\[B^0\] lifetime measurement in the CP-odd decay channel \(B^0 \rightarrow J/\psi f_0(980)\)
The lifetime of the $B^0_s$ meson is measured in the decay channel $B^0_s \rightarrow J/\psi \pi^+\pi^-$ with $880 \leq M_{\pi^+\pi^-} \leq 1080$ MeV/$c^2$, which is mainly a CP-odd state and dominated by the $f_0(980)$ resonance. In $10.4 \, fb^{-1}$ of data collected with the D0 detector in Run II of the Tevatron, the lifetime of the $B^0_s$ meson is measured to be $\tau(B^0_s) = 1.70 \pm 0.14$ (stat) $\pm 0.05$ (syst) ps. Neglecting CP violation in $B^0_s/B^0_s$ mixing, the measurement can be translated into the width of the heavy mass eigenstate of the $B^0_s$, $\Gamma_H = 0.59 \pm 0.05$ (stat) $\pm 0.02$ (syst) ps$^{-1}$.

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The $B^0_s$ and $B^0$ mesons are produced as flavor eigenstates at hadron colliders, but the particles propagate as mass eigenstates. There are two mass eigenstates, the so-called heavy and light states, which are linear combinations of the flavor eigenstates. In the absence of CP-violation in mixing, the mass eigenstates are also CP eigenstates, with the heavier state expected to be the CP-odd state. The lifetimes of the two mass eigenstates can be different from each other and different from the average $B^0_s$ lifetime. A measurement of the $B^0_s$ lifetime in either a pure CP-odd state or pure CP-even state would give important additional information about the $B^0_s$ system.

The $B^0_s \rightarrow J/\psi f_0(980)$ decay channel corresponds to a pure CP-odd eigenstate decay due to angular momen-
rapidity of $|\eta| < 3$ [10]. For charged particles, the resolution on the distance of closest approach as provided by the tracking system is approximately 50 µm for tracks with $p_T \approx 1$ GeV/c, where $p_T$ is the component of the momentum perpendicular to the beam axis. It improves asymptotically to 15 µm for tracks with $p_T > 10$ GeV/c. Preshower detectors and electromagnetic and hadronic calorimeters surround the tracker. The muon system is located outside the calorimeter, and consists of multilayer drift chambers and scintillation counters inside 1.8 T iron toroidal magnets, and two similar layers outside the toroids. Muon identification and tracking for $|\eta| < 1$ relies on 10 cm wide drift tubes, while 1 cm minidrift tubes are used for $1 < |\eta| < 2$. We base our data selection on reconstructed charged tracks and identified muons. Events used in this analysis are collected with both single muon and dimuon triggers. To avoid a trigger bias in the lifetime measurement, we reject events that satisfy only impact parameter-based triggers. We simulate signal events with PYTHIA [11] and EvtGen [12], followed by full detector simulation using GEANT3 [13]. To correct for trigger effects, we weight simulated events so that the $p_T$ distributions of the muons match the distributions in data.

The $B^0_s$ reconstruction begins by reconstructing $J/\psi$ candidates followed by searching for $\pi^+\pi^-$ candidates. To reconstruct $J/\psi \rightarrow \mu^+\mu^-$ candidates, events with at least two muons of opposite charge reconstructed in the tracker and the muon system are selected. For at least one of the muons, hits are required in the muon system both inside and outside of the toroids. Both muons must have hits in the SMT and have $p_T > 2.5$ GeV/c. The muon tracks are constrained to originate from a common vertex with a $\chi^2$ probability greater than 1%. Each $J/\psi$ candidate is required to have a $p_T$ greater than 1.5 GeV/c and a mass in the range 2.80–3.35 GeV/c$^2$.

We require two oppositely charged tracks, assumed to have the pion mass, each with at least two SMT hits and at least two CFT hits, and at least eight total hits in the tracking system. These two tracks are constrained to a common vertex with a $\chi^2$ probability greater than 1%. Each $\pi^+\pi^-$ candidate is required to have a mass in the range 880 $\leq M_{\pi^+\pi^-} \leq$ 1080 MeV/c$^2$ and a $p_T$ greater than 1.5 GeV/c. The $B^0_s$ candidates are reconstructed by performing a constrained fit to a common vertex for the two pions and the two muon tracks, with the latter constrained to the $J/\psi$ mass of 3.097 GeV/c$^2$ [6]. The $B^0_s$ candidates are reconstructed by requiring a mass within the range 5.1–5.8 GeV/c$^2$, and to have a $p_T$ greater than 6.0 GeV/c.

To determine the decay time of the $B^0_s$, the distance traveled by the candidate projected in a plane transverse to the beam direction is measured, and then a correction for the Lorentz boost is applied. The transverse decay length is defined as $L_{xy} = \mathbf{L}_{xy} \cdot \mathbf{p}_T / p_T$, where $\mathbf{L}_{xy}$ is the vector that points from the primary vertex [14] to the $B^0_s$ decay vertex, and $\mathbf{p}_T$ is the transverse momentum vector of the $B^0_s$ candidate. The event-by-event value of the proper transverse decay length, $\lambda$, for the $B^0_s$ candidate is given by:

$$
\lambda = L_{xy} \frac{cM_B}{p_T},
$$

where $M_B$ is the world average mass value of the $B^0_s$ meson [6]. In order to remove background, $B^0_s$ candidates are required to have $\lambda > 0.02$ cm and uncertainties on $\lambda$ of less than 0.01 cm.

A simultaneous unbinned maximum likelihood fit to the mass and proper decay length distributions is performed to measure the lifetime. The likelihood function $\mathcal{L}$ is defined by:

$$
\mathcal{L} = \prod_{j=1}^{N} \left[ \frac{N_{\text{sig}} F_j^{\text{sig}} + N_{\text{comb}} F_j^{\text{comb}} + N_{\text{xf}} F_j^{\text{xf}} + N_{B^0} F_j^{B^0}}{N_{\text{data}}} \right],
$$

where $N$ is the total number of events and $N_{\text{sig}}$, $N_{\text{comb}}$, $N_{\text{xf}}$ and $N_{B^0}$ are the expected number of signal, combinatorial background, cross-feed contamination and $B^0$ events, respectively. All these parameters are determined in the fit. The different background contributions are discussed below.

The functions $F$ are the product of three probability density functions that model distributions of the mass $m$, the proper transverse decay length $\lambda$, and the uncertainty on the proper decay length $\sigma_\lambda$ for the signal, combinatorial background, cross-feed contamination, and $B^0$ events

$$
F_a = M_a(m_j) T_a(\lambda_j | \sigma_\lambda) E_a(\sigma_\lambda); \quad \alpha = \{\text{sig}, \text{comb}, \text{xf}, B^+\},
$$

where $m_j$, $\lambda_j$, and $\sigma_\lambda$ represent the mass, the transverse proper decay length, and its uncertainty, respectively, for a given event $j$. The use of the probability density functions $T$ and $E$ follows the method of reference [15]. The specific models and parameters used in the fit are described below.

For the signal, the mass distribution is modeled by a Gaussian function, $M_{\text{sig}}(m_j) = G(m_j; \mu_m, \sigma_m)$, where

$$
G(m_j; \mu_m, \sigma_m) = \frac{1}{\sqrt{2\pi}\sigma_m} e^{-(m_j-\mu_m)^2/(2\sigma_m^2)},
$$

with $\mu_m$ and $\sigma_m$ the mean and the width of the Gaussian, determined from the fit.

The combinatorial background is primarily due to random combinations of $J/\psi$’s with additional tracks in the event, and its mass distribution is described by an exponential function

$$
M_{\text{comb}}(m_j; a_0) = e^{a_0 m_j},
$$
with $a_0$ determined from the likelihood fit.

The physics cross-feed contamination is mainly produced by the combination of $J/\psi$ mesons from $b$ hadron decays with other particles produced in the collision, including from the same $b$ hadron. Other $b$ hadron decays with final states such as $B^0 \rightarrow J/\psi K\pi$, $B^0 \rightarrow J/\psi\pi\pi$ and $B^0_s \rightarrow J/\psi KK$ are reconstructed at mass below the signal of the $B^0_s$, either due to the lower mass of the $B^0$ or the incorrect mass assignment of the pion mass to a kaon track. Simulations of these decays show that the cross-feed contamination can be described by a single Gaussian component

$$M_{\text{sf}}(m_j) = G(m_j; \mu_{\text{sf}}, \sigma_{\text{sf}}),$$

where $\mu_{\text{sf}}$ and $\sigma_{\text{sf}}$ are the mean and the width of the Gaussian, determined from the likelihood fit.

The final contribution arises from $B^\pm \rightarrow J/\psi K^\pm$ decays in which the kaon has been assigned a pion mass, and an additional track accidentally forms a vertex with the $J/\psi K^\pm$. The candidate mass is reconstructed in the region of real $B^0$ events. If the higher $p_T$ non-muon track in $B^0_s$ candidates is assigned a kaon mass, a clear $B^\pm$ signal emerges. Events in this $B^\pm$ mass peak, when interpreted as $J/\psi\pi\pi$, are used as a template [10] to determine the shape of the mass distribution of the $B^\pm \rightarrow J/\psi K^\pm$ contamination in the $B^0_s$ candidates.

The $\lambda$ distribution for the signal is parameterized by an exponential decay convoluted with a resolution function

$$T_{\text{sig}}(\lambda_j|\sigma_{\lambda_j}) = \frac{1}{\lambda_B} \int_0^\infty G(x; \lambda_j, \sigma_{\lambda_j}) \exp\left(\frac{-x}{\lambda_B}\right) dx,$$

with $\lambda_B = c \tau$ of the $B^0_s$ to be measured. The $\lambda$ distribution for the background components is parametrized by the sum of two exponential decay functions modeling combinatorial background $T_{\text{comb}}(\lambda_j)$, an exponential decay for the cross-feed contamination $T_{\text{sf}}(\lambda_j)$, and an exponential decay function that describes $T_{B^\pm}(\lambda_j)$ for $B^\pm$ contamination.

The distribution of the $\lambda$ uncertainty $E_{\text{sig}}(\sigma_{\lambda_j})$ is described by a phenomenological model, using an exponential with decay constant $1/\zeta$, convoluted with a Gaussian with mean $\epsilon$ and width $\delta$:

$$E_{\text{sig}}(\sigma_{\lambda_j}; \zeta, \epsilon, \delta) = \frac{1}{\zeta} e^{-\sigma_{\lambda_j}/\zeta} \otimes G(\sigma_{\lambda_j}; \epsilon, \delta),$$

where the parameters $\zeta$, $\epsilon$ and width $\delta$ are determined from the fit in the sample of events. The uncertainties in $\lambda$ for the background components are treated in the same manner.

The fit yields $c\tau(B^0_s) = 504 \pm 42 \; \mu$m and the numbers of signal decays to be $494 \pm 85$. Figure 1 shows the mass, $\lambda$ and $\lambda$ uncertainty distributions for data with the fit results superimposed. Figure 2 shows the $M(\pi^+\pi^-)$ mass distribution for events with $M(\mu^+\mu^-\pi^+\pi^-)$ within one

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**FIG. 1:** Distributions of (a) invariant mass, (b) proper transverse decay length, and (c) proper transverse decay length uncertainty for $B^0_s$ candidates, with the fit results superimposed. Each of the different background components is indicated in the figure. The fit yields $c\tau(B^0_s) = 504 \pm 42 \; \mu$m.
The bias has a value of -4.4 \( \mu \)m, the result is a slight underestimate of the signal lifetime. The background has a shorter lifetime than the signal, to imperfect separation of signal and background. Since the modeling and fitting method used to estimate the lifetime of one of them fixed to the world average of the heavy mass eigenstate of the \( B_s^0 \) mass. We test the modeling and fitting method used to estimate the lifetime using data generated in pseudoexperiments with a range of lifetimes from 300 to 800 \( s \). A bias arises due to imperfect separation of signal and background. Since the background has a shorter lifetime than the signal, the result is a slight underestimate of the signal lifetime. The bias has a value of -4.4 \( \mu \)m for an input lifetime of 500 \( \mu \)m and 500 signal events. We have corrected the lifetime for this bias and a 100\% uncertainty on the correction has been applied to the result. We estimate the systematic uncertainty due to the models for the \( \lambda \) and mass distributions by varying the parameterizations of the different components: (i) the cross-feed contamination is modeled by two Gaussian functions instead of one, (ii) the exponential mass distribution for the combinatorial background model is replaced by a first order polynomial, (iii) the smoothing of the non-parametric function that models the \( B^\pm \) contamination is varied, and (iv) the exponential functions modelling the background \( \lambda \) distributions are smeared with a Gaussian resolution similar to the signal. To take into account correlations between the effects of the different models, a fit that combines all different model changes is performed. We quote the difference between the result of this fit and the nominal fit as the systematic uncertainty.

Several cross-checks of the lifetime measurement are performed. The mass windows are varied, the reconstructed \( B_s^0 \) mass is used instead of the world average value, and the data sample is split into different regions of pseudorapidity and of azimuthal angle. All results obtained with these variations are consistent with the nominal measurement. Using the \( B^\pm \) background sample extracted from the data, we performed a fit for the lifetime of this component of the background. The result is in good agreement with the values obtained from the global fit. We have also fit the lifetime of the cross-feed contamination from the simulation and again good agreement with the global fit is observed.

In order to estimate the effect of a small non CP-odd component in the analysis, we performed the fit with two exponential decay components for the signal, with the lifetime of one of them fixed to the world average of the CP-even \( B_s^0 \) lifetime, and its fraction to be 0.01 as found by the LHCb experiment. The lifetime fit finds a variation of 1 \( \mu \)m with respect to the nominal fit result.

In summary, the lifetime of the \( B_s^0 \) is measured to be:

\[
\sigma(B_s^0) = 508 \pm 42 \text{ (stat)} \pm 16 \text{ (syst)} \mu m,
\]

from which we determine:

\[
\tau(B_s^0) = 1.70 \pm 0.14 \text{ (stat)} \pm 0.05 \text{ (syst)} \text{ ps},
\]

in the decay channel \( B_s^0 \to J/\psi \pi^+ \pi^- \) with \( 880 \leq M_{\pi^+ \pi^-} \leq 1080 \text{ MeV}/c^2 \). In the absence of CP violation in mixing, this measurement can be translated into the width of the heavy mass eigenstate of the \( B_s^0 \):

\[
\Gamma_H = 0.59 \pm 0.05 \text{ (stat)} \pm 0.02 \text{ (syst)} \text{ ps}^{-1}.
\]

This result is in good agreement with previous measurements and provides an independent confirmation of the longer lifetime for the CP-odd eigenstate of the \( B_s^0/B_s^0 \) system.

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