Rotation measure synthesis at the 2 m wavelength of the FAN region: Unveiling screens and bubbles.

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ABSTRACT

Context. Rotation Measure synthesis of the Westerbork Synthesis Radio Telescope (WSRT) observations at $\lambda \sim 2$ m of the FAN region at $b=\pm 3^\circ$ shows the morphology of structures in the ionized interstellar medium. 

Aims. We interpret the diffuse polarized synchrotron emission in terms of coherent structures in the interstellar medium and the properties of the interstellar magnetic field.

Methods. We performed statistical analysis of the polarization data cube obtained through Rotation Measure synthesis. For the first time, cross-correlation is applied to identify and characterize polarized structures in Faraday depth space. Complementary information about the medium are derived from H\textsc{v} emission, properties of nearby pulsars, and optical polarized starlight measurements.

Results. We find an overall asymmetric Faraday dispersion function in a Faraday depth range of $[-13, +5]$ rad m$^{-2}$, which is peaked around $-1$ rad m$^{-2}$. Three morphological patterns are recognized, showing structures on scales from degrees down to the beam size. The first structure is a nearby synchrotron emission component with low Faraday depth, filling the entire field of view. The second is a circular polarization structure with enhanced (negative) Faraday depth, which has the same morphology as a low-emission region within the third component. This third component is interpreted as the background in which the circular structure is embedded. At low Faraday depth values, a low gradient across the imaged field is detected, almost aligned with the Galactic plane. Power spectra of polarized structures in Faraday depth space provide evidence of turbulence.

Conclusions. A sign reversal in Faraday depth from the nearby component to the circular component indicates a reversal of the magnetic field component along the line of sight, from towards the observer and nearby to away from the observer at large distances. The distance to the nearby, extended component is estimated as $\lesssim 100$ pc, which suggests that this structure corresponds to the Local Bubble wall. For the circular component, various physical interpretations are discussed. The most likely explanation is that the circular component seems to be the presence of a nearby ($\sim 200$ pc away) relic Strömgren sphere, associated with an old unidentified white dwarf star and expanding in a low-density environment.

Key words. ISM:general - ISM:bubble - ISM:magnetic fields - Galaxy:local interstellar matter - techniques:polarimetric - radio continuum:ISM

1 Introduction

The study of the magneto-ionic properties of the interstellar medium (ISM) by multi-frequency polarimetry started in 1960 with the Dwingeloo radio telescope (Westerhout et al. 1962). A breakthrough came much later when Wieringa et al. (1993) acknowledged the importance of small angular scale structures (down to a few arcmins) in polarized intensity (PI) or polarization angle with no detection in total intensity. Such a fine structure was explained in terms of Faraday rotation of the diffuse, linearly polarized, Galactic synchrotron radiation background by a highly structured foreground magneto-ionic medium. The cosmic rays propagating through the Galactic magnetic field are responsible for the radio synchrotron emission, and the magneto-ionic medium is primarily the warm ionized ISM. As a result polarimetric observations of the Galaxy provide insight into the ionized ISM and the Galactic magnetic field.

The FAN region is a highly polarized, extended region in the second Galactic quadrant at low Galactic latitudes. Its polarization properties were first investigated by Bingham & Shakeshaft (1967), who discovered a circular structure in the rotation measure (RM) map. From higher angular resolution observations, Verschuur (1969) suggested a connection of the observed structure with the B2 IV:e star HIP 15520 that is located close to the centre of the circular structure.

Haverkorn et al. (2003) presents multi-frequency polarimetry radio observations at five wavelengths in the range of $\lambda = 0.80 - 0.88$ m. They point out a ring structure in PI along with an extended pattern of depolarization canals in maps of polarized intensity. They constructed an RM map from these five wavelengths and interpret the ring as a purely magnetic flux tube.

Bernardi et al. (2009) observed the FAN region at $\lambda = 1.93 - 2.16$ m in order to characterize the properties of the foreground for epoch of re-ionization experiments. They detected total intensity and polarization fluctuations for the first time in the Galactic diffuse foreground emission at this wavelength. Rotation measure synthesis (RM-synthesis) was used to image this region in the sky revealing a complex and structured distribution of polarized signals.

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In this paper, we re-analyse the data from Bernardi et al. to study the diffuse Galactic polarized emission. In Section 2 we present the data and illustrate the working principle of RM synthesis technique. In Section 3 we describe the main properties of total and polarized intensity. In Section 4 the polarized data in Faraday depth space are discussed. In Section 5 we describe the main components and their properties. In Section 6 we present a simple model to explain the observed structures and their features. Finally in Section 7 we summarize and conclude.

2. Data analysis

The data were collected with the east-west Westerbork Synthesis Radio Telescope (WSRT) array in 2007. Baselines between 36 m and 2.7 km were used to obtain good $\delta\nu$-coverage. Data reduction was performed by Gianni Bernardi using the AIPS++ package, and for a description of their reduction we refer to [Bernardi et al. 2009]. The corresponding main properties are given in Table 1. Ionospheric propagation effects are direction- and time-dependent and affect the phase of the signal received by the interferometer. They also affect the polarization, giving rise to time-variable Faraday rotation. Moreover, differential Faraday rotation by the ionosphere will alter Stokes Q and U, which could lead to depolarization but could also lead to spurious extra polarization, thus affecting the results of the polarization imaging. Over the six days of observation the mean total electron content ($N_e$) and the mean intensity of the geomagnetic field (using the International Geomagnetic Reference Field (IGRF10)) give us a typical $RM_{ion} \lesssim 0.3$ rad m$^{-2}$, which implies a phase shift of about 80 degrees at the lower observed frequency. The spread of the $RM_{ion}$ over days of observation is 0.1 rad m$^{-2}$. Since the resolution in Faraday depth is about 3 rad m$^{-2}$ (see Table 1), ionospheric Faraday rotation will hardly change the analysis or conclusions, so that corrections for the ionospheric Faraday rotation were not applied.

To enhance sensitivity for diffuse emission, the resolution of the Stokes Q and U maps was decreased. In this paper we use the full angular resolution Stokes I map (i.e. $\Delta \theta = 2$ arcmin) and Stokes Q,U maps with angular resolution $\Delta \theta = 4.2$ arcmin. No correction was performed for the primary beam attenuation in order to preserve a uniform noise level across the images. In the following section, we summarize the principle of the RM-synthesis technique.

2.1. RM-synthesis

Low frequency polarimetric studies of the diffuse Galactic radio emission are a valuable tool to investigate the ionized and magnetized components of the interstellar medium. Generally, these studies have been based on RM measurements calculated as the slope of a linear fit to the polarization angle as a function of the wavelength squared. However, a new analysis technique has recently been applied, the so-called RM-synthesis [Burn 1966]. This technique has only recently become practically applicable due to technical and computational advances, and was developed and used for the first time by [Brentjens & de Bruyn 2005]. Its main advantages with respect to the standard RM technique are that it provides a mapping of the linearly polarized emission as a function of Faraday depth ($\phi$), the Faraday dispersion function ($F(\phi)$), and that bandwidth depolarization and depth depolarization are much less severe. RM-synthesis is implemented as a weighted (by the sampling function $W(\lambda^2)$) Fourier transform between $F(\phi)$ and the measured complex polarization vector $P(\lambda^2)$:

$$P(\lambda^2) = W(\lambda^2) \int_{-\infty}^{\infty} F(\phi) e^{2i\phi \lambda^2} d\phi,$$

(1)

with the Faraday depth

$$\phi = 0.81 \int_{d_{1}[pc]}^{d_{2}[pc]} n_e B \cdot dl$$

(2)

where the electron density $n_e$ and the magnetic field $B$ are given in cm$^{-3}$ and $\mu G$, respectively. Since we can only sample a finite positive range of wavelengths, the inversion of the Fourier transform is incomplete, and we only get an approximation of $F(\phi)$. However, three physical quantities directly linked to the experimental set up (the channel width $\delta \lambda^2$, the width of the $\lambda^2$ distribution $\Delta \lambda^2$, and the shortest wavelength squared $\lambda^2_{min}$) can be used to characterize the detection capability:

- the maximum detectable Faraday depth, constrained by the channel width $\delta \lambda: \phi_{max} = \sqrt{3/\delta \lambda^2}$;
- the maximum scale detectable in Faraday depth to which the sensitivity is reduced to 50%, which is constrained by the lowest observed wavelength $\lambda_{min}$: $\delta \phi_{scale} = \pi/\lambda^2_{min}$;
- the resolution in Faraday depth space defined as the half power width of the rotation measure spread function (RMSF), constrained by the total wavelength range $\Delta \lambda^2$: $\Delta \phi = 2\sqrt{\Delta \lambda^2/\Delta \lambda^2}$.

This defines the minimum separation between separate synchrotron emitting structures that is detectable.

For our frequency coverage, $\phi_{max} \approx 2650$ rad m$^{-2}$, $\delta \phi_{scale} \approx 0.85$ rad m$^{-2}$, and $\Delta \phi \approx 3$ rad m$^{-2}$. With these data we can therefore only detect Faraday thin structures, since the resolution is greater than the maximum detectable scale. Since the polarized radiation is a vector quantity, astrophysical information is stored in both intensity and angle. However, due to the generally low signal-to-noise ratio (S/N) per resolution element, the solution of the $nn$-ambiguity is challenging so we do not use polarization angle maps for a quantitative derivation, but only to infer some basic properties. For this reason, we focus on polarized intensity maps and maps of Stokes U. Maps of Stokes Q show similar characteristics to Stokes U.

2.2. RM-synthesis data cubes

Maps for Stokes Q,U, and PI were obtained in Faraday depth space by applying the RM-synthesis technique to the 4.2 arcmin Stokes Q,U maps in the frequency domain. No bias correction was applied to the polarized intensity maps but owing to the high side lobe level of the RMSF, an RM CLEAN [Heald et al. 2009] was performed with a threshold of 5 mJy. The polarized emission from our Galaxy is expected at low Faraday depth values $|\phi| \lesssim 10^2$ rad m$^{-2}$ (see Clegg et al. 1992). Inspection of this range of Faraday depth reveals the presence of significant polarized emission only within a few tens of frames around $\phi = 0$ rad m$^{-2}$ [Bernardi et al. 2009]. The PI content of the data out of this range of Faraday depths has not been checked. For the data analysis, we limited the Faraday depth range of this data set to $[-50, +50]$ rad m$^{-2}$.

1 The point spread function in Faraday depth space is generally called the rotation measure spread function.
The only extended Galactic object detected is the H\textsubscript{II} region complex W3/W4/W5 in the south-west corner, approximately from \((\alpha, \delta)_{2000} \approx (02^h25^m, 62^\circ.0)\) to \((\alpha, \delta)_{2000} \approx (02^h53^m, 60^\circ.4)\). The Stokes I emission is also seen from the spiral galaxy IC 342 at \((\alpha, \delta)_{2000} \approx (03^h47^m, 68^\circ.0)\) and from the giant double radio galaxy WNB 0313+683 at \((\alpha, \delta)_{2000} \approx (03^h18^m, 68^\circ.3)\). No large-scale diffuse emission is seen in the primary beam at 150 MHz because the interferometer filters away power on a scale of \(\sim 12\) arcmin for these Stokes I fluctuations.

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### Table 1. Observational set up and basic properties of the RM-synthesis cube, from [Bernardi et al. (2009)]

<table>
<thead>
<tr>
<th>Data</th>
<th>Galactic coordinates</th>
<th>Number of spectral bands</th>
<th>Central frequency of each band</th>
<th>Width of each band</th>
<th>Frequency resolution</th>
<th>Beam size</th>
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<tr>
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<td>2000</td>
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<td></td>
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</tr>
<tr>
<td>(N_{band})</td>
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</tr>
<tr>
<td>(V_{band})</td>
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<td></td>
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<tr>
<td>(\Delta V_{band})</td>
<td>2.5 MHz</td>
<td></td>
<td></td>
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</tr>
<tr>
<td>(\Delta f)</td>
<td>9.8 kHz</td>
<td></td>
<td></td>
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<td></td>
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</tr>
<tr>
<td>(\Delta \phi)</td>
<td>2\arcmin \times 2.2\arcmin</td>
<td></td>
<td></td>
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<td></td>
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<tr>
<td>((\alpha, \delta, \phi))-cube</td>
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<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>(\Delta \phi)</td>
<td>3 rad m(^{-2})</td>
<td></td>
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<td>RMSF width</td>
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<tr>
<td>(\delta \phi_{scale})</td>
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<td>Max scale in (\phi)</td>
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<td>(\delta \theta)</td>
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<td></td>
<td></td>
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</tr>
<tr>
<td>(\xi)</td>
<td>1 mJy beam(^{-1}) = 1 K</td>
<td></td>
<td></td>
<td></td>
<td></td>
<td>Conversion factor</td>
</tr>
</tbody>
</table>

### 3. Observational results

Two well known basic properties of the diffuse polarized emission (see [Wieringa et al. (1993)]) are visible in the images (see e.g. Figs. 2 and 8):

- The intensity attenuation due to the WSRT primary beam (about 2.5\arcmin at 150 MHz). This is a strong argument for excluding an instrumental origin of the polarization fluctuations, and it suggests a wider extent on the sky of the detected emission;
- The absence of a correlation between total intensity and polarized intensity, which indicates that the polarization fluctuations are caused by Faraday rotation of the diffuse synchrotron emission background by the intervening magnetized medium.

In the following sections, we describe the global properties of the signals detected in polarized intensity and total intensity.

#### 3.1. Total intensity

The Stokes I map displayed in Fig. 1 has a size of about 12\arcmin in declination and 12\arcmin in right ascension, and its dynamic range is about 1450:1 at an angular resolution of 2\arcmin \times 2.2\arcmin FWHM. The only extended Galactic object detected is the H\textsubscript{II} region complex W3/W4/W5 in the south-west corner, approximately from \((\alpha, \delta)_{2000} \approx (02^h25^m, 62^\circ.0)\) to \((\alpha, \delta)_{2000} \approx (02^h53^m, 60^\circ.4)\). Faint Stokes I emission is also seen from the spiral galaxy IC 342 at \((\alpha, \delta)_{2000} \approx (03^h47^m, 68^\circ.0)\) and from the giant double radio galaxy WNB 0313+683 at \((\alpha, \delta)_{2000} \approx (03^h18^m, 68^\circ.3)\). No large-scale diffuse emission in the primary beam is seen at 150 MHz because the interferometer filters away power on the largest scales. However, [Bernardi et al. (2009)] detected extended faint, mottled, small-scale total intensity emission from the Galactic foreground. From the power spectrum these authors suggest a minimum spatial scale of \(\sim 12\) arcmin for these Stokes I fluctuations.

#### 3.2. Polarized intensity

Figure 2 shows the polarized intensity at a Faraday depth \(\phi = -1\) rad m\(^{-2}\). Grating rings are seen around brighter compact sources, but owing to their multiplicative nature, such error patterns are only visible around bright Stokes I sources, so their effect is negligible in the map except in the direct vicinity of bright point sources. Unwanted instrumental signals are visible in the Stokes Q, U, and PI maps as elongated stripes and/or waves crossing the field. As pointed out by [de Bruyn & Brentjens (2005)] and [Pizzo et al. (2011)], the WSRT off axis polarization has a strong frequency dependence with a period of 17 MHz, which causes peaks in the Faraday spectrum at about 42 rad m\(^{-2}\).

![Fig. 1. Total intensity map at 150 MHz with an angular resolution of \(\approx 2\arcmin \times 2.2\arcmin\). The diffuse structures towards the upper left and lower right corner are the galaxy IC 342 and the H\textsubscript{II} region complex W3/W4/W5 respectively.](image)

At our frequency range, this 17 MHz ripple appears as a broad peak at the edges of the selected Faraday depth range (see Fig. 2). These are due to sources Cas A and Cyg A entering the telescope side lobes.

The overall properties of the polarized signal distribution as a function of Faraday depth are shown in Figure 3 and an example of Faraday dispersion spectrum is displayed in Figure 3. The distribution of polarized signal includes the whole field, i.e. 480 \times 480 lines of sight. We counted at each Faraday depth the number of pixels having a polarized intensity above a 5 mJy beam\(^{-1}\) threshold (\(\sim 5\) times the PI mean noise level). Polarized emission is detected over a wide range from positive to negative \(\phi\) values. Two main features are clearly seen:

- A central peak at slightly negative \(\phi\) where the most of polarized emission is,
Fig. 2. Frame of the RM-synthesis cube at Faraday depth $\phi = -1 \text{ rad m}^{-2}$ displaying the extended polarized emission. Grating rings can be seen around the bright point sources at $(\alpha, \delta)_{\text{J}2000} \approx (02^h38^m, 59^\circ.1)$ (close to the edge of the image), and $(\alpha, \delta)_{\text{J}2000} \approx (03^h06^m, 62^\circ.5)$. The drawn boxes are chosen to infer the noise behaviour (box 1) and derive the cross-correlation profile (box 2), see text.

Fig. 3. Example of Faraday dispersion spectrum with emission at a single Faraday depth along the line of sight, averaged over a beam-sized box region. The noise level is indicated by $1\sigma$ error bars.

Fig. 4. Distribution of polarized intensity as a function of Faraday depth, above a threshold of 5 mJy. At $|\phi| \geq 40 \text{ rad m}^{-2}$ the residual signal from side lobes of Cyg A and Cas A are visible, while the Galactic emission occurs around $-1 \text{ rad m}^{-2}$ and has an asymmetric profile.

4. The polarization cube in Faraday depth space

In this section we discuss the noise properties and the connection between RMSF width and cross-correlation in Faraday space.

4.1. Noise properties and errors

Since we are dealing with the measurement of a pseudo-vector - i.e. the polarization - in the presence of random noise we look at noise behaviour. While the two Stokes $Q$ and $U$ parameters are Gaussian distributed, the linearly polarized intensity $PI = \sqrt{Q^2 + U^2}$ (3) follows an asymmetric positive definite distribution: the Rice distribution, which is dependent on signal-to-noise and responsible for a bias towards too high values of $PI$ at low $S/N$ [Wardle & Kronberg (1974)].

We tested the Gaussian behaviour of Stokes $Q$ and $U$ maps and estimated the noise in $PI$ as a function of Faraday depth under the assumption of a Rayleigh distribution of polarized intensities. The noise was determined from a small region assumed to contain no emission from the sky, so that all detected emission is noise (see box 1 in figure 2). We assume uniformity of the noise across the field. Since in every Faraday depth frame we detect emission (either from the ISM or from grating lobes from strong out-of-field sources), this uniformity could not be tested. Noise values in Stokes $Q$ and $U$ are similar; also, the assumption of Gaussian noise in Stokes components $Q$ and $U$ is satisfied, because the standard deviation of the sample and the width of fitted normal distribution agree with each other.

The noise properties of $PI$ as a function of the Faraday depth under the assumption of Rayleigh distribution statistics are shown in figure 5. Good agreement is found for the expected (i.e. $\sigma_{PI} = 0.66\sigma_U$) and the measured noise variance, as well as for the expected (i.e. $< \mu_{PI} > = 1.25\sigma_U$) and the measured noise mean value. A mean noise level of $\approx 1 \text{ mJy beam}^{-1}$ is found in $PI$ over a $\phi$ range of $[-50, +25] \text{ rad m}^{-2}$ while an increase in the mean and variance values is seen in the Faraday depth range.

Figure 4 makes it evident that the Galactic emission from this region is concentrated in a very narrow $\phi$ range from about $-10$ to $+5 \text{ rad m}^{-2}$. The main central feature in the distribution is clearly asymmetric; we interpret this as an evidence of a multi-component signal and we discuss this in Sects. 5 and 7.

– two wings towards the edges of our $\phi$ range, due to the residuals from Cas A and Cyg A.

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range above +25 rad m$^{-2}$ due to the presence of residual signal from side lobes of Cyg A and Cas A. Because the Rayleigh statistics a clipping of PI values at 3$\sigma$ allows to mitigate the impact of Ricean bias below 10% level. Since our analysis does not depend on exact values of polarized intensity, but rather uses rough estimates of ISM parameters, bias corrections were not applied.

No corrections for the off-axis instrumental polarization were applied. We estimated its magnitude and radial dependence from the fractional polarization values at $\phi = 0$ rad m$^{-2}$, where instrumental polarization is expected. We found a mean level of $\approx 2\%$ within $3''$ (primary beam), which rises to $\approx 9\%$ at the edges of the field of view. There are not enough sources left in the maps after the subtraction to derive the angular dependence of the antenna pattern.

In analogy to radio interferometric observations, the standard errors in Faraday depth measurements can be obtained in an RM-synthesis cube as: $\sigma_\delta = 0.5\Delta\phi/(S/N) \sim 1.5/(S/N)$ rad m$^{-2}$, where $\Delta\phi$ is the RMSF width and S/N the PI signal-to-noise ratio. Because we mostly deal with spatially extended emission over several ranges of Faraday depths, we prefer to provide a general upper limit for the $\phi$ uncertainty at each frame as set by the mean $S/N$ of the emission across the maps. Because the chosen 3$\sigma$ clip level (i.e., $S/N \geq 3.0$): $\sigma_\phi \leq 0.50$ rad m$^{-2}$. Therefore the total Faraday depth estimation error in our 2 m data consists of two main contributions: the systematic error due to the ionospheric Faraday rotation (as discussed in Section 2), and the standard error (as shown in Figs. 3 and 9), having comparable amplitudes.

4.2. Cross-correlation in $\phi$ space

In RM-synthesis the standard estimator for the nominal resolution in Faraday space is the RMSF width. However, as in aperture synthesis, there is some information present on scales smaller than the beam size, as can be seen in figure 7. This figure shows polarized intensity changes between neighbouring frames (i.e., $\Delta\phi = 1$ rad m$^{-2}$), about one third of the RMSF width. An effective approach to investigating $\phi$-resolution is cross-correlation. Cross-correlation between frames can be used as a probe to infer the presence of structures in the data and their Faraday thickness. We calculate the cross-correlation coefficient for the frames $a$ and $b$ with a frame gap $\delta\phi$ ($C_{\delta\phi}$) as

\[
C_{\delta\phi} = \frac{1}{N-1} \sum_{i,j} \frac{(a_{ij} - \bar{a})(b_{ij} - \bar{b})}{\sigma_a \sigma_b},
\]

where $N$ is the total number of pixels, $(\bar{a}, \bar{b})$ are the mean values of the frame, and $(\sigma_a, \sigma_b)$ are their standard deviations. The frame gap $\delta\phi = |a - b|$ is the distance between frames $a$ and $b$ in rad m$^{-2}$.

We studied the correlation length in Faraday depth space of the PI data by considering the whole field of view and by focusing on a single region of the centre of the field (given by box 2 in figure 2). In figure 6 we show the cross-correlation coefficients for different frame gaps ($\delta\phi$).

For a fixed convolving RMSF, the reference level for data correlation/anti-correlation is shifted from zero to a certain positive value. This offset is due to the convolution of the noise of each frame with the RMSF, which introduces a degree of correlation of the noise in the frames. The cross-correlation of frame gaps $\delta\phi = 1, 2, 3$ rad m$^{-2}$ for noise-dominated frames convolved with an RMSF of 3 rad m$^{-2}$ is approximately 0.68, 0.22 and 0.1, respectively. Therefore the average levels in Figs. 6 correspond to a convolving function with a width of $\approx 2.95$ rad m$^{-2}$, in good agreement with the width of the RMSF. This means that outside the range of Galactic signal of the Faraday depth, from about $-10$ to $+5$ rad m$^{-2}$, the cross-correlation profile is consistent with a pure noise signal. Therefore for $\delta\phi = 1$ rad m$^{-2}$, a correlation coefficient above 0.68 indicates a positive correlation between two frames, a correlation coefficient of about 0.68 indicates no correlation while a correlation coefficient below 0.68 indicates an anti-correlation.

Several features in the cross-correlation profile for $\delta\phi = 1$ can be seen, which disappear as the frame gap increases. Therefore they are not broader than the RMSF width, which means these structures are Faraday thin. For a frame gap of $\delta\phi = 1$ rad m$^{-2}$, prominent peaks are seen at $\phi \approx -5$ rad m$^{-2}$ and $\phi \approx -2$ rad m$^{-2}$. Three more tentative, small peaks, possibly related to fainter extended emission, are observed around $\phi \approx -10$ rad m$^{-2}$, $\phi \approx 1$ rad m$^{-2}$, $\phi \approx 5$ rad m$^{-2}$.

Calculating the cross-correlation coefficients with the same frame gap of $\delta\phi = 1$ rad m$^{-2}$ in the smaller box indicated as 2 in Figure 2 shows interesting results. Correlated peaks at $\phi \approx -10, -6, -2$ rad m$^{-2}$ are still seen, although their amplitudes have changed. However, the most conspicuous changes are seen in the range of Faraday depth $\phi \sim [-2, +4]$ rad m$^{-2}$ where the cross-correlation profile is turned into anti-correlation, with two possible small peaks at $\phi \approx 0$ rad m$^{-2}$ and $\phi \approx +2$ rad m$^{-2}$. The polarized emission in this $\phi$-range is spatially anti-correlated. Simple simulations show that qualitatively this behaviour can be caused by a spatial gradient in Faraday depth space across these frames. The presence of multiple Faraday components within the peak was also confirmed by comparing the width of the peaks in the spectrum with the width of the RMSF. We checked the behaviour of some representative lines of sight through the "bubble", "ring", and "curtain" components. From the fitting of the limited sample of Faraday dispersion spectra, we find clues of multiple poorly separated components, in agreement with the cross correlation result.
- The RM peaks associated with the noise or artefacts (e.g. due to the lobes of the RMSF) show a systematically low $FWHM < 2.7 \text{ rad m}^{-2}$, while RM peaks associated with the three components have $FWHM \sim [2.9, 3.2] \text{ rad m}^{-2}$, in agreement with the expected RMSF width.
- Some lines of sight show excess of widths or complex morphology (see e.g. spectrum of line of sight 4 in Figure 9), which make them unsuitable for a single component fitting step. These cases can be found in all three components, but are more evident for the “curtain” component;
- Often spectra also have associated main lobes that are higher than the $\sim 35\%$ level expected from the RMSF profile. In conclusion we find agreement between the result of this test and the cross-correlation.

5. Definition and description of structures

The $(\alpha, \delta, \phi)$-cube contains a wealth of structures. In this section we briefly describe the main morphological features in the PI and Stokes U maps as a function of Faraday depth. First, there are spatially compact and isolated structures, such as Galactic and extragalactic Stokes I sources. These objects primarily “illuminate” the intervening Galactic ISM, and reveal its Faraday dispersion can be significant and they may actually show emission over a range of Faraday depths. Their definition is based on their compactness in $(\alpha, \delta)$ and, occasionally, on association with known objects. The second class of structure is the spatially (very) extended emission detected in polarization. These can be characterized by their properties of PI, Q, or U in Faraday space, in combination with the distribution of polarization angles.

We identified various components in the RM-synthesis cube based on morphological consistency and coherence in Faraday depth and name these components the “bubble”, the “ring”, and the “curtain”. These components are shown in polarized intensity in Figure 8.

- The discrete PI emission from the “bubble” appears at $\phi \sim -10 \text{ rad m}^{-2}$ in the centre of the field of view. A circular filled structure develops and expands with a maximum of polarized intensity at $\phi \sim -5 \text{ rad m}^{-2}$ and an angular diameter of $\sim 3^\circ$. Also, close to the center a hole in the emission develops and expands until the next structure - the “ring” - comes up. The Stokes U map (see Fig. 7 upper left panel) depicts a complex pattern of small-scale wrapped structures surrounded by larger and smoother ones.
- The “ring” structure consists of extended emission combined with narrow canals of low polarized intensity around a central, almost circular, edge. The “ring” can be considered as a smooth transition from the “bubble”. Its polarized emission reaches a maximum around $\phi \sim -1 \text{ rad m}^{-2}$ and shows bright PI emission occurring in the north-western part of the field with longer depolarization canals (Haverkorn et al. 2000), with lengths up to a few degrees. The orientation of these canals is mostly parallel to the Galactic plane, in agreement with the observation of Haverkorn et al. (2003). The Stokes (Q and) U maps (see Fig. 7 upper right panel) show a rapid sinusoidal behaviour at the edge of the “ring”, corresponding to a gradient in polarization angle.
- Finally, a significant pattern of faint, extended polarized emission -the “curtain”- is found at $\phi \sim [0, +5] \text{ rad m}^{-2}$. A fast transition is seen around $\phi \approx +2 \text{ rad m}^{-2}$ from the previous “ring” component to the “curtain”. We interpret this as a spatial gradient of polarized emission in Faraday space around $\phi \sim -2 \text{ rad m}^{-2}$ and $\phi \sim 0 \text{ rad m}^{-2}$, which is responsible for the abrupt decrease in correlation. Stokes U emission (Fig. 7 lower panels) reveals extended features on larger scales than the “bubble” and “ring” components. Also, whereas the “bubble” and “ring” show morphological correspondences, these are not present for the “curtain”.

These three components in the RM-synthesis cube correspond to the peaked features seen in the cross-correlations profiles (Figure 6) around $\phi \sim -6, -2, +2 \text{ rad m}^{-2}$, respectively.

5.1. Diffuse foreground polarized emission

To emphasize properties of linearly polarized emission in $\phi$ space, the PI emission was integrated in the frames from $-13 \text{ rad m}^{-2}$ to $-5 \text{ rad m}^{-2}$, from $-4 \text{ rad m}^{-2}$ to $-1 \text{ rad m}^{-2}$, and from $0 \text{ rad m}^{-2}$ to $+5 \text{ rad m}^{-2}$ as (Brentjens 2007)

$$P(\Delta \phi) = B^{-1} \sum_{\phi_{\min}}^{\phi_{\max}} (PI(\phi) - \sigma_{PI} \sqrt{\frac{\pi}{2}}),$$

where the normalization factor $B$ is the area of the RMSF beam after RM-CLEAN divided by the interval between two frames of the data cube, and $\sigma_{PI}$ is the noise in PI estimated from figure 5. These maps were clipped at a level of $3\sigma$ and then combined into a composite false-colour image as shown in the left-hand upper plot in figure 8.

Figure 8 shows a sample of Faraday depth spectra, obtained averaging over a beam-sized box region, for several lines of sight. The lines of sight were selected to show widely varying spectra, with a strong main peak (e.g. spectrum 7) or with double and multiple peaks (e.g. spectra 1, 3, and 5 respectively). A peak in the Faraday depth spectrum indicates an emission component in Faraday space. However, due to the limited frequency
Fig. 7. Stokes U emission at four representative Faraday depth values. The images correspond to $\phi = -5$ rad m$^{-2}$ (upper left panel), $\phi = -1$ rad m$^{-2}$ (upper right panel), $\phi = 0$ rad m$^{-2}$ (lower left panel) and $\phi = +1$ rad m$^{-2}$ (lower right panel).

Table 2. Properties of the three components.

<table>
<thead>
<tr>
<th>Structure</th>
<th>Colour</th>
<th>$\phi$ range [rad m$^{-2}$]</th>
<th>$\phi_{\text{peak}}$ [rad m$^{-2}$]</th>
<th>$&lt;P&gt;$ [Jy beam$^{-1}$]</th>
</tr>
</thead>
<tbody>
<tr>
<td>Bubble</td>
<td>Red</td>
<td>8.0</td>
<td>-5</td>
<td>$(1.72 \pm 0.58) \times 10^{-3}$</td>
</tr>
<tr>
<td>Ring</td>
<td>Green</td>
<td>4.0</td>
<td>-2</td>
<td>$(1.78 \pm 0.26) \times 10^{-3}$</td>
</tr>
<tr>
<td>Curtain</td>
<td>Blue</td>
<td>5.0</td>
<td>+2</td>
<td>$(1.53 \pm 0.22) \times 10^{-3}$</td>
</tr>
</tbody>
</table>

Notes. The columns denote: 1) Name of component, 2) Colour in figure, 3) Range in Faraday depth in which component is visible, 4) Faraday depth of peak, 5) Polarized surface brightness averaged over Faraday depth range.

coverage, components in Faraday space may be represented in the Faraday depth spectrum incompletely or not at all.

We estimated the mean polarized surface brightness for each component (see Table 2). These mean values are of the same order of magnitude. Interestingly the “bubble” and “ring” components have comparable polarized surface brightness, slightly higher than the “curtain”. The mean polarized brightness temperature over the range $\phi \in [-13, +5]$ is $T_b \sim 5.6$ K.
5.2. Polarized extragalactic background sources

Although we are primarily interested in the Galactic emission we briefly point out a few interesting discrete extragalactic objects within 5° of the field centre. These are

- The spiral galaxy IC 342, which is visible both in polarized and total intensity. Large scale disk/halo emission at $\phi = (-3.0 \pm 0.5)$ rad m$^{-2}$ is observed, in agreement with Krause et al. (1989) who find RM values between $-10$ rad m$^{-2}$ and $10$ rad m$^{-2}$.

- The giant double-lobe radio galaxy WNB 0313+683, which shows prominent linearly polarized emission from the south lobe (at $(\alpha, \delta)_{2000} \approx (03^h 17^m, 68^\circ.2)$) and the core (at $(\alpha, \delta)_{2000} \approx (03^h 18^m, 68^\circ.3)$) in a range $\phi \approx [-17, -5]$ rad m$^{-2}$ consistent with values reported by Schoenmakers et al. (1998) and Haverkorn et al. (2003).

However, no polarized emission is detected from the north lobe, which is pointing away from the observer. Since the Stokes I map shows a sharp difference in brightness for the lobes (the north to south lobe mean brightness ratio is $\sim 0.2$), the non-detection of polarized emission from the north lobe can be explained as a consequence of relativistic beaming and/or additional Faraday depolarization (Heald et al. 2009).

We used discrete polarized background sources to search for a latitude and/or longitude dependence of the Faraday depth across the field of view. From the NVSS RM catalogue (Taylor et al. 2009) we selected a sample of polarized sources with known RM, which covers the observed field of view and its surroundings (see Fig. 10). To average out intrinsic RM components of
the extragalactic sources, we re-sampled the data over square bins with an angular scale of $5^\circ$ (about half the size of the imaged field). We find a clear gradient in Galactic latitude of $\Delta \text{RM}/\Delta \theta \approx 4.6 \text{ rad m}^{-2} \text{ deg}^{-1}$, while no evident Galactic longitude dependence is found. The dominant negative RM values imply overall negative $B_\parallel$ values, in accordance with the observed negative Faraday depths. A systematic increase in RM values for sources below $b = 5^\circ$ is observed as expected because of the presence of the Galactic disk. In the longitude range $l \in [125^\circ, 140^\circ]$ the presence of extended HII regions (i.e. the W3/W4/W5/HB3 HII region supernova remnant (SNR) complex in the Perseus arm), as well as the H$\alpha$ maps (Haffner et al. 2003) suggests that the increase in RM towards lower latitudes is at least partially a consequence of enhanced thermal electron density. We note that both the diffuse emission and polarized point sources show predominantly negative Faraday depth and RM, respectively. However, RMs from the extragalactic point sources are much more negative than the Faraday depths of the diffuse emission, suggesting that (a) the diffuse emission is nearby and does not span the full line of sight through the Galaxy, and (b) that $|\text{RM}|$ increases through the outer Galaxy without large-scale magnetic field reversals.

6. Model for the diffuse polarized emission

In this section, we discuss plausible sources in the ISM that correspond to the three polarized components identified in Section 5. Interpretation of these polarized components in terms of synchrotron emitting and/or Faraday rotating regions is not straightforward for a number of reasons. First, these are interferometric data, which are missing short spacings in the uv-plane and are therefore insensitive to structure on scales larger than two degrees. This explains why a large amount of polar-
ized emission is observed, but only very weak total intensity (Bernardi et al. 2009), providing an apparent polarization degree far above 100%. This indicates that the synchrotron radiation is emitted on large scales, but its polarization is altered on smaller scales by Faraday effects. In this case we can calculate the missing large-scale structure contribution for Stokes Q and U for a uniformly polarized background propagating through a small-scale Faraday screen (Haverkorn 2002). The expected offset for Stokes Q and U ($Q_0$ and $U_0$) depends on the wavelength ($\lambda$) and the width of the Faraday depth distribution ($\sigma_\phi$) as

$$e^{-2\sigma_\phi^2\lambda^2} \rightarrow 0 \Rightarrow Q_0 = U_0 = 0.$$  

(6)

At low frequency this condition is typically well satisfied and we do not expect large-scale undetected Stokes Q and U structures. Although there is missing large-scale structure in total intensity Stokes I, there is no missing large-scale structure in Stokes Q and U, therefore the polarization data are reliable. Second, the limited frequency range of the data set precludes the detection of Faraday depth components that have a width $\delta\phi > 1$ rad m$^{-2}$ (Section 6.1). Therefore, by definition, the Faraday depth components that we observe are unresolved in Faraday depth. Analogously to the missing short-spacing problem, this indicates that there likely is Faraday-thick polarized emission (e.g. emission over a wide range of Faraday depths), which we cannot detect. Last, depolarization effects can decrease the polarized intensity of the observed structures.

First, we calculate some properties of the global interstellar medium in the direction of the FAN region, below. Then we discuss what information is available on the absolute and relative distances of the three components in Section 6.1. Finally, we present our model in Section 6.5.

From the mean dust-corrected Hz surface brightness across the (half upper part of the) field of view ($I_\text{Hz} \approx 3.3$ R) and adopting an electron temperature in the diffuse ionized interstellar medium $T = 8000$ K, we derive the related emission measure $EM_\text{field} = 7.43$ pc cm$^{-6}$. This corresponds to a large-scale mean free electron density of $n_e \approx 3 \times 10^{-2}$ cm$^{-3}$ over an assumed total path length of 7 kpc, a value, which is in good agreement with the literature (Hill et al. 2008, Ferrière 2001, de Avillez et al. 2012).

The FAN region has a high degree of polarization, which indicates a relatively regular, large-scale magnetic field topology. This can be either uniform or anisotropically random magnetic fields.

The uniform magnetic field component following the spiral arms is almost perpendicular to the line of sight in this direction. Therefore, the impact of the large-scale interstellar magnetic field on Faraday depth values toward the FAN region is expected to be small. We can test this assumption by estimating the path-averaged magnetic field amplitude along the line of sight up to a few hundred parsecs. We consider a sample of nearby pulsars around the imaged field (see Table 3) and apply the general relation:

$$\langle B_\| \rangle = 1.24 \frac{RM}{DM}.$$  

(7)

With the exception of object 1, all pulsars have estimated distances lower than $\approx 600$ pc. The scatter in $B_\|$ is high, and its sign changes for different pulsars, confirming that the uniform magnetic field component is much smaller than the random component in this direction. We calculate a mean parallel magnetic field $\langle B_\| \rangle \approx 1.2$ $\mu$G.

6.1. Distance estimates to the structures

Most of the polarized emission can be found at slightly negative Faraday depths, consistent with earlier observations (Brouw & Spoelstra 1970, Taylor et al. 2009), which suggests that the radiation is emitted at a short distance from the observer. Wilkinson & Smith (1974) and Uyaniker et al. 2003 deduce that this polarized emission and the low RM values in the second quadrant around $l \sim 150^\circ$ must be nearby, possibly at a distance $\leq 500$ pc. Also, the NVSS gradient show a mean RM value at the FAN latitude of $RM_{\text{NVSS}} \approx 32$ rad m$^{-2}$, which is higher than the observed Faraday depths. We conclude that the detected structures are not representative of the general behaviour through the entire line of sight; as a consequence, these structures must be close.

We can roughly estimate the distance to the “bubble”, assuming uniform conditions for the medium along the entire line of sight, as

$$d_0 = \frac{\phi_{\text{OBS}}}{\phi_{\text{REF}}} D_{\text{REF}} [\text{pc}],$$  

(8)

where $\phi_{\text{OBS}}$ is the measured Faraday depth, and $\phi_{\text{REF}}$ the reference value of Faraday depth (or rotation measure) corresponding to the line of sight total length $D_{\text{REF}}$. We consider the rotation measure of nearby radio pulsar B0226+70 at $(\alpha, \delta)_{\odot 2000} \approx (02^h31^m, 70^\circ 26^\prime)$ as a reference. The distance of this pulsar is $d_{\text{PSR}} = (2.25 \pm 0.56)$ kpc and its rotation measure $RM_{\text{PSR}} = (-56 \pm 21)$ rad m$^{-2}$ from the ATNF Pulsar Database2 (Manchester et al. 2005). Equation (8) then gives $d_{\text{bubble}} \approx (201 \pm 90)$ pc, which is consistent with a previous estimate (Haverkorn et al. 2003). At such a distance and considering the angular size of the “bubble” ($\approx 3^\circ$), a physical size in the plane of the sky of $\approx 10$ pc is obtained.

Considering the intrinsic Faraday depth for the “curtain” and “ring” components along with the large-scale electron density field and magnetic field component estimated above along the line of sight, we obtain an estimate of the distance needed to build up this Faraday depth. We find ranges of $\approx 70$ pc and $\approx 140$ pc for the “curtain” and the “ring”, respectively. These distance estimates do have considerable error margins due to the strong assumptions.

These distance estimates can be tested by comparing the amount of polarized intensity built up over that distance to the observed polarized intensity in the component. At 408 MHz, the total polarized emissivity is $I_{\text{pol}}^{150} \sim (11 \pm 3)$ K kpc$^{-1}$ or 0.011 K pc$^{-1}$ (Beuermann, Kanbach & Berkhuijsen 1985). With a spectral index of $-2.3$, the conversion factor from 408 to 150 MHz is $\approx 12.2$. Thus the total intensity emissivity at 150 MHz is $\epsilon_{\text{pol}}^{150} \sim 12.2 \times \epsilon_{\text{pol}}^{408} = (134 \pm 37)$ K kpc$^{-1}$ or 0.13 K pc$^{-1}$. If we assume a polarization degree of 8% (Haverkorn et al. 2008), then $\epsilon_{\text{pol}}^{150} \sim \epsilon_{\text{pol}}^{408} \times 0.08 = (10.72 \pm 2.96)$ K kpc$^{-1}$ or 0.0094 K pc$^{-1}$. Therefore, for a constant $\epsilon_{\text{pol}}^{408}$ (which implies a constant polarization degree of 7%) over the line of sight through the “curtain” component, we need about $140 \pm 39$ pc to build up the polarized intensity of the “curtain” of $\approx 1.2$ K. This estimate is higher than our estimate above, probably because the “curtain” component is likely to show enhanced synchrotron emission in a narrow emission region (see Section 6.4). The “ring” component would need about $168 \pm 46$ pc to build up the proper polarized intensity, consistent with the estimate above.

We can also give information about the relative positions and distances of the components. The “curtain” component is the
Notes. For each object the inferred magnetic field component along the line of sight \( \langle B_i \rangle \) is also listed. Data are taken from the ATNF Pulsar Database (Manchester et al. 2005).

(a) Dist is the best estimate to the pulsar distance (kpc). (b) DistDM is the distance based on the Taylor & Cordes (1993) electron density model.

6.2. The foreground "curtain" component

The change in sign of Faraday depth between the "curtain" and the other components indicates a reversal of the magnetic field component along the line of sight \( B_i \) behind the "curtain". A plausible magnetic field configuration of how this can be achieved is, e.g., a localized, ordered, magnetic field in the Galactic plane perpendicular to the observer, which fans out locally to produce oppositely directed parallel field components. This magnetic field configuration has a maximum synchrotron emission at the location of the perpendicular magnetic field lines, possibly corresponding to the synchrotron emission from the "curtain".

We propose that this component corresponds to the wall of the Local Bubble. The above size estimates for this foreground component roughly agree with the dimension of the Local Bubble in this direction (Snowden et al. 1998). A tomography of the interstellar gas within 250 pc was recently obtained by Welsh et al. (2010) combining interstellar absorption data for stars with a Hipparcos measured parallax. Maps of spatial distribution for the neutral gas and neutral plus ionized gas components were derived from Na\textsc{i}, Ca\textsc{i} tracers, displaying the Local Bubble as a region that is poor in neutral gas (and dust) but with several diffuse and highly ionized clouds. A visual inspection of both Na\textsc{i} and Ca\textsc{i} galactic projected maps (see their Figs. 12 and 15) toward the direction \( l = 137^\circ, b = +7^\circ \) reveals the presence of an extended and high-density wall of partially ionized medium at about 100 pc of the Sun, as well as a rarefied medium inside the wall, in agreement with our estimate. Moreover, optical starlight measurements in the Fan region from Heiles (2000) show a rise in polarization degree from a distance \( \sim 100 \text{ pc} \), as shown in Fig. 11. This can be explained by an increase in the dust density, denoting the edge of the Local Bubble. The few high polarization degrees at \( \sim 10 \text{ pc} \) can be explained by a compact and cold cloud in the very local interstellar medium. In this picture, the magnetic field would be aligned with the Local Bubble wall, i.e. mostly perpendicular to the line of sight, which indicates enhanced synchrotron emission in the Bubble wall. The Faraday rotation of that emission by the Local Bubble interior is small, i.e. \( \lesssim 2 \text{ rad m}^{-2} \). Using the computed mean parallel magnetic field component of \( \langle B_i \rangle \approx 1.2 \mu \text{G} \) and a path length of 70 pc, the mean electron density is \( n_e \parallel \approx 1.5 \times 10^{-2} \text{ cm}^{-3} \) in the Local Bubble, which agrees with literature (Spangler 2009).

Previously, an association of the extended polarized Galactic radio synchrotron foreground with the Local Bubble was made by Brem et al. (2011), who observed the area around the Perseus cluster near \( l = 150^\circ, b = +13^\circ \) at \( \lambda = 0.80 - 0.88 \text{ m} \). In this region, negative Faraday depth values are expected from the inferred direction of the large-scale magnetic field, while he finds a positive Faraday depth component at \( \phi = +6 \text{ rad m}^{-2} \) and estimates its size of approximately 200 pc. These values differ from our estimations by about a factor two and may indicate density variations and irregular shape of the Local Bubble wall.

6.3. The background "ring" component

The "ring" component shows a small south-east to north-west gradient in Faraday depth \( \lesssim 1 \text{ rad m}^{-2} \text{ degree}^{-1} \). This gradient does not correspond to the large-scale gradient in RM expected from the NVSS data (Taylor et al. 2009), but is directed almost perpendicular to that. If, as we argue below, the "bubble" component is just an additional Faraday rotation of synchrotron emission in the "ring" component, we would expect this gradient across the field to also be present in the "bubble". However, since the Faraday depth gradient of \( \sim 2 \text{ rad m}^{-2} \) is measured over the entire imaged field, the expected \( \phi \) gradient over the bub-
ble size (about 1/3 of the entire field) turns out to be less than 1 rad m$^{-2}$ degree$^{-1}$ (i.e. less than 1/3 of RMSF width), hence undetectable with our observational set up.

6.4. The “bubble” component

The “bubble” component is detected in polarized intensity, but not in total intensity. This could be due to the lack of short spacings. However, if the bubble were significantly emitting, its polarized intensity would be higher than the ring component. Instead, their polarized brightness temperatures are comparable, suggesting that the “bubble” is a Faraday rotating structure, retro-illuminated by the synchrotron emission from the “ring”.

We interpret these observations as a consequence of the configuration with the “bubble” located in the spatially extended “ring” structure. Two configurations are possible for the “bubble”: it can be assumed to be either a filled sphere or a shell surrounding a density depletion. We prefer the first configuration because PI emission at the greatest Faraday depths is observed in the centre of the “bubble”. Indeed under the assumption of pressure balance a depletion of warm ionized medium relative to its surroundings may imply an enhancement of neutral gas or dust, which is not observed (e.g. the total H I or IRAS 100 µm maps). Instead since the early work of Verschuur (1969), a considerable lack of H I is observed, as well a very good agreement between higher RM / Faraday depth values and lack of H I. Also, for a filled sphere it is easier to build up the higher Faraday depths observed through the “bubble”.

The additional Faraday rotation in the “bubble” component can be caused by increased $B_0$, increased $n_e$, or a combination of these two options. Observations of Hz emission measures set an upper limit for the increase in $n_e$ in the bubble. The bubble is not detected (Haverkorn et al. 2003) in the WHAM Northern Sky Survey (Haffner et al. 2003), which has a sensitivity of 0.05 R. For the emission not to be detected at $3\sigma$ (i.e. 0.15 R), the emission measure has to be $EM_{3\sigma} \lesssim 0.34$ pc cm$^{-6}$.

Assuming that the bubble is spherical, the magnetic field component along the line of sight $B_l$ can be estimated as

$$\Delta \phi_{max,Bubble} \approx 0.81 \times n_e,Bubble \times B_{0,Bubble} \times \Delta L_{Bubble} \cdot$$  \hspace{1cm} (9)

We can express both the size and the free electron density as a function of the distance to the “bubble”: $\Delta L_{Bubble} \approx \tan^3 \frac{\theta}{\Delta \phi}$ and $n_e, Bubble \approx \sqrt{EM/\Delta L_{Bubble}}$. By using these expressions we can check the variation in the magnetic field component along the line of sight, the free electron density and the magnetic field strength along the line of sight by a factor of a few as shown in figure 12. A reference distance of about 200 pc implies a path strength along the line of sight by a factor of a few as shown in figure 12. Also, for a reference distance of about 200 pc (vertical dot dashed black lines) the upper limit for the “bubble” electron density ($n_e, Bubble \approx 0.18$ cm$^{-3}$), the magnetic field component along the line of sight $B_{0,Bubble} \approx 5.25 \mu$G and its size $\Delta L_{Bubble} \approx 10.5$ pc are indicated by the horizontal black dashed lines.

![Fig. 12. Variation in $B_{0,Bubble}$, $n_e,Bubble$, and $\Delta L_{Bubble}$ as a function of “bubble” distance. Also, for a reference distance of ~200 pc (vertical dot dashed black lines) the upper limit for the “bubble” electron density ($n_e,Bubble \approx 0.18$ cm$^{-3}$), the magnetic field component along the line of sight $B_{0,Bubble} \approx 5.25 \mu$G and its size $\Delta L_{Bubble} \approx 10.5$ pc are indicated by the horizontal black dashed lines.](image)

The chaotic and patchy appearance of observed features both in polarized intensity and polarization angle imply a large amount of depolarization and may be the result of the turbulent state of the probed magnetized medium. The power-law behaviour of the power spectrum indicates a turbulent medium. In figure 14 we show power spectra of the bubble and background components; the spectral energy distributions are close to, but slightly flatter than, a Kolmogorov spectrum. Furthermore, the presence of an inertial range is apparent, which extends for more than a decade and flattens at modes $k \gtrsim 10^3$. Such an increase in power on small scales agrees with the expected large amount of depolarization.

6.5. The model in physical space

These considerations lead us to a qualitative model in physical space as depicted in figure 15. The region nearest to the observer

1 Due to the finite size of the field of ~12°, the smallest mode we can consider is $k_{min} \sim 10^2$, while the largest mode $k_{max} \sim 2.6 \times 10^3$ is defined by the angular resolution.
is bordered by a synchrotron emission layer that corresponds to
the Local Bubble wall, about 70 pc away (the “curtain”). This
region has a small Faraday depth and is therefore (partially) ion-
ized and has a parallel magnetic field component towards the
observer. The border region has enhanced synchrotron emission,
which points to an increase in magnetic field perpendicular to
the observer.

Behind this region is an extended, magnetized region corre-
sponding to the “ring”, a volume of warm partially ionized and
weakly emitting medium which contains the “bubble” compo-
nent. The parallel component of the large-scale magnetic field in
this direction is expected to point slightly away from us (Sun et
al. 2008), in agreement with these two components at negative
Faraday depths. Since most of the diffuse synchrotron emission
is thought to be emitted in the spiral arms and the spatial dis-
tances we infer are within a few hundreds of parsec, we conclude
that the overall detected PI emission originates primarily in the
Local arm.

6.6. Possible associations

Circularly shaped, polarized objects without counterparts in
other tracers have been observed before (e.g. Gray et al. 1998;
Uyaniker & Landecker 2002). These observations differ in two
ways from the previous ones.

Firstly, we observe much more small-scale fluctuations in
the polarization angle patterns. However, this can be caused by
the different observing frequencies: Faraday effects are much
stronger at low frequencies, so that angle variations are expected
to be more evident. Secondly, Gray et al. (1998) and Uyaniker &
Landecker (2002) explain their polarization structures in terms
of enhancement in electron density, while we (and Haverkorn
et al. 2003) argue that some of the structure must be due to en-
hanced magnetic field. The importance of the magnetic effects

Fig. 13. Grey scale images of polarization angle at selected Faraday depths at $\phi = [-7, -5, -3, -1]$ rad m$^{-2}$ from top left to bottom
right. The gray scale runs from +90° (black) to -90° (white).
For the background “ring” component, with Boltzmann constant, and $T$ where Table 4. Power spectral density of polarized intensity of the “ring” (stars) and “bubble” (circles) components as derived from a 6 degree inner square of the PI images integrated over the relevant Faraday depths. Also statistical errors and the Kolmogorov spectral slope are shown by 1σ error bars and a black solid line, respectively.

and their coupling with the particle density is supported by the ratio of thermal to magnetic pressure $\beta_{pr}$ which is given by

$$\beta_{pr} = \frac{16\pi n_e kT_e}{B^2}$$

where $B \geq B_\parallel$ is the total magnetic field strength, $k$ the Boltzmann constant, and $T_e$ the electron temperature in K. For the background “ring” component, with $T_e \approx 8000$ K, $B_{\parallel} \sim 1.2 \mu G$, and $n_e \sim 3 \times 10^{-2} \text{ cm}^{-3}$, we find $\beta_{pr} \approx 1.15$, which indicates a non-negligible role played by the magnetic field with respect to the thermal motion. For the bubble (with $n_e \leq n_{e,\text{bubble}}$ and $B_{\parallel} \leq B_{\parallel,\text{bubble}}$) we find a lower value $\beta_{pr} \leq 3.62 \times 10^{-3} (T_e/8000 \text{ K})$, indicating that magnetic effects dominate thermal effects over a wide range of temperatures (i.e. $T_e \approx 2.2 \times 10^4$ K); therefore the observed morphology can be shaped by the magnetic pressure of the surrounding ISM. Because of the low thermal electron density, the estimated $\beta_{pr}$ value is far outside the commonly observed range ($\beta_{pr} > 1$) for an H II region unless a strong gradient of temperature with respect to the surrounding is considered. To address the origin of the bubble we now examine several possible origins of this component: an old supernova remnant, an old planetary nebula, and a photo-ionized region.

6.6.1. Old supernova remnant

The presence of a Faraday depth gradient across the bubble, the abundance of small scales and an evident polarization intensity pattern could indicate a supernova remnant. The absence of Stokes I emission, as well as the low ratio of thermal to magnetic pressure could be explained by a very old remnant. However, no traces of shocks are found at other wavelengths, and the radial Faraday depth gradient within the bubble does not agree with the expected $\phi$-profile for supernova remnants (Uyaniker et al. 2002; Harvey-Smith et al. 2010). Finally, a supernova remnant is a shell, while the bubble is thought to be a filled spherical structure.

6.6.2. H II region

We consider the case of an H II region in an unusually low-density medium and a possible association with the nearby B-type star HIP 15520 $d_{LOS} \approx (234 \pm 24) \text{ pc}$ (Van Leeuwen 2007). The distance, position and proper motion of this star (see Table 4 and figure 16) lie within the constraints for the bubble. A link between this star and the Fan region was first suggested by Verschuur (1969), who pointed out the neutral gas depletion around the position of this star. He explained the disturbance in the H I by the motion of this star through the interstellar medium. However, an active H II region is a strong source of Hα. We calculated the estimates Hα flux from the bubble if it is an H II region. The ionization flux ($Q_0$) for a a B2 type is $Q_0 \leq 10^{45} \text{ ph s}^{-1}$ (Sternberg et al. 2003), which can be used to constrain the density in the Strömgren sphere as

$$n_s \approx 10^3 \text{cm}^{-3} \left(\frac{1.2 \text{ pc}}{R_\ast}\right)^{3/2} \left(\frac{Q_0}{5 \times 10^{49} \text{ photons s}^{-1}}\right)^{1/2}.$$
At a distance of 234 pc and for an angular size of \(\sim 3^\circ\), we find a corresponding radius of 3.9 pc, a density of \(\sim 0.4\) cm\(^{-3}\) and an emission measure of \(EM_{\text{HIP15520}} \sim 5.25\) pc cm\(^{-6}\). This expected emission measure value is well above the WHAM sensitivity, thus it appears that a steady H\(\alpha\) region is not likely to be responsible for the observed bubble.

6.6.3. Old planetary nebula

A more likely scenario would be provided by the final stage of the life of a star, forming a compact object. For a white dwarf star, some outer shells of materials have to be expelled in the surrounding ISM before the collapse by a weak shock. After this ISM sweeping stage, the hot star can ionize the surrounding medium quickly, producing a photo-ionized region. Indeed, evolved planetary nebula nuclei can have Lyman continuum photon luminosities comparable to those of early B stars (Reynolds 1986), enabling rapid ionization of the surroundings. The observational work of Tweedy & Kwitter (1996), focussed on old planetary nebulae, indicates there is a class of nebulae that appear to be filled, in agreement with the bubble.

Indeed, the white dwarf star WD 0314+648 (see Table 4 and figure 16) on the edge of the bubble, moving outwards, is an obvious first candidate. Its distance and radial motion are not known. However, the white dwarf has a high proper motion, which can be due to a small distance to the observer, or due to a kick acceleration at its formation. If we assume that this white dwarf was born at the approximate centre of the bubble, we can obtain an estimate of its age as the time needed for the star traveling from the bubble centre. We find an age of \(\gtrsim 15000\) yr for the star WD 0314+648 close to the edge of the bubble (for a proper motion and an estimated radial distance from the bubble centre of \(pmn \sim 0.2\) arcsec yr\(^{-1}\) [Lepine & Shara 2005] and \(r \sim 0.83^\circ\), respectively). This age is much shorter than the recombination time, thus supporting the inferred high ionization degree.

The effective temperature for white dwarf WD 0314+648 is 17500 K [Sion et al. 1988]. This temperature is so low that the white dwarf will not ionize its surroundings, in agreement with the lack of any bubble features around WD 0314+648. However, for it to be able to explain the bubble, it must have been much hotter and ionizing its surroundings when it was located near the centre of the current bubble.

From the above reasoning, it is possible that the bubble is a fossil Strömgren sphere created out of an old planetary nebula and associated with a white dwarf star. Owing to the old age of the relic, interaction with the surrounding interstellar medium is expected, and the high symmetry of the observed morphology suggests that the surrounding medium is rather uniform. For a white dwarf at a distance of 200 pc, with a density of the bubble of \(n_e \lesssim 0.18\) cm\(^{-3}\), the required ionization flux \(Q_0\) is \(Q_0 \lesssim 10^{43}\) ph s\(^{-1}\). This corresponds to an emission measure \(EM \lesssim 0.34\) pc cm\(^{-6}\), consistent with observations.

From the Lyman continuum fluxes of Panagia (1973) and the white dwarf temperature and radius, we estimate the minimum temperature needed for sustaining the bubble: \(T^{\text{WD}}_{\text{min}} \gtrsim 26000\) K. The time needed for the white dwarf to cool from \(T^{\text{WD}}_{\text{min}}\) to the current value is \(\Delta t \sim 10^7\) yr (roughly estimated from the cooling time in [Mestel 1952]), which does not agree with the age estimated from its proper motion. Therefore, this particular white dwarf is probably not the cause of the bubble. However, other white dwarfs, at even greater angular distances from the centre of the bubble, may have created the bubble.

6.7. Comparison of the model at other wavelengths

We compare our model to two radio observations of this field at higher frequencies, the 85 cm WSRT observation by Haverkorn et al. (2003) and the PI survey at 21 cm by Wolleben et al. (2006). In our framework the bulk of the emission must build up within and beyond the foreground “ring” component, at a few hundred parsec from the observer, in agreement with the conclusion of Wolleben et al. (2006). Also, in agreement with their claim of multiple emitting components over a wide range of spatial scales, we suggest there are at least two emitting and Faraday thin components: the very nearby “curtain” component and the “ring” component; however, the “bubble” component is not seen in their polarized intensity map. We explain this lack of detection as due to the low synchrotron emissivity of the “bubble” feature at this frequency (the “bubble” does not manifest in emission) and to the low depolarizing impact it has on the background emission. For a maximum \(\Phi_{\text{bubble}} \sim 8\) rad m\(^{-2}\) the expected modulation of the polarization angle at 21 cm is \(\sim 21\) degrees, but over the beam of the map the mean \(\Phi_{\text{bubble}}\) is \(\lesssim 4\) rad m\(^{-2}\) providing a variation in the polarization angle \(\lesssim 10\) degrees. Interesting is also the comparison with the 85 cm data of Haverkorn et al. (2003). Indeed, the standard RM values estimated by Haverkorn et al. (2003) are in good agreement with the Faraday depths of the “bubble” and “ring” components we present in this paper. Moreover, the spatial distribution of RM values matches the observed Faraday depths observed at 2 m. However, the PI map at 85 cm displays a ring-like feature instead of a filled one. This difference is not likely to be explained by beam or depth depolarization (the resolution of PI maps is similar at 1 m and 2 m) but may be the consequence of the missing short spacing on Stokes Q and U maps at 85 cm, as also noted by Bernardi et al. (2009). Finally, we note the similarity of our model with the one provided by Bernardi et al. (2009), who consider the presence of three separated components: a synchrotron-emitting plus a separated Faraday-rotating components beyond the “bubble”, which correspond to our spatially extended, synchrotron-emitting and Faraday-rotating “ring” component, which surrounds the “bubble”. The main differences from their model are the absence of...
the very nearby “curtain” component and the position of the “bubble” with respect to the “ring” component.

7. Summary and conclusion

We used the RM-synthesis technique on WSRT radio polarization data at ~2 m to reveal a complex Galactic synchrotron-emission foreground in a field in the Fan Region centred at \((l, b) = (137^\circ, 7^\circ)\). We detected polarized signals with Faraday depth between -13 and +5 rad m\(^{-2}\), which can be separated into three distinct components around -5, -2, and +2 rad m\(^{-2}\), based on morphological consistency and coherence in Faraday depth space. For the first time, cross-correlation was applied to identify and characterize these polarized structures in Faraday depth space. The low Faraday depth values of all components suggest nearby locations of the emission.

The structure at \(0^\circ, +5^\circ\) rad m\(^{-2}\) (called the “curtain”) very likely corresponds to enhanced synchrotron emission due to compressed magnetic fields in the Local Bubble wall at around 70 pc distance, in agreement with the location of the wall from optical polarized starlight data. The low but positive Faraday depth of this component suggests a parallel magnetic field component directed towards the observer.

The second component centred at \(-1^\circ\) rad m\(^{-2}\) (called the “ring” component) is located just behind the Local Bubble. It is expected to be spatially extended and Faraday-thick, and therefore only partially detected in these data.

The third component (the “bubble”) is located within the extended “ring”. Its circular regular shape suggests relatively uniform electron density and magnetic field structure, as is expected within the Fan region. The Faraday depth of the “bubble” in combination of its non-detection in H\(\alpha\) indicates that it cannot be created by density enhancement alone, but needs to have enhanced magnetic field strength as well, contrary to earlier detected regular polarization structures (Gray et al. [1998, Uyaniker & Landecker 2002, Uyaniker et al. 2003]). Several possible associations of the bubble with ISM objects we discussed, but the most likely explanation is the presence of a nearby \((\sim 200\) pc\) relic Strömgren sphere, associated with old unidentified white dwarf star and expanding in a low-density environment.

Polarized intensity from both the “ring” and the “bubble” components show a power spectrum that has a power law, which is indicative of turbulence. Also, the discrete Faraday depth components show a power spectrum that has a power law, which is expected to be spatially extended and Faraday-thick, and therefore only partially detected in these data.

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