if any jet is classified as a b-jet. Remaining events with an invariant mass of the two leading-\( p_T \) jets \( m_{jj} \) greater than 500 GeV are selected. This selection level defines the inclusive signal region (denoted by “Inclusive SR”), and both the electroweak and strong production of \( W^\pm W^\pm jj \) are treated as signal. The VBS signal region (denoted by “VBS SR”) is defined to consist of events in the inclusive signal region for which the separation in rapidity between the two leading-\( p_T \) jets \( (\Delta y_{jj}) \) is greater than 2.4. In this region only the electroweak production is considered as signal. The third signal region (denoted by “aQGC SR”) additionally requires the estimated transverse mass of the WW system to be greater than 400 GeV in order to optimize the sensitivity to the new-physic parameters \( \alpha_d \) and \( \alpha_s \). The variable, \( m_{WW,T} \), is defined as

\[
m_{WW,T} = \sqrt{(P_{\ell_1} + P_{\ell_2} + P_{E_T^{\text{miss}}})^2}
\]

where \( P_{\ell_1}, P_{\ell_2} \) are the four-momenta of the two selected lepton candidates and \( P_{E_T^{\text{miss}}} \) is the massless four-vector constructed from the \( E_T^{\text{miss}} \) measurement with the z-component of \( P_{E_T^{\text{miss}}} \) defined as zero. In the aQGC SR, both the electroweak and strong production predicted by the SM are considered as background, and only the contributions due to aQGCs are considered as signal.

Table I summarizes the kinematic selection criteria used for the three signal regions.

### IV. MONTE CARLO SIMULATION AND THEORETICAL PREDICTIONS

Monte Carlo (MC) events are simulated at \( \sqrt{s} = 8 \) TeV and processed through the full ATLAS detector simulation \([47]\) based on geant4 \([48]\). Additional proton – proton interactions modeled by PYTHIA 8 \([49,50]\) are included and reweighted to reproduce the observed distribution of the average number of proton – proton interactions per event. Contributions from interactions in nearby bunch crossings are also considered in the MC simulations. Events generated in the Inclusive and VBS signal regions are used to measure the production cross sections, provide normalization factors for MC samples, and to compare with theoretical predictions. This section concentrates on the theoretical cross sections and uncertainties for the \( W^\pm W^\pm jj \)-QCD processes in these two regions.

### A. Definition of Inclusive and VBS fiducial phase-space regions at the particle level

Two fiducial phase-space regions are defined at particle level by selection criteria similar to the “Inclusive SR” and “VBS SR” described in Section III. Particle level jets are reconstructed by running the anti-\( k_T \) algorithm with radius parameter \( R = 0.4 \) on all observable final-state stable particles after parton showering and hadronization. The Inclusive

<table>
<thead>
<tr>
<th>Signal Region</th>
<th>Selection Criteria</th>
</tr>
</thead>
<tbody>
<tr>
<td>Lepton</td>
<td>Exactly two tight same-electric-charge leptons with ( p_T &gt; 25 ) GeV</td>
</tr>
<tr>
<td>Jet</td>
<td>At least two jets with ( p_T &gt; 30 ) GeV and (</td>
</tr>
<tr>
<td>( m_{\ell\ell} )</td>
<td>( m_{\ell\ell} &gt; 20 ) GeV</td>
</tr>
<tr>
<td>( E_T^{\text{miss}} )</td>
<td>( E_T^{\text{miss}} &gt; 40 ) GeV</td>
</tr>
<tr>
<td>( Z ) veto</td>
<td>(</td>
</tr>
<tr>
<td>Third-lepton veto</td>
<td>No third-lepton veto</td>
</tr>
<tr>
<td>( b )-jet veto</td>
<td>No identified ( b )-jets with ( p_T &gt; 30 ) GeV and (</td>
</tr>
<tr>
<td>( m_{jj} )</td>
<td>( m_{jj} &gt; 500 ) GeV</td>
</tr>
<tr>
<td>VBS (</td>
<td>\Delta y_{jj}</td>
</tr>
<tr>
<td>aQGC (</td>
<td>\Delta y_{jj}</td>
</tr>
</tbody>
</table>
fiducial phase-space region is defined with the following criteria: exactly two charged leptons (only considering electrons and muons) of the same electric charge, each with \( p_T > 25 \text{ GeV} \) and \( |\eta| < 2.5 \), and at least two particle level jets with \( p_T > 30 \text{ GeV} \) and \( |\eta| < 4.5 \). The jets are required to be separated by \( \Delta R(\ell, j) > 0.3 \). The events are further required to have a dilepton invariant mass \( m_{\ell\ell} > 20 \text{ GeV} \) and \( p_T^{\gamma_1+\gamma_2} > 40 \text{ GeV} \), where \( p_T^{\gamma_1+\gamma_2} \) is the magnitude of the vectorial sum of \( p_T \) of the two particle level neutrinos. The lepton four-momentum includes contributions from photons within \( \Delta R(\ell, \gamma) = 0.1 \) of the lepton direction. The two leptons are also required to be separated by \( \Delta R > 0.3 \). The two leading-\( p_T \) jets are required to have \( m_{jj} > 500 \text{ GeV} \). An additional requirement of \( |\Delta y_{jj}| > 2.4 \) is applied for the VBS fiducial phase-space region.

**B. \( W^\pm W^\pm jj \)-EW and \( W^\pm W^\pm jj \)-QCD cross sections and uncertainties**

Both electroweak and strong production of \( W^\pm W^\pm jj \) events are generated using the SHERPA version 1.4.5 event generator [51] at leading order (LO) in QCD with up to three partons. Matrix-element and parton-shower matching for the two final-state jets are performed with the CKKW scheme [52]. Dynamic factorization (\( \mu_F \)) and renormalization (\( \mu_R \)) scales are set to be

\[
\mu_{F,R} = \frac{1}{2} \sum_{i=1,2} \left[ p_T(j_i) + \sqrt{m^2(W_i) + p_T^2(W_i)} \right].
\]

where \( p_T(j_i) \) is the momentum of the \( i \)th leading-\( p_T \) jet, and \( m(W_i) \) and \( p_T(W_i) \) are the mass and transverse momentum of the \( i \)th \( W \) boson. CT10 parton distribution functions (PDFs) [53] are used.

The \( W^\pm W^\pm jj \) SHERPA samples are updated from those in the previous publication of the measurement of \( W^\pm W^\pm jj \) [29] to include a more accurate representation of the QED final-state radiation. The impact of this effect reduces the final acceptance due to an additional 5% loss of leptons in the lepton–jet overlap removal in both fiducial phase-space regions.

The SHERPA cross sections are scaled to account for the next-to-leading-order (NLO) cross section predictions using POWHEG-BOX [54–56] with PYTHIA 8 for parton shower and hadronization in the fiducial phase-space regions. The dynamic scales defined in Eq. (3) are used. Contributions from nonresonant production are included, but are highly suppressed. Interference effects between the electroweak and strong production are studied using separated and combined electroweak and strong-mediated samples. The cross section for the combined sample minus the sum of the cross sections of purely electroweakly-mediated and purely strongly-mediated samples gives the size of the interference effect. The interference is found to enhance the total signal production cross section by 10.7% in the Inclusive phase-space region and 6.5% in the VBS phase-space region.

The prediction for \( W^\pm W^\pm jj \)-EW production is cross-checked using VBFNLO [57–59] and the results from the two generators are found to be consistent to within 5%. This 5% difference is taken as the generator uncertainty. Scale- and PDF-induced uncertainties are evaluated using VBFNLO. Scale-induced uncertainties are estimated by varying separately the factorization and renormalization scales from the central values as listed in Eq. (3) by factors \( \xi_F \) and \( \xi_R \). The largest difference in the cross section resulting from variations of \( (\xi_F, \xi_R) \) where \( \xi_F, \xi_R = 0.5, 1 \), or 2 excluding extremum combinations \( (\xi_F = 0.5, \xi_R = 2) \) and \( (\xi_F = 2, \xi_R = 0.5) \) of scale variations is taken as the uncertainty. The PDF uncertainty is determined by adding in quadrature the CT10 eigenvector variations [53] and the difference of central values with respect to MSTW2008 [60].

Due to the selection criteria applied to jet transverse momenta and dijet mass, the parton shower has an effect on the fiducial cross sections [61–64]. Two different parton-shower algorithms are applied to POWHEG-BOX NLO events and the difference in the signal yield is used to determine the uncertainty. The default algorithm relies on the PYTHIA 8 parton-shower model using the AU2 set of tuned parameters [65] for the underlying-event modeling. The second algorithm uses the HERWIG [66] parton-shower model with JIMMY [67] to model the underlying event.

The NLO cross sections for the \( W^\pm W^\pm jj \)-QCD production are also calculated using the POWHEG-BOX generator. Uncertainties due to the scale, PDF, and parton-shower model are evaluated in the same way as for the \( W^\pm W^\pm jj \)-EW production.

Theoretical uncertainties in the predictions for \( W^\pm W^\pm jj \)-EW and \( W^\pm W^\pm jj \)-QCD production in the Inclusive and VBS fiducial phase-space regions are detailed in Table II. The \( W^\pm W^\pm jj \)-EW (\( W^\pm W^\pm jj \)-QCD) production cross section is predicted to be \( 1.00 \pm 0.06 \text{ fb} \) (\( 0.35 \pm 0.05 \text{ fb} \) in the Inclusive phase-space region and \( 0.88 \pm 0.05 \text{ fb} \) (\( 0.098 \pm 0.018 \text{ fb} \) in the VBS phase-space region. The interference between \( W^\pm W^\pm jj \)-EW and \( W^\pm W^\pm jj \)-QCD production enhances the cross section by \( 0.16 \pm 0.08 \text{ fb} \) in the Inclusive phase-space region and \( 0.07 \pm 0.04 \text{ fb} \) in the VBS phase-space region. Both the

<table>
<thead>
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<th>Source of uncertainty</th>
<th>( W^\pm W^\pm jj )-EW</th>
<th>Inclusive</th>
<th>VBS</th>
<th>Inclusive</th>
<th>VBS</th>
</tr>
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</tbody>
</table>

The prediction for \( W^\pm W^\pm jj \)-EW production is cross-checked using VBFNLO [57–59] and the results from the two generators are found to be consistent to within 5%. This 5% difference is taken as the generator uncertainty. Scale- and PDF-induced uncertainties are evaluated using VBFNLO. Scale-induced uncertainties are estimated by varying separately the factorization and renormalization scales from the central values as listed in Eq. (3) by factors \( \xi_F \) and \( \xi_R \). The largest difference in the cross section resulting from variations of \( (\xi_F, \xi_R) \) where \( \xi_F, \xi_R = 0.5, 1 \), or 2 excluding extremum combinations \( (\xi_F = 0.5, \xi_R = 2) \) and \( (\xi_F = 2, \xi_R = 0.5) \) of scale variations is taken as the uncertainty. The PDF uncertainty is determined by adding in quadrature the CT10 eigenvector variations [53] and the difference of central values with respect to MSTW2008 [60].

Due to the selection criteria applied to jet transverse momenta and dijet mass, the parton shower has an effect on the fiducial cross sections [61–64]. Two different parton-shower algorithms are applied to POWHEG-BOX NLO events and the difference in the signal yield is used to determine the uncertainty. The default algorithm relies on the PYTHIA 8 parton-shower model using the AU2 set of tuned parameters [65] for the underlying-event modeling. The second algorithm uses the HERWIG [66] parton-shower model with JIMMY [67] to model the underlying event.

The NLO cross sections for the \( W^\pm W^\pm jj \)-QCD production are also calculated using the POWHEG-BOX generator. Uncertainties due to the scale, PDF, and parton-shower model are evaluated in the same way as for the \( W^\pm W^\pm jj \)-EW production.

Theoretical uncertainties in the predictions for \( W^\pm W^\pm jj \)-EW and \( W^\pm W^\pm jj \)-QCD production in the Inclusive and VBS fiducial phase-space regions are detailed in Table II. The \( W^\pm W^\pm jj \)-EW (\( W^\pm W^\pm jj \)-QCD) production cross section is predicted to be \( 1.00 \pm 0.06 \text{ fb} \) (\( 0.35 \pm 0.05 \text{ fb} \) in the Inclusive phase-space region and \( 0.88 \pm 0.05 \text{ fb} \) (\( 0.098 \pm 0.018 \text{ fb} \) in the VBS phase-space region. The interference between \( W^\pm W^\pm jj \)-EW and \( W^\pm W^\pm jj \)-QCD production enhances the cross section by \( 0.16 \pm 0.08 \text{ fb} \) in the Inclusive phase-space region and \( 0.07 \pm 0.04 \text{ fb} \) in the VBS phase-space region. Both the
electroweak and strong production of \( W^\pm W^\mp jj \) and their interference are treated as signal in the Inclusive phase-space region. The total predicted signal cross section in the Inclusive phase-space region is \( 1.52 \pm 0.11 \text{ fb} \). For the VBS phase-space region, the electroweak production and the interference term are included in the total predicted cross section, which is determined to be \( 0.95 \pm 0.06 \text{ fb} \). For the rest of the paper, \( W^\pm W^\mp jj \)-EW is used to indicate the combined contribution from the electroweak production and the interference effect, while \( W^\pm W^\mp jj \)-EW+QCD indicates contributions from both electroweak and strong production as well as the interference effect.

V. BACKGROUNDS

SM background processes producing the signature of two same-electric-charge leptons and \( E_{\text{T}}^{\text{miss}} \) with at least two jets in the final state are grouped in three categories: prompt background, nonprompt background, and conversions. The prompt background is due to \( WZ + \text{jets} \), \( ZZ + \text{jets} \), or \( t\bar{t}V \) production when one or more leptons are either not reconstructed or not identified while the remaining two prompt leptons have the same electric charge. The nonprompt background is due to processes with one or two jets mis-reconstructed as tight leptons. The main contributions come from \( W + \text{jets} \), \( t\bar{t} \), single top quark, and multijet production. The conversion background events are mainly due to processes where two prompt electrons of opposite electric charge are produced but one radiates a photon that converts to \( e^+e^- \). The main contribution comes from \( Z + \text{jets} \) production where the \( Z \) boson decays to \( e^+e^- \). The background estimation for the prompt background category is based on MC-simulated samples, while estimations for the other two categories are based on data-driven methods. The modeling of the backgrounds is checked in several control regions.

A. Prompt background

The main source of prompt background is \( WZjj \) production where both bosons decay leptonically and one lepton lies outside of the detector acceptance or fails the lepton identification requirements. Similarly to \( W^\pm W^\mp jj \), there are strong and electroweak production mechanisms for \( WZjj \), which contribute about 75\% and 15\% of the prompt background, respectively. The two production mechanisms are generated using the SHERPA event generator at LO in QCD with up to three partons and normalized to NLO cross sections calculated with VBFNLO in each fiducial phase-space region. The CT10 PDF set is used. The normalization of the electroweak production of \( WZjj \) contains a further complication. This process receives a contribution from the production of a top quark in association with a \( Z \) boson and an additional parton \((tZj)\), where the top quark further decays to a \( W \) boson and a \( b \)-quark. This class of diagrams is taken into account in SHERPA but is neglected in VBFNLO, even though it contributes almost a third of the events populating both phase-space regions. To account for this, a new normalization is derived using the \( b \)-quark in the initial state to select for \( t\bar{t}Zj \) events. The samples are split into events that contain a \( b \)-quark in the initial state (using SHERPA at LO) and events without an initial \( b \)-quark (using VBFNLO at NLO). The cross section used to normalize the SHERPA sample is given by \( \sigma_{\text{VBFNLO}} / (A + \sigma_{\text{fid}}) \times f_b \), where \( \sigma_{\text{VBFNLO}} \) is the NLO cross section calculated using VBFNLO, \( \sigma_{\text{fid}} \) is the sum of LO cross sections calculated with and without a \( b \)-quark in the initial state using SHERPA, \( A \) is the parton-level acceptance of the SHERPA subsamples without any \( b \)-quarks in the initial state, and \( f_b \) is the fraction of generated events containing a \( b \)-quark in the initial state. The overall cross section for the electroweak \( W^\pm Zjj \) production used for the normalization is \( 0.40 \pm 0.09 \text{ fb} \) \((0.34 \pm 0.09 \text{ fb})\) in the Inclusive (VBS) SR, while the corresponding cross section for the strong production is \( 1.04 \pm 0.17 \text{ fb} \) \((0.64 \pm 0.08 \text{ fb})\).

Other processes with two prompt leptons with the same electric charge in the final state include the \( t\bar{t}V \) process, \( ZZjj \) production, and multiple parton – parton interactions (MPI) in one proton – proton interaction. The sum of these backgrounds contributes less than 10\% of the total prompt background. The \( t\bar{t}V \) events are generated using MADGRAPH [68] with PYTHIA 8 used for parton shower and hadronization. The CTEQ6L1 PDF [69] is used. The \( ZZjj \) events are simulated using SHERPA with the CT10 PDF set. MPI processes such as \( W^\pm j + W^\pm j \), \( W^\pm j + Zj \), or \( Zj + Zj \) are simulated with PYTHIA 8 with CTEQ6L1 and the overall contribution is found to be negligible.

B. Nonprompt background

Nonprompt backgrounds come from processes with jets misidentified as leptons or leptons from hadron decays (including \( b \)- and \( c \)-hadron decays). Since the MC simulation may not accurately model the details of these processes, a data-driven fake-factor method is employed to estimate this contribution.

The fake-factor method estimates a fake factor using the ratio of the number of jets satisfying the tight lepton identification criteria to the number of jets satisfying the loose lepton identification criteria in a jet-enriched sample. A new data sample, referred to as the “tight + loose” sample, is selected with the same set of criteria as the signal region but one lepton is required to be a loose lepton. This sample is dominated by contributions from \( W + \text{jets} \), \( t\bar{t} \), and single-top-quark processes. The fake factor is measured, as discussed below, as a function of the loose lepton \( p_T \) and applied to the tight + loose sample event-by-event as a global event weight to estimate the nonprompt background. The contribution from multijet background with two jets satisfying the tight lepton requirements is estimated by selecting events with two loose leptons and
using the product of the two factors computed for each lepton as the event weight. The contribution from multijet background is found to be less than 3.5% of the total nonprompt background.

The lepton fake factors are measured using a dijet sample. Events are selected with a “tag” jet and a loose or tight lepton back-to-back in the azimuthal plane with $\Delta \phi(\ell, j) > 2.8$. The lepton is also referred to as an “underlying jet” since it originates from a jet or hadronic decay. Both the lepton and the jet are required to have $p_T > 25$ GeV. The transverse mass of the lepton and $E_T^{miss}$ is required to be less than 40 GeV to suppress the $W +$ jets contamination. The tag jet and underlying jet recoil in the transverse plane and are assumed to have the same $p_T$. The underlying jet $p_T$ is calculated as the sum of the lepton $p_T$ plus the transverse energy deposited in a cone of radius $\Delta R < 0.3$ around the lepton. To account for the reduction in $p_T$ from energy deposited outside the lepton isolation cone or loss due to neutrinos, the tag jet $p_T$ distribution in the dijet sample is reweighted to match the underlying jet in the tight + loose sample. The energy loss is linearly dependent on $p_T$ where the tag jet has 18% higher $p_T$ than the underlying jet associated with an electron and 72% more for underlying jets associated with a muon. The energy loss for non-prompt muons is accountable by the loss from neutrinos given these events are derived mainly from $c$- and $b$-hadron decays. In addition, a correction factor is applied to the tight + loose sample to take into account the lower trigger efficiency of isolated lepton triggers for loose leptons. The final fake factors are on the order of 2% for electrons and less than 1% for muons.

C. Conversion background

The conversion background is divided into two categories: events containing two prompt leptons with opposite electric charge, which can mimic the same final state if the electric charge of one lepton is misidentified (denoted by “Charge misID”), and $W$-$\gamma$ production with the photon misreconstructed as an electron (denoted by “$W_\gamma$”).

The dominant mechanism responsible for charge misidentification of prompt electrons is the radiation of an energetic photon, which subsequently converts into an $e^+e^-$ pair. The charge misidentification rate for muons is negligible and is therefore not considered. Events entering the signal regions due to conversions consist mainly of fully leptonic $t\bar{t}$ decays and Drell–Yan lepton pair production. The rate of electron charge misidentification is measured in a data sample enriched in $Z \rightarrow e^+e^-$ events. This sample is required to have two tight electrons with the dielectron invariant mass between 70 GeV and 100 GeV. The asymmetric window around the pole mass of the $Z$ boson is used to account for the reduced reconstructed energy when an electron’s charge is misidentified. Contributions to this mass region from other processes are found to be less than 1%. No requirement is made on the charges of the two electrons. The per-electron misidentification rate is derived from the number of same-electric-charge events and the total number of dielectron events.

A likelihood fit is used to measure the charge misidentification rate as a function of the electron $p_T$ and $\eta$, taking into account that either electron in a same-electric-charge pair could be the misidentified one. The numbers of dielectron events and same-electric-charge events are counted in bins of the electron $p_T$ and $\eta$. While the process of charge misidentification is inherently binomial, the large number of events and the relatively small charge-flip rate a Poisson distribution is assumed. Given the total number of observed dielectron events, $N_{i,j}$, and the charge misidentification rates, $e^i$ and $e^j$, where the efficiency is given for bins of $p_T$ and $\eta$ for the two electrons, $i$ and $j$, the expected number of same-electric-charge events ($\tilde{N}_{SS}^{i,j}$) is given by

$$\tilde{N}_{SS}^{i,j} = [e^i(1-e^j) + e^j(1-e^i)]N_{i,j} \approx (e^i + e^j)N_{i,j}. \quad (4)$$

The approximation is valid for very small charge misidentification rates. The log-likelihood function for the number of observed dielectron events with same electric charge ($N_{SS}^{i,j}$) with respect to an expectation of $\tilde{N}_{SS}^{i,j}$ is therefore given by

$$\ln L_{\text{misID}} = \ln \prod_{i,j} \frac{[e^i + e^j]N_{SS}^{i,j} \varepsilon_{SS}^{i,j}}{N_{SS}^{i,j}!} \times e^{-(e^i + e^j)N_{SS}^{i,j}} - N_{SS}^{i,j}(e^i + e^j) - \ln N_{SS}^{i,j}!. \quad (5)$$

Charge misidentification rates are determined for each $p_T$ and $\eta$ bin by maximizing the above log-likelihood function given the observed counts. Since the rates for bremsstrahlung and photon conversion depend on the amount of material traversed, the charge misidentification rate exhibits a strong dependence on the $\eta$ of the electron with the rate generally increasing with $|\eta|$. The charge misidentification rate is observed to be a few tenths of a percent over most of the $\eta$ range with a maximum of about 2% near $|\eta| = 2.5$.

The measured electron charge misidentification rate is cross-checked using a tag-and-probe method applied to the $Z \rightarrow e^+e^-$ sample. Tighter requirements on the quality of the cluster in the calorimeter and the matched track are imposed on the tag electron to make sure its electric charge is correctly determined. The electric charge of the second electron is used to measure the electron charge misidentification rate. Good agreement between the estimates from these two methods is found.

To predict the amount of background from charge misidentification, data events are selected using all of the signal region criteria but requiring the two leptons to have opposite-sign electric charges. For each electron in this data sample, the corresponding charge misidentification rate is included in the global event weight. In the case of events
with two electrons, this procedure is applied to each electron separately. In addition, an energy correction is applied to the electron with the charge misidentification rate assigned to take into account that electrons with misidentified charge tend to have lower reconstructed energy than their correctly identified counterparts and also yield a wider dielectron invariant mass peak for the $Z$ boson. This energy correction is determined using the electron generator-level and reconstructed energies in MC-simulated $Z \rightarrow e^+e^-$ events.

Production of $W\gamma$ events can yield same-electric-charge leptons if the photon converts in the detector and one conversion electron is not reconstructed. Both electroweak and strong $W\gamma jj$ production can arise and their contributions are also estimated using MC-simulated samples. The electroweak production is estimated using SHERPA, while the strong production is estimated using alpgen [70]. The CTEQ6L1 PDF set is used for both samples.

### D. Control regions

Four control regions (CRs), referred to as the “$\leq 1$ jet CR”, “trilepton CR”, “$b$-tag CR”, and “low-$m_{jj}$ CR”, are used to validate background predictions. For all CRs, the contributions from $W^\pm W^\pm jj$-EW and $W^\pm W^\pm jj$-QCD production are normalized to the SM prediction. The definitions of all four control regions, the number of observed data events and the SM predictions as well as a few kinematic distributions in each region are presented below. The comparison between the data and the prediction is checked using a $\chi^2$/ndf test and good agreement is observed.

#### TABLE III. Predicted and observed numbers of events in the $\leq 1$ jet control region separately for the $e^+e^-$, $e^+\mu^-$, and $\mu^+\mu^-$ channels as well as for the sum of all three. The uncertainty is the combination of statistical and systematic uncertainties; correlations among systematic uncertainties are taken into account in the calculation of the total.

<table>
<thead>
<tr>
<th>$\leq 1$ jet Control Region</th>
<th>$e^+e^-$</th>
<th>$e^+\mu^-$</th>
<th>$\mu^+\mu^-$</th>
<th>Total</th>
</tr>
</thead>
<tbody>
<tr>
<td>$W^\pm W^\pm jj$-EW + QCD</td>
<td>$2.2 \pm 0.3$</td>
<td>$7.0 \pm 0.7$</td>
<td>$4.5 \pm 0.5$</td>
<td>$13.7 \pm 1.4$</td>
</tr>
<tr>
<td>Prompt</td>
<td>$WZ$, $ZZ$</td>
<td>$46 \pm 8$</td>
<td>$130 \pm 23$</td>
<td>$75 \pm 13$</td>
</tr>
<tr>
<td></td>
<td>$\ell\ell + W/Z$</td>
<td>$0.3 \pm 0.2$</td>
<td>$0.8 \pm 0.4$</td>
<td>$0.6 \pm 0.3$</td>
</tr>
<tr>
<td>Conversions</td>
<td>Charge misID</td>
<td>$152 \pm 17$</td>
<td>$24 \pm 4$</td>
<td>$\ldots$</td>
</tr>
<tr>
<td></td>
<td>$W\gamma$</td>
<td>$39 \pm 11$</td>
<td>$59 \pm 17$</td>
<td>$0.04 \pm 0.04$</td>
</tr>
<tr>
<td>Non-prompt</td>
<td>$38 \pm 15$</td>
<td>$65 \pm 26$</td>
<td>$8 \pm 5$</td>
<td>$111 \pm 30$</td>
</tr>
<tr>
<td>Total predicted</td>
<td>$278 \pm 28$</td>
<td>$290 \pm 40$</td>
<td>$88 \pm 14$</td>
<td>$650 \pm 70$</td>
</tr>
<tr>
<td>Data</td>
<td>$288$</td>
<td>$328$</td>
<td>$101$</td>
<td>$717$</td>
</tr>
</tbody>
</table>
FIG. 5. The $m_{jj}$ distribution (left) and the distribution of the difference in rapidity (right) of the two jets with the highest $p_T$ is shown summed over all lepton channels for the trilepton CR. Nonprompt background in this region is estimated using MC simulation. The error bars on the data points include statistical uncertainty only. The hatched band represents the systematic uncertainty of the total prediction. The lower plot shows the ratio of the data to the expected background where the brown band indicates the systematic uncertainty including the MC statistical uncertainty. The last bin includes overflow events.

1. ≤ 1 jet control region

The ≤ 1 jet CR is used to test the modeling of lepton kinematics in the $WZ/ZZ$ background where one of the leptons from the $Z$ boson decay is not reconstructed. It is defined by inverting the signal region selection on the jet multiplicity to accept only events with at most one jet. As a consequence, selection criteria using jet-based quantities such as $m_{jj}$ and $\Delta y_{jj}$ are also dropped. Figure 4 shows the dilepton invariant mass distribution and the leading-lepton $p_T$ distribution for the $e^\pm\mu^\pm$ and $\mu^\pm\mu^\pm$ channels with the $Z$ boson veto dropped. Table III shows the number of data events compared to the predictions from signal and various background sources.

2. Trilepton control region

The trilepton CR provides a test of the modeling of lepton and jet kinematics of the $WZjj$ production. It is defined by selecting events with three charged leptons where the third lepton passes the veto-lepton requirements. Events containing a fourth lepton passing the veto-lepton definition are still rejected. In contrast, $m_{jj}$ and $\Delta y_{jj}$ selection criteria are also dropped to obtain more events. The $m_{jj}$ and $|\Delta y_{jj}|$ distributions are shown in Fig. 5. Table IV shows the number of data events compared to the predictions from signal and various background sources.

| Table IV. Predicted and observed numbers of events in the trilepton control region separately for the $e\pm e^\pm$, $e^\pm\mu^\pm$, and $\mu^\pm\mu^\pm$ channels as well as for the sum of all three. The third lepton is required to pass the veto-lepton requirements. The uncertainty is the combination of statistical and systematic uncertainties; correlations among systematic uncertainties are taken into account in the calculation of the total. The conversion background is found to be negligible. |
|---------------------------------|-----------------|-----------------|-----------------|-----------------|-----------------|-----------------|
|                                 | $e^\pm e^\pm\ell^\pm$ | $e^\pm\mu^\pm\ell^\pm$ | $\mu^\pm\mu^\pm\ell^\pm$ | Total            |
| $W^+W^-jj$/EW+QCD              | 0.05 ± 0.02      | 0.13 ± 0.03      | ...             | 0.168 ± 0.029   |
| Prompt                         | $WZ$            | 32 ± 5           | 96 ± 16         | 57 ± 10         | 186 ± 31        |
|                                | $ZZ$            | 2.2 ± 0.6        | 5.3 ± 1.3       | 1.8 ± 0.5       | 9.2 ± 2.1       |
|                                | $t\bar{t} + W/Z$| 0.7 ± 0.3        | 2.4 ± 1.0       | 1.0 ± 0.5       | 4.1 ± 1.7       |
| Non-prompt                     | 0.5 ± 0.3        | 4 ± 4            | ...             | 4 ± 4           |
| Total predicted                | 36 ± 6           | 108 ± 18         | 60 ± 10         | 204 ± 33        |
| Data                           | 40               | 104              | 48              | 192             |
3. b-tag control region

The b-tag CR provides a test of the modeling of $t\bar{t} + W/Z$ and nonprompt background. It is defined by inverting the $b$-jet veto criteria to require the presence of at least one $b$-tagged jet in the event. The $m_{jj}$ and $|\Delta y_{jj}|$ selection criteria are also dropped. Transverse momentum distributions for the leading- and sub-leading-lepton CRs are shown in Fig. 6. Table V shows the number of data events compared to the predictions from signal and various background sources. The $b$-tagging efficiency is included in the systematic uncertainty described in Sec. VI.

4. Low-$m_{jj}$ control region

The low-$m_{jj}$ control region is used to check the background modeling in a region with background composition similar to the signal regions. It is defined by inverting the $m_{jj}$ selection and dropping the $|\Delta y_{jj}|$ selection. The $|\Delta y_{jj}|$ and leading-jet $p_T$ distributions in the low-$m_{jj}$ control region are shown in Fig. 7. Table VI shows the number of data events compared to the predictions from signal and various background sources.

TABLE V. Predicted and observed numbers of events in the $b$-tag control region separately for the $e^+e^-$, $e^+\mu^-$, and $\mu^+\mu^-$ channels as well as for the sum of all three. The uncertainty is the combination of statistical and systematic uncertainties; correlations among systematic uncertainties are taken into account in the calculation of the total.

<table>
<thead>
<tr>
<th>b-tag Control Region</th>
<th>$e^+e^-$</th>
<th>$e^+\mu^-$</th>
<th>$\mu^+\mu^-$</th>
<th>Total</th>
</tr>
</thead>
<tbody>
<tr>
<td>$W^+W^-jj$-EW + QCD</td>
<td>0.8 $\pm$ 0.1</td>
<td>2.6 $\pm$ 0.3</td>
<td>1.5 $\pm$ 0.2</td>
<td>4.9 $\pm$ 0.5</td>
</tr>
<tr>
<td>Prompt</td>
<td>2.3 $\pm$ 0.5</td>
<td>4.9 $\pm$ 0.9</td>
<td>2.2 $\pm$ 0.4</td>
<td>9.4 $\pm$ 1.6</td>
</tr>
<tr>
<td>$t\bar{t} + W/Z$</td>
<td>7.1 $\pm$ 3.1</td>
<td>18 $\pm$ 8</td>
<td>11 $\pm$ 4</td>
<td>36 $\pm$ 15</td>
</tr>
<tr>
<td>Conversions</td>
<td>22 $\pm$ 5</td>
<td>27 $\pm$ 6</td>
<td>...</td>
<td>49 $\pm$ 11</td>
</tr>
<tr>
<td></td>
<td>1.7 $\pm$ 0.7</td>
<td>2.3 $\pm$ 0.9</td>
<td>0.2 $\pm$ 0.2</td>
<td>4.2 $\pm$ 1.4</td>
</tr>
<tr>
<td>Non-prompt</td>
<td>6.7 $\pm$ 2.5</td>
<td>20 $\pm$ 8</td>
<td>10 $\pm$ 5</td>
<td>37 $\pm$ 10</td>
</tr>
<tr>
<td>Total predicted</td>
<td>41 $\pm$ 6</td>
<td>75 $\pm$ 13</td>
<td>25 $\pm$ 7</td>
<td>141 $\pm$ 22</td>
</tr>
<tr>
<td>Data</td>
<td>46</td>
<td>82</td>
<td>36</td>
<td>164</td>
</tr>
</tbody>
</table>
TABLE VI. Predicted and observed numbers of events in the low-$m_{jj}$ control region separately for the $e^\pm e^\mp$, $e^\pm \mu^\mp$, and $\mu^\pm \mu^\mp$ channels as well as for the sum of all three. The uncertainty is the combination of statistical and systematic uncertainties; correlations among systematic uncertainties are taken into account in the calculation of the total.

<table>
<thead>
<tr>
<th>Low $m_{jj}$ Control Region</th>
<th>$e^\pm e^\pm$</th>
<th>$e^\pm \mu^\mp$</th>
<th>$\mu^\pm \mu^\mp$</th>
<th>Total</th>
</tr>
</thead>
<tbody>
<tr>
<td>$W^\pm W^\pm jj$-EW + QCD</td>
<td>$5.9 \pm 0.6$</td>
<td>$17.4 \pm 1.8$</td>
<td>$10.6 \pm 1.1$</td>
<td>$33.9 \pm 3.4$</td>
</tr>
<tr>
<td>Prompt</td>
<td>$WZ, ZZ$</td>
<td>$25 \pm 4$</td>
<td>$54 \pm 9$</td>
<td>$18.4 \pm 3.1$</td>
</tr>
<tr>
<td></td>
<td>$t\bar{t} + W/Z$</td>
<td>$1.7 \pm 0.7$</td>
<td>$3.8 \pm 1.6$</td>
<td>$2.4 \pm 1.0$</td>
</tr>
<tr>
<td>Conversions</td>
<td>Charge misID</td>
<td>$19.4 \pm 2.3$</td>
<td>$8.4 \pm 1.4$</td>
<td>$\cdots$</td>
</tr>
<tr>
<td></td>
<td>$W\gamma$</td>
<td>$14 \pm 4$</td>
<td>$20 \pm 6$</td>
<td>$\cdots$</td>
</tr>
<tr>
<td>Total predicted</td>
<td>$75 \pm 9$</td>
<td>$125 \pm 16$</td>
<td>$39 \pm 6$</td>
<td>$240 \pm 27$</td>
</tr>
<tr>
<td>Data</td>
<td>$78$</td>
<td>$120$</td>
<td>$30$</td>
<td>$228$</td>
</tr>
</tbody>
</table>

The experimental systematic uncertainties affecting the signal and prompt-background estimates include: the uncertainties due to the lepton energy scale, energy resolution, and identification efficiency [40,71]; the uncertainties due to the jet energy scale and resolution, which among systematic uncertainties are taken into account in the calculation of the total.

The uncertainty in the nonprompt-background estimate is between 39% and 52% depending on region and channel. It is dominated by the prompt-lepton contamination in the dijet sample used to estimate the fake factors, the uncertainty in the extrapolation of fake factors into the signal region, and the statistical uncertainty in the number of “tight+loose” events used to estimate the background.

The dominant systematic uncertainties from the conversion background arise from a possible method bias and integrated luminosity is 2.8%, affecting the overall normalization of both the signal and background processes estimated from MC simulation. It is derived following the methodology detailed in Ref. [35].

FIG. 7. The distribution of the rapidity difference between the two jets with the highest $p_T$ (left) and the distribution of the $\eta$ of the leading-jet (right) for the sum of events in the $e^\pm e^\pm$, $e^\pm \mu^\mp$, and $\mu^\pm \mu^\mp$ channels for the low-$m_{jj}$ CR. The conversions background has been split into $W\gamma$ events and events with two prompt OS leptons. The error bars on the data points include statistical uncertainty only. The hatched band represents the systematic uncertainty of the total prediction. The lower plot shows the ratio of the data to the expected background where the brown band indicates the systematic uncertainty including the MC statistical uncertainty. The last bin includes overflow events.
TABLE VII. The decomposition of the relative systematic uncertainties in the estimated number of background and signal events for the Inclusive and VBS SRs. The left columns represent the uncertainties of the total background predictions in each channel from the listed source, while the right columns represent the uncertainties of the total signal predictions from each source. Three numbers in the same cell indicate the uncertainties for the $e^+e^−$, $e^+\mu^−$ and $\mu^+\mu^−$ channels, respectively. If only one number is present in a given cell, it means all three channels have the same systematic uncertainty.

<table>
<thead>
<tr>
<th>Relative Systematic Uncertainties $e^+e^-/e^+\mu^-/\mu^+\mu^-$ [%]</th>
<th>Background Yield</th>
<th>Signal Yield</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td>Inclusive SR</td>
<td>VBS SR</td>
</tr>
<tr>
<td>$W^+W^-jj$-EW cross section</td>
<td></td>
<td></td>
</tr>
<tr>
<td>$W^+W^-jj$-QCD cross section</td>
<td></td>
<td></td>
</tr>
<tr>
<td>$W^\pm Zjj$-EW cross section</td>
<td>6/8/11</td>
<td>5/5/8</td>
</tr>
<tr>
<td>$W^\pm Zjj$-QCD cross section</td>
<td>...</td>
<td>0.9/1.5/2.6</td>
</tr>
<tr>
<td>MC statistics</td>
<td>8/6/8</td>
<td>9/6/8</td>
</tr>
<tr>
<td>Luminosity</td>
<td>1.7/2.1/2.4</td>
<td>1.7/2.1/2.4</td>
</tr>
<tr>
<td>Trigger efficiency</td>
<td>0.1/0.2/0.4</td>
<td>0.1/0.2/0.4</td>
</tr>
<tr>
<td>Lepton reconstruction and identification</td>
<td>1.6/1.2/1.2</td>
<td>1.7/1.1/1.1</td>
</tr>
<tr>
<td>Jet-related uncertainties</td>
<td>11/13/13</td>
<td>13/20/20</td>
</tr>
<tr>
<td>$E_T^{miss}$ reconstruction</td>
<td>2.2/2.4/1.8</td>
<td>2.9/3.2/1.4</td>
</tr>
<tr>
<td>$b$-tagging efficiency</td>
<td>1.0/1.1/1.0</td>
<td>0.8/0.9/0.7</td>
</tr>
<tr>
<td>Non-prompt</td>
<td>4/7/7</td>
<td>4/7/7</td>
</tr>
<tr>
<td>Conversions</td>
<td>6/4/6</td>
<td>6/4/6</td>
</tr>
<tr>
<td>$W_T$ cross section</td>
<td>2.8/2.6/6</td>
<td>3.1/2.6/5</td>
</tr>
<tr>
<td>Total</td>
<td>17/19/21</td>
<td>18/20/21</td>
</tr>
</tbody>
</table>

the statistical uncertainty in the charge misidentification rate measurement. The total uncertainty in the estimation of the conversion background is found to be between 15% and 32% depending on signal region and lepton flavor.

The dominant theoretical uncertainty in the prompt background estimation comes from the predicted cross-section uncertainties for the $W^\pm Zjj$-EW and $W^\pm Zjj$-QCD production. Systematic uncertainties in the $W^\pm Zjj$-EW background estimation are determined separately for the contribution with and without $b$-quarks. Uncertainties due to the choice of factorization and renormalization scales and PDF uncertainties are calculated with VBFNLO. Parton-shower effects are determined by applying two parton showering algorithms. LO VBFNLO events are used, since no NLO events are available. The difference between the *PYTHIA 8* parton-shower model with the AU2 tune for the underlying-event modeling and the *HERWIG* parton shower with *JIMMY* for the underlying-event modeling is used to estimate the parton-shower uncertainty. The same procedures are used to calculate the total NLO cross sections, scale, PDF, and parton-shower uncertainties for the $W^\pm Zjj$-QCD production. The $W^\pm Zjj$-QCD final state also occurs through diagrams with

TABLE VIII. Predicted and observed numbers of events in the Inclusive SR are shown separately for the $e^+e^-$, $e^+\mu^-$ and $\mu^+\mu^-$ channels as well as for the sum of all three. The uncertainty is the combination of statistical and systematic uncertainties; correlations among systematic uncertainties are taken into account in the calculations of the total. The contributions from $W^\pm W^\pm jj$-EW and $W^\pm W^\pm jj$-QCD production are normalized to the SM prediction.

<table>
<thead>
<tr>
<th>Inclusive Signal Region</th>
<th>$e^+e^-$</th>
<th>$e^+\mu^-$</th>
<th>$\mu^+\mu^-$</th>
<th>Total</th>
</tr>
</thead>
<tbody>
<tr>
<td>$W^\pm W^\pm jj$-EW</td>
<td>2.82 ± 0.28</td>
<td>7.8 ± 0.7</td>
<td>4.6 ± 0.4</td>
<td>15.2 ± 1.3</td>
</tr>
<tr>
<td>$W^\pm W^\pm jj$-QCD</td>
<td>0.86 ± 0.15</td>
<td>2.3 ± 0.4</td>
<td>1.45 ± 0.24</td>
<td>4.6 ± 0.7</td>
</tr>
<tr>
<td>Prompt</td>
<td>3.0 ± 0.7</td>
<td>6.1 ± 1.3</td>
<td>2.6 ± 0.6</td>
<td>11.6 ± 2.5</td>
</tr>
<tr>
<td>Conversions</td>
<td>Charge misID</td>
<td>2.1 ± 0.4</td>
<td>0.77 ± 0.27</td>
<td>...</td>
</tr>
<tr>
<td></td>
<td>$W_T$</td>
<td>1.1 ± 0.6</td>
<td>1.6 ± 0.8</td>
<td>...</td>
</tr>
<tr>
<td>Nonprompt</td>
<td>0.61 ± 0.30</td>
<td>1.9 ± 0.8</td>
<td>0.41 ± 0.22</td>
<td>2.9 ± 0.8</td>
</tr>
<tr>
<td>Total predicted</td>
<td>10.4 ± 1.3</td>
<td>20.3 ± 2.5</td>
<td>9.1 ± 1.0</td>
<td>40 ± 4</td>
</tr>
<tr>
<td>Data</td>
<td>12</td>
<td>26</td>
<td>12</td>
<td>50</td>
</tr>
</tbody>
</table>
TABLE IX. Predicted and observed numbers of events in the VBS SR are shown separately for the $e^+e^-$, $e^+\mu^-$, and $\mu^+\mu^-$ channels as well as for the sum of all three. The uncertainty is the combination of statistical and systematic uncertainties; correlations among systematic uncertainties are taken into account in the calculations of the total. The contributions from $W^\pm W^\pm jj$-EW and $W^\pm W^\pm jj$-QCD production are normalized to the SM prediction.

<table>
<thead>
<tr>
<th>VBS Signal Region</th>
<th>$e^+e^-$</th>
<th>$e^+\mu^-$</th>
<th>$\mu^+\mu^-$</th>
<th>Total</th>
</tr>
</thead>
<tbody>
<tr>
<td>$W^\pm W^\pm jj$-EW</td>
<td>2.34 ± 0.23</td>
<td>6.3 ± 0.6</td>
<td>3.77 ± 0.35</td>
<td>12.4 ± 1.1</td>
</tr>
<tr>
<td>$W^\pm W^\pm jj$-QCD</td>
<td>0.26 ± 0.06</td>
<td>0.67 ± 0.14</td>
<td>0.43 ± 0.09</td>
<td>1.36 ± 0.27</td>
</tr>
<tr>
<td>Prompt</td>
<td>2.2 ± 0.5</td>
<td>4.2 ± 1.0</td>
<td>1.9 ± 0.5</td>
<td>8.2 ± 1.9</td>
</tr>
<tr>
<td>Conversions</td>
<td>Charge misID</td>
<td>1.39 ± 0.27</td>
<td>0.64 ± 0.24</td>
<td>...</td>
</tr>
<tr>
<td>Nonprompt</td>
<td>$W_\gamma$</td>
<td>0.7 ± 0.4</td>
<td>1.3 ± 0.7</td>
<td>...</td>
</tr>
<tr>
<td>Total predicted</td>
<td>7.4 ± 1.0</td>
<td>14.5 ± 1.9</td>
<td>6.4 ± 0.7</td>
<td>28.3 ± 3.4</td>
</tr>
<tr>
<td>Data</td>
<td>6</td>
<td>18</td>
<td>10</td>
<td>34</td>
</tr>
</tbody>
</table>

zero or one parton but containing two jets after parton showering. This contribution is included in the SHERPA sample and has an additional parton-shower uncertainty. This effect is determined using a dedicated MADGRAPH sample with two different parton-shower models. A 52% uncertainty is obtained from this comparison, which results in an uncertainty of 6% in the total $W^\pm Zjj$-QCD contribution. The theoretical uncertainties of the other background contributions include 30%, 19%, and 17% uncertainties in the predicted cross sections of the $t\bar{t} + V$, electroweak and strong production of ZZjj, and $W_\gamma$ processes, respectively.

A summary of the decomposition of the systematic uncertainties in the estimated number of background and signal events for the two SRs is given in Table VII. Most uncertainties do not have an inherent dependence on the flavor of the two leptons, but the size of the contribution to the total background uncertainty does depend on the channel due to differences in the composition of the background between channels. The fractional uncertainties listed are quoted as the effect on the background yield or signal yield in the $e^+e^-$, $e^+\mu^-$, and $\mu^+\mu^-$ channels separately. The largest uncertainty is the jet-related uncertainty for both the signal and background estimations.

FIG. 8. The $m_{jj}$ distribution for the combined channels in the Inclusive SR prior to applying the requirement that $m_{jj} > 500$ GeV. The error bars on the data points represent statistical uncertainty only. The hatched band represents the systematic uncertainty of the total prediction. The lower plot shows the ratio of the data to the expected background where the brown band indicates systematic uncertainty including the MC statistical uncertainty. The ratio of the sum of the expected signal ($W^\pm W^\pm jj$-EW and $W^\pm W^\pm jj$-CQD) and background to the expected background is also shown.

FIG. 9. The rapidity difference distribution between the two jets with the highest $p_T$ in the Inclusive SR for the combined channels. The region with $|\Delta y_{jj}| > 2.4$ denoted by the vertical dotted line indicates the VBS SR. The error bars on the data points include statistical uncertainty only. The hatched band represents the systematic uncertainty of the total prediction. The contributions from $W^\pm W^\pm jj$-EW and $W^\pm W^\pm jj$-QCD production are normalized to the SM prediction.
VII. EVENTS YIELDS IN THE SIGNAL REGIONS

The observed and predicted event yields in the Inclusive and VBS SRs are shown in Tables VIII and IX, broken down by $e^+e^-$, $e^+\mu^-$, and $\mu^+\mu^-$ channels as well as the sum of all three. The observed data events are consistent with the SM predictions including $W^\pm W^\pm jj$ production. Several kinematic distributions are shown in Figs. 8–10. The uncertainties displayed are the systematic and statistical uncertainties added in quadrature. All three channels are combined in these plots, and correlations of a given systematic uncertainty with others are maintained across signal and background processes and channels. The contributions from electroweak and strong $W^\pm W^\pm$ production are normalized to the SM predictions. Figure 8 presents the dijet invariant mass distribution for the Inclusive SR before the final $m_{jj} > 500$ GeV selection is applied. Figure 9 presents the $|\Delta y_{jj}|$ distribution for the VBS SR before the $|\Delta y_{jj}| > 2.4$ selection is applied.

The lepton centrality is a measure of how central the leptons are with respect to the jets and is defined by $\zeta = \min(\eta(\ell_2) - \eta(j_2), \eta(\ell_1) - \eta(j_1))$, where $j_{1,2}$ refers to the two jets and $\ell_{1,2}$ refers here to the two jets with $\eta(j_1) > \eta(j_2)$, and $\eta(\ell_1) > \eta(\ell_2)$. Events tend to have a lepton centrality greater than zero in the VBS topology. The lepton centrality distribution together with the distribution of the scalar sum of the two leading leptons’ transverse momenta in the VBS SR are shown in Figure 10. Good agreement between data and SM predictions with $W^\pm W^\pm jj$ production included is found for all distributions.

The data are also divided into $W^+W^+$ and $W^-W^-$ channels. The $W^+W^+$ channel is favored by data and SM prediction as the LHC is a $pp$ collider. These two channels are not split by leptonic final states due to the limited number of events. The event yields are shown in Table X, and the observed charge distribution in data is found to be consistent with SM predictions.

| TABLE X. Event yields for predicted signal and background events as well as observed data in the VBS SR for the $W^+W^+$ and $W^-W^-$ channels. The uncertainty is the combination of statistical and systematic uncertainties; correlations among systematic uncertainties are taken into account in the calculations of the total. |
|------------------|-----------------|------------------|-----------------|-----------------|-----------------|-----------------|-----------------|-----------------|
|                   | Inclusive Signal Region | VBS Signal Region |
|                   | $W^+W^+$          | $W^-W^-$          | $W^+W^+$          | $W^-W^-$          |
| $W^\pm W^\pm jj$-EW | $13.0 \pm 1.2$   | $3.9 \pm 0.4$    | $9.4 \pm 0.8$    | $2.90 \pm 0.27$  |
| $W^\pm W^\pm jj$-QCD | $3.6 \pm 0.6$   | $1.14 \pm 0.19$  | $1.08 \pm 0.21$  | $0.26 \pm 0.06$  |
| Prompt            | $8.0 \pm 1.7$    | $3.7 \pm 0.8$    | $6.0 \pm 1.4$    | $2.2 \pm 0.6$    |
| Conversions       | $1.27 \pm 0.28$  | $1.57 \pm 0.35$  | $0.90 \pm 0.23$  | $1.13 \pm 0.28$  |
| $W_T$             | $1.7 \pm 0.8$    | $1.0 \pm 0.6$    | $1.4 \pm 0.7$    | $0.6 \pm 0.4$    |
| Nonprompt         | $1.7 \pm 0.5$    | $1.2 \pm 0.4$    | $1.4 \pm 0.4$    | $0.95 \pm 0.33$  |
| Total predicted   | $29.3 \pm 3.3$   | $12.5 \pm 1.6$   | $20.2 \pm 2.5$   | $8.1 \pm 1.4$    |
| Data              | 35               | 15               | 23               | 11               |
VIII. EXTRACTION OF PRODUCTION CROSS SECTIONS

The excesses in data over the background-only predictions in the Inclusive and VBS SRs are consistent with the event topology for $W^\pm W^\mp jj$ production. The numbers of observed data and expected signal and background events are used to calculate the fiducial cross sections in these two signal regions.

A. Cross-section extraction method

A likelihood function is used to extract the cross sections in the two fiducial regions. The likelihood function uses Poisson distributions for each channel and global constraints for the nuisance parameters $\theta_j$, which parametrize effects of systematic uncertainties. The number of expected events in a given decay channel $c$, $N^\text{exp}_c$, is a product of the integrated luminosity $L$, the measured fiducial cross section $\sigma_{W^\pm W^\mp jj}$, the relative acceptance for each channel, $A_c$, and the signal efficiency $\varepsilon_c$ in addition to the total number of background events in this channel, $\sum_b N_{c,b}$:

$$N^\text{exp}_c = L \cdot \sigma_{W^\pm W^\mp jj} \cdot A_c \cdot \varepsilon_c + \sum_b N_{c,b}.$$  \hspace{1cm} (6)

The likelihood function is given by

$$L = \prod_c \text{Pois}(N^\text{obs}_c | N^\text{exp}_c) \prod_j g(0|\theta_j, 1).$$  \hspace{1cm} (7)

The function $g$ is a Gaussian probability density function. The effect due to systematic uncertainties in $\varepsilon_c$ and $N_{c,b}$ are parameterized by the nuisance parameters according to

$$\varepsilon_c(\theta_j) = \varepsilon^0_c \prod_j (1 + \theta_j \delta^c_{e,j}),$$  \hspace{1cm} (8)

$$N_{c,b}(\theta_j) = N^0_{c,b} \prod_j (1 + \theta_j \delta^b_{c,j}),$$  \hspace{1cm} (9)

with $\varepsilon^0_c$ and $N^0_{c,b}$ being the nominal estimates for the signal reconstruction efficiency and the background yields in channel $c$. The constants $\delta^c_{e,j}$ and $\delta^b_{c,j}$ represent the relative uncertainty in the signal reconstruction efficiency and the nominal background prediction, respectively, in channel $c$ due to the source of systematic uncertainty, $j$.

The relative acceptances within the fiducial region are determined at particle level from the decay branching ratios of the two $W$ bosons to $e^\pm e^\pm$, $e^\pm \mu^\pm$, and $\mu^\pm \mu^\pm$. Small deviations arise from the jet object definition at particle level, which accepts electrons as input objects to the jet clustering algorithm while muons are ignored. The acceptances in the corresponding channels are 0.232, 0.524, and 0.265 in the Inclusive SR and 0.235, 0.527, and 0.257 in the VBS SR, respectively.

The signal efficiency for channel $c$, $\varepsilon_c$, is estimated from simulated signal events. It is given by the number of events reconstructed in a given signal region divided by the number of events passing the corresponding definition of the fiducial phase-space region at the particle level. It accounts for the detector reconstruction, particle identification, and trigger efficiency as well as for the migration into and out of the fiducial volume due to detector resolution effects. The signal efficiency definition includes contributions from leptons originating from $\tau$ decays at the reconstruction level, while those events are vetoed at the particle level. The fraction of events where the electron or muon originates from a $\tau$ lepton in the signal yield at the reconstruction level is found to be 10%. The efficiencies in the $e^\pm e^\pm$, $e^\pm \mu^\pm$, and $\mu^\pm \mu^\pm$ channels are (56.2 ± 1.5)%, (71.7 ± 0.8)%, and (77.0 ± 0.9)% in the Inclusive signal region and (57.2 ± 1.6)%, (72.7 ± 1.0)% and (82.7 ± 1.2)% in the VBS signal region, respectively.

The measured cross sections are taken as those maximizing the log-likelihood function shown in Eq. (7). The quoted uncertainties are derived using the profile likelihood method [74] and correspond to likelihood intervals with a confidence level (CL) of 68.3%.

B. Measured fiducial cross sections

The measured fiducial cross section is $\sigma^\text{fid}_{\text{Incl.}W^\pm W^\mp jj} = 2.3 \pm 0.6 \text{(stat)} \pm 0.3 \text{(syst)} \text{ fb}$ for the $W^\pm W^\mp jj$ production, including both electroweak and strong production as well as...

FIG. 11. The measured cross sections for the Inclusive SR (left) and the VBS SR (right) compared to the predictions for each channel and for the combined measurement. The inner error band represents the statistical uncertainty and the outer band represents the total uncertainty of each measurement.
as the interference in the Inclusive SR. The measured fiducial cross section is 
\[ \sigma_{\text{fid}}^{W^\pm W^\mp jj} = 1.5 \pm 0.5(\text{stat}) \pm 0.2(\text{syst}) \text{ fb} \]
for electroweak \( W^\pm W^\mp \) production, including interference with strong production in the VBS region. The measured cross sections are in agreement with the respective SM predictions of 1.52 \pm 0.11 \text{ fb} \) and 0.95 \pm 0.06 \text{ fb}. The cross sections are shown in Fig. 11 for each channel and for the combined measurement. The observed combined significance over the background-only hypothesis is 4.5\( \sigma \) in the Inclusive SR and 3.6\( \sigma \) in the VBS SR, while the corresponding expected significances for a SM \( W^\pm W^\mp jj \) signal are 3.1\( \sigma \) and 2.3\( \sigma \), respectively.

**IX. EXTRACTION OF ANOMALOUS QUARTIC GAUGE COUPLINGS**

VBS events receive contributions from quartic gauge boson interactions and thus can be used to search for aQGCs. In general, the effective Lagrangian described in Sec. I does not ensure unitarity. The Higgs boson in the SM ensures unitarity of the SM VBS process, which is destroyed if anomalous couplings or additional resonances are added. A unitarization scheme has to be applied in order to avoid nonphysical predictions. In the case of VBS with aQGC, the unitarization significantly impacts the differential and total cross sections. The K-matrix unitarization scheme [17] is applied in this analysis where the elastic scattering eigenamplitude \( \mathcal{A}(s) \) is projected on the Argand circle \( \mathcal{A}(s) \rightarrow \mathcal{A}(s) \) such that \( |\mathcal{A}(s) - i/2| = 1/2 \). This condition is derived from the optical theorem and ensures that the projected scattering amplitude meets the unitarity condition exactly. As a result, the cross section saturates at the maximum value allowed by unitarity. The whizrun [75] event generator is used to calculate cross sections and generate events with aQGCs at LO in QCD. The CTEQ6L1 PDF set is used. All samples use the parametrization in terms of \( \alpha_4 \) and \( \alpha_5 \). The invariant mass of the system of two charged leptons and two neutrinos from the decay of the two \( W \) bosons, \( m_{\ell\ell\nu\nu} \), is used as the renormalization and factorization scales, \( \mu_R = \mu_F = m_{\ell\ell\nu\nu} \).

The events are interfaced to PYTHIA for modeling the parton shower, QED final-state radiation, decays of \( \tau \) leptons, and the underlying event.

The expected sensitivity to \( \alpha_4 \) and \( \alpha_5 \) is improved significantly compared to the results obtained in the previous publication [29] by selecting a phase-space region that is more sensitive to anomalous contributions to the \( WWWW \) vertex. This is achieved by an additional requirement: \( m_{WW,T} > 400 \text{ GeV} \). The effects from new-physics processes are expected to be seen predominantly at larger mass scales, which motivates the definition of the aQGC SR as defined in Sec. III. The distribution of the transverse mass of the \( W \) system before applying the final selection criteria is shown in Fig. 12.

The signal in the aQGC region is defined as the \( \alpha_4 \) -dependent excess of the \( W^\pm W^\mp jj\)-EW production cross section over the SM prediction of this process. No interference effects of the aQGC contribution with either the SM \( W^\pm W^\mp jj\)-QCD or \( W^\pm W^\mp jj\)-EW production are considered. The combined signal reconstruction efficiency in the three final states is found to be \( (68.7 \pm 2.2)\% \) with no significant dependence on \( \alpha_4 \) and \( \alpha_5 \).

Table XI summarizes the expected and observed event yields in the aQGC SR. The theoretical uncertainties in the aQGC signal region are less than in the VBS region and the systematic uncertainties are consistent with those in the VBS signal region. Therefore, the VBS signal region systematic uncertainties as described in Sec. VI are applied.

**TABLE XI.** Expected and observed event yields in the aQGC SR. The first quoted uncertainty is statistical and the second is systematic. The row corresponding to the BSM contribution indicates the additional events expected given \( \alpha_4 = 0.1 \) and \( \alpha_5 = 0 \).

<table>
<thead>
<tr>
<th>aQGC Signal Region</th>
<th>Non-prompt</th>
<th>Conversions</th>
<th>Prompt</th>
<th>SM ( W^\pm W^\mp jj )-EW</th>
<th>SM ( W^\pm W^\mp jj )-QCD</th>
<th>Total background</th>
<th>( \alpha_4 = 0.1, \alpha_5 = 0 )</th>
<th>Data</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td>0.2 \pm 0.1 \pm 0.1</td>
<td>0.7 \pm 0.2 \pm 0.1</td>
<td>0.8 \pm 0.1 \pm 0.3</td>
<td>1.7 \pm 0.1 \pm 0.2</td>
<td>0.4 \pm 0.0 \pm 0.1</td>
<td>3.8 \pm 0.3 \pm 0.5</td>
<td>7.3 \pm 0.4 \pm 0.6</td>
<td>8</td>
</tr>
</tbody>
</table>

FIG. 12. The \( m_{WW,T} \) distribution for all channels combined in the VBS SR prior to applying the requirement of \( m_{WW,T} > 400 \text{ GeV} \). The \( m_{WW,T} \) requirement is represented by a vertically dashed line. The expected signal contribution for the aQGC parameter point \( \alpha_4 = 0.1 \) and \( \alpha_5 = 0 \) is overlaid as a histogram and includes the aQGC signal and the background prediction. The error bars on the data points include statistical uncertainty only. The hatched band represents the systematic uncertainty of the total prediction. The last bin includes overflow events.
A total of $3.8 \pm 0.6$ events are expected from SM background processes. The expected number of additional events for the aQGC parameter point $\alpha_4 = 0.1$ and $\alpha_5 = 0$ is also shown. In total 8 events are observed in data, which corresponds to an excess with a significance of 1.8$\sigma$.

A CL$_s$ upper limit [76] on the visible cross section in the aQGC SR is reported. The visible cross section $\sigma^{\text{vis}}$ is defined at the detector level as the excess of data events ($N^{\text{obs}}$) over the background prediction ($N^{\text{bkg}}$) divided by the integrated luminosity:

$$\sigma^{\text{vis}} = \frac{N^{\text{obs}} - N^{\text{bkg}}}{L}. \quad (10)$$

The CL$_s$ upper limit is derived with a likelihood function equivalent to the one defined in Eq. (7) for a single channel by replacing $\alpha_{W^\pm W^\mp jj}$ with $\sigma^{\text{vis}}$ in Eq. (6) where $\sigma^{\text{vis}}$ is affected by uncertainties in the background prediction and the integrated luminosity, but not by reconstruction efficiencies or uncertainties in the theoretical cross sections of the SM $W^\pm W^\mp jj$ production. The observed (expected) 95% CL upper limit on $\sigma^{\text{vis}}$ in the aQGC SR is 0.50 fb (0.25 fb). These limits are converted to upper limits on the fiducial cross section, assuming the same signal reconstruction efficiency as that of the $W^\pm W^\mp jj$-EW production. Models predicting contributions to the aQGC fiducial phase-space region at the particle level of more than 0.72 fb (0.37 fb) are excluded at the 95% CL.

The upper limits on the fiducial cross section in the aQGC phase-space region at the particle level are used to derive constraints in the $(\alpha_4, \alpha_5)$ parameter space. The expected and observed two-dimensional exclusion contours are shown in Fig. 13. The expected one-dimensional confidence intervals at the 95% CL are $\alpha_4 \in [-0.06, 0.07]$, and $\alpha_5 \in [-0.10, 0.11]$ (expected).

The observed one-dimensional confidence intervals at the 95% CL are $\alpha_4 \in [-0.14, 0.15]$, and $\alpha_5 \in [-0.22, 0.22]$ (observed).

This result constitutes a 35% improvement in the expected aQGC sensitivity with respect to the analysis published in Ref. [29]. The observed exclusion is only marginally more restrictive because of the small excess observed in the aQGC signal region. The sensitivity is similar to that in Ref. [32], where the observed results are more constraining.

X. SUMMARY

This paper presents results from the ATLAS detector at the LHC using 20.3 fb$^{-1}$ of proton–proton collision data at $\sqrt{s} = 8$ TeV from the measurement of the $W^\pm W^\mp jj$ production cross sections. Events with two leptons (electrons or muons) with the same electric charge, $E_T^{\text{miss}}$, and at least two jets are investigated in the Inclusive signal region. An additional selection on the rapidity difference of the leading jets is used to measure the fiducial cross section for the $W^\pm W^\mp jj$-EW production in the VBS signal region. The further requirement of a high transverse mass of the system of two leptons and $E_T^{\text{miss}}$ is used to define a restricted phase-space region more sensitive to aQGC parameters.

In the Inclusive signal region, a total of 50 signal candidates are observed and 20 background events are expected. The excess of events over the background-only prediction is interpreted as evidence for the sum of the $W^\pm W^\mp jj$-EW and $W^\pm W^\mp jj$-QCD processes. The measured fiducial cross section for $W^\pm W^\mp jj$ production is $2.3 \pm 0.6$ (stat) $\pm 0.3$ (syst) fb, with a significance of 4.5$\sigma$ (3.1$\sigma$ expected). In the VBS signal region, the background-only prediction includes the $W^\pm W^\mp jj$-QCD production, and a total of 34 events are observed and 16 background events are predicted. The excess is interpreted as evidence for the $W^\pm W^\mp jj$-EW processes. The measured fiducial cross section for the $W^\pm W^\mp jj$-EW production, including the interference with the $W^\pm W^\mp jj$-QCD production, is $1.5 \pm 0.5$ (stat) $\pm 0.2$ (syst) fb with a significance of 3.6$\sigma$ (2.3$\sigma$ expected). The measured cross sections are consistent with the SM predictions.

In the aQGC signal region, the background prediction includes both the $W^\pm W^\mp jj$-EW and $W^\pm W^\mp jj$-QCD processes. A total of 8 events are observed and 3.8 background events are expected. These numbers are used to constrain the aQGC parameters $\alpha_4$ and $\alpha_5$. The observed one-dimensional 95% confidence level intervals are $-0.14 < \alpha_4 < 0.15$ and $-0.22 < \alpha_5 < 0.22$. The expected 95% confidence level intervals are $-0.06 < \alpha_4 < 0.07$ and $-0.10 < \alpha_5 < 0.11$. These intervals constitute a 35%
improvement in the expected aQGC sensitivity with respect to the analysis published in Ref. [29].

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