Selective Excitation of Terahertz Magnetic and Electric Dipoles in Er$^{3+}$ Ions by Femtosecond Laser Pulses in ErFeO$_3$

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We show that femtosecond laser pulse excitation of the orthoferrite ErFeO$_3$ triggers picosecond- and subpicosecond-dynamics of magnetic and electric dipoles associated with the low energy electronic states of the Er$^{3+}$ ions. These dynamics are readily revealed by using polarization sensitive terahertz emission spectroscopy. It is shown that by changing the polarization of the femtosecond laser pulse one can excite either electric dipole-active or magnetic dipole-active transitions between the Kramers doublets of the $^4I_{15/2}$ ground state of the Er$^{3+}$ ($4f^{11}$) ions. These observations serve as a proof of principle of polarization-selective control of both electric and magnetic degrees of freedom at terahertz frequencies, opening up new vistas for optical manipulation of magnetoelectric materials.

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The coupling of femtosecond laser pulses to magnetic excitations is a heavily debated topic in several areas of contemporary physics, including ultrafast magnetism [1], multiferroics [2,3], spintronics [4–6], and magnonics [7,8]. The results of this fundamental research may have tremendous impact on information storage technologies. Impulsive stimulated Raman scattering (ISRS) offers a proven way to excite magnetic resonances in media by light at the subpicosecond time scale [1]. By choosing the polarization of light or propagation direction, it is possible to attain a selective excitation of a particular resonance mode [9,10]. To date, such a selective excitation of magnetization dynamics was demonstrated only for magnetic dipole-active modes. In this Letter, we show that ISRS can selectively excite not only magnetic dipoles, but also electric dipole-active magnetic resonances, greatly extending the potential for optically encoding information in solids.

To this end, we have conducted terahertz (THz) emission spectroscopy measurements on single crystals of erbium orthoferrite ErFeO$_3$. Er$^{3+}$ ions in ErFeO$_3$ have magnetic and electric-dipole active transitions which have slightly different frequencies lying in the THz range. The magnetic and electric-dipole transitions must be excited by laser pulses with different polarizations as they have different selection rules. Despite extensive investigations of the laser-induced spin dynamics in rare-earth orthoferrites [11–17], to date the laser excitation of the electronic transitions in the rare-earth ions has been mostly ignored.

ErFeO$_3$ has a distorted perovskite crystal structure with $D_{2h}^{16}$ space group. Its unit cell contains four magnetic Fe$^{3+}$ ions forming two antiferromagnetically ordered sublattices with a small canting due to the presence of the Dzyaloshinskii-Moriya interaction. The Néel temperature for the iron sublattices is $T_{\text{N}}^{\text{Fe}} \approx 650$ K. Below $T_1 = 80$ K the magnetic phase has $\Gamma_2$ symmetry with the iron spins oriented along the crystallographic $z$ axis with a canting towards the $x$ axis [see Fig. 1(a)]. Above $T_2 = 95$ K the magnetic phase has the $\Gamma_4$ symmetry with the iron spins oriented along the $x$ axis with a canting towards the $z$ axis [see Fig. 1(b)]. In the temperature interval between $T_1$ and $T_2$ the erbium orthoferrite exhibits a spin reorientation when the iron spins continuously rotate in the $(xz)$ plane. The Er$^{3+}$ ions are in a paramagnetic state above their Néel temperature $T_{\text{N}}^{\text{Er}} \approx 4$ K, being polarized by the exchange interaction with the iron sublattices and forming a canted configuration in the $(xz)$ and $(yz)$ planes in the $\Gamma_3$ and $\Gamma_4$ magnetic phases, respectively [18]. The net magnetic moment of the Er$^{3+}$ ions is always oriented antiparallel with respect to the weak magnetic moment of the Fe$^{3+}$ sublattices and rotates by 90° together with the spin reorientation of the latter (see Fig. 1) [19].

FIG. 1. Arrangement of magnetic moments of the Fe$^{3+}$ and Er$^{3+}$ sublattices of ErFeO$_3$ in the $\Gamma_2$ (a) and $\Gamma_4$ phases (b).

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The rare-earth Er$^{3+}$ ions occupy off-centrosymmetric sites with $C_x$ local symmetry thus allowing electric-dipole active transitions of their electrons within the $4f$ shell [20]. However, the presence of a macroscopic electric polarization at equilibrium is prohibited by symmetry [21]. The low local symmetry of the rare-earth sites leads to the complete splitting of the ground state $4I_{15/2}$ of the Er$^{3+}$ ions into eight doublets with Kramers-conjugated states [18]. The Er-Fe exchange leads to the breaking of the time-reversal symmetry and, consequently, splitting of the Kramers doublets. The energy-level structure of the ground multiplet of the Er$^{3+}$ ion in the orthoferrite is schematically shown in Fig. 2. The symmetry of the macroscopic normal modes arising from the transitions in Er$^{3+}$ ions is determined by the irreducible representations of the space group $D_{2h}^{16}$, and they are summarized in Table I [20,22–24]. The transitions between the states belonging to the different doublets are fourfold degenerate consisting of two electric dipole and two magnetic dipole modes of different symmetry in the $\Gamma_4$ and $\Gamma_2$ phases. During the spin reorientation from the $\Gamma_2$ to the $\Gamma_4$ phase the polarization of the rare-earth modes changes, following the rotation of the corresponding dipole components in the $(xz)$ plane. We note that the modes with different symmetry corresponding to the same transition have slightly different frequencies [20].

To study the optical excitation of low-energy electronic transitions in Er$^{3+}$ ions we employed the THz emission spectroscopy setup described in Ref. [25]. We studied ErFeO$_3$ single crystal plates cut perpendicularly to the $y$ and $x$ crystallographic axes, respectively. The samples were excited by 40 fs laser pulses with their photon energy centered at 1.55 eV (wavelength 800 nm). The terahertz radiation generated in the sample was collected and refocused by a pair of off-axis parabolic mirrors onto a 1 mm thick electro-optic ZnTe crystal. The crystal was gated by the femtosecond pulses split from the pump beam. As the gating pulse copropagates with the THz wave it acquires ellipticity proportional to the terahertz electric field. By measuring this ellipticity and varying the time delay between the pump and the gate we are able to record the time evolution of the emitted terahertz waveform [26].

To measure orthogonal polarizations of the THz emission the samples were rotated around their normal with respect to the axis of the detecting ZnTe crystal. The geometry of the experiments for the $y$-cut and $x$-cut samples is schematically drawn in Figs. 3(a) and 3(b), respectively. Note that our experimental method allows detection of the THz emission polarized in the $(xz)$ plane and $(yz)$ plane for the $y$-cut and $x$-cut sample, respectively. The expected polarization of the emitted electric field for the different Er modes in these two cases is shown in the two last columns of Table I. The strong point of the THz technique is its sensitivity to both electric and magnetic dipole active modes.

The ISRS-based excitation of magnetic resonances is described, invoking the effective field model [9]. The magnetic dipole-active modes can be excited by an effective magnetic field $\mathbf{B}_{\text{eff}} = -\partial W / \partial \mathbf{M}$, where $W$ is the free energy and $\mathbf{M}$ is the magnetization. One may anticipate that the magnetic dipole-active modes of Er$^{3+}$ ions will be excited via processes phenomenologically described using

![Fig. 2. The energy level structure of the ground state $4I_{15/2}$ of the Er$^{3+}$ ion in ErFeO$_3$ [18] and the possible transitions marked by arrows.](Image 89x621 to 218x744)

**FIG. 2.** The energy level structure of the ground state $4I_{15/2}$ of the Er$^{3+}$ ion in ErFeO$_3$ [18] and the possible transitions marked by arrows.

**TABLE I.** Eigenmodes of the Kramers rare-earth ions in the orthoferrites. The oscillating components of the terahertz electric dipole moment $\mathbf{d}$ and the electric dipole moment $\mathbf{d}$ are indicated with respect to the crystallographic $x$, $y$, and $z$ axes. The corresponding polarization of the emitted electric field is shown for the crystal plates cut perpendicularly to the $y$ and $x$ axes.

<table>
<thead>
<tr>
<th>Magnetic phase</th>
<th>Mode symmetry (representation of group $D_{2h}^{16}$)</th>
<th>Transition between doublets</th>
<th>Electric dipole</th>
<th>Degeneracy</th>
<th>THz emission polarization</th>
</tr>
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<tbody>
<tr>
<td>$\Gamma_4$</td>
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<tr>
<td>$\Gamma_{14}$</td>
<td>$m_z$</td>
<td>$\cdots$</td>
<td>4</td>
<td>$E_x$</td>
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</tr>
<tr>
<td>$\Gamma_{23}$</td>
<td>$m_x, m_y$</td>
<td>$\cdots$</td>
<td>4</td>
<td>$E_z$</td>
<td>$E_z$</td>
</tr>
<tr>
<td>$\Gamma_{58}$</td>
<td>$\cdots$</td>
<td>$d_z$</td>
<td>4</td>
<td>$E_z$</td>
<td>$E_z$</td>
</tr>
<tr>
<td>$\Gamma_{67}$</td>
<td>$\cdots$</td>
<td>$d_z$</td>
<td>4</td>
<td>$E_z$</td>
<td>$E_z$</td>
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<tr>
<td>$\Gamma_2$</td>
<td></td>
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<tr>
<td>$\Gamma_{12}$</td>
<td>$m_x$</td>
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<td>$\cdots$</td>
<td>4</td>
<td>$E_x$</td>
<td>$E_x, E_z$</td>
</tr>
<tr>
<td>$\Gamma_{56}$</td>
<td>$\cdots$</td>
<td>$d_x$</td>
<td>4</td>
<td>$E_x$</td>
<td>$E_x, E_z$</td>
</tr>
<tr>
<td>$\Gamma_{78}$</td>
<td>$\cdots$</td>
<td>$d_x$</td>
<td>4</td>
<td>$E_z$</td>
<td>$E_z$</td>
</tr>
</tbody>
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an effective magnetic field \( \mathbf{B}_{\text{eff}} = \hat{\mathbf{z}}(m) \mathbf{E}_{\text{opt}} \), where \( \mathbf{E}_{\text{opt}} \) is the complex envelope of the optical electric field and \( \hat{\mathbf{z}}(m) \) is a phenomenological tensor describing ISRS involving virtual electric dipole transitions at the pump optical wavelength. In the simplest case of an isotropic medium the effective magnetic field \( \mathbf{B}_{\text{eff}} \) is generated by circularly polarized light.

To excite electric dipole-active modes one must act on the electronic system with an effective electric field \( \mathbf{E}_{\text{eff}} \). In centrosymmetric crystals, such as ErFeO\(_3\), the generation of the effective electric field via electric dipole-active optical transitions is forbidden. The lowest order process for generating such a field reads phenomenologically as \( \mathbf{E}_{\text{eff}} = \hat{\mathbf{z}}(e) \mathbf{E}_{\text{opt}} \mathbf{H}_{\text{opt}} \), where \( \mathbf{H}_{\text{opt}} \) is the complex envelope of the magnetic optical field and \( \hat{\mathbf{z}}(e) \) is a tensor describing ISRS involving virtual magnetic dipole transitions at optical wavelengths. For photon energies around 1.55 eV, several \( f-f \) magnetic dipole optical transitions in Er\(^{3+}\) ions are clearly seen in the absorption spectrum of ErFeO\(_3\) [27].

Indicative THz waveforms generated at \( T = 20 \) K by circularly polarized laser pulses of opposite helicities in the \( y\)-cut ErFeO\(_3\) sample are shown in Fig. 4(a). The complex emission spectrum consists of several narrow bands. Some of them with frequencies below 1 THz correspond to the magnetic resonances of the Fe\(^{3+}\) sublattices as it was reported earlier [25,28]. Here we focus on the spectral components lying above 1 THz [Fig. 4(b)].

We found that the spectral components lying above 1 THz are observed below \( \sim 150 \) K. Some of them are excited by the circularly polarized pump pulses with their initial phase determined by the pump helicity, while others were found to be sensitive neither to the circular nor to the linear polarization of the pump. The emitted THz waves have an electric field polarized along the \( x \) and \( z \) axes in the \( y\)-cut sample, but only along the \( y \) axis in the \( x\)-cut sample.

Figures 5(a), 5(b), and 5(c) summarize the frequencies of all spectral components lying above 1 THz as a function of temperature [29].

As one can see from Fig. 5, the spectrum of THz emission above 1 THz consists of several components with frequencies lying at \( \sim 1.3, \sim 1.5, \) and \( \sim 1.8 \) THz. These values are close to the expected transitions between the states belonging to the three lowest doublets of the Er\(^{3+}\) ions [see Fig. 2]. Note that the helicity-dependent and helicity-independent THz waves change their polarizations by 90\(^\circ\) in the temperature interval \( \sim 50–70 \) K (see also the Supplemental Material [29], Fig. S4), which corresponds to the spin reorientation as was determined from the behavior of the spin resonances of the Fe\(^{3+}\) sublattices [28]. For example, in the \( y\)-cut sample the helicity-dependent emission below 50 K has an electric field polarized along the \( x \) axis [Fig. 5(a), open circles], while above 70 K it is along the \( z \) axis [Fig. 5(b), open circles].

These facts show that the observed THz emission arises from the light-induced coherence within the \( ^4I_{15/2} \) ground state of the Er\(^{3+}\) ions. The emission disappears above 150 K when the population of the lowest sublevels within the ground state equalizes. Based on the frequencies of the observed modes we attribute them to various transitions between the states belonging to the different Kramers doublets as shown in Fig. 2. The polarizations of the observed components allow us to assign them to the modes of different symmetry in accordance with Table I. The transitions within the doublets have frequencies below the cutoff frequency of our THz spectrometer (\( \sim 100 \) GHz) [30] and are not resolved here.

The helicity-dependent THz emission is only observed in the \( y\)-cut ErFeO\(_3\) sample. Below the spin reorientation temperature interval the helicity-sensitive emitted THz electric field is parallel to the \( x \) axis, while above the spin reorientation it is polarized along the \( z \) axis [open circles in Figs. 5(a) and 5(b)]. The emission comprises three spectral bands at \( \sim 1.3, \sim 1.5, \) and \( \sim 1.8 \) THz in the \( \Gamma_3 \) phase, while in the \( \Gamma_1 \) phase only two bands at \( \sim 1.5 \) and \( \sim 1.8 \) THz are observed. The absence of the 1.3 THz band shows that the Raman susceptibility that determines the helicity-dependent excitation is very small for this mode in the

![Figure 3](image1.png)  
**FIG. 3.** The geometry of the optical pump/THz emission experiment. The direction of the laser pulse propagation and of the THz emission; the measured polarization of the THz electric field are shown with respect to the crystallographic axes. (a) The \( y\)-cut sample emits electric field polarized in the \( (xy) \) plane. (b) The \( x\)-cut sample emits electric field polarized in the \( (yz) \) plane.

![Figure 4](image2.png)  
**FIG. 4.** (a) The THz waveforms generated in the \( y\)-cut ErFeO\(_3\) at 20 K by circularly polarized light of opposite helicities. The half-difference of these waveforms is shown shifted along the vertical axis. (b) The spectrum of the helicity-dependent contribution obtained by Fourier transformation of the waveform shown in (a) and fitted with three Lorentzian contours.
Polarization-independent THz emission has components polarized along both the $x$ and $z$ axes above and below the spin reorientation temperature interval in the $y$-cut sample. Again, there are three bands centered at $\sim 1.3$, $\sim 1.5$, and $\sim 1.8$ THz. However the frequencies of these components are slightly, but noticeably shifted with respect to the helicity-dependent bands. The polarization-independent emission can be divided into the main component polarized along the $z$ axis in the $\Gamma_2$ phase and along the $x$ axis in the $\Gamma_4$ phase [squares in Figs. 5(a) and 5(b)] and a smaller orthogonal component most pronounced for the $\sim 1.3$ THz band [triangles in Figs. 5(a) and 5(b)]. Therefore, at each $\sim 1.3$, $\sim 1.5$, and $\sim 1.8$ THz frequency, the pump laser pulse excites three oscillating sources of THz emission. Again the polarization of these components rotates by $90^\circ$ in the $(xz)$ plane within the spin-reorientation temperature interval. The polarization-independent emission must be assigned not only to the longitudinal-like electric dipole $\Gamma_{56}$ and $\Gamma_{58}$ modes, but also to the magnetic dipole $\Gamma_{12}$ and $\Gamma_{14}$ modes. Indeed, the polarization-independent mechanism of ultrafast excitation of the magnetic-dipole longitudinal-like magnetic modes of $\text{Fe}^{3+}$ ions has been recently demonstrated in orthoferrites [25,28].

In the $x$-cut sample the THz emission is independent of the pump polarization and consists of three spectral bands centered at $\sim 1.3$, $\sim 1.5$, and $\sim 1.8$ THz shown in Fig. 5(c). However, the frequencies of the bands below the spin-reorientation temperature interval are slightly shifted compared to those above this interval. Therefore, we suggest that the emission in the $x$-cut sample arises from the $\Gamma_{78}$ electric dipole excitations in the low temperature $\Gamma_2$ phase. In the high temperature $\Gamma_4$ phase the emission arises from the $\Gamma_{14}$ magnetic dipole modes.

The absence of the helicity-dependent emission in the $x$-cut sample suggests that the $\Gamma_{23}$ modes are highly elliptical with $m_\gamma \gg m_x$. Indeed, the precessional mode of the iron sublattices in the orthoferrites is strongly elliptical [31]. The Er magnetic moments are coupled to the Fe spins and, consequently, this coupling favors the high ellipticity of the rare-earth magnetic precession.

In summary, we have demonstrated the possibility of selective ultrafast excitation of magnetic dipole and electric dipole-active modes of the rare-earth ions in $\text{ErFeO}_3$ crystals via ISRS. By varying the polarization of light and its propagation direction with respect to the crystallographic axes we have addressed different dipole components of the $4f^{11}$ transitions in the $\text{Er}^{3+}$ ions. Importantly, in the case when not only the electric dipole transitions (mostly in the iron sublattices), but also magnetic dipole transitions (mostly in the rare-earth sublattices) contribute to the optical dielectric function, the magnetic dipole-active THz modes respond preferentially to the electric dipole virtual optical transitions, whereas the electric dipole-active THz modes respond mostly to the magnetic dipole virtual optical transitions. Thus, our observations call for

![Graphical Figure 5](image-url)
theoretical models beyond the conventional electric dipole approximation. We anticipate the demonstrated ultrafast ISRS is applicable to other rare-earth oxides, as practically in all of them the low-energy states are present. Finally, we note that the magnetic order throughout a broad class of magnetic oxides containing both 3d and 4f ions can be manipulated by controlling the rare-earth states [32]. Therefore, by femtosecond pumping of rare-earth ions one could exploit coupling between the rare-earth and magnetic oxides containing both.

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