LORA: A scintillator array for LOFAR to measure extensive air showers


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Abstract

The measurement of the radio emission from extensive air showers, induced by high-energy cosmic rays is one of the key science projects of the LOFAR radio telescope. The LOfar Radboud air shower Array (LORA) has been installed in the core of LOFAR in the Netherlands. The main purpose of LORA is to measure the properties of air showers and to trigger the read-out of the LOFAR radio antennas to register extensive air showers. The experimental set-up of the array of scintillation detectors and its performance are described.

Keywords: cosmic rays, extensive air showers, radio detection, scintillation detectors, LOFAR, LORA

1. Introduction

The search for the origin of the highest energy particles in the Universe is a big challenge in astroparticle physics [1–3]. From the experimental point of view, a precise measurement of the elemental composition of cosmic rays at the highest energies is crucial. The present work is part of an endeavor to establish a new method to measure air showers at high energies and determine the mass composition of cosmic rays with nearly 100% duty cycle: the radio detection of air showers [4]. To contribute to the measurement of radio signals from air showers with the LOFAR telescope [5], we have installed an air shower array in the LOFAR core.

High-energy cosmic rays impinging onto the atmosphere of the Earth, induce cascades of secondary particles. The bulk of the charged particles are electrons and positrons. They are deflected in the magnetic field of the Earth, while in addition, there is an excess of negative charge. This yields the emission of coherent radiation with frequencies of tens of MHz, e.g. [6–9].

The feasibility of quantitative radio measurements of air showers has been demonstrated with the LOPES experiment (LOFAR prototype station) [10–12]. It has been shown that radio emission can be detected using low-noise amplifiers and fast digitizers in combination with sufficient computing power to analyze the registered signals.

Radio emission from air showers is detected with the LOFAR radio telescope in the framework of the LOFAR key science project Cosmic Rays [13]. The LOw Frequency ARray (LOFAR) is a digital observatory [5]. The main focus of the astronomy community is to observe the radio Universe in the frequency range of (10 − 240) MHz.

More than 40 stations with fields of relatively simple antennas work together as a digital radio interferometer, i.e. the measured signals are digitized with fast ADCs and correlations are formed in a central processing unit. The antenna fields are distributed over several countries in Europe with a dense core in the Netherlands. The latter consists of 24 stations on an area measuring roughly 5 km2. Each station comprises 96 low-band antennas, simple inverted V-shaped dipoles, operating in the frequency range of (10 − 80) MHz. Each antenna has two dipoles, oriented perpendicular to each other. In addition, fields of high band antennas cover the frequency range of (110−240) MHz. The signals from the antennas are digitized and stored in a ring buffer (transient buffer board, TBB). A triggered read-out of these buffers will send the raw data to a central processing facility.

An ultimate goal is to independently detect radio emission from air showers with LOFAR. This requires a sophisticated trigger algorithm that analyses the digitized antenna signals in real time. To assist with the development of the trigger algorithm and to measure basic air shower parameters, an array of particle detectors has been at LOFAR.

The LOFAR Radboud Air Shower Array (LORA) is an array of scintillation counters, located in the innermost center of LOFAR, the superterp. It has been designed to register air showers initiated by primary particles with energies exceeding 1016 eV. Strong radio signals are expected from air showers in...
In the following, we describe the set-up of LORA and its properties. The experimental set-up is described in Sect. 2 and the detector calibration in Sect. 3. The various steps involved in the reconstruction of air shower parameters are described in Sect. 5 and in Sect. 6 the reconstruction accuracies are discussed, followed by a review of the array performance in Sect. 7.

Figure 1: Layout of LORA in the dense core in the center of LOFAR. The squares represent the positions of the particle detectors. The crosses and open squares represent the two different types of LOFAR radio antennas. The dotted lines indicate the grouping of the detectors for the data acquisition.

Figure 2: Schematic view of a scintillation detector. Sheets of plastic scintillator are read out by photomultiplier tubes via wavelength shifter bars [14]. This energy regime is also of astrophysical interest, as a transition is expected from a Galactic to an extra-galactic origin of cosmic rays at energies between $10^{17}$ and $10^{18}$ eV [2, 3].

2. Experimental set-up

LORA comprises 20 detector units, located on a circular area with a diameter of about 320 m. The positions of the detectors in the innermost core of LOFAR are illustrated in Fig. 1. The array is sub-divided into five units, each comprising four detectors. The detectors are located on circles with a radius of about 40 m around a central electronics unit, with a spacing of 50 to 100 m between the detectors, respectively.

Each detector unit contains two pairs of scintillators (NE 114) with the dimensions $47.5 \times 47.5 \times 3$ cm$^3$, read out via wavelength shifter bars (NE 174 A) through a photomultiplier tube (EMI 9902 A). A detector unit, containing the two pairs of scintillators and two photomultiplier tubes is sketched in Fig. 2. The detectors are installed inside weatherproof shelters.

The two photomultipliers in one detector unit share a common high-voltage channel. To match the gain of the two tubes, we use a resistor network to adjust the voltage correspondingly. The signals of the two photomultiplier tubes in each detector are read out via RG223 coaxial cables and a passive connection into a single digitizer channel. 12-bit ADCs are used, which sample the incoming voltage with a time resolution of 2.5 ns [15]. A field programmable gate array (FPGA) provides a trigger signal in real time.

Four detectors form (electronically) a unit, comprising two digitizer units (with two electronic channels each) [15, 16]. the detectors were previously operated in the KASCADE calorimeter [13].

2 The detectors were previously operated in the KASCADE calorimeter [13].

3 Internally, two ADCs are used per channel, sampling the same input signal at 200 MHz with an offset of half a clock cycle.
trolled by a Linux-operated, single-board mini PC. The two digitizer units operate in a master and slave combination like a four-channel oscilloscope, where the master generates a common trigger for both the digitizer units. The master digitizer contains a GPS receiver (Trimble, Resolution T), which provides GPS time stamps to both the digitizer units. Each digitizer contains a 200 MHz clock counter to assign a time stamp with nanoseconds accuracy to each triggered signal.

The pulse per second signals (1PPS) from this type of GPS receiver can introduce a timing uncertainty of up to a maximum of 20 ns. This error is stored every second during the data taking. It is corrected for the event time stamp in the offline data analysis using a proper correction formula \[17\]. The time stamp calculation also takes into account the fluctuations in the number of clock periods of the 200 MHz clock counter between two PPS signals.

The two digitizers are connected to the PC through an USB interface. The PC also controls a four-channel high-voltage supply through one of the digitizer units. The FPGA inside the digitizer unit controls an input-output register, which is connected to the high-voltage supply, allowing to set the individual voltages on the four channels remotely. A block diagram of the electronics components is depicted in Fig. 3.

When the four input signals from the PMTs in an electronics unit satisfy a local trigger condition, usually three out of four detectors in coincidence within 400 ns the digitizers send the data to the local computer. The data from the five mini PCs consequently are sent via Ethernet to a central, Linux-operated master computer, where the main data acquisition (DAQ) runs. Within 100 ns all data are collected from the other electronics units. The received time stamps, which are each assigned according to the first threshold crossing in a detector, are checked for coincidences (500 ns window) and are combined to an event file that is stored locally. A simple analysis is performed on these data, which reconstructs arrival direction and core position to allow for monitoring. This computer also an additional high-level trigger can be formed, based on the number of sub-arrays that have detected an air shower. This high-level trigger is used to trigger the read-out of the radio antennas. The overall processing takes about 130 ms (including the wait time), which is fast compared to the 5 s of data that are stored in the ring buffers of the radio antennas.

The main DAQ program also controls the DAQ programs running on the mini PCs. All input parameters, including those required by the DAQ on the local computers are set on the master computer. The whole DAQ is controlled and monitored using an online monitoring panel, which can be accessed remotely. The display panel provides continuous monitoring of the performance of the electronics and the detectors during operations. Both, the monitoring panel and the DAQ software use several features from the ROOT package \[18\].

3. Detector calibration

For each event, traces of the PMT signals are stored in a time window of 10 µs. We have chosen to start the recorded data 2 µs before to 8 µs after the trigger for each event. A typical ADC trace is depicted in Fig. 4. The inset shows a closer view around the pulse of a through-going particle.

To calculate the total signal produced by a charged particle (which corresponds to the total energy deposited by the particle) from the recorded time traces, the following procedure is applied: The average pedestal is calculated from the 2 µs window before the trigger. This pedestal is subtracted from the ADC values and the signal trace is integrated over the time window from \(t_{\text{peak}} - 40 \text{ ns}\) to \(t_{\text{peak}} + 250 \text{ ns}\). \(t_{\text{peak}}\) is the time of the maximum ADC count in the trace.

The resulting measured energy deposition of singly charged particles in a detector is shown in Fig 5 (top). A Landau function is fitted to the measured distribution. The most probable value corresponds to the energy deposition of the through-going charged particle. This value is taken for the energy calibration of each detector. The high voltage applied to each photomultiplier is adjusted such that the Landau distribution peaks at \(\approx 400 \text{ ADC counts}\).

In order to determine the energy deposition of singly charged particles, we conducted simulations with the GEANT4 package \[19\]. The scintillators are made of polyvinyl-toluene (\(\text{CH}_2\text{CH(C}_6\text{H}_5\text{CH}_3\)), which is simulated as a C:H mixture of 9:10, with a density of 1.032 \(\text{g/cm}^3\). The plates are enclosed in a lighttight box, made of aluminum plates of 1 mm thickness. Thus, the detectors are also sensitive to the photon component of air showers, since a significant fraction of high-energy photons undergoes pair production and thus, contributes to the signal. The rest of the volume is filled with air.

Muons of 4 GeV are shot through the detector to find the distribution of the energy deposition. It has been found experimentally that muons arrive under directions, distributed according to a \(\cos^2 \theta\) zenith angle distribution \[20\]. To get a realistic distribution we take a random ground location in a square of \(1.5 \times 1.5 \text{ m}\) with a LORA detector in the center. A random azimuth angle is chosen, and a zenith angle is chosen from a
The low number of scintillation photons that induce a signal approximated if we take into account the statistical noise, due to the noise level, registered during the last hour. The threshold is set to a value of $(N + 4\sigma)$ where $N$ and $\sigma$ denote the mean value and the fluctuation of the noise for the last hour, respectively.

The photomultipliers, placed in weather-proof shelters, are exposed to the ambient temperature. It is well known that the gain of a photomultiplier changes as a function of its operating temperature. A stable gain is necessary for a good performance of the experiment. The measured gain of a detector during about 6 months of operation is depicted in Fig. 6. Each point represents a value, averaged over three days. The gain variation is calculated with respect to the averaged gain. The variation is found to be within $\pm 10\%$. The overall stability looks good for 18 out of the 20 detectors, showing gain variations within $\pm 10\%$ for more than $\approx 93\%$ of the total operation time. The remaining two detectors showed variations up to $\pm 10\%$ within about 70% and 85% of the total operation time, respectively.

4. Data taking

For data taking, a coincidence trigger condition of 3 out of 4 detectors has been set for each sub-array. An event is accepted by the master computer if at least one sub-array has been triggered. These trigger settings generate a total event rate of $\approx 0.15$ Hz from the full array (five sub-arrays). The total daily data output amounts to about 180 MB.

Full operation of LORA started in June 2011. Since then, air showers are continuously recorded with the set-up. For this article around 162 days of clean data have been collected with the array. This amounts to a total of 2.1 million air showers. For the analysis presented below, showers which trigger a minimum of 5 detectors (at least 2 sub-arrays) are considered. In total, we have recorded 114659 such air showers.

5. Reconstruction of air shower parameters

For a registered air shower, the arrival time of the first particle and the energy deposition in each detector are measured. Air showers have recorded 114659 such air showers.

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shower properties are derived from these quantities, in particular: the arrival time of the shower, the direction and the position of the shower axis, the lateral density distribution of charged particles, and the total number of charged particles contained in the shower. The latter is used to estimate the energy of the shower-inducing primary particle.

An example of a measured air shower is given in Fig. 7. The left panel represents the measured arrival times and the right panel shows the energy depositions in the detectors.

5.1. Arrival direction

The arrival time of the particles in the detector is taken as the time at which the recorded signal crosses the threshold. The measured values are corrected for time offsets from different electron transit times in the photomultiplier tubes, different signal propagation speeds in different electronic channels, and different signal cable lengths. The average offset for each detector is determined from the distribution of the differences of the air shower arrival times in two detectors. The main time offsets result from different cable lengths.

Using the relative signal arrival times between the detectors, the arrival direction of the primary cosmic ray is reconstructed. We assume that the air shower particles move in a plane towards the ground and we neglect the small, but finite curvature of the shower front \([\ref{2}]\). We assume this plane moves with the speed of light \(c\) in the direction of its normal towards the ground. The normal to the shower plane is taken as the arrival direction of the primary cosmic ray (or the direction of the shower axis).

The direction of the shower axis is calculated by minimizing the function

\[
\delta^2 = \sum_{i=1}^{k} \left[ l x_i + m y_i + n z_i + c(t_i - t_0) \right]^2, \tag{1}
\]

where the summation is over the total number of detectors \(k\), \((x_i, y_i, z_i)\) denote the position of the \(i^{th}\) detector on the ground, \(t_i\) the relative signal arrival time in that detector, measured with respect to the first hit detector, and \(t_0\) denotes the time at which the shower plane passes through the origin of the coordinate system. The origin is taken as the center of the LORA detector array. \((l, m, n)\) denote the direction cosines of the normal to the plane and are related to the orientation of the shower axis.

Minimizing \((1)\), we obtain the best fit values of \((l, m, n, t_0)\). The zenith angle of the shower axis, measured from the vertical direction is obtained as,

\[
\theta = \sin^{-1} \left( \sqrt{l^2 + m^2} \right), \tag{2}
\]

and the azimuthal angle, measured clockwise from the North through East is obtained using

\[
\phi = \cos^{-1} \left( \frac{m}{\sqrt{l^2 + m^2}} \right). \tag{3}
\]

5.2. Position of shower axis and lateral density distribution

The measured energy deposition in each detector is corrected for the increase in track length inside the detector due to the inclination angle of the air shower by multiplying by a \(\cos(\theta)\) factor. Dividing the amount of energy deposition in
each detector by the mean energy deposit per particle, delivers the number of charged particles, hitting the detector.

The particle density \( n_i \) in each detector is calculated by dividing the measured number of particles by the effective detector area \( A_d \cos \theta \). \( A_d \) denotes the actual geometrical area of the detector and the factor \( \cos \theta \) takes into account the reduction in the effective area of the detector for inclined showers with zenith angle \( \theta \).

Plotting the measured particle density in the shower plane as function of the distance to the shower axis yields the lateral density distribution of the hadronic or muonic component of extensive air showers, see e.g., \([24]\). In such a case, \( r_M \) is usually treated as a free parameter, its value depends on the particle types a detector is sensitive to (electrons, converted photons, muons, hadrons) and the detection thresholds for the various particle species.

For the reconstruction of the shower parameters, it is convenient to transform the detector coordinates into the shower frame of reference. The origin of the shower frame is taken as the center of the detector array with the z-axis taken along the shower axis and the x-y plane containing the shower plane. The reconstruction needs to be done in several steps. First, proper starting values of the air shower parameters need to be provided to initiate the minimization procedure. For the position of the shower axis \((X_c, Y_c)\) in the shower frame, a good starting value can be obtained, using the center of gravity of the energy depositions

\[
X_c = \frac{\sum_i X_i n_i}{\sum_i n_i} ; \quad Y_c = \frac{\sum_i Y_i n_i}{\sum_i n_i}.
\]  

where \((X_i, Y_i)\) denote the coordinates of the detectors in the shower frame and the summation is over the 4 detectors which recorded the highest energy depositions.

Using \((4)\), the measured lateral density at the position of the \(i^{th}\) detector \((X_i, Y_i)\) in the shower frame can be written as

\[
n_i(X_i, Y_i) = N_{ch} F_i(X_i, Y_i).
\]  

\(F_i(X_i, Y_i)\) represents the normalized lateral density distribution function

\[
F_i(X_i, Y_i) = C(s) \left( \frac{r_i}{r_{M}} \right)^{s-2} \left( 1 + \frac{r_i}{r_{M}} \right)^{-s-4.5},
\]  

where \(r_i = \sqrt{(X_i - X_c)^2 + (Y_i - Y_c)^2}\) is the distance of \((X_i, Y_i)\) from the position of the shower axis \((X_c, Y_c)\) in the shower frame. Summing \((7)\) over the number of detectors, we obtain

\[
\sum_{i=1}^{k} n_i(X_i, Y_i) = N_{ch} \sum_{i=1}^{k} F_i(X_i, Y_i).
\]  

We determine the staring value of \(N_{ch}\) using \((9)\). Averaged values of \(r_M\) and \(s\) for the measured showers are \(r_M = 30\) m and \(s = 1.7\). We take this value for \(r_M\) as initial value for the fit, while \(s\) is kept constant throughout the minimization process. Fitting \(r_M\) and \(s\) simultaneously is known to give poor results because of the strong correlation between them. Simulation studies with CORSIKA have shown that fixing \(s\) gives better results than fixing \(r_M\) (see \([24]\)). We have checked that choosing the starting value of \(r_M\) in the range of \((20 - 90)\) m produces almost the same final values of the fit parameters.

In the first minimization step, we fix \(r_M\) and keep the others \((X_c, Y_c, N_{ch})\) as free parameters. In the second step, we take two parameters \(r_M\) and \(s\). The NKG function has been originally derived for electromagnetic cascades with a constant \(r_M\). However, in practice the NKG function is also used to fit lateral distributions of the hadronic or muonic component of extensive air showers, see e.g., \([22, 23]\). In such a case, \(r_M\) is usually treated as a free parameter, its value depends on the particle types a detector is sensitive to (electrons, converted photons, muons, hadrons) and the detection thresholds for the various particle species.
the results given by the first fit as starting values. Then, we fix $(X_c, Y_c)$ and fit the parameters $(r_M, N_{ch})$. These minimization steps are typically iterated three times with the outputs of each iteration, taken as the starting values for the next iteration. For the position of the shower axis, the result of the last iteration is taken as final value. This value can be further transformed into the position of the shower axis on the ground $(x_c, y_c)$, following a proper coordinate transformation. For $N_{ch}$ and $r_M$, we go one step further. After the last iteration, we determine the lateral density distribution as a function of the radial distance from the position of the shower axis. Then, we fit the measured lateral distribution with (4) and determine the final values of $N_{ch}$ and $r_M$.

The reconstructed quantities are shown in Fig. 7 for illustration. The reconstructed azimuth angle $\phi$ is indicated by the arrow on the left panel. The star in the right panel represents the reconstructed position of the shower axis on the ground. The lateral distribution of the event shown in Fig. 7 is depicted in Fig. 8. The reconstructed number of charged particles and the radius parameter are found to be $N_{ch} = (5.5 \pm 0.2) \times 10^6$ and $r_M = 37.2 \pm 2.3$ m, respectively.

6. Reconstruction accuracies

The accuracies in the reconstruction of air shower parameters are determined from the data itself using the divided-array method. We divide the full array into two arrays with larger spacing and compare the reconstructed parameters of the two parts. This technique has its limitations as it will not be sensitive to systematic biases and an additional penalty is applied by reducing the number of measurements per event. However, it gives a good impression of the capabilities of the array. A study based on air shower simulations is currently underway. This will give a more accurate picture, which is needed for more in-depth analyses of the data.

For the accuracy in the position of the shower axis, we calculate the difference between the estimates of the two half arrays

$$\Delta_{pos}^{12} = \sqrt{(x_1 - x_2)^2 + (y_1 - y_2)^2},$$

where $(x_1, y_1)$ and $(x_2, y_2)$ are the reconstructed positions of the shower axis on the ground with the two sub-arrays, respectively. Then, the reconstruction accuracy for the full array $\sigma_{pos}$ is calculated as,

$$\sigma_{pos} = \frac{\Delta_{pos}^{12}}{\sqrt{2}}$$

where $\sigma_{pos}^{12}$ denote the spread of the distribution of $\Delta_{pos}^{12}$.

For the arrival direction accuracy, we calculate the space angle difference between the estimates of the two sub-arrays as,

$$\Delta_{ang}^{12} = \cos^{-1} \left[ \sin\theta_1 \sin\theta_2 \cos(\phi_1 - \phi_2) + \cos\theta_1 \cos\theta_2 \right]$$

where $(\theta_1, \phi_1)$ and $(\theta_2, \phi_2)$ are the arrival directions (zenith and azimuth angle) reconstructed with the two sub-arrays. For the accuracy in the number of charged particles, the difference between the two sub-arrays is calculated relative to the number given by the full array as,

$$\Delta_{ch}^{12} = \left( \frac{N_{ch}^1 - N_{ch}^2}{N_{ch}} \right)$$

where $N_{ch}^1$, $N_{ch}^2$ are the number of particles given by the two sub-arrays and $N_{ch}$ is the number given by the full array. The reconstruction accuracies for the arrival direction and the number of particles are then calculated using a similar relation as given by (11).

Figure 9 shows the reconstruction accuracies, derived from the data as a function of the number of particles determined from the full array, see Table 1 for the applied quality criteria. The panels in the figure correspond to the number of particles, arrival direction, and the position of the shower axis, respectively. The reconstruction accuracies for showers with a number of charged particles $lg N_{ch} \gtrsim 6$ are within approximately 32% for the number of charged particles, 0.7° for the arrival direction, and 6 m for the position of the shower axis on the ground.

7. Performance of the array

For the following analysis air showers have been selected that trigger at least 5 detectors with a minimum particle density of 1 particle m$^{-2}$ and which have characteristic radii in the range of (10 – 200) m, see also Table 1. The spatial distribution of the reconstructed shower axes is depicted in Fig. 10. The left-hand panel shows the positions for all showers. On the right-hand side, only showers with a total number of charged particles $lg N_{ch} > 6.25$ are selected. The full set is dominated by low-energy showers, which show inhomogeneities, caused by the non-regular spatial arrangement of the scintillation detectors (left-hand side). This threshold effect vanishes at higher energies, which correspond to larger values of $N_{ch}$. Above $lg N_{ch} = 6.25$ one recognizes that the showers are reconstructed more uniformly. The squares in the figure represent detector positions and the circle represents a fiducial area of radius 150 m around the array center. For our analysis in the following, we only select those air showers with position of the shower axis falling within this fiducial area. This area is chosen such that we include in our analysis only those air showers with reliable estimates of the position of the shower axis and at the same time, retain as many showers as possible.

Figure 11 shows the zenith angle and the azimuthal angle distribution of the reconstructed showers. The zenith angle distribution is fitted in the range of $(45^\circ - 40^\circ)$ with the distribution
Figure 9: Measured reconstruction accuracies: number of charged particles $N_{ch}$ (left), arrival direction (right) and position of the shower axis on the ground (bottom) as a function of the number of charged particles in a shower. For showers with $\lg N_{ch} \gtrsim 6$, the accuracies are $\lesssim 32\%$ for the number of particles, $\lesssim 0.7^\circ$ for the arrival direction, and $\lesssim 6\,\text{m}$ for the position of the shower axis. These values are indicated by the dashed lines in the figures.

The fit parameters are found to be $a_1 = (1.073 \times 10^4 \pm 71)$ and $a_2 = (8.786 \pm 0.062)$. The thick curve in the figure represents the fit result. The peak of the distribution is found to be at $\theta \sim 19^\circ$. The steep rise in the distribution below the peak is due to the increase in the solid angle with the zenith angle. The steep fall above the peak is due the combined effect of the decrease in the effective collection area of the array and the increase in the shower attenuation at larger zenith angles. The effect of the attenuation is expected to be more significant for showers initiated by low-energy primaries.

The azimuth distribution is almost uniform at all angles. This is expected because of the high level of isotropy in the arrival directions of cosmic rays of this energy range which is related to their diffusive nature of propagation in the Galaxy. However, there is some structure visible. This is due to the irregular positioning of the detectors. For different azimuth angles the projected distances between detectors get smaller or wider, which affects the reconstruction. The structure is, however, not severely affecting the uniformity. This is illustrated by the horizontal line in Fig.11 which represents a straight line fit to the measured distribution, illustrating what equally distributed azimuth angles would look like. This fit shows a $\chi^2/\text{ndof}$ of close to one.

8. Conclusions

LORA is an air shower array that has been built for cosmic-ray measurements with LOFAR. Its primary purpose is to trigger the read-out of the LOFAR radio antennas for cosmic-ray events and to provide basic air shower properties, such as the position of the shower axis, the arrival direction, and the energy of the primary particle. The full set-up of the LORA array was completed in June 2011. It currently operates as standard triggering tool for the air shower detection with LOFAR.

The array is comprised of 20 scintillation detectors and measures the arrival direction of high-energy air showers (with $\lg N_{ch} > 6$) on average with an accuracy better than $0.7^\circ$, the position of the shower axis better than $6\,\text{m}$, and the number of charged particles better than $32\%$. 

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Figure 10: Distribution of the reconstructed positions of the axis for measured air showers. Left: all showers. Right: only showers with a number of charged particles \( \log N_{ch} > 6.25 \). Only showers with characteristic radii in the range \( 10 \text{ m} \leq r_M \leq 200 \text{ m} \) are included in the distribution. The open squares denote detector positions and the circle represents a fiducial area of radius 150 m around the center of LORA, chosen for our analysis.

Figure 11: Distribution of angles of the arrival direction of air showers measured with positions of the shower axis within the fiducial area (within 150 m from the center of LOFAR) and characteristic radii in the range \( 10 \text{ m} \leq r_M \leq 200 \text{ m} \). Left: Zenith angle distribution. The thick line is a fit using (14) in the range of \( 4^\circ \leq \theta \leq 40^\circ \). The fit parameters are found to be \( a_1 = (1.073 \times 10^4 \pm 71) \) and \( a_2 = (8.786 \pm 0.062) \). Right: Azimuth distribution. The azimuth is measured eastwards from the north. The horizontal line represents a straight line fit to the distribution.

The air-shower information determined by LORA is used as input for the reconstruction of air shower properties with the LOFAR radio antennas. The measured air showers are also used to optimize a radio-only trigger for LOFAR.

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References