Measurement of the inclusive cross-sections of single top-quark and top-antiquark $t$-channel production in $pp$ collisions at $\sqrt{s} = 13$ TeV with the ATLAS detector

The ATLAS collaboration

E-mail: atlas.publications@cern.ch

Abstract: A measurement of the $t$-channel single-top-quark and single-top-antiquark production cross-sections in the lepton+jets channel is presented, using 3.2 fb$^{-1}$ of proton-proton collision data at a centre-of-mass energy of 13 TeV, recorded with the ATLAS detector at the LHC in 2015. Events are selected by requiring one charged lepton (electron or muon), missing transverse momentum, and two jets with high transverse momentum, exactly one of which is required to be $b$-tagged. Using a binned maximum-likelihood fit to the discriminant distribution of a neural network, the cross-sections are determined to be $\sigma(tq) = 156 \pm 5\,(\text{stat.}) \pm 27\,(\text{syst.}) \pm 3\,(\text{lumi.})$ pb for single top-quark production and $\sigma(\bar{t}q) = 91 \pm 4\,(\text{stat.}) \pm 18\,(\text{syst.}) \pm 2\,(\text{lumi.})$ pb for single top-antiquark production, assuming a top-quark mass of 172.5 GeV. The cross-section ratio is measured to be $R_t = \sigma(tq)/\sigma(\bar{t}q) = 1.72 \pm 0.09\,(\text{stat.}) \pm 0.18\,(\text{syst.})$. All results are in agreement with Standard Model predictions.

Keywords: Hadron-Hadron scattering (experiments)

ArXiv ePrint: 1609.03920
1 Introduction

After its restart in 2015, the Large Hadron Collider (LHC) [1] has been producing proton-proton (pp) collisions at a centre-of-mass energy of $\sqrt{s} = 13$ TeV, giving the collider experiments access to a so far unexplored kinematic range. It is important to measure all accessible Standard Model (SM) processes at the new centre-of-mass energy, compare the results to the corresponding theoretical SM predictions, and look for deviations which might result from energy-dependent non-SM couplings. In this article, inclusive cross-section measurements of the dominant single-top-quark production mechanism are presented.

At leading order (LO) in perturbation theory, single top-quark production is described by three subprocesses that are distinguished by the virtuality of the exchanged $W$ boson. The dominant process is the $t$-channel exchange depicted in figure 1, which is the subject of the measurements presented in this article. A light quark from one of the colliding protons interacts with a $b$-quark from another proton by exchanging a virtual $W$ boson. Since the valence $u$-quark density of the proton is about twice as high as the valence $d$-quark density, the production cross-section of single top-quarks $\sigma(tq)$ is expected to be higher than the cross-section of top-antiquark production $\sigma($\bar{t}$q$). At LO, the subleading single-top-quark processes are the associated production of a $W$ boson and a top quark ($Wt$) and the s-channel production of $t\bar{b}$ and $\bar{t}b$. 

---

**Contents**

1 Introduction ........................................... 1
2 Data and simulation samples ....................... 3
3 Object reconstruction ............................... 5
4 Event selection ........................................ 6
5 Background estimation ............................... 7
6 Discrimination of signal and background events .. 9
7 Systematic uncertainties ............................ 10
8 Statistical analysis .................................. 14
9 Cross-section measurement ......................... 15
10 Conclusion ............................................ 19
The ATLAS collaboration ................................. 26
Figure 1. Representative leading-order Feynman diagrams of (a) single-top-quark production and (b) single-top-antiquark production via the $t$-channel exchange of a virtual $W$ boson ($W^+$), including the decay of the top quark and top antiquark, respectively.

In this article, measurements of $\sigma(tq)$ and $\sigma(\bar{t}q)$ in proton-proton collisions at a centre-of-mass energy of $\sqrt{s} = 13$ TeV are presented. The analysis is based on the ATLAS data set collected in 2015 corresponding to an integrated luminosity of 3.2 fb$^{-1}$. Separate measurements of $tq$ and $\bar{t}q$ production provide sensitivity to the parton distribution functions (PDFs) of the $u$-quark and the $d$-quark [2], exploiting the different initial states of the two processes as shown in figure 1. In addition, the cross-section ratio $R_t \equiv \sigma(tq)/\sigma(\bar{t}q)$ is measured, featuring smaller systematic uncertainties than the individual cross-sections because of partial cancellations of common uncertainties.

In general, measurements of single top-quark production provide insights into the properties of the $Wtb$ vertex. The cross-sections are proportional to the square of the coupling at the production vertex. In the SM, the coupling is given by the Cabibbo-Kobayashi-Maskawa (CKM) matrix element $V_{tb}$ [3, 4] multiplied by the universal electroweak coupling constant. Non-SM contributions can be encapsulated by an additional left-handed form factor $f_{LV}$ [5], assumed to be real. The sensitivity for these non-SM contributions could be increased for the higher centre-of-mass energy, if there is new physics at high scales. The combined cross-section $\sigma(tq + \bar{t}q)$ is determined as the sum of $\sigma(tq)$ and $\sigma(\bar{t}q)$ and used to determine $f_{LV} \cdot |V_{tb}|$. All measurements presented in this paper are based on the assumption that the production and the decay of top quarks via $Wts$ and $Wtd$ vertices is suppressed due to the fact that the CKM matrix elements $V_{ts}$ and $V_{td}$ are much smaller than $V_{tb}$. Currently, the most precise determination of $f_{LV} \cdot |V_{tb}|$ has an uncertainty of 4%, obtained from a combination of measurements performed by the CMS Collaboration [6] under the same assumption as the one stated above.

In $pp$ collisions at $\sqrt{s} = 13$ TeV, the predicted production cross-section of the $t$-channel single-top-quark process is $\sigma(tq) = 136.0^{+5.4}_{-4.6}$ pb for top-quark production and $\sigma(\bar{t}q) = 81.0^{+4.1}_{-3.6}$ pb for top-antiquark production. These predictions have been calculated for a top-quark mass of 172.5 GeV at next-to-leading order (NLO) [7] in perturbative QCD using Hathor v2.1 [8]. The uncertainties connected with PDFs and the strong coupling constant, $\alpha_s$, are calculated using the PDF4LHC prescription [9] with the MSTW2008 NLO [10, 11], CT10 NLO [12] and NNPDF 2.3 NLO [13] PDF sets, and are added in quadrature to the scale uncertainty. The cross-sections of all three single-top-quark production processes have also been calculated at approximate next-to-next-to-leading-order (NNLO) precision [14–16]. NNLO results are available for the $t$-channel cross-section [17] and the NNLO/NLO $K$-factor is 0.985. However, the NLO calculation of this process features a more comprehensive uncertainty treatment, including a complete treatment of the PDF and scale uncertainties, compared to the NNLO one, and is therefore used to extract $f_{LV} \cdot |V_{tb}|$. 

– 2 –
In this analysis, the event selection targets $tq$ and $\bar{t}q$ events with leptonically decaying $W$ bosons. The lepton is either an electron or a muon, where events involving $W \rightarrow \tau \nu$ decays with a subsequent decay of the $\tau$ lepton to $e\nu, \nu\tau, \mu\nu$, or $\mu\tau$ are included in the signal. The experimental signature of selected events is thus given by one prompt isolated electron or muon, missing transverse momentum, $E_T^{\text{miss}}$, and two hadronic jets with high transverse momentum, $p_T$, where one of these jets originates from a $b$-quark ($b$-jet) and the second one is produced primarily in the forward direction. The presence of additional jets is vetoed to suppress background from $t\bar{t}$ production.

Several other processes feature the same signature as single-top-quark events; the main backgrounds are $W$+jets production and top-quark-antiquark ($t\bar{t}$) pair production. In order to improve the sensitivity of the signal extraction, an artificial neural network (NN) \cite{18} is used to discriminate between signal and background events, following the same strategy that was used in comprehensive measurements of $t$-channel single top-quark production at $\sqrt{s} = 7$ TeV \cite{19}.

This article is organised as follows. Section 2 gives an overview of the data and simulated event samples that are used in the analysis. The definitions of physics objects are given in section 3 and the event selection criteria as well as the definition of the signal and validation regions are presented in section 4. Section 5 describes the estimation of the background processes and compares the predicted kinematic distributions to data. Section 6 discusses the discriminating variables and the training and the performance of the NN used to improve the measurement sensitivity, while in section 7 the estimation of systematic uncertainties is discussed. Section 8 is devoted to the statistical analysis and section 9 to the measurement of the signal cross-sections and their ratio, and the extraction of $f_{LV} \cdot |V_{tb}|$. Finally, the conclusion is given in section 10.

2 Data and simulation samples

The ATLAS experiment \cite{20} at the LHC is a multi-purpose particle detector with a forward-backward symmetric cylindrical geometry and a near $4\pi$ coverage in solid angle. It consists of an inner tracking detector surrounded by a thin superconducting solenoid providing a 2 T axial magnetic field, electromagnetic and hadron calorimeters, and a muon spectrometer. The inner tracking detector (ID) covers the pseudorapidity range $|\eta| < 2.5$. It consists of silicon pixel, silicon microstrip, and transition-radiation tracking detectors. The innermost layer of the pixel detector, the insertable B-layer \cite{21}, was added between Run 1 (2009-2013) and Run 2 of the LHC at a radius of 33 mm around a new and thinner beam pipe. Lead/liquid-argon (LAr) sampling calorimeters provide electromagnetic (EM) energy measurements with high granularity. A hadron (iron/scintillator-tile) calorimeter covers the central pseudorapidity range ($|\eta| < 1.7$). The endcap and forward regions are instrumented with LAr calorimeters for both the EM and hadronic energy measurements up to $|\eta| = 4.9$. The muon spectrometer surrounds the calorimeters and is based on three large air-core toroid superconducting magnets with eight coils each. Its bending power ranges from 2.0 to 7.5 T m. It includes a system of precision tracking chambers and fast detectors

---

1ATLAS uses a right-handed coordinate system with its origin at the nominal interaction point in the centre of the detector and the $z$-axis is along the beam direction; the $x$-axis points towards the centre of the LHC ring and the $y$-axis points upwards. The pseudorapidity $\eta$ is defined as $\eta = -\ln(\tan(\theta/2))$, where the polar angle $\theta$ is measured with respect to the $z$-axis. The azimuthal angle, $\phi$, is measured with respect to the $x$-axis. Transverse momentum and energy are defined as $p_T = p \sin \theta$ and $E_T = E \sin \theta$, respectively. The $\Delta R$ distance in $(\eta, \phi)$ space is defined as $\Delta R = \sqrt{(\Delta \eta)^2 + (\Delta \phi)^2}$. 

---
for triggering. A two-level trigger system [22] is used to select events. The first-level trigger is implemented in hardware and uses a subset of the detector information to reduce the accepted rate to at most 75 kHz. This is followed by a software-based high-level trigger (HLT), which has access to full detector granularity and is used to further reduce the event rate to 1 kHz.

This analysis is performed using $pp$ collision data recorded at a centre-of-mass energy of $\sqrt{s} = 13$ TeV with the ATLAS detector in 2015 in the periods when the LHC was operating with 25 ns bunch spacing. Only the periods in which all the subdetectors were operational are considered, resulting in a data sample with a total integrated luminosity of $\mathcal{L} = 3.2$ fb$^{-1}$.

All generated samples are passed through the simulation of the ATLAS detector [23] based on Geant4 [24]. The same offline reconstruction methods used with data events are applied to the simulated events samples. Minimum-bias events generated by Pythia 8 [25] are used to simulate multiple $pp$ interactions in the same and nearby bunch crossings (pile-up). The simulated pile-up events are reweighted to reproduce the luminosity spectrum in the data.

Electroweak $t$-channel single-top-quark production can be simulated in different schemes concerning the treatment of the initial $b$-quark. In the five-flavour scheme (5FS) the $b$-quarks are treated massless and the LO Feynman diagram is represented by the $2 \rightarrow 2$ process with a $b$ quark in the initial state, depicted in figure 1. In the four-flavour scheme (4FS), the PDFs only contain parton distributions for the quarks lighter than the $b$-quark and therefore the LO Feynman diagram is represented by a $2 \rightarrow 3$ process including the $g \rightarrow b\bar{b}$ splitting in the initial state. In this scheme, the $b$-quarks are treated massive.

Signal $t$-channel single-top-quark events are generated in the 4FS using the Powheg-Box V1 (r2556) [26, 27] generator. Events are generated with the fixed four-flavour PDF set CT10f4 [12] and the renormalisation and factorisation scales, $\mu_r$, and, $\mu_f$, are set following the recommendation given in ref. [26]. Top quarks are decayed at LO using MadSpin to preserve all spin correlations. The parton shower, hadronisation, and the underlying event are modelled using the Pythia 6 (v6.428) [28] generator and the Perugia2012 set of tuned parameters (P2012 tune) [29]. In order to study effects of the choice of parton-shower model, the same events are showered using Herwig++ (v.2.7.1) [30] and the energy-extrapolated underlying event set of tuned parameters (UE-EE-5 tune) [31]. A second NLO generator capable of generating $t$-channel single-top-quark events in the 4FS is MadGraph5_aMC@NLO [32] (v2.2.2). Samples are generated using the CT10f4 PDF set and $\mu_r$ and $\mu_f$ are set to be the same as those implemented in Powheg-Box. Again, the top quarks produced in the ME are decayed using MadSpin to preserve all spin correlations. The events are showered using Herwig++ (v.2.7.1) and the UE-EE-5 tune. For the generation of SM single top-quarks in the $Wt$ and the $s$-channel ($t\bar{b}+\bar{t}b$) the Powheg-Box V1 (r2819) generator [33, 34] with the CT10 PDF set is used. Samples of $t\bar{t}$ events are generated with the Powheg-Box V2 (r3026) [35] and the CT10 PDF set. The $h_{\text{damp}}$ parameter, which controls the $p_T$ of the first additional emission beyond the Born configuration, where its main effect is to regulate the high-$p_T$ emission against which the $t\bar{t}$ system recoils, is set to the top-quark mass. The parton shower, hadronisation, and the underlying event are added using Pythia 6 and the P2012 tune.

All top-quark processes are generated assuming a top-quark mass of 172.5 GeV. The top quark is set to decay exclusively to $t \rightarrow Wb$, and the EvtGen v1.2.0 program [36] is used to model bottom- and charm-hadron decays.
To model the $W$+jets and $Z$+jets background, the SHERPA v2.2.0 [37] generator is used. Matrix elements are calculated for up to two partons at NLO and up to four partons at LO using the Comix [38] and OpenLoops [39] ME generators and merged with the SHERPA parton shower [40] using the ME+PS@NLO prescription [41]. The NNPDF 3.0 PDF set [42] is used in conjunction with dedicated parton-shower tuning developed by the SHERPA authors.

Diboson events, denoted $VV$, are also simulated using the SHERPA v2.1.1 generator. Matrix elements contain all diagrams with four electroweak vertices. They are calculated for zero partons at NLO and up to three partons at LO using the same methodology as for $W/Z+$jets production. The CT10 PDF set is used in conjunction with dedicated parton-shower tuning developed by the SHERPA authors.

The only background for which no simulated events are used is the multijet background. Multijet events may be selected if a jet is misidentified as an isolated lepton ("fake" lepton) or if a non-prompt lepton from a hadronic decay appears to be isolated. In the electron channel, the matrix method is used, while in the muon channel, the so-called ‘anti-muon’ method is employed to estimate the multijet background [43]. More details are given in section 5.

3 Object reconstruction

In this section, the reconstruction and selection of electrons, muons, jets and $E_T^{\text{miss}}$ is described.

Electron candidates are defined as clusters of energy deposits in the electromagnetic calorimeter associated with a well-measured track fulfilling several quality requirements [44, 45]. They are required to satisfy $p_T > 30$ GeV and $|\eta_{\text{clus}}| < 2.47$, where $\eta_{\text{clus}}$ is the pseudorapidity of the cluster of energy deposits in the calorimeter. Electron candidates in the calorimeter barrel-endcap transition region $1.37 < |\eta_{\text{clus}}| < 1.52$ are excluded. Isolation criteria are applied to reduce background events, in which a hadronic jet is misidentified as a prompt electron or electrons from the decay of heavy quarks. The criteria are optimised such that by adjusting the isolation threshold the selection efficiency of the isolation criteria is uniform across $\eta$. It increases from 90 % for $p_T = 25$ GeV to 99 % for $p_T = 60$ GeV. The $p_T$ of all tracks within a cone of size $\Delta R = \sqrt{\Delta\eta^2 + \Delta\phi^2} = 0.3$ around the electron direction, excluding the track belonging to the electron candidate (track isolation), is restricted to be below a threshold depending on the electron $p_T$. In addition, calorimeter isolation in a cone size of 0.2 around the electron is required [46].

Muon candidates are reconstructed by matching track segments or complete tracks in the muon spectrometer with inner detector tracks. The candidates are required to have a transverse momentum $p_T > 25$ GeV and to be in the pseudorapidity region $|\eta| < 2.5$. Additional requirements on the transverse impact parameter significance of $|d_0/\sigma_{d_0}| < 3$ and on the longitudinal impact parameter ($z_0$) of $|z_0 \sin \theta| < 0.5$ mm are imposed. Isolation criteria similar to those for electron candidates are imposed.

Jets are reconstructed using the anti-$k_t$ algorithm [47] with a radius parameter of 0.4. They are calibrated using a combination of an energy- and $\eta$-dependent simulation-based scheme and a scheme based on data [48]. Only jets with $p_T > 30$ GeV and $|\eta| < 3.5$ are accepted. The rapidity range is determined using a $W$+jets-dominated validation region and defined by requiring good agreement between simulated and measured data.
If any jet is close to an electron, with $\Delta R < 0.2$, the closest jet is removed, as in these cases the jet and the electron are very likely to correspond to the same physical object. Remaining electron candidates overlapping with jets within $\Delta R < 0.4$ are subsequently rejected. To reduce contributions from muons which stem from heavy-flavour decays inside a jet, muons are removed if they are separated from the nearest jet by $\Delta R < 0.4$. However, jets with fewer than three tracks and separated from a muon by $\Delta R < 0.4$ are removed to reduce fake jets from muons depositing a large fraction of their energy in the calorimeters.

To discriminate between jets from the hard-scatter process and those from pile-up, a discriminant called the jet vertex tagger (JVT) [49] is constructed from tracking and vertexing information using a two-dimensional likelihood method. The JVT variable is required to be larger than 0.64 for the jets with $p_T < 50\text{ GeV}$ and $|\eta| < 2.4$, corresponding to 92% efficiency and 2% misidentification rate.

In this analysis, a $b$-tagging algorithm based on boosted decision trees which is optimised to reject $c$-quark jets as well as light-quark jets is used. The $b$- and $c$-tagging efficiencies, and the mistag rate for the taggers, are measured using the methods described in refs. [50, 51]. The $b$-tagging algorithm has an efficiency of about 60% for $b$-jets in simulated $t\bar{t}$ events, while 0.06% of light-quark jets and 4.7% of $c$-quark jets are mistagged as $b$-quark jets. The algorithm can only be applied to jets within the coverage of the ID, i.e. $|\eta| < 2.5$.

The magnitude of the missing transverse momentum vector is defined as $E_T^{\text{miss}} = |E_T^{\text{miss}}|$, where $E_T^{\text{miss}}$ is calculated using the calibrated three-dimensional calorimeter energy clusters associated with the selected jets together with either the calibrated calorimeter energy cluster associated with an electron or the $p_T$ of a muon track (hard components). Contributions from soft particles, not associated with these identified particles, are accounted for using tracks associated to the vertex but not associated with a jet, electron, or muon (soft components).

4 Event selection

Events are considered only if they are accepted by at least one of two single-muon or single-electron triggers [52]. Events in the electron channel are triggered by a calorimeter cluster matched to a track, and the trigger electron object is required to have either $E_T > 60\text{ GeV}$ or $E_T > 24\text{ GeV}$ and satisfy isolation criteria. Events in the muon channel are triggered by either requiring an isolated muon with $p_T > 20\text{ GeV}$ or requiring a muon with $p_T > 50\text{ GeV}$.

Only events containing exactly one isolated charged lepton (electron or muon) with $p_T > 30\text{ GeV}$ and $|\eta| < 2.5$ are accepted. Candidate events must have exactly two jets satisfying the criteria described in section 3. Jets reconstructed in the range $2.75 < |\eta| < 3.5$, covering the endcap-forward calorimeter transition region, must have $p_T > 35\text{ GeV}$. At least one of the selected jets is required to be identified ($b$-tagged) as a $b$-jet.

In order to reduce the number of multijet background events, which are characterised by low $E_T^{\text{miss}}$ and low $W$-boson transverse mass\(^2\) $m_T(E_T^{\text{miss}})$, the event selection requires $E_T^{\text{miss}} > 30\text{ GeV}$ and $m_T(E_T^{\text{miss}}) > 50\text{ GeV}$. To further suppress the multijet background a requirement on the $p_T$ of

\(^2\) The $W$-boson transverse mass is defined as: $m_T(E_T^{\text{miss}}) = \sqrt{2p_T(t)E_T^{\text{miss}} - \vec{p}_T(t) \cdot E_T^{\text{miss}}}$, where $\vec{p}_T(t)$ denotes the transverse momentum of the electron or muon and $p_T(t)$ its modulus.
the charged lepton and the azimuthal angle between the charged lepton and jet is applied:
\[ p_T(\ell) > \max \left( 30 \text{GeV}, 40 \text{GeV} \cdot \frac{\left| \Delta \phi (j_1, \ell) \right|}{\pi} \right), \] (4.1)

where \( \ell \) denotes the identified charged lepton and \( j_1 \) the reconstructed jet with the highest \( p_T \).

Contributions from processes with two isolated leptons in the final state are suppressed by rejecting any event with an additional electron or muon as defined above satisfying \( p_T > 10 \text{GeV} \).

Three kinematic regions are defined in this analysis, all three being subject to the same event selection requiring one electron or muon, missing transverse momentum and one or two \( b \)-tagged jets:

- The signal region (SR) is defined by using the default \( b \)-tagging requirement and selecting exactly one \( b \)-tagged jet.
- The \( W \)-boson validation region (\( W \) + jets VR) requires exactly one \( b \)-tagged jet, but with a less stringent \( b \)-tagging requirement with a \( b \)-tagging efficiency of 85\%. Events contained in the SR are rejected. The validation region is defined such, that the composition of the resulting sample is dominated by \( W \) + jets production with a purity of 77\% and the same reconstruction of the top-quark kinematics can be used as in the signal region, in order to check the modelling of kinematic variables.
- Events in the \( t \bar{t} \) validation region (\( t \bar{t} \) VR) are required to have exactly three jets of which exactly two are \( b \)-tagged jets using the default \( b \)-tagging requirement. This validation region is highly enriched in \( t \bar{t} \) events with a purity of 85\%.

### 5 Background estimation

For all background processes, except the multijet background, the number of expected events are obtained from Monte Carlo (MC) simulation scaled to the theoretical cross-section predictions. The associated production of an on-shell \( W \) boson and a top quark (\( Wt \)) has a predicted production cross-section of 71.1 pb [15] calculated at approximate NNLO accuracy. Predictions of the \( s \)-channel production are calculated at NLO using the same methodology as for the \( t \)-channel production and yield a cross-section of 10.3 pb. The predicted \( t \bar{t} \) cross-section is \( \sigma_{t \bar{t}} = 831.8 \) pb. It has been calculated at NNLO in QCD including resummation of next-to-next-to-leading logarithmic (NNLL) soft gluon terms with top++2.0 [53–58]. All quoted cross-sections are given for \( m_{\text{top}} = 172.5 \) GeV. The inclusive cross-sections of \( W \) + jets and \( Z \) + jets production are calculated at NNLO with FEWZ [59]. Diboson events are normalised to the NLO cross-section provided by the \textsc{Sherpa} generator.

The matrix method [43] is used to determine the multijet background in the electron channel. This method estimates the number of multijet background events in the signal region by applying efficiency factors to the number of events passing the signal tight and a loose lepton selection, the former selection being a subset of the latter. The number of multijet events \( N_{\text{fake}}^{\text{light}} \) passing the signal requirements can be expressed as

\[ N_{\text{fake}}^{\text{light}} = \frac{\epsilon_{\text{fake}}}{\epsilon_{\text{real}} - \epsilon_{\text{fake}}} \cdot (N_{\text{loose}}^{\text{light}} - N_{\text{fake}}^{\text{light}}), \] (5.1)
where $\epsilon_{\text{real}}$ and $\epsilon_{\text{fake}}$ are the efficiencies for real and fake loose leptons being selected as tight leptons, $N_{\text{loose}}$ is the number of selected events in the loose sample, and $N_{\text{tight}}$ is the number of selected events in the signal sample. The fake-lepton efficiencies are determined from a data sample dominated by non-prompt and fake-lepton background events. This sample is selected by requiring exactly one loose lepton and low $E_T^{\text{miss}}$ as well as low $m_T^{\ell_1(E_T^{\text{miss}})}$. The real-lepton efficiencies are also estimated from collision data using a “tag-and-probe” method in $Z \to \ell\ell$ events.

Multijet-background events containing non-prompt muons are modelled with a sample of events enriched in non-isolated muons [43]. Most of these events originate from $b$-hadron or $c$-hadron decays in jets. These events pass the same kinematic requirements as the events of the signal sample. Only some of the muon identification cuts are modified, ensuring that there is no overlap with the signal selection. The normalisation is determined using a binned maximum-likelihood fit.

The fit is performed to the observed data in the $m_T^{\ell_1(E_T^{\text{miss}})}$ distribution after applying all selection criteria, except the requirement on $m_T^{\ell_1(E_T^{\text{miss}})}$. The multijet template is fit together with templates derived from MC simulation for all other processes. The rate uncertainties are accounted for in the fitting process in the form of additional constrained nuisance parameters. For the purpose of this fit, three different template distributions are used. One template is built from simulated $W$+jets events, one consists of events from $t\bar{t}$ and single top-quark production, and one consists of contributions from $Z$+jets and $VV$ production. As the shape of the joint template of $Z$+jets and $VV$ events is very similar to that of $W$+jets events, the rates are fixed in the fitting process.

The estimated event rates obtained from the binned maximum-likelihood fit for the combined contributions of $W$+jets, $t\bar{t}$ and single top-quark production are not used in the later analysis and are only applied to scale the respective processes in order to check the modelling of the kinematic distributions. For the neural-network training, as well as for the final statistical analysis, the normalisation for all but the multijet background is taken from MC simulations scaled to their respective cross-section predictions.

In the signal region, 34459 events in the $\ell^+$ channel and 31056 events in the $\ell^-$ channel are observed in data, while the expected SM background amounts to 33600 ± 2600 events and 30200 ± 2300 events, respectively. The quoted uncertainties are statistical uncertainties and the uncertainty in the number of multijet events. Table 1 summarises the event yields in the signal region for each of the background processes considered together with the event yields for the signal process. The yields are calculated using the acceptance from MC samples normalised to their respective theoretical cross-sections including the (N)NLO $K$ factors.

In the following, the electron and muon channel are combined for all figures and fits. Different processes are also grouped together in the following way. The top-quark background consists of all background processes that include the production of top quarks. These processes are $t\bar{t}$ production and single top-quark production in the $Wt$ and $t\bar{b}+\bar{t}b$ channel. The $W$+jets process describes the production of a real $W$ boson in association with jets, while the production of a $Z$ boson or two vector bosons $VV$ in association with jets are grouped together to $Z$, $VV$+jets. Finally, multijets represents events with a fake lepton originating from multijet production.
<table>
<thead>
<tr>
<th>Process</th>
<th>$\ell^+$ channel</th>
<th>$\ell^-$ channel</th>
</tr>
</thead>
<tbody>
<tr>
<td>$tq$</td>
<td>$4200 \pm 170$</td>
<td>$8 \pm 3$</td>
</tr>
<tr>
<td>$\bar{t}q$</td>
<td>$5 \pm 2$</td>
<td>$2710 \pm 140$</td>
</tr>
<tr>
<td>$t\bar{t}$</td>
<td>$13100 \pm 790$</td>
<td>$13100 \pm 790$</td>
</tr>
<tr>
<td>$Wt$</td>
<td>$1640 \pm 110$</td>
<td>$1640 \pm 110$</td>
</tr>
<tr>
<td>$t\bar{b}+\bar{t}b$</td>
<td>$298 \pm 25$</td>
<td>$199 \pm 18$</td>
</tr>
<tr>
<td>$W^+ + \text{jets}$</td>
<td>$10500 \pm 2200$</td>
<td>$\leq 1$</td>
</tr>
<tr>
<td>$W^- + \text{jets}$</td>
<td>$&lt; 1$</td>
<td>$8730 \pm 1800$</td>
</tr>
<tr>
<td>$Z, VV + \text{jets}$</td>
<td>$1530 \pm 320$</td>
<td>$1410 \pm 300$</td>
</tr>
<tr>
<td>Multijets</td>
<td>$2400 \pm 1200$</td>
<td>$2400 \pm 1200$</td>
</tr>
<tr>
<td>Total expected</td>
<td>$33600 \pm 2600$</td>
<td>$30200 \pm 2300$</td>
</tr>
<tr>
<td>Data observed</td>
<td>$34459$</td>
<td>$31056$</td>
</tr>
</tbody>
</table>

Table 1. Predicted and observed event yields for the signal region. The quoted uncertainties include uncertainties in the theoretical cross-sections, in the number of multijet events, and the statistical uncertainties.

6 Discrimination of signal and background events

To separate $t$-channel single-top-quark signal events from the background, several kinematic variables are combined into one discriminant by employing a neural network [18, 60]. A large number of potential input variables were studied, including kinematic variables of the identified physics objects, as well as variables obtained from the reconstruction of the $W$ boson and the top quark. A detailed description of the algorithm including the reconstruction of the longitudinal component of the neutrino momentum is given in ref. [19]. As a compromise between the discrimination power and the need for a manageable number of variables, the ten highest-ranking variables are chosen and are listed in table 2. The two most discriminating variables are the reconstructed top-quark mass $m(lb)$ and the invariant mass of the two jets $m(jb)$. Figures 2(a) and 2(b) show the $m(lb)$ and $m(jb)$ distributions (normalised to unit area) in the SR for the $\ell^+$ channel. Figures 2(c)–2(f) show the $m(lb)$ and $m(jb)$ distributions in the $W+\text{jets}$ VR and $t\bar{t}$ VR for the $\ell^+$ channel. In the $t\bar{t}$ VR the $b$-jet used to calculate $m(lb)$ and $m(jb)$ is the $b$-jet with the higher $p_T$. The distributions from the different processes, apart from the multijet background in the electron channel, are normalised to match the number of observed events. In the case of the electron channel, the relative contribution of each simulated process is estimated using its predicted cross-section. In the case of the muon channel, the distributions are normalised to the expected number of events obtained from the fit to the $m_T(lE_T^{\text{miss}})$ distributions described in section 5. Satisfactory agreement is seen between the data and the predictions.

The NN infrastructure consists of one input node for each input variable plus one bias node, an arbitrary user-defined number of hidden nodes, and one output node which gives a continuous output in the interval $[0, 1]$. In this specific case, 15 nodes in the hidden layer are used and equal numbers of signal and background events were used in the training, where the different background processes are weighted according to their expected number of events. The shapes of the resulting NN discriminant distributions ($O_{NN}$) for the signal and the two largest backgrounds are shown in figure 3 together with the data distributions compared to the predictions in the two validation regions. Good agreement between the predicted and observed distributions is found.
<table>
<thead>
<tr>
<th>Variable</th>
<th>Definition</th>
</tr>
</thead>
<tbody>
<tr>
<td>$m(\ell b)$</td>
<td>top-quark mass reconstructed from the charged lepton, neutrino, and $b$-tagged jet</td>
</tr>
<tr>
<td>$m(jb)$</td>
<td>invariant mass of the $b$-tagged and untagged jet</td>
</tr>
<tr>
<td>$m_T(TEmiss)$</td>
<td>transverse mass of the reconstructed $W$ boson</td>
</tr>
<tr>
<td>$</td>
<td>\eta(j)</td>
</tr>
<tr>
<td>$m(\ell b)$</td>
<td>invariant mass of the charged lepton ($\ell$) and the $b$-tagged jet</td>
</tr>
<tr>
<td>$\eta(\ell)$</td>
<td>rapidity of the reconstructed $W$ boson</td>
</tr>
<tr>
<td>$\Delta R(\ell b, j)$</td>
<td>$\Delta R$ of the reconstructed top quark and the untagged jet</td>
</tr>
<tr>
<td>$\cos(\theta^* (\ell, j))$</td>
<td>cosine of the angle $\theta^*$ between the charged lepton and the untagged jet in the rest frame of the reconstructed top quark</td>
</tr>
<tr>
<td>$\Delta R_T(\ell b, j)$</td>
<td>$\Delta R_T$ of the reconstructed top quark and the untagged jet</td>
</tr>
<tr>
<td>$\Delta R(\ell, j)$</td>
<td>$\Delta R$ of the charged lepton and the untagged jet</td>
</tr>
</tbody>
</table>

Table 2. The ten variables that are used in the training of the neural network ordered by their discriminating power as determined by Neurobayes [19, 60].

7 Systematic uncertainties

Systematic uncertainties in the normalisation of the individual backgrounds and in the signal acceptance as well as uncertainties in the shape of the NN discriminant distribution of the individual predictions affect the individual top-quark and top-antiquark cross-section measurements and their ratio. The uncertainties are split into the following categories.

Reconstruction efficiency and calibration uncertainties. Systematic uncertainties affecting the reconstruction and energy calibration of jets, electrons, and muons are propagated through the analysis. The dominant source for this measurement arises from the jet energy scale (JES) calibration, including the modelling of pile-up, and from the $b$-jet tagging efficiencies.

The uncertainties due to lepton reconstruction, identification and trigger efficiencies are estimated using tag-and-probe methods in $Z \rightarrow \ell\ell$ events. Correction factors are derived to match the simulation to observed distributions in collision data and associated uncertainties are estimated. To estimate uncertainties in the lepton momentum scale and resolution, also $Z \rightarrow \ell\ell$ events are used [61–63]. The lepton-charge misidentification is estimated with simulated events and found to be below 0.1%, see table 1. The uncertainty on the lepton-charge misidentification is evaluated and found to be negligible.

Several components of the JES uncertainty are considered [64, 65]. Uncertainties derived from different dijet-$p_T$-balance measurements as well as uncertainties associated with in-situ calibration techniques are considered. Furthermore, the presence of nearby jets and the modelling of pile-up affects the jet calibration. The uncertainty in the flavour composition covers effects due to the difference in quark-gluon composition between the jets used in the calibration and the jets used in this analysis. Also an uncertainty due to limited knowledge of the calorimeter response to light-quark jets and gluon jets is considered. Finally, the JES uncertainty is estimated for $b$-quark jets by varying the modelling of $b$-quark fragmentation. The uncertainty in the jet energy resolution is modelled by varying the $p_T$ of the jets according to the systematic uncertainties of the
Figure 2. Distributions of the two most discriminating variables, (left) the reconstructed top-quark mass $m(lvb)$ and (right) the invariant mass of the jet pair $m(jb)$, for the $\ell^+\nu$ channel. In the $t\bar{t}$ VR the $b$-jet used to calculate $m(lvb)$ and $m(jb)$ is the $b$-jet with the higher $p_T$. (a)-(b): signal and background distributions normalised to unit area. (c)-(f): observed distributions in the $W$+jets VR and the $t\bar{t}$ VR compared to the model obtained from simulated events. The simulated distributions are normalised to match the number of observed events as described in the main text. The hatched and grey error bands represent the uncertainty in the number of multijet events and the uncertainty due to the size of the MC samples. The ratio of observed to predicted (Pred.) number of events in each bin is shown in the lower distributions. Events in the overflow are contained in the last bin.
Figure 3. Distributions of the NN discriminant $O_{NN}$ (left) for the $\ell^+\ell^-$ channel and (right) for the $\ell^-\ell^+$ channel. (a)-(b): signal and background distributions normalised to unit area. (c)-(f): observed distributions in the $W$+jets VR and the $t\bar{t}$ VR compared to the model obtained from simulated events. The simulated distributions are normalised to match the number of observed events as described in the main text. The hatched and grey error bands represent the uncertainty in the number of multijet events and the uncertainty due to the size of the MC samples. The ratio of observed to predicted (Pred.) number of events in each bin is shown in the lower distributions.
resolution measurement [66]. The effect of uncertainties associated with the JVT requirement is also considered.

The impact of a possible miscalibration on the soft track component of $E_T^{\text{miss}}$ is derived from data-MC comparisons of the $p_T$ balance between the hard and soft $E_T^{\text{miss}}$ components.

Since the analysis makes use of $b$-tagging, the uncertainties in the $b$- and $c$-tagging efficiencies and the mistag rate are taken into account. These uncertainties were determined using $\sqrt{s} = 8$ TeV data as described in ref. [51] for $b$-jets and ref. [50] for $c$-jets and light jets, with additional uncertainties to account for the presence of the newly added Insertable B-Layer and the extrapolation to $\sqrt{s} = 13$ TeV.

**Monte Carlo generators.** Systematic effects from MC modelling of the signal and the $t\bar{t}$ background process are either estimated by comparing different generators or by comparing parameter variations in the POWHEG-BOX + PYTHIA 6 setup. The POWHEG-BOX + HERWIG++ sample is used for parton shower and hadronisation modelling studies, while MadGraph5_aMC@NLO + HERWIG++ is used for studies of the NLO-matching method. Variations of the amount of additional radiation are studied by changing $\mu_t$ and $\mu_h$ and the scales in the parton shower simultaneously. In these samples, an up-variation of $\mu_t$ and $\mu_h$ by a factor of two is combined with the P2012 tune with lower radiation (P2012radLo tune) than the nominal P2012 set, and a variation of both scales by a factor of one half is combined with the P2012 tune with higher radiation (P2012radHi tune). In the case of the up-variation of $t\bar{t}$ production, the $h_{\text{damp}}$ parameter is also changed and set to two times the top-quark mass [67].

The uncertainty in the pile-up reweighting as well as the statistical uncertainties of the simulated event samples are also taken into account.

**PDF.** The systematic uncertainties in the signal and background acceptance related to the parton distribution functions are taken into account for all single-top-quark processes and $t\bar{t}$ production. The procedure follows the updated PDF4LHC recommendation [68] by using the 30 eigenvectors of the PDF4LHC15 NLO PDF set. The events are reweighted according to each of the PDF uncertainty eigenvectors. In addition, the acceptance difference between PDF4LHC15 and CT10 is considered, since the latter PDF set is used in the MC samples and is not covered by the uncertainty obtained with PDF4LHC15 PDF sets.

**Background normalisation.** The $t\bar{t}$, Wt and $t\bar{b}$ backgrounds are normalised to their theory predictions, where a combined uncertainty of 6% is derived from the weighted average of the individual uncertainties. The PDF- and $\alpha_s$-induced uncertainties for the $t\bar{t}$ process are calculated using the PDF4LHC prescription [9] with the MSTW2008 68 % CL NNLO, CT10 NNLO and NNPDF PDF sets and added in quadrature to the uncertainty due to the scale, leading to a total uncertainty of 5.5%. The uncertainty in the Wt cross-section, calculated at approximate NNLO, is the sum in quadrature of the effects of the PDF uncertainty obtained using the MSTW2008 68 % CL NNLO PDF sets and the scale uncertainty, and is found to be 5.4%. The $s$-channel production cross-section is calculated at NLO with a total uncertainty of 3.8%.

For the W+jets and Z+jets backgrounds, an uncertainty of 21% is assigned. This uncertainty is estimated based on parameter variations in the generation of the SHERPA samples. It was found that correlated variations of the factorisation and renormalisation scales have the biggest
impact on the kinematic distributions and produces change covering the unfolded data and their uncertainties [69].

Diboson processes have an uncertainty of 6% in the inclusive cross-section including uncertainties on the choice of the factorisation and renormalisation scales and the PDF uncertainty.

The multijet background estimate has an uncertainty of 50%, based on comparisons of the rates obtained using alternative methods described in previous analyses [19, 43, 70].

Luminosity and beam energy. The uncertainty in the integrated luminosity is ±2.1%. It is derived, following a methodology similar to that detailed in refs. [71] and [72], from a calibration of the luminosity scale using x–y beam-separation scans performed in August 2015. Given the level of precision of the measurement the uncertainty in the beam energy is negligible for this analysis.

All systematic uncertainties discussed above cause variations in the signal acceptance, the background rates and the shape of the NN discriminant distribution. Both the rate and shape uncertainties are taken into account by generating correlated pseudo-experiments as detailed in the next section.

8 Statistical analysis

To extract the top-quark and top-antiquark inclusive cross-sections, a binned maximum-likelihood fit to the NN discriminant distribution is performed in the $\ell^+$ channel and $\ell^-$ channel, treating $t$-channel top-quark and $t$-channel top-antiquark production as independent processes. The likelihood function used is built from Poisson probability terms and includes Gaussian priors to constrain the rates of the $W$+jets and top-quark background processes; more details are given in ref. [19].

The fit parameters of the likelihood function are scale factors, $\beta_i$, that multiply the expected value of the number of events, $\nu_i$, for each fitted process $i$. The background normalisation constraints are 21% for $W$+jets production, and 6% for top-quark backgrounds ($t\bar{t}$, $Wt$ and $t\bar{b} + \bar{t}b$), while the contributions from $Z$+jets, $VV$, and multijet processes are fixed to their predictions. The fitted rates of the $W$+jets background and the top-quark backgrounds are mainly driven by the background-dominated region with low $O_{NN}$ values. The cross-section ratio is subsequently computed as $R_t = \sigma(tq)/\sigma(\bar{t}q)$.

The fit finds the minimum of the negative log-likelihood function for the parameter values shown in table 3. Figure 4 compares the observed NN discriminant distributions to the compound model of signal and backgrounds with each contribution normalised to the fit results from table 3. The three most discriminating variables are presented in figure 5. The model agrees with the data, within uncertainties.

The systematic uncertainties in the cross-section measurements are determined from pseudo-experiments which vary the signal acceptance, the background rates, and the shape of the NN discriminant. By using samples of simulated events with variations reflecting the sources of systematic uncertainty, all of the effects are estimated and the pseudo-experiments are varied accordingly. Rate and shape uncertainties are treated in a correlated way. All systematic uncertainties apart from those related to the Monte Carlo statistics are also treated in a correlated way between the $\ell^+$ channel and the $\ell^-$ channel. Table 4 shows the contributions to the total uncertainty in the inclusive cross-section measurements. The table provides the uncertainties estimated for the observed signal and back-
Table 3. Estimated scale factors, $\hat{\beta}$, and number of events, $\hat{\nu} = \hat{\beta} \cdot \nu$, for the $\ell^+$ and $\ell^-$ channel from the minimisation of the likelihood function. The quoted uncertainties in $\hat{\beta}$ and $\hat{\nu}$ include the statistical uncertainty and the uncertainties from the constraints on the background normalisation as used in the likelihood function.

<table>
<thead>
<tr>
<th>Process</th>
<th>$\hat{\beta}$</th>
<th>$\hat{\nu}(\ell^+)$</th>
<th>$\hat{\nu}(\ell^-)$</th>
</tr>
</thead>
<tbody>
<tr>
<td>$tq$</td>
<td>$1.15 \pm 0.03$</td>
<td>$4,840 \pm 140$</td>
<td>$-$</td>
</tr>
<tr>
<td>$\bar{t}q$</td>
<td>$1.12 \pm 0.05$</td>
<td>$-$</td>
<td>$3,040 \pm 130$</td>
</tr>
<tr>
<td>$t\bar{t}, Wt, t\bar{b} + \bar{t}b$</td>
<td>$0.91 \pm 0.03$</td>
<td>$13,700 \pm 510$</td>
<td>$13,600 \pm 510$</td>
</tr>
<tr>
<td>$W^+ \text{+ jets}$</td>
<td>$1.13 \pm 0.05$</td>
<td>$12,000 \pm 550$</td>
<td>$-$</td>
</tr>
<tr>
<td>$W^- \text{+ jets}$</td>
<td>$1.21 \pm 0.06$</td>
<td>$-$</td>
<td>$10,500 \pm 550$</td>
</tr>
<tr>
<td>$Z, VV + \text{jets}$</td>
<td>$-$</td>
<td>$1,530$</td>
<td>$1,410$</td>
</tr>
<tr>
<td>Multijet background</td>
<td>$-$</td>
<td>$2,420$</td>
<td>$-$</td>
</tr>
<tr>
<td>Total estimated</td>
<td>$-$</td>
<td>$34,500 \pm 760$</td>
<td>$31,000 \pm 760$</td>
</tr>
<tr>
<td>Total observed</td>
<td>$-$</td>
<td>$34,459$</td>
<td>$31,056$</td>
</tr>
</tbody>
</table>

Figure 4. NN discriminant distribution (a) for the $\ell^+$ channel and (b) for the $\ell^-$ channel in the SR. The signal and backgrounds are normalised to the fit result and the hatched and grey error bands represent the post-fit uncertainty. The ratio of observed to predicted (Pred.) number of events in each bin is shown in the lower histogram.

9 Cross-section measurement

After performing the binned maximum-likelihood fit to the NN discriminant distribution and estimating the total uncertainty, the inclusive cross-sections of top-quark and top-antiquark production in the $t$-channel are measured to be:

$$\sigma(tq) = 156 \pm 5 \text{ (stat.)} \pm 27 \text{ (syst.)} \pm 3 \text{ (lumi.)} \text{ pb}$$

$$\sigma(\bar{t}q) = 91 \pm 4 \text{ (stat.)} \pm 18 \text{ (syst.)} \pm 2 \text{ (lumi.)} \text{ pb}$$

$$R_t = 1.72 \pm 0.09 \text{ (stat.)} \pm 0.18 \text{ (syst.)}$$
Figure 5. Distributions of the three most important variables (left) for the $\ell^+$ channel and (right) for the $\ell^-$ channel normalised to the fit result. (a)-(b): reconstructed top-quark mass $m(\ell\nu)$. (c)-(d): invariant mass of the jet pair $m(jb)$. (e)-(f): transverse mass of the $W$ boson $m_T(E_T^{miss})$. The hatched and grey error bands represents the post-fit uncertainty. The ratio of observed to predicted (Pred.) number of events in each bin is shown in the lower histogram. Events beyond the x-axis range are included in the last bin.
<table>
<thead>
<tr>
<th>Source</th>
<th>$\frac{\Delta \sigma(tq)}{\sigma(tq)}$ [%]</th>
<th>$\frac{\Delta \sigma(\bar{t}q)}{\sigma(\bar{t}q)}$ [%]</th>
<th>$\frac{\Delta R_t}{R_t}$ [%]</th>
</tr>
</thead>
<tbody>
<tr>
<td>Data statistics</td>
<td>± 2.9</td>
<td>± 4.1</td>
<td>± 5.0</td>
</tr>
<tr>
<td>Monte Carlo statistics</td>
<td>± 2.8</td>
<td>± 4.2</td>
<td>± 5.1</td>
</tr>
</tbody>
</table>

**Reconstruction efficiency and calibration uncertainties**

- Muon uncertainties: ± 0.8 ± 0.9 ± 1.0
- Electron uncertainties: < 0.5 ± 0.5 ± 0.7
- JES: ± 3.4 ± 4.1 ± 1.2
- Jet energy resolution: ± 3.9 ± 3.1 ± 1.1
- $E_T^{\text{miss}}$ modelling: ± 0.9 ± 1.2 < 0.5
- $b$-tagging efficiency: ± 7.0 ± 6.9 < 0.5
- $c$-tagging efficiency: < 0.5 < 0.5 < 0.5
- Light-jet tagging efficiency: < 0.5 < 0.5 < 0.5
- Pile-up reweighting: ± 1.5 ± 2.2 ± 3.8

**Monte Carlo generators**

- **$tq$ parton shower generator** ± 13.0 ± 14.3 ± 1.9
- **$tq$ NLO matching** ± 2.1 ± 0.7 ± 2.8
- **$tq$ radiation** ± 3.7 ± 3.4 ± 3.7
- **$t\bar{t}$, $Wt$, $t\bar{b}$ + $\bar{t}b$ parton shower generator** ± 3.2 ± 4.4 ± 1.2
- **$t\bar{t}$, $Wt$, $t\bar{b}$ + $\bar{t}b$ NLO matching** ± 4.4 ± 8.6 ± 4.6
- **$t\bar{t}$, $Wt$, $t\bar{b}$ + $\bar{t}b$ radiation** < 0.5 ± 1.1 ± 0.7
- **PDF** ± 0.6 ± 0.9 < 0.5

**Background normalisation**

- Multijet normalisation: ± 0.3 ± 2.0 ± 1.8
- Other background normalisation: ± 0.4 ± 0.5 < 0.5
- Luminosity: ± 2.1 ± 2.1 < 0.5

**Total systematic uncertainty** ± 17.5 ± 20.0 ± 10.2
**Total uncertainty** ± 17.8 ± 20.4 ± 11.4

Table 4. List of systematic uncertainties contributing to the total uncertainty in the measured values of $\sigma(tq)$, $\sigma(\bar{t}q)$, and $R_t = \sigma(tq)/\sigma(\bar{t}q)$. The estimation of the systematic uncertainties has a statistical uncertainty of 0.3%. Uncertainties contributing less than 0.5% are marked with “< 0.5”.

assuming a top-quark mass of $m_{\text{top}} = 172.5$ GeV. Figure 6 compares the measured value of $R_t$ to NLO predictions [7] obtained with Hathor [8] using different PDF sets. PDF sets are available from various groups worldwide: CTEQ [12, 73], MSTW2008 [10]/MMHT14 [74], NNPDF [42, 75], JR [76], ABM [77], and HERAPDF [78, 79]. Also, the first PDF set provided by the ATLAS Collaboration is considered [80]. The PDFs provided by the different groups differ in the data used, the value of $\alpha_s$, the values of the quark masses, and the treatment of heavy-quark masses. Other differences concern the way higher-order corrections are implemented, the parametrisation of the PDF fitting-model, the way of treating systematic uncertainties and the criteria for estimating con-
Figure 6. Comparison between observed and predicted values of $R_t = \frac{\sigma_{t\bar{t}}}{\sigma_{tq}}$. Predictions are calculated at NLO precision [7, 8] in the five-flavour scheme and given for different NLO PDF sets. The uncertainty includes the uncertainty in the renormalisation and factorisation scales, as well as the combined internal PDF and $\alpha_s$ uncertainty. The dotted black line indicates the measured value. The combined statistical and systematic uncertainty of the measurement is shown in green, while the statistical uncertainty is represented by the yellow error band. Predictions for all presented PDF sets are within the statistical uncertainty of the measurement.

For the purpose of determining $f_{LV}\cdot |V_{tb}|$, the measured inclusive cross-sections of the $tq$ and the $\bar{t}q$ process are combined, assuming that each uncertainty is 100% correlated between the two channels. The statistical uncertainty of the data and the uncertainty due to the limited size of the MC samples, are treated as uncorrelated. The combined cross-section is calculated to be:

$$\sigma(tq + \bar{t}q) = 247 \pm 6 \text{ (stat.)} \pm 45 \text{ (syst.)} \pm 5 \text{ (lumi.) pb}$$

$$= 247 \pm 46 \text{ pb}.$$

To estimate the dependence of the measured cross-sections on the assumed top-quark mass, simulated samples with $m_{\text{top}} = 170 \text{ GeV}$ and $m_{\text{top}} = 175 \text{ GeV}$ are used. The measurement is repeated for each top-quark mass. In table 5, the measured cross-sections and their ratio are given.

Single top-quark production in the $t$-channel proceeds via a $Wtb$ vertex and the measured cross-section is proportional to $(f_{LV}\cdot |V_{tb}|)^2$ as discussed in section 1. The $f_{LV}\cdot |V_{tb}|$ measurement via single top-quark production is independent of assumptions about the number of quark generations or about the unitarity of the CKM matrix. The assumptions made are: $|V_{td}|$ is much bigger than $|V_{ts}|$ and $|V_{ts}|$, which is in agreement with the measurement of $R = \mathcal{B}(t \rightarrow Wb)/\sum_{q=d,s,b} \mathcal{B}(t \rightarrow Wq)$ [81], the top quark decays exclusively into a $W$ boson and a $b$-quark, and the $Wtb$ interaction is a left-
Table 5. Measured values of the cross-sections $\sigma(tq)$, $\sigma(\bar{t}q)$, $\sigma_{\text{tot}}(tq + \bar{t}q)$, and $R_t$ for different simulated top-quark masses. The quoted uncertainties are statistical only.

<table>
<thead>
<tr>
<th>$m_{\text{top}}$ [GeV]</th>
<th>$\sigma(tq)$ [pb]</th>
<th>$\sigma(\bar{t}q)$ [pb]</th>
<th>$\sigma(tq + \bar{t}q)$ [pb]</th>
<th>$R_t$</th>
</tr>
</thead>
<tbody>
<tr>
<td>170.0</td>
<td>156 ± 5</td>
<td>93 ± 4</td>
<td>249 ± 6</td>
<td>1.69 ± 0.09</td>
</tr>
<tr>
<td>172.5</td>
<td>156 ± 5</td>
<td>91 ± 4</td>
<td>247 ± 6</td>
<td>1.72 ± 0.09</td>
</tr>
<tr>
<td>175.0</td>
<td>155 ± 5</td>
<td>92 ± 4</td>
<td>247 ± 6</td>
<td>1.68 ± 0.09</td>
</tr>
</tbody>
</table>

handed weak coupling like that in the SM. A strategy to relax the first two assumptions and account for production and decay of top quarks via $Wts$ and $Wtd$ vertices is delineated in Ref. [82].

The value of $f_{LV} \cdot |V_{tb}|$ is extracted by dividing the measured $\sigma(tq + \bar{t}q) = 247 \pm 46 \text{ pb}$ by its value predicted at NLO, $\sigma^{\text{NLO}}(tq + \bar{t}q) = 217 \pm 10 \text{ pb}$. Changes in $f_{LV} \cdot |V_{tb}|$ also affect $Wt$ and $t\bar{b} + \bar{t}b$ production. However, their contributions are small and their variation does not change the $t$-channel fit result. The result obtained is

$$f_{LV} \cdot |V_{tb}| = 1.07 \pm 0.01 \text{ (stat.)} \pm 0.09 \text{ (syst.)} \pm 0.02 \text{ (theor.)} \pm 0.01 \text{ (lumi.)}$$

The internal uncertainty is 0.09, including the statistical uncertainty, the systematic uncertainties, and the uncertainty in the luminosity. The theoretical uncertainty is 0.02, including scale uncertainties and PDF uncertainties.

Setting $f_{LV} = 1$ as required by the SM, and assuming a uniform prior of one in $|V_{tb}|^2$ in the interval [0, 1] and a Gaussian-shaped likelihood curve for $|V_{tb}|^2$, a Bayesian lower limit giving $|V_{tb}| > 0.84$ at 95 % CL, is obtained.

### 10 Conclusion

A measurement of the $t$-channel single-top-quark and single-top-antiquark production cross-sections is performed in events with a leptonically decaying W boson with 3.2 fb$^{-1}$ of $pp$ collision data at $\sqrt{s} = 13 \text{ TeV}$ recorded with the ATLAS detector at the LHC in 2015. Events are selected by requiring exactly one electron or muon, missing transverse momentum, and two jets with high transverse momentum, exactly one of which is required to be $b$-tagged.

A binned maximum-likelihood fit to neural-network discriminant distributions yields the following cross-sections:

$$\sigma(tq) = 156 \pm 28 \text{ pb},$$
$$\sigma(\bar{t}q) = 91 \pm 19 \text{ pb},$$
$$\sigma(tq + \bar{t}q) = 247 \pm 46 \text{ pb}$$

in agreement with SM predictions. The cross-section ratio of $tq$ and $\bar{t}q$ production is found to be $R_t = 1.72 \pm 0.20$. The coupling at the $Wtb$ vertex is determined to be $f_{LV} \cdot |V_{tb}| = 1.07 \pm 0.09$ and a lower limit on the CKM matrix element is set, giving $|V_{tb}| > 0.84$ at the 95 % CL. These measurements are dominated by systematic uncertainties, from which the uncertainties connected with MC generators are the biggest ones. Further improvements in these generators could lead to smaller expected uncertainties and therefore higher precision in the course of Run 2.
Acknowledgments

We thank CERN for the very successful operation of the LHC, as well as the support staff from our institutions without whom ATLAS could not be operated efficiently.

We acknowledge the support of ANPCyT, Argentina; YerPhI, Armenia; ARC, Australia; BMWF and FWF, Austria; ANAS, Azerbaijan; STFC, Belarus; CNPq and FAPESP, Brazil; NSERC, NRC and CFI, Canada; CERN; CONICYT, Chile; CAS, MOST and NSFC, China; COLCIENCIAS, Colombia; MSMT CR, MPO CR and VSC CR, Czech Republic; DNRF and DNSRC, Denmark; IN2P3-CNRS, CEA-DSM/IRFU, France; GNSF, Georgia; BMBF, HGF, and MPG, Germany; GSRT, Greece; RGC, Hong Kong SAR, China; ISF, I-CORE and Benoziyo Center, Israel; INFN, Italy; MEXT and JSPS, Japan; CNRST, Morocco; FOM and NWO, Netherlands; RCN, Norway; MNiSW and NCN, Poland; FCT, Portugal; MNE/IFA, Romania; MES of Russia and NRC KI, Russian Federation; JINR; MESTD, Serbia; MSSR, Slovakia; ARRS and MIZŠ, Slovenia; DST/NRF, South Africa; MINECO, Spain; SRC and Wallenberg Foundation, Sweden; SERI, SNSF and Cantons of Bern and Geneva, Switzerland; MOST, Taiwan; TAEK, Turkey; STFC, United Kingdom; DOE and NSF, United States of America. In addition, individual groups and members have received support from BCKDF, the Canada Council, CANARIE, CRC, Compute Canada, FQRNT, and the Ontario Innovation Trust, Canada; EPLANET, ERC, ERDF, FP7, Horizon 2020 and Marie Skłodowska-Curie Actions, European Union; Investissements d’avenir Labex and Idex, ANR, Région Auvergne and Fondation Partager le Savoir, France; DFG and AvH Foundation, Germany; Herakleitos, Thales and Aristeia programmes co-financed by EU-ESF and the Greek NSRF; BSF, GIF and Minerva, Israel; BRF, Norway; CERCA Programme Generalitat de Catalunya, Generalitat Valenciana, Spain; the Royal Society and Leverhulme Trust, United Kingdom.

The crucial computing support from all WLCG partners is acknowledged gratefully, in particular from CERN, the ATLAS Tier-1 facilities at TRIUMF (Canada), NDGF (Denmark, Norway, Sweden), CC-IN2P3 (France), KIT/GridKA (Germany), INFN-CNAF (Italy), NL-T1 (Netherlands), PIC (Spain), ASGC (Taiwan), RAL (U.K.) and BNL (U.S.A.), the Tier-2 facilities worldwide and large non-WLCG resource providers. Major contributors of computing resources are listed in ref. [83].

Open Access. This article is distributed under the terms of the Creative Commons Attribution License (CC-BY 4.0), which permits any use, distribution and reproduction in any medium, provided the original author(s) and source are credited.

References


The ATLAS collaboration

145 Department of Physics, Simon Fraser University, Burnaby BC, Canada
146 SLAC National Accelerator Laboratory, Stanford CA, United States of America
147 (a) Faculty of Mathematics, Physics & Informatics, Comenius University, Bratislava; (b) Department of Subnuclear Physics, Institute of Experimental Physics of the Slovak Academy of Sciences, Kosice, Slovak Republic
148 (a) Department of Physics, University of Cape Town, Cape Town; (b) Department of Physics, University of Johannesburg, Johannesburg; (c) School of Physics, University of the Witwatersrand, Johannesburg, South Africa
149 (a) Department of Physics, Stockholm University; (b) The Oskar Klein Centre, Stockholm, Sweden
150 Physics Department, Royal Institute of Technology, Stockholm, Sweden
151 Departments of Physics & Astronomy and Chemistry, Stony Brook University, Stony Brook NY, United States of America
152 Department of Physics and Astronomy, University of Sussex, Brighton, United Kingdom
153 School of Physics, University of Sydney, Sydney, Australia
154 Institute of Physics, Academia Sinica, Taipei, Taiwan
155 Department of Physics, Technion: Israel Institute of Technology, Haifa, Israel
156 Raymond and Beverly Sackler School of Physics and Astronomy, Tel Aviv University, Tel Aviv, Israel
157 Department of Physics, Aristotle University of Thessaloniki, Thessaloniki, Greece
158 International Center for Elementary Particle Physics and Department of Physics, The University of Tokyo, Tokyo, Japan
159 Graduate School of Science and Technology, Tokyo Metropolitan University, Tokyo, Japan
160 Department of Physics, Tokyo Institute of Technology, Tokyo, Japan
161 Tomsk State University, Tomsk, Russia
162 Department of Physics, University of Toronto, Toronto ON, Canada
163 (a) INFN-TIFPA; (b) University of Trento, Trento, Italy
164 (a) TRIUMF, Vancouver BC; (b) Department of Physics and Astronomy, York University, Toronto ON, Canada
165 Faculty of Pure and Applied Sciences, and Center for Integrated Research in Fundamental Science and Engineering, University of Tsukuba, Tsukuba, Japan
166 Department of Physics and Astronomy, Tufts University, Medford MA, United States of America
167 Department of Physics and Astronomy, University of California Irvine, Irvine CA, United States of America
168 (a) INFN Gruppo Collegato di Udine, Sezione di Trieste, Udine; (b) ICTP, Trieste; (c) Dipartimento di Chimica, Fisica e Ambiente, Università di Udine, Udine, Italy
169 Department of Physics and Astronomy, University of Uppsala, Uppsala, Sweden
170 Department of Physics, University of Illinois, Urbana IL, United States of America
171 Instituto de Fisica Corpuscular (IFIC) and Departamento de Fisica Atomica, Molecular y Nuclear and Departamento de Ingeniería Electrónica and Instituto de Microelectrónica de Barcelona (IMB-CNM), University of Valencia and CSIC, Valencia, Spain
172 Department of Physics, University of British Columbia, Vancouver BC, Canada
173 Department of Physics and Astronomy, University of Victoria, Victoria BC, Canada
174 Department of Physics, University of Warwick, Coventry, United Kingdom
175 Waseda University, Tokyo, Japan
176 Department of Particle Physics, The Weizmann Institute of Science, Rehovot, Israel
177 Department of Physics, University of Wisconsin, Madison WI, United States of America
178 Fakultät für Physik and Astronomie, Julius-Maximilians-Universität, Würzburg, Germany
179 Fakultät für Mathematik und Naturwissenschaften, Fachgruppe Physik, Bergische Universität Wuppertal, Wuppertal, Germany
180 Department of Physics, Yale University, New Haven CT, United States of America
181 Yerevan Physics Institute, Yerevan, Armenia
182 Centre de Calcul de l’Institut National de Physique Nucléaire et de Physique des Particules (IN2P3), Villeurbanne, France