Improved Direct Measurement of $A_b$ and $A_c$ at the $Z^0$ Pole Using a Lepton Tag

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The parity violation parameters $A_b$ and $A_c$ of the $Z b b$ and $Z c c$ couplings have been measured directly, using the polar angle dependence of the polarized cross sections at the $Z^0$ pole. Bottom and charmed hadrons were tagged via their semileptonic decays. Both the electron and muon analyses...
Parity violation in the $Zf\bar{f}$ coupling can be measured via the observables $A_f = 2v_f a_f/(v_f^2 + a_f^2)$, where $v_f$ and $a_f$ represent the vector and axial vector couplings to fermion $f$. In particular, for $f = b$, $A_b$ is largely independent of propagator effects that modify the effective weak mixing angle, and thus provides an unambiguous test of the standard model.

The Born-level differential cross section for the process $e^+e^- \rightarrow Z^0 \rightarrow f\bar{f}$ is

$$d\sigma_f/dz \propto (1 - A_e P_e) (1 + z^2) + 2A_f(A_e - P_e)z,$$

(1)

where $P_e$ is the electron beam longitudinal polarization [$P_e > 0$ for right-handed (R) polarization] and $z$ is the cosine of the polar angle of the outgoing fermion with respect to the incident electron. The ability to modulate the sign of $P_e$ allows the final-state quark coupling $A_f$ to be extracted independently of $A_e$ from a fit to the differential cross section. Thus, the measurements of $A_f$ described here are unique, and complementary to other electroweak measurements performed at the $Z^0$ pole [1].

This Letter reports the results of the 1996–1998 SLD lepton tag analysis, for which identied electrons and muons were used to tag the flavor of the underlying heavy quark. The data sample used in this analysis is roughly three times larger than that of previously reported results [2]. Further statistical and systematic advantage is provided by improvements to the data analysis which take advantage of the precise information provided by the new vertex detector (VXD3) [3] that was installed just prior to the 1996 data run.

The Stanford Linear Collider (SLC) and its operation with a polarized electron beam have been described elsewhere [4]. During the 1996–1998 run, the SLC Large Detector (SLD) [5] recorded an integrated luminosity of 14.0 pb$^{-1}$ at a mean center of mass energy of 91.24 GeV, with a luminosity-weighted electron beam polarization of $|P_e| = 0.7336 \pm 0.0038$ [6].

Charged particle tracks are reconstructed in the central drift chamber (CDC) and the charge-coupled-device-based vertex detector in a uniform axial magnetic field of 0.6 T. For the 1996–1998 data, the combined CDC and VXD3 impact parameter resolution in the transverse (longitudinal) direction with respect to the beam is 7.7 (9.6) $\mu$m at high momentum, and 34 (34) $\mu$m at $p_\perp \sqrt{\sin \theta} = 1$ GeV/$c^2$, where $p_\perp$ and $\theta$ are the momentum transverse to and angle relative to the electron beam direction. The liquid argon calorimeter (LAC) measures the energy and shower profile of charged and neutral particles with an electromagnetic energy resolution of $\sigma_E/E = 15\%/\sqrt{E}(\text{GeV})$ and is used in the electron identification. The warm iron calorimeter (WIC) detects charged particles that penetrate the 3.5 interaction lengths of the LAC and magnet coil. The Cherenkov Ring Imaging Detector (CRID) measures the velocity of charged tracks in the region $|\cos \theta| < 0.68$ using the number and angle of Cherenkov photons emitted in liquid and gaseous radiators; electrons are well separated from pions in the region between 2 and 5 GeV/$c$, while pion (kaon) rejection reduces backgrounds to the muon sample in the region $2 < p < 5(2 < p < 15)$ GeV/$c$.

The axis of the jet nearest in angle to the lepton candidate is used to approximate $z$, the cosine of the polar angle of the underlying quark. Jets are formed from calorimeter energy clusters (including any associated with the lepton candidate) using the JADE algorithm [7] with parameter $x_{\text{cut}} = 0.005$. The analyses presented here make substantial use of “secondary” decay vertices which are displaced from the primary interaction point, identified via the ZVTOP topological vertexing algorithm [8], as well as the invariant mass of the tracks comprising the secondary vertex (“vertex mass”), corrected to account for unmeasured neutral particles [9].

The selection of electron and muon candidates with $p > 2$ GeV/$c$ in hadronic $Z^0$ decays has been described previously [2]. Electrons are identified with both LAC and CRID information for CDC tracks in the angular range $|\cos \theta| < 0.72$. Electrons from photon conversions are recognized and removed with 73% efficiency. WIC information is also included for muons, providing an essential measurement of their penetration. Muons are identified in the angular region $|\cos \theta| < 0.70$, although the identification efficiency falls rapidly for $|\cos \theta| > 0.60$ due to the limited angular coverage of the WIC. To reduce backgrounds from misidentification, the 29% of events containing electron candidates that had no reconstructed secondary vertices were removed from the sample, precluding the use of the electron sample for the measurement of $A_e$.

For $p > 2$ GeV/$c$, Monte Carlo (MC) studies indicate efficiencies (purities) of 64% (64%) and 81% (68%) for the electron and muon samples, respectively, where the remaining electrons from photon conversion account for 5% of the 12862 electron candidates. In the case of the muon sample (21199 candidates), the background is due both to misidentification (8% of muon candidates) and to real muons from light hadron decays (25%). In both cases, the MC simulation has been verified with a control sample of pions from $K_0^\pm \rightarrow \pi^+\pi^-$ decays. The fraction of such pions misidentified as electrons is (1.02 ± 0.06)%, consistent with the MC expectation of (1.06 ± 0.03)%.

For muons, the measured pion misidentification fraction is (0.342 ± 0.028)%, somewhat higher than the MC expectation of (0.279 ± 0.012)%.

This difference has been accounted for by raising the background level in the
maximum likelihood fit to the muon sample by $(20 \pm 10)\%$ of itself.

The sample of events containing identified leptons is composed of the following event types (charge conjugates implied): $Z^0 \to b\bar{b}, b \to l$ ("$bl$"), $Z^0 \to b\bar{b}, b \to \bar{c} \to l$ ("$b\bar{c}l$"); $Z^0 \to b\bar{b}, \bar{b} \to \bar{c} \to l$ ("$b\bar{c}l$"); $Z^0 \to c\bar{c}, \bar{c} \to l$ ("$c\bar{c}l$"); and background from light hadron and vector meson decays, photon conversions, and misidentified hadrons ("$bk$")

Identification of electron candidate event types is based on the values of eight discriminating variables [10]: track momentum ($p_t$), momentum transverse to the nearest jet ($p_\perp$), the estimate of the underlying B hadron boost [11], and when available, same hemisphere secondary vertex mass, opposite hemisphere vertex mass, same hemisphere vertex momentum resultant, same hemisphere vertex signficance (separation $D$ between the interaction point and secondary vertex, divided by its uncertainty), and $L/D$ (where $L$ is the distance from the interaction point to the point on the secondary vertex trajectory closest to the electron candidate trajectory). These variables are used as inputs to an artificial neural network with three output nodes $N_{bl}$, $N_{c\ell}$, and $N_{cl}$, optimized for the $bl$, $b\bar{c}l + b\bar{c}l$, and $c\bar{c}l$ signals, respectively. Event type probabilities are estimated according to the composition of MC electron candidate events with similar output node values. The measured and simulated distributions of the three output node candidates are compared in Fig. 1.

The neural network is trained on the SLD MC sample of hadronic $Z^0$ decays, generated with JETSET 7.4 [12]. Semileptonic decays of $B$ mesons are generated according to the ISGW formalism [13] with a $23\% D^{*+}$ fraction, while semileptonic decays of $D$ mesons are simulated according to branching ratios reported by the Particle Data Group [14]. Experimental constraints are provided by the $B \to l$ and $B \to D$ inclusive momentum spectra measured by the CLEO Collaboration [15,16] and the $D \to l$ momentum spectrum measured by the DELCO Collaboration [17]. The detailed simulation of the SLD detector response has been realized using GEANT [18].

Muon candidate event type probabilities are estimated according to the composition of MC muon candidate events with similar values of the following discriminating variables [19]: $p_t$, $p_\perp$, and, when available, $L/D$ and $M_{max}$, the largest of the secondary vertex invariant masses. The measured and simulated distributions of these variables are compared in Fig. 2.

A maximum likelihood analysis of all selected hadronic $Z^0$ events containing lepton candidates is used to determine $A_b$ and $A_c$. The likelihood function contains the following probability term for each lepton, with measured charge sign $Q$:

$$P(P_{e}, z; A_b) \propto (1 + z^2)(1 - A_e P_{e}) - 2Q(A_e - P_{e})[(f_{bl}(1 - 2\bar{x}_b) - f_{b\bar{c}l}(1 - 2\bar{x}_{b\bar{c}}) + f_{b\bar{c}l}(1 - 2\bar{x}_{b\bar{c}}))(1 - \Delta^2_{QCD}(z))A_b - f_{c\bar{c}l}(1 - \Delta^2_{QCD}(z))A_c + f_{bk}A_{bk}z].$$

(2)

The lepton source fractions $f_{bl}, f_{b\bar{c}l}, f_{k\bar{c}l}, f_{c\bar{c}l}$, and $f_{bk}$ are functions of the three neural net output node values (electron candidates) or the four discriminating variables (muon candidates). For the fit to muon candidates, both $A_b$ and $A_c$ are left as free parameters, whereas $A_e$ is fixed to its SM value (see Table I) for the fit to electron candidates.

FIG. 1. Distribution of data and MC electron candidates in the various NN output node variables.

FIG. 2. Distributions of data and MC muon candidates.
Correction factors $1 - 2\bar{\chi}_x$, where $\chi_x$ is the mixed fraction for lepton source $x$, are applied to $b$-quark lepton sources to account for asymmetry dilution due to $B^0\bar{B}^0$ mixing. The value of $\bar{\chi}_{b\bar{b}}$ is taken from LEP measurements of the average mixing in semileptonic $B$ decays [1], but must be corrected to take into account selection and fitting bias, including that due to the enhanced likelihood for $b\bar{c}$ cascade leptons to have come from a $B$ meson which has mixed [20]. For the electron sample, MC studies indicated that the mixing probability $\bar{\chi}_{b\bar{b}}$ for $bl$ decays was independent of the value of the NN output parameters, but was increased by a relative 1.7% overall by the bias of the vertex requirement towards the selection of $B^\circ$ over $B^\pm$ decays. For the muon sample, the effective values of $\bar{\chi}_{b\bar{b}}$ and $\bar{\chi}_{bb\bar{b}}$ were evaluated on an event-by-event basis, based on MC events with values of the muon-sample discriminating variables close to those of the given data event.

The asymmetry in the background $A_{bb}$ is parametrized as a function of $p$ and $p$. For the electron sample, the parametrization is determined from tracks in the data not identified as leptons. For the muon sample, MC studies indicated a substantial difference between the true background asymmetry and that of nonleptonic tracks, and so the background asymmetry parametrization was determined directly from the MC simulation.

A $z$-dependent correction factor $[1 - \Delta_{QCD}(z)]$ is included in the likelihood function to incorporate the effects of gluon radiation. Calculation of the quantity $\Delta_{QCD}(z)$ has been performed by several groups [21]. For an unbiased sample of $bb$ or $c\bar{c}$ events with $|z| < 0.7$, correcting for this effect increases the measured asymmetry by $\sim 3\%$ overall. However, a MC simulation of the analysis chain indicates that biases which favor $q\bar{q}$ events over $q\bar{g}$ and $g\bar{g}$ events mitigate the effects of leading order gluon radiation by about 30%. Effects due to gluon splitting to $b\bar{b}$ and $c\bar{c}$ have been estimated by rescaling the JETSET simulation to world average gluon splitting measurements [22]. Additional radiative effects, such as those due to initial-state radiation and $\gamma/Z$ interference, lead to a further correction of $-0.2\%(-0.1\%)$ on the value of $A_b(A_c)$.

A list of systematic errors is shown in Table I. The purity of the separation of $Z^0 \to bb$ and $Z^0 \to c\bar{c}$ events via secondary vertex information introduces an uncertainty dominated by the efficiency of charged track reconstruction, which has been constrained by reweighting MC tracks by the ratio of the number of tracks in data and MC as a function of $p$ and $p$. The ability of the L/D variable to discriminate between $bl$ and $b\bar{c}l$ decays is sensitive to the fraction of $B \to D\bar{D}$ decays, which has been constrained from SLD data [19].

### TABLE I. Systematic errors.

<table>
<thead>
<tr>
<th>Source</th>
<th>Parameter variation</th>
<th>$\delta A_b(\mu)$</th>
<th>$\delta A_b(\epsilon)$</th>
<th>$\delta A_c(\mu)$</th>
</tr>
</thead>
<tbody>
<tr>
<td>Monte Carlo statistics</td>
<td>Includes neural net training for $e$</td>
<td>$\pm 0.005$</td>
<td>$\pm 0.014$</td>
<td>$\pm 0.023$</td>
</tr>
<tr>
<td>Jet axis simulation</td>
<td>10 mrad smearing</td>
<td>$\pm 0.002$</td>
<td>$\pm 0.006$</td>
<td>$\pm 0.002$</td>
</tr>
<tr>
<td>Background level</td>
<td>$\pm 10%$ relative</td>
<td>$\pm 0.003$</td>
<td>$\pm 0.004$</td>
<td>$\pm 0.010$</td>
</tr>
<tr>
<td>Background asymmetry</td>
<td>$\pm 40%$ relative</td>
<td>$\pm 0.002$</td>
<td>$\pm 0.003$</td>
<td>$\pm 0.007$</td>
</tr>
<tr>
<td>$BR(Z^0 \to bb\bar{b})$</td>
<td>$R_b = 0.2164 \pm 0.0007$</td>
<td>$\pm 0.000$</td>
<td>$\pm 0.000$</td>
<td>$\pm 0.001$</td>
</tr>
<tr>
<td>$BR(Z^0 \to c\bar{c})$</td>
<td>$R_c = 0.1674 \pm 0.0038$</td>
<td>$\pm 0.001$</td>
<td>$\pm 0.000$</td>
<td>$\pm 0.008$</td>
</tr>
<tr>
<td>$BR(b \to l)$</td>
<td>$(10.62 \pm 0.17)%$</td>
<td>$\pm 0.003$</td>
<td>$\pm 0.003$</td>
<td>$\pm 0.003$</td>
</tr>
<tr>
<td>$BR(b \to \bar{c} \to l)$</td>
<td>$(8.07 \pm 0.25)%$</td>
<td>$\pm 0.003$</td>
<td>$\pm 0.003$</td>
<td>$\pm 0.003$</td>
</tr>
<tr>
<td>$BR(b \to \bar{c} \to l)$</td>
<td>$(1.62 \pm 0.40)%$</td>
<td>$\pm 0.006$</td>
<td>$\pm 0.001$</td>
<td>$\pm 0.011$</td>
</tr>
<tr>
<td>$BR(b \to \tau \pm l)$</td>
<td>$(0.452 \pm 0.074)%$</td>
<td>$\pm 0.003$</td>
<td>$\pm 0.001$</td>
<td>$\pm 0.002$</td>
</tr>
<tr>
<td>$BR(b \to l/P^\pm l)$</td>
<td>$(0.07 \pm 0.02)%$</td>
<td>$\pm 0.003$</td>
<td>$\pm 0.002$</td>
<td>$\pm 0.000$</td>
</tr>
<tr>
<td>$BR(c \to l)$</td>
<td>$(9.85 \pm 0.32)%$</td>
<td>$\pm 0.001$</td>
<td>$\pm 0.001$</td>
<td>$\pm 0.012$</td>
</tr>
<tr>
<td>$B$ lept. spect. - $D^{**}$ fr.</td>
<td>$(23 \pm 10)%, B^+; (32 \pm 10)%, B_s$</td>
<td>$\pm 0.003$</td>
<td>$\pm 0.002$</td>
<td>$\pm 0.001$</td>
</tr>
<tr>
<td>$D$ lept. spect.</td>
<td>ACCMM1 (&quot;MCCM2&quot;) [23]</td>
<td>$\pm 0.004$</td>
<td>$\pm 0.004$</td>
<td>$\pm 0.002$</td>
</tr>
<tr>
<td>$B_t$ fraction in $bb$ event</td>
<td>$0.115 \pm 0.050$</td>
<td>$\pm 0.001$</td>
<td>$\pm 0.004$</td>
<td>$\pm 0.001$</td>
</tr>
<tr>
<td>$B_{bb}$ fraction in $bb$ event</td>
<td>$0.072 \pm 0.030$</td>
<td>$\pm 0.002$</td>
<td>$\pm 0.002$</td>
<td>$\pm 0.001$</td>
</tr>
<tr>
<td>$b$ fragmentation</td>
<td>$e_b = 0.0045-0.0075$ [12]</td>
<td>$\pm 0.001$</td>
<td>$\pm 0.004$</td>
<td>$\pm 0.002$</td>
</tr>
<tr>
<td>$c$ fragmentation</td>
<td>$e_c = 0.045-0.070$ [12]</td>
<td>$\pm 0.003$</td>
<td>$\pm 0.000$</td>
<td>$\pm 0.012$</td>
</tr>
<tr>
<td>Polarization</td>
<td>$P_{P} = 73.4 \pm 0.4$</td>
<td>$\pm 0.005$</td>
<td>$\pm 0.005$</td>
<td>$\pm 0.003$</td>
</tr>
<tr>
<td>QCD corrections</td>
<td>$\alpha_s$, gluon splitting, selection bias</td>
<td>$\pm 0.005$</td>
<td>$\pm 0.005$</td>
<td>$\pm 0.005$</td>
</tr>
<tr>
<td>Gluon splitting</td>
<td>$g_{cc} = (2.33 \pm 0.50)%; g_{bb} = (0.27 \pm 0.07)%$</td>
<td>$\pm 0.001$</td>
<td>$\pm 0.001$</td>
<td>$\pm 0.002$</td>
</tr>
<tr>
<td>$B$ mixing $\chi_b$</td>
<td>$\chi = 0.1186 \pm 0.0043$</td>
<td>$\pm 0.010$</td>
<td>$\pm 0.011$</td>
<td>$\pm 0.000$</td>
</tr>
<tr>
<td>$N_{b}/N_{D_s}$ in $B$ decay</td>
<td>$\pm 10%$</td>
<td>$\pm 0.002$</td>
<td>$\pm 0.001$</td>
<td>$\pm 0.003$</td>
</tr>
<tr>
<td>$B$ tag purity</td>
<td>Track efficiency</td>
<td>$\pm 0.012$</td>
<td>$\pm 0.014$</td>
<td>$\pm 0.053$</td>
</tr>
<tr>
<td>L/D variable</td>
<td>Data/MC comparison</td>
<td>$\pm 0.002$</td>
<td>$\pm 0.000$</td>
<td>$\pm 0.005$</td>
</tr>
<tr>
<td>Neural net training</td>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>$B \to D\bar{D} \to l$</td>
<td>$(11.5 \pm 2.5)%$</td>
<td>$\pm 0.010$</td>
<td>$\pm 0.008$</td>
<td>$\pm 0.003$</td>
</tr>
<tr>
<td>$A_c$</td>
<td>$0.667 \pm 0.030$</td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>Total systematic</td>
<td></td>
<td>$\pm 0.024$</td>
<td>$\pm 0.028$</td>
<td>$\pm 0.064$</td>
</tr>
</tbody>
</table>
For the 1996–1998 muon sample, we find that $A_b = 0.938 \pm 0.044$(stat) $\pm 0.024$(syst) and $A_c = 0.560 \pm 0.063$(stat) $\pm 0.064$(syst), with a statistical correlation coefficient of 0.108. For the corresponding electron sample, we find $A_b = 0.896 \pm 0.050$(stat) $\pm 0.028$(syst). Combined with the result of [2], we find overall SLD average results via semileptonic $B$ and $D$ hadron decay of

$$A_b = 0.919 \pm 0.030$(stat) $\pm 0.024$(syst)$$

$$A_c = 0.583 \pm 0.055$(stat) $\pm 0.055$(syst).$$

In conclusion, we have directly measured the extent of parity violation in the coupling of $Z^0$ bosons to $b$ and $c$ quarks using identified charged leptons from semileptonic decays. The results presented here take advantage of an additional sample of 400,000 $Z^0$ decays, and employ a new method of signal source separation, resulting in substantial increases in precision relative to previous measurements [2]. These results are in agreement with the standard model predictions $A_b = 0.935$ and $A_c = 0.667$, which are insensitive to uncertainties in standard model parameters such as the strong and electromagnetic coupling strengths, and the top quark and Higgs boson masses.

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[18] GEANT 3.21 program, CERN Applications Software Group, CERN Program Library.
[20] See I. Dunietz, Fermilab-Pub-96/104-T. For the SLD sample, the magnitude of this effect was estimated from the MC to increase the mean mixing parameter for $b \rightarrow c(c) \rightarrow l$ decays by 8.7%.